# SGN-16006, IMAGE PROCESSING ASSIGNMENT

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## 1. INTRODUCTION

In this assignment we implemented two methods to detect the DTMF frequencies. We used National Instruments myRIO-1900 and LabVIEW coding environment. Both methods calculated the value of certain frequency in the input signal. This value is compared to threshold, and if the value is greater than the threshold, a correspondig LED in myRIO-1900 will light.

## 2. BACKGROUND THEORY

In telephone networks the dialed number is transmitted with DTMF signals. Every number is a result of two frequencies, as seen in figure 1. We used two algorithms that detected the vertical frequencies and calculated the amount of this frequency in the signal. This amount is then compared to a threshold, and if it is greater than the threshold, a corresponding LED will light.

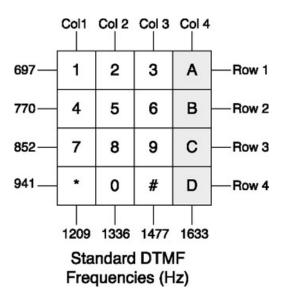


Fig. 1: DTMF frequencies [1]

Two different methods were used in this assignment, Correlation detection and Goertzel -algorithm. In the first method we calculated the correlation between the input data and and the signals 1 and 2.

$$c_{697}(n) = \cos(2\pi \times 697 \times n/F_n) \tag{1}$$

$$s_{697}(n) = \sin(2\pi \times 697 \times n/F_n)$$
 (2)

The correlations are defined by equations 3 and 4.

$$c_{\cos}(697) = \sum_{n=0}^{N-1} c_{697}(n) \times x(n)$$
 (3)

$$c_{\sin}(697) = \sum_{n=0}^{N-1} s_{697}(n) \times x(n)$$
 (4)

Next we estimated the signal power using equation 5.

$$var = \sum_{n=0}^{N-1} x(n)^2$$
 (5)

Finally, we tested the presence of the frequency using equation 6 In this case, we tested the presence of the 697Hz component. By replacing the 697 value in the equations, we can test the presence of the other components.

$$w_{697} = \frac{c_{cos}^2(697) + c_{sin}^2(697)}{var}$$
 (6)

The Goertzel-algorithm uses an unstable IIR filter that amplifies the selected frequencies. Detecting the frequency f with sampling frequency  $F_s$  can be done using Goetzel filter 8.

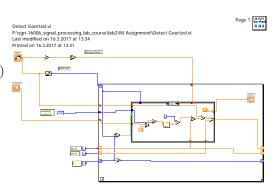
$$y(n) = x(n) + 2\cos(2\pi f/F_s)y(n-1) - y(n-2)$$
 (7)

$$y(n) = x(n) + 2\cos(2\pi f/F_s)y(n-1) - y(n-2)$$
 (8)

However, we cannot use this equation as a direct indication on which LED should light. Instead, we can use equation 9.

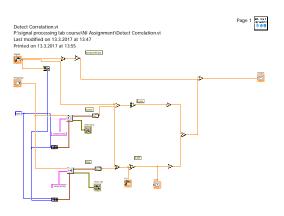
$$|Y(e^{(i\omega)})|^2 = y^2(N-1) + y^2(N-1) - 2\cos(2\pi f/F_s)y(N-2)y(N-1)$$
(9)

The Goertzel algorithm itself consists of three steps. We loop through all the steps, increasing the value of n with every step. Step 1. we initialize n , y(n-1) and y(n-2) as 0. Then in step 2, if n; N we calculate y(n) using 8, increment n=n+1 and return to step 2.In step 3, if n is equal to N, we calculate 9. and divide it with variance, using equation 5. This value is compared to the thresholdn and if it is greater than the threshold, LED is turned on, otherwise it's turned off. Again, we increment n=n+1 and return to step 1.

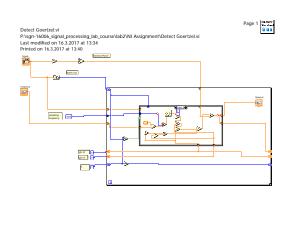


### 3. METHODS

The sampling rate for both algorithms is 3000HZ and the period is 333s. Both methods will calculate the frequency value for four different frequencies. Below are the Lab-VIEW algorithms for calculating the value. The Goertzel-algorithms in figures 3 and ?? correspond to steps 2 and 3 from the algorithm.



**Fig. 3**: Goertzel-algortihm in LabView when n < N



**Fig. 4**: Goertzel-algortihm in LabView when n = N

After the value of the frequency is calculated, we compared it to the threshold. We used the following MATLAB

code to calculate the thresholds. The first part of the code goes through all the frequencies, lighting one LED at a time. The others test on one or two frequencies. We adjusted the threshold until onle the LEDs that correspond to the test signal frequency are lit. For example, second part of the Matlab code should only lit the LED that corresponds to frequency 697Hz.

```
t = 0:1/2000:5;
x = chirp(t, 0, 5, 1000);
soundsc(x, 2000);
%%
fs = 8192;
f = 697; % This is the studied frequency
t = 0:1/fs:5;
x = \sin(2*pi*t*f);
soundsc(x, fs);
%%
f = 697; % This is the studied frequency
n = 1:8192;
x = \sin(2*pi*n*f / 8192);
soundsc(x);
%%
fs = 8192;
f1 = 770;
f2 = 1336;
t = 0:1/fs:5;
x = \sin(2*pi*t*f1) + \sin(2*pi*t*f2);
soundsc(x, fs);
%%
fs = 8192;
f1 = 852;
f2 = 1209;
t = 0:1/fs:5;
x = \sin(2*pi*t*f1) + \sin(2*pi*t*f2);
soundsc(x, fs);
```

# 4. RESULTS

Using both correlation detection and Goertzel-algorithm we calculated the values of the frequencies in the input signal. Then, we compared these values to a threshold. If the value is greater thn this threshold, a corresponding LED will light. Using the Matlab tests we were able to pinpoint a threshold which would be able to distinguish the different frequencies. With sampling frequency of 3000HZ and period of period 333s the threshold is 8 in both methods.

#### 5. CONCLUSIONS

With correct parameters the threshold can be found experimentally using input signal that contain only one frequency. Then only one LED should be lit. Experimenting with different frequencies will give the most accurate threshold.

At first, we tested correlation detection with sampling frequency of 44100Hz and period of 10s. These parameters worked with the first part of the Matlab code, resulting in threshold of 90. However, this threshold wouldn't work with the other Matlab tests. Then we changed the values to 3000HZ and 333s and all test worked with threshold of 8. Goertzel-algorithm passed the tests with same values, but we had to start indexing n from 1.

Using these methods we can detect the used signal and also the number pressed in a phone using DTMF signals.

### REFERENCES

[1] J. R. Smith, "Chapter 17: Dtmf tone decoding and telephone interface," http://www.globalspec.com/reference/24976/203279/chapter-17-dtmf-tone-decoding-and-telephone-interface, accessed: 2017-03-17.