```
TUTORIAL-4
      T(n)= 3T(1/2) + n2
砂)
       T(n) = aT(Nb) +f(n)
             a > 1; 6 > 1
      on company, a= 1, b= 2, f(n)=n2
      c= logs = log2 = 1.584
          nc = n.584 < n2
         -: +(n) > n°
         -. + (n) = 0 (n2)
    T(n) = T(n/2) + 2"
        6=2
      f(n) = 2^n
       c = logba = logz = 0.
        Nc = n° = 1
        4 (NJ> Nc
        T(n) = (2^)
    T(N) = 16T (NA) + N
        a=16, b=4, f(m)=n
      (= log + 16 = 2
         nc = n2
         f(n) ene
         :. + (n)= O(H)
Q.7) T(n) = 2T(N2) + n/log n
      a=1, b= 1, f(w)= n/log n
       C= Log2 2 = 1
       n = n = n
       n en
       Han cne
       : T(")= 0(")
```

Q2) 
$$T(n) = 4T(n/2) + n^2$$
 $a > 1, b > 1$ 
 $a = 4, b = 2, f(n) = n^2$ 
 $c = log_2 4 = 2$ 
 $n' = n^2 = f(n) = n^2$ 
 $T(n) = 2^n + (n/2) + n^n$ 
 $a = 2^n, b = 2, f(n) = n^n$ 
 $c = log_2 a = log_2 2^n = n$ 
 $r(n) = n^n$ 
 $f(n) > n^n$ 

```
T(n)= 0.5 T(1/2) + 1/2
                                                  T(M)= 16T (MA) + M!
09)
    a=0.5, b=2
                                                     a=16, b=4, f(n)=n!
      a> 1 but here a is 05,
                                                     c= dog 6 a= log 4 16 = 2
    so we cannot apply
                                                         nc= n2
        Marter's theorem.
                                                        As ni > n2
                                                         11/1 = (N) = (N!)
                                              T(n) 2 sqrt (n) + (n/2) + log n
     +(n)= 4+ (n/2)+ lag n
211)
                                                  a= JM, b=2
      a=4, b=2, +(n)=logn
                                              c= logba = log_ In = 1 logzh
     c= log, 4= .2
                                                  1 lugan < log (m)
        n = n2
                                                 : +(n)>nc
        timen
                                                    :- T(m)= @( Log n)
        : T(n) = D(n2)
                                               +(n)= 3+ (n/3) + 5n
                                        0:14)
Q13) +(n)= 3+(n/2) + n
                                                  a=3, b=3
                                                C= logo = log2 3 = 1.
        a= 3, b= 2, f(n)= n
    (= logba = lug2) = 1.5849
                                                    Nc= N, = N
        nc = n1.5489
                                                     tim che
                                                    2.T(n)= 0(n),
         f(n) < n°
      - T(n) = @(n"5849)
                                              +(n)=3mt(n/4) + nlog n
                                       0,(6)
    T(n)= 4T(n/2)+n
Q.15)
                                                 a= 3, b= 4, f(m= nlogn
        a = 4, b=2
                                                 (= logba = log = 3 = 0.792
     c= lugo a= 2
                                                      N = No. 79 2
         ne = ne
                                                        f(n) Zhlogn > ne
         fin) en
                                                         :. T(m= 0(nlogn)
      :. T(n)= O(n2)
                                             T(n)= 16T(n/3) + n2 log n
                                      Q. [B)
     T(n)= 3T(n/3)+ 11/2
                                                 a = 6, b= 1, f(n) = n2 logn
017)
        a=3, b=3
                                                C= log3 6 = 1.6309
        c= log 6 = 1
                                                   n = n 1.6309
         f(n1 = n/2
                                                     f(n) > nc
                                                 - :. T(n)= O(n2hgn)
          f(n) Lnc
          =+(n)= 0(n)
                                              trouble.
```

2:

$$\frac{Q_1(9)}{a=4}$$
  $+ \frac{n}{\log n}$   $+ \frac{n}{\log n}$ 

$$\frac{n^{2}}{\log n} \leq n^{2}$$

$$\frac{n}{\log n} \leq n^{2}$$

$$\therefore T(m = O(n^{2})$$

$$Q.21)$$
 + (n) = 7+ (N2) + N<sup>2</sup>  
 $a=7$ ,  $b=3$ ,  $f(n)=n^2$ 

$$C = \log_3 7 = 1.7712$$

$$N^2 = N^{1.7712}$$

$$f(n) > n^2$$

$$f(n) = O(n^2)$$

$$e = 2$$
 $y' = y^2$ 
 $+(y) > y'$ 
 $-: +(y) = 0(y^2 | y')$ 

$$\frac{q.22}{a=1, b=2}$$
 + (n)=  $\frac{q.22}{a=1, b=2}$  , + (n)=  $\frac{q.22}{a=1, b=2}$ 

$$C_2 \log_2 1 = 0$$
 $n' = n'' = 1$ 
 $f(n) > n^c$ 
 $f(n) = O(n (2 - (os n)))$ 

Alany