

...Question 3 continued

Useful equation:

$$\Delta T_i = \frac{\frac{1}{U_i}}{\frac{1}{U_1} + \frac{1}{U_2}} (T_s - T_2)$$

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#### QUESTION 4 DRYING

Green tea extract is spray dried to produce instant tea. The tea extract is sprayed as a fine mist into the top of the spray dryer together with hot air at 90°C dry bulb temperature and 32°C wet bulb temperature. Assume all drying is by convection only.

The flow rate of tea extract into the dryer is 500 kg h<sup>-1</sup> and enters the dryer with a moisture content of 70% water. The instant tea powder exiting has a moisture content of 3.7% water, dry solid density of 650 kg m<sup>-3</sup> and mean particle size of 300 µm. The critical moisture content for dried green tea extract is 1.5 kg water/kg dry solids.

- (a) Determine the time required to dry green tea extract to a moisture content of 1.5 kg water/kg dry solids. The mass transfer coefficient  $k_H$ , during the constant rate drying period, is 9.25 kg m<sup>-2</sup> s<sup>-1</sup>.

[6 marks]

- (b) Estimate the time required in the spray dryer to dry the green tea extract to a final  $m$ , moisture content of 3.7% water if capillary drying dominates in the falling rate period. The equilibrium moisture content for the dried green tea extract powder is 0.002 kg water/kg dry solids.

[Note: If you did not find  $R_c$  in part (a) use 0.2 kg m<sup>-2</sup>s<sup>-1</sup>.]

[4 marks]

Question 4 continued over...

... Question 4 continued

- (c) Calculate the flow rate of air required in the dryer to dry  $500 \text{ kg h}^{-1}$  green tea extract solution to the final moisture content of 3.7% water if the exit air has a humidity of  $0.015 \text{ kg kg}^{-1}$ .

**[4 marks]**

- (d) Based on a flow rate of  $500 \text{ kg h}^{-1}$ , how much water is evaporated in the dryer ( $\text{kg s}^{-1}$ )?

**[1 mark]**

- (e) What is the exit temperature of the air leaving the dryer?

**[1 mark]**

- (f) If the dryer air is recycled back into the dryer, what impact will this have on the overall drying process?

[Note: No calculations required]

**[2 marks]**

- (g) Recommend operating conditions or procedures to ensure the required drying rate is maintained with recycling of dryer air.

**[2 marks]**

**[Total: 20 marks]**

*A high temperature psychrometric chart is provided on page 14, if used, please attach it to your exam script.*

*Question 4 continued over...*

Dry 2014

$$\theta_{air} = 90^{\circ}\text{C}$$

$$\theta_{wb} = 32^{\circ}\text{C}$$

$$M_i = 500 \text{ kg h}^{-1} = 0.139 \text{ kg/s}$$

$$\text{moisture content}_i = 70\%$$

$$X_i = \frac{70}{30} = 2.3 \text{ kg/kg}$$

$$\text{moisture content}_d = 3.7\%$$

$$X_d = \frac{3.7}{96.3} = 0.038 \text{ kg/kg}$$

$$X_c = 1.2 \text{ kg/kg}$$

$$\rho_s = 650 \text{ kg m}^{-3}$$

$$\text{diameter} = 300 \mu\text{m}$$

$$(a) \quad R_c = \frac{k_H A (H_s - H_{air})}{A}$$

$$k_H = 9.25 \text{ kg m}^{-2} \text{ s}^{-1}$$

$$H_s = 0.030$$

$$H_{air} = 0.0075$$

$$R_c = 9.25 (0.03 - 0.0075) = 0.208 \text{ kg m}^{-2} \text{ s}^{-1}$$

$t_d$  to  $1.5 \text{ kg/kg}$ . constant rate

$$t_d = \frac{r \rho_s (X_i - X_2)}{3 R_c}$$

$$= \frac{150 \times 10^{-6} \times 650}{3 \times 0.208} (2.3 - 1.5) = 0.125 \text{ s}$$

(\*) air recycled back into dryer

- humidity of air  $\uparrow$

- rate of drying  $\downarrow$

- drying time ~~there~~ will increase to achieve same final moisture content

- air temperature after recycling ~~back~~  $\downarrow$

(g) pass recycle air over heater to increase temperature  
 purge some of the recycled moist air  
 introduce make up air of low humidity to keep  
 humidity  $\downarrow$

(d) constant rate + falling rate drying.

$$t_d = \frac{r_{ps} (X_1 - X_c)}{3 R_c} + \frac{r_{ps} (X_c - X^*)}{3 R_c} \ln \left[ \frac{X_c - X^*}{X_2 - X^*} \right]$$

$$= \frac{150 \times 10^{-6} \cdot 650 (2.3 - 1.5)}{3 \times 0.208}$$

$$+ \frac{150 \times 10^{-6} \cdot 650 (1.5 - 0.002)}{3 \times 0.208} \ln \left[ \frac{1.5 - 0.002}{0.038 - 0.002} \right]$$

$$= 0.125 + 0.8726$$

$$\approx 0.9975 = 1 \text{ s.}$$

(e)  $M_i \frac{1}{1+X_i} = M_o \frac{1}{1+X_o}$

$$\text{Mass } 0.139 \times \frac{1}{1+2.3} = M_o \frac{1}{1+0.038}$$

$$M_o = 0.044 \text{ kg/s. } 158.4 \text{ g/hr}$$

$$H_i = H_{Ei} = 0.0075$$

$$H_o = 0.015 \text{ kg/kg.}$$

$$M_i \frac{X_i}{1+X_i} + (F_{H_2O}) H_{Ei} = M_o \frac{X_o}{1+X_o} + (F_{H_2O}) H_o$$

$$M_i \frac{X_i}{1+X_i} - M_o \frac{X_o}{1+X_o} = (F_{H_2O}) (H_o - H_{Ei})$$

$$\left[ 0.139 \frac{23}{1+2.3} - 0.044 \frac{0.038}{1+0.038} \right] = (F_{\text{air}}) (0.015 - 0.0075)$$

$$0.0953 = F (0.0075)$$

$$F = 12.69 \text{ kg/s.}$$

$$12.7 \text{ kg/s.}$$

$$45,720 \text{ kg/hr.}$$

~~to~~

$$(d) \text{ mass } H_2O \text{ evaporated} = 0.0953 \text{ kg/s.}$$

$$343 \text{ kg/hr.}$$

$$(e) \text{ exit air temperature} = 70^\circ\text{C}$$

# PSYCHROMETRIC CHART

HIGH TEMPERATURES

1013.25 MILLIBARS

