

1. Pseudo Code

My pseudo code is the same as the professor's pseudo code, I just followed what the lecture told and tried to implement it.

```

struct node
{
    int level;           // the node's level in the tree
    ordered_set path;
    number bound;
};

void travel2 (int n,
              const number W[] [],
              ordered_set& opttour,
              number& minlength)
{
    priority_queue_of_node PQ;
    node u, v;

    initialize(PQ);           // Initialize PQ to be empty.
    v.level = 0;
    v.path = [1];           // Make first vertex the
    v.bound = bound(v);      // starting one.
    minlength = ∞;
    insert(PQ, v);
    while (!empty(PQ)){
        remove(PQ, v);       // Remove node with best bound.
        if (v.bound < minlength){
            u.level = v.level + 1;           // Set u to a child of v.
            for (all i such that 2 ≤ i ≤ n && i is not in v.path){
                u.path = v.path;
                put i at the end of u.path;
                if (u.level == n - 2){       // Check if next vertex
                    put index of only vertex // completes a tour.
                    not in u.path at the end of u.path;
                    put 1 at the end of u.path; // Make first vertex last one.
                    if (length(u) < minlength){ // Function length computes the
                        minlength = length(u); // length of the tour.
                        opttour = u.path;
                    }
                }
            }
            else{
                u.bound = bound(u);
                if (u.bound < minlength)
                    insert(PQ, u);
            }
        }
    }
}

```

2. Flow chart

- (1) Initialize an array for the tour, with all of the data being 0;
- (2) Initialize a visited array to store the visited, array[i] 's value will be the position in the tour.
- (3) Calculate the bound for the root
- (4) Push the root into the priority queue
- (5) Starting from the priority queue, visit all nodes using the adjacency matrix
- (6) Calculate the bound for each node we visit
- (7) Starting with the node with the smallest bound, we go deeper and repetitively calculate the bound.
- (8) Update the Min_path_cost when hitting a leaf
- (9) If another branch has higher bound than current Min_path_cost, we prune it
- (10) Repeat the process until obtaining the best tour.

3. Time complexity analysis

Suppose we have N cities left unvisited (including the root), we have to create all possible extensions for the unvisited cities which are $N-1$ (excluding the root).

Following this thought, the complexity for generating the permutation is

$$O((n-1)!),$$

which is equal to

$$O(2^{(n-1)})$$

However, for each node, we have to calculate the cost, following the method below.

```
int calcbound(node n){
    int canvisit[31];
    for(int i = 0; i<31; i++)
        canvisit[i]=1;
    vector<int>::iterator end = n.path.end();
    for(vector<int>::iterator it = n.path.begin(); it != end; ++it){
        canvisit[*it-1] = 0;
    }
    canvisit[nd.label-1] = 1;
    int min = INF;
    int bound = 0;
    for(int i = 0; i<N; i++){
        min = INF
        if(canvisit[i]==0)continue;
        for(int j = 0; j<N; j++){
            if((canvisit[j]==0 || j ==nd.label-1) && j!=1 && nd.label != 1){}
            else if(w[i][j]<min)min = w[i][j];
        }
        if(min!=INF){
            bound += min;
        }
    }
    return bound;
}
```

Since there is a double for loop inside the function, which iterates through the N cities. This generates a time complexity of

$$O(n^2)$$

So, combining the above, the total time complexity should be

$$O(n^2 \times 2^n)$$