Naive Bayes (Iris)

October 30, 2023

0.0.1 MST IASD 2023-2024 (Département Génie Informatique)

Module "Apprentissage automatique" (M. AIT KBIR)

Bayes Naif appliqué la classification des Iris de Fisher

Dataset présenté en 1936 par Ronald Fisher

Fischer propose une méthode multiparamétrique pour distinguer trois classes de fleurs Iris (setosa, versicolor et virginica) à l'aide de quatre paramètres biométriques de détermination aisée (la longueur et la largeur des sépales ainsi que la longueur et la largeur des pétales, en cm), la base de données concerne 50 individus de chaque espèce.

Désactiver les commentaires pour voir les résultats intermédaires

```
[2]: import pandas as pd
import numpy as np
from scipy.stats import norm
from sklearn import metrics
import seaborn as sns
```

```
[3]: dataSet = sns.load_dataset("iris")
dataSet
```

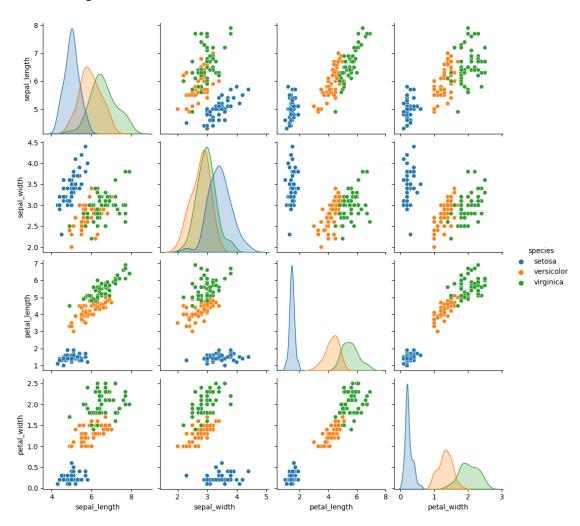
| [3]: | sepal_length | sepal_width | petal_length | $petal_width$ | species |
|------|--------------|-------------|--------------|----------------|-----------|
| 0 | 5.1 | 3.5 | 1.4 | 0.2 | setosa |
| 1 | 4.9 | 3.0 | 1.4 | 0.2 | setosa |
| 2 | 4.7 | 3.2 | 1.3 | 0.2 | setosa |
| 3 | 4.6 | 3.1 | 1.5 | 0.2 | setosa |
| 4 | 5.0 | 3.6 | 1.4 | 0.2 | setosa |
| | ••• | ••• | ••• | | |
| 145 | 6.7 | 3.0 | 5.2 | 2.3 | virginica |
| 146 | 6.3 | 2.5 | 5.0 | 1.9 | virginica |
| 147 | 6.5 | 3.0 | 5.2 | 2.0 | virginica |
| 148 | 6.2 | 3.4 | 5.4 | 2.3 | virginica |
| 149 | 5.9 | 3.0 | 5.1 | 1.8 | virginica |

[150 rows x 5 columns]

0.0.2 Charger le fichier csv dans un objet du module pandas : DataFrame

```
[4]: sns.pairplot(dataSet, hue="species")
```

