

# Formula Sheet

for Final Exam (ch1-12)

Basic Stats (mth14100)

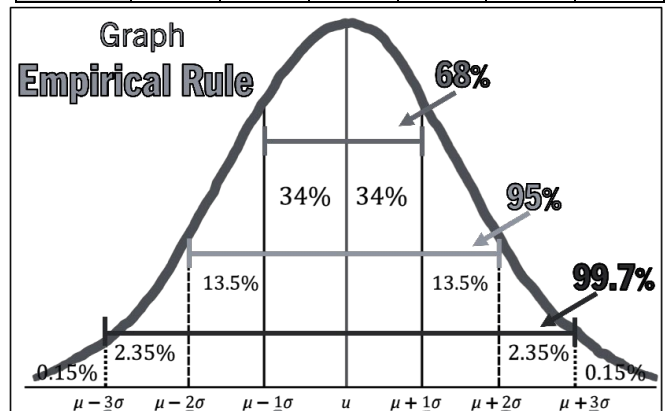
Let  $A$  and  $B$  be events. Then  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ ;  $P(A, \text{ given } B) = \frac{P(A \text{ and } B)}{P(B)}$ ;  $P(A) = 1 - P(A^c)$

If  $E$  and  $F$  are Independent, then  $P(E \text{ and } F) = P(E) * P(F)$ ;

If  $E$  and  $F$  are Mutually Exclusive (disjoint), then  $P(E \text{ and } F) = 0$

	Mean	Variance/ St. Dev.
Population	$\mu = \frac{\sum X}{N}$	$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$
Sample	$\bar{x} = \frac{\sum X}{n}$	$s^2 = \frac{\sum (X - \bar{x})^2}{n - 1}$
Probability Distribution	$\mu = \sum X * P(X)$	$\sigma^2 = \sum X^2 * P(X) - \mu^2$
Binomial Distribution	$\mu = np$	$\sigma = \sqrt{np(1 - p)}$
Uniform Distribution	$\mu = \frac{c + d}{2}$	$\sigma = \frac{d - c}{\sqrt{12}}$
Sample Mean Normal Distribution	$\mu_{\bar{x}} = \mu$	$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$
Sample Proportion Normal Distribution	$\mu_{\hat{p}} = p$	$\sigma_{\hat{p}} = \sqrt{\frac{p(1 - p)}{n}}$

$\beta$	0.80	0.85	0.90	0.95	0.98	0.99
$\alpha$	0.20	0.15	0.10	0.05	0.02	0.01
$Z_{\alpha/2}$	1.282	1.440	1.645	1.960	2.326	2.576



Population z-score:  $z = \frac{X - \mu}{\sigma}$ ; Sample z-score:  $z = \frac{X - \bar{x}}{s}$

Interquartile Formulas:  $IQR = Q_3 - Q_1$ ; Lower Fence =  $Q_1 - 1.5(IQR)$ ; Upper Fence =  $Q_3 + 1.5(IQR)$

Smallest Sample Size for CI: for Population Mean  $n = \left( Z_{\alpha/2} \frac{\sigma}{E} \right)^2$ ; for Population Proportion  $n = p(1 - p) \left( \frac{Z_{\alpha/2}}{E} \right)^2$

## Excel Functions:

Mean value,  $\bar{x}$  (or  $\mu$ ) = **AVERAGE**(cell: cell);

Mode value = **MODE.MULT**(cell: cell)

Minimum value = **MIN**(cell: cell); Median value = **MEDIAN**(cell: cell); Maximum value = **MAX**(cell: cell)

Standard Deviation and Variance:  $\sigma$  = **STDEV.P**(cell: cell),  $\sigma^2$  = **VAR.P**(cell: cell); and  $s$  = **STDEV.S**(cell: cell),  $s^2$  = **VAR.S**(cell: cell)

k% percentile,  $P_k$  = **PERCENTILE.INC**(cell: cell, k%);

Quartiles  $Q_1, Q_2, Q_3$ :  $Q_k$  = **QUARTILE.INC**(cell: cell, k)

Linear Regression:  $\hat{y} = a * x + b$ , where  $a$  = **SLOPE**(y\_data, x\_data),  $b$  = **INTERCEPT**(y\_data, x\_data)

The linear correlation coefficient is  $r$  = **CORREL**(y\_data, x\_data)

Binomial Distribution:  $P(X = k)$  = **BINOM.DIST**(k, n, p, 0),  $P(X \leq k)$  = **BINOM.DIST**(k, n, p, 1)

Uniform Distribution: uniformly distributed on  $[c, d]$ ;  $P(a \leq X \leq b) = \frac{b - a}{d - c}$

Normal Distribution:  $P(X \leq k)$  = **NORM.DIST**(k,  $\mu$ ,  $\sigma$ , 1)

Inverse Normal: Find  $k$  so that  $P(X \leq k) = prob$ . Then,  $k$  = **NORM.INV**(prob,  $\mu$ ,  $\sigma$ )

$\frac{\text{value}}{\text{value}}$  = value / value

$\text{value}^2$  = value ^ 2

$\sqrt{\text{value}}$  = **SQRT**(value)

	Confidence Interval	Hypothesis Test
Population Mean, $\mu$	<b>Z-Interval:</b> $\bar{x} \pm z_{\alpha/2} * \frac{\sigma}{\sqrt{n}}$ OR $(\bar{x} - \epsilon, \bar{x} + \epsilon)$ where $\epsilon$ = <b>CONFIDENCE.NORM</b> (1- $\beta$ , $\sigma$ , n)	<b>Z-Test:</b> If $\leq$ , use $p$ = <b>NORM.S.DIST</b> (z, 1) $z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$ If $>$ , use $p$ = 1 - <b>NORM.S.DIST</b> (z, 1) If $\neq$ , use $p$ = 2 * (1 - <b>NORM.S.DIST</b> (ABS(z), 1))
	<b>T-Interval:</b> $\bar{x} \pm t_{\alpha/2} * \frac{s}{\sqrt{n}}$ OR $(\bar{x} - \epsilon, \bar{x} + \epsilon)$ where $\epsilon$ = <b>CONFIDENCE.T</b> (1- $\beta$ , s, n)	<b>T-Test:</b> If $\leq$ , use $p$ = <b>T.DIST</b> (t, n - 1, 1) $t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$ If $>$ , use $p$ = <b>T.DIST.RT</b> (t, n - 1) If $\neq$ , use $p$ = <b>T.DIST.2T</b> (ABS(t), n - 1)
Population Proportion, prop	<b>Z-Interval:</b> $\hat{p} \pm z_{\alpha/2} * \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$ OR $(\hat{p} - \epsilon, \hat{p} + \epsilon)$ where $\epsilon$ = <b>CONFIDENCE.NORM</b> (1- $\beta$ , $\sqrt{\hat{p}(1 - \hat{p})}$ , n)	<b>Z-Test:</b> If $\leq$ , use $p$ = <b>NORM.S.DIST</b> (z, 1) $z = \frac{\hat{p} - p_0}{\sqrt{p_0(1 - p_0)/n}}$ If $>$ , use $p$ = 1 - <b>NORM.S.DIST</b> (z, 1) If $\neq$ , use $p$ = 2 * (1 - <b>NORM.S.DIST</b> (ABS(z), 1))