[4]: <seaborn.axisgrid.PairGrid at 0x2199c5e1c10>



0.0.3 Créer une Base des exemples tests

```
[5]: nbreTest = 30; # 10 exemples par classe
# Elaborer les listes des indices des exemples utilisés dans
| "l'apprentissage(trainingInd) et dans le test(testInd)

trainingInd = list(range(len(dataSet))); testInd=[]

for i in range(nbreTest):
    randIndex = int(np.random.uniform(0,len(trainingInd)))
    testInd.append(trainingInd[randIndex])
    del(trainingInd[randIndex])
```

```
[5]:
                         sepal_width petal_length petal_width
           sepal_length
                                                                         species
     48
                                  3.7
                    5.3
                                                  1.5
                                                                0.2
                                                                          setosa
     23
                    5.1
                                   3.3
                                                  1.7
                                                                0.5
                                                                          setosa
                                                                2.2
     104
                    6.5
                                   3.0
                                                  5.8
                                                                      virginica
     121
                    5.6
                                  2.8
                                                  4.9
                                                                2.0
                                                                      virginica
     42
                    4.4
                                   3.2
                                                  1.3
                                                                0.2
                                                                          setosa
                                                  3.9
     82
                    5.8
                                  2.7
                                                                1.2 versicolor
     148
                    6.2
                                   3.4
                                                  5.4
                                                                2.3
                                                                      virginica
     45
                    4.8
                                  3.0
                                                  1.4
                                                                0.3
                                                                          setosa
                                                  4.2
     61
                    5.9
                                   3.0
                                                                1.5 versicolor
     53
                    5.5
                                  2.3
                                                  4.0
                                                                1.3 versicolor
     108
                                                  5.8
                    6.7
                                  2.5
                                                                1.8
                                                                      virginica
     72
                    6.3
                                   2.5
                                                  4.9
                                                                1.5 versicolor
     128
                    6.4
                                  2.8
                                                  5.6
                                                                2.1
                                                                      virginica
                    6.5
     116
                                   3.0
                                                  5.5
                                                                1.8
                                                                      virginica
     24
                    4.8
                                  3.4
                                                  1.9
                                                                0.2
                                                                          setosa
     79
                    5.7
                                                                1.0 versicolor
                                   2.6
                                                  3.5
     49
                                   3.3
                    5.0
                                                  1.4
                                                                0.2
                                                                          setosa
     91
                    6.1
                                   3.0
                                                  4.6
                                                                1.4 versicolor
                                                                      virginica
     110
                    6.5
                                   3.2
                                                  5.1
                                                                2.0
     129
                    7.2
                                   3.0
                                                  5.8
                                                                1.6
                                                                      virginica
     60
                    5.0
                                  2.0
                                                  3.5
                                                                1.0 versicolor
     139
                    6.9
                                  3.1
                                                  5.4
                                                                2.1
                                                                      virginica
     102
                    7.1
                                  3.0
                                                  5.9
                                                                2.1
                                                                      virginica
     27
                    5.2
                                  3.5
                                                                0.2
                                                  1.5
                                                                          setosa
                    5.4
                                  3.7
                                                  1.5
                                                                0.2
     10
                                                                          setosa
     133
                    6.3
                                   2.8
                                                  5.1
                                                                1.5
                                                                      virginica
     68
                    6.2
                                  2.2
                                                  4.5
                                                                1.5 versicolor
     31
                    5.4
                                   3.4
                                                  1.5
                                                                0.4
                                                                          setosa
     119
                    6.0
                                  2.2
                                                  5.0
                                                                1.5
                                                                      virginica
     111
                    6.4
                                  2.7
                                                  5.3
                                                                1.9
                                                                      virginica
```

0.0.4 Calcul des moyennes et des variances

```
[6]: mean_dataSet = dataSet.groupby('species').mean()
std_dataSet = dataSet.groupby('species').std()
print(mean_dataSet)
print(std_dataSet)
```

sepal_length sepal_width petal_length petal_width species

```
4.997561
                             3.436585
                                            1.448780
                                                         0.241463
setosa
                5.959524
                             2.814286
                                            4.283333
                                                         1.330952
versicolor
virginica
                6.624324
                             3.005405
                                            5.594595
                                                         2.064865
            sepal_length sepal_width petal_length petal_width
species
setosa
                0.360200
                             0.406667
                                            0.171933
                                                         0.104823
versicolor
                0.533310
                             0.287607
                                            0.464819
                                                         0.196913
                                            0.607795
                                                         0.272046
virginica
                0.694584
                             0.325701
```

0.0.5 Calcul des probabilités

```
[7]: dataSet['species'].value_counts()
[7]: versicolor
                  42
    setosa
                  41
                  37
    virginica
    Name: species, dtype: int64
[8]: # Probabilités à priori
    nbresParClass = dataSet['species'].value_counts()
    probApriori = {label: float(nbresParClass[label])/dataSet.shape[0] for label in_

¬dataSet['species'].unique()}
    probApriori
[8]: {'setosa': 0.341666666666667,
     'versicolor': 0.35,
     [9]: # Des fonctions
    # P(xi/wj)
    def p xi wj(xi, wj, attrib):
        return norm.pdf(xi, loc = mean_dataSet.loc[wj, attrib], scale = std_dataSet.
     ⇔loc[wj, attrib])
    \# P(X/wj) * P(wj)
    def p_X_wj(exemple, wj):
        prob = probApriori[wj]
        for attrib, valeur in exemple.items():
            prob*=p_xi_wj(valeur, wj, attrib)
        return prob
```

0.0.6 Test

```
[10]: labels = dataSet['species'].unique()

# Extraire les colonnes sans classes
data = testSet.iloc[:,:-1]
```

```
# Ajouter des colonnes
      testSet['classe calculée'] = np.nan
      for i in range(len(labels)):
          testSet[labels[i]]
                                   = np.nan
      # Faire pour chaque exemple test
      for index, row in data.iterrows():
          probCond = [p_X_wj(row, label) for label in labels]
          testSet.loc[index, 'classe calculée'] = labels[probCond.
       →index(max(probCond))]
          for i in range(len(labels)):
               testSet.loc[index, labels[i]] = probCond[i]/sum(probCond)
      testSet
[10]:
           sepal_length sepal_width petal_length petal_width
                                                                        species \
                     5.3
                                   3.7
                                                 1.5
                                                               0.2
                                                                         setosa
      23
                     5.1
                                   3.3
                                                 1.7
                                                               0.5
                                                                         setosa
                     6.5
                                                               2.2
      104
                                   3.0
                                                 5.8
                                                                     virginica
      121
                     5.6
                                   2.8
                                                 4.9
                                                               2.0
                                                                     virginica
                     4.4
      42
                                   3.2
                                                 1.3
                                                               0.2
                                                                         setosa
      82
                     5.8
                                   2.7
                                                 3.9
                                                               1.2 versicolor
      148
                     6.2
                                   3.4
                                                 5.4
                                                               2.3
                                                                     virginica
      45
                     4.8
                                   3.0
                                                 1.4
                                                               0.3
                                                                         setosa
                     5.9
                                   3.0
                                                 4.2
                                                               1.5 versicolor
      61
                                   2.3
                                                 4.0
                                                               1.3 versicolor
      53
                     5.5
      108
                     6.7
                                   2.5
                                                 5.8
                                                               1.8
                                                                     virginica
      72
                     6.3
                                   2.5
                                                 4.9
                                                               1.5 versicolor
      128
                     6.4
                                  2.8
                                                 5.6
                                                               2.1
                                                                     virginica
      116
                     6.5
                                   3.0
                                                 5.5
                                                               1.8
                                                                     virginica
      24
                     4.8
                                   3.4
                                                 1.9
                                                               0.2
                                                                         setosa
      79
                     5.7
                                   2.6
                                                 3.5
                                                               1.0 versicolor
      49
                     5.0
                                   3.3
                                                 1.4
                                                               0.2
                                                                         setosa
      91
                     6.1
                                   3.0
                                                 4.6
                                                               1.4 versicolor
                                   3.2
      110
                     6.5
                                                 5.1
                                                               2.0
                                                                     virginica
      129
                     7.2
                                   3.0
                                                 5.8
                                                               1.6
                                                                     virginica
      60
                     5.0
                                   2.0
                                                 3.5
                                                               1.0 versicolor
                     6.9
      139
                                   3.1
                                                 5.4
                                                               2.1
                                                                     virginica
      102
                     7.1
                                   3.0
                                                 5.9
                                                               2.1
                                                                     virginica
      27
                     5.2
                                   3.5
                                                 1.5
                                                               0.2
                                                                         setosa
      10
                     5.4
                                   3.7
                                                 1.5
                                                               0.2
                                                                         setosa
      133
                     6.3
                                   2.8
                                                 5.1
                                                               1.5
                                                                     virginica
      68
                     6.2
                                  2.2
                                                 4.5
                                                               1.5 versicolor
      31
                     5.4
                                   3.4
                                                 1.5
                                                               0.4
                                                                         setosa
```

classe calculée setosa versicolor virginica

2.2

2.7

119

111

6.0

6.4

5.0

5.3

1.5

1.9

virginica

virginica

```
1.000000e+00
                                         1.744349e-18 1.843061e-23
                   setosa
      23
                            1.000000e+00
                                          2.258513e-11
                                                       2.024727e-17
                   setosa
      104
                virginica
                          2.337726e-218
                                         5.141155e-07
                                                       9.999995e-01
      121
                virginica
                          1.959558e-148
                                         2.174954e-02
                                                       9.782505e-01
      42
                  setosa
                           1.000000e+00
                                         6.263519e-19
                                                       2.099499e-24
      82
              versicolor
                           8.476400e-64 9.999726e-01
                                                       2.737453e-05
      148
               virginica 8.521716e-200
                                         4.055125e-07
                                                       9.999996e-01
      45
                  setosa
                            1.000000e+00
                                         1.822398e-16
                                                       1.680990e-22
              versicolor
                           2.866325e-88 9.970978e-01
                                                       2.902229e-03
      61
              versicolor
      53
                           3.826510e-71
                                         9.999541e-01
                                                       4.594494e-05
      108
               virginica 7.367246e-192
                                         1.033718e-03
                                                       9.989663e-01
      72
              versicolor
                                                       3.996515e-02
                          6.309595e-122 9.600349e-01
      128
               virginica 4.317706e-198 2.455291e-05
                                                       9.999754e-01
      116
               virginica
                          6.587197e-172 4.606437e-03
                                                       9.953936e-01
      24
                  setosa
                            1.000000e+00
                                         1.208785e-14
                                                       2.272228e-20
      79
              versicolor
                           1.242807e-42 9.999980e-01
                                                       1.969915e-06
      49
                   setosa
                           1.000000e+00
                                         3.310396e-18
                                                       9.302500e-24
      91
              versicolor
                          1.554265e-101
                                         9.944058e-01
                                                       5.594171e-03
      110
               virginica
                          3.474417e-162
                                        8.515264e-04
                                                       9.991485e-01
      129
               virginica
                          1.208998e-182
                                         2.019375e-03
                                                       9.979806e-01
      60
              versicolor
                           2.517430e-41 9.999989e-01
                                                       1.072257e-06
      139
               virginica 1.325593e-188
                                         1.270737e-05
                                                       9.999873e-01
      102
               virginica
                          7.965538e-221
                                         4.153847e-07
                                                       9.999996e-01
      27
                  setosa
                            1.000000e+00
                                        6.137836e-18
                                                       2.873093e-23
      10
                   setosa
                            1.000000e+00
                                         2.835812e-18
                                                       3.149385e-23
      133
              versicolor 9.221692e-132 8.562367e-01 1.437633e-01
      68
              versicolor 6.865847e-103 9.948745e-01
                                                       5.125542e-03
      31
                  setosa
                           1.000000e+00 1.969289e-14 4.090427e-20
      119
              versicolor 5.474972e-126
                                         9.664764e-01
                                                       3.352364e-02
      111
               virginica 1.661143e-166 6.132511e-03 9.938675e-01
[11]: # Taux de la classification correcte
      metrics.accuracy_score(testSet['species'], testSet['classe calculée'])
[11]: 0.9333333333333333
[12]: metrics.confusion_matrix(testSet['species'], testSet['classe calculée'])
[12]: array([[ 9, 0, 0],
             [ 0,
                      0],
             [ 0, 2, 11]], dtype=int64)
```

48