

(1) It is easiest to carry out calculations for a nominal 1 m tube length and then to scale the results.

$$L_{sc} = 0.42 \text{ m}$$

$$d = 0.0004 \text{ m}$$

$$k = 200 \text{ W/mK}$$

$$h_2 = 23 \text{ W/m}^2\text{K}$$

$$L_p = 1 \text{ m}$$

$$N_s = 1/0.00635 = 157 \quad x = 0.00175 \text{ m}$$

$$L_y = 0.85 \text{ m}$$

$$b = 0.053 \text{ m}$$

$$h_1 = 525 \text{ W/m}^2\text{K}$$

$$N_p = 120$$

$$d_o = 0.0215 \text{ m}$$

$$\alpha = 0.00175 \text{ m}$$

$$A_p = \pi \times 0.0215 \times 120 \times (1 - 157 \times 0.0004) = 7.60 \text{ m}^2$$

$$A_s = 2 \times 157 \times (0.85 \times 0.42 - 120 \frac{\pi}{4} \times 0.0215^2) = 98.4 \text{ m}^2$$

$$\text{Triangular pitch } H = (0.95 \times 0.053 - 0.0215)/2 \\ = 0.0144 \text{ m}$$

$$1 + 2H/d_o = 1 + 2 \times 0.0144/0.0215 = 2.34$$

$$H \sqrt{2h_2/dk} = 0.0144 (2 \times 23 / 0.0004 / 200)^{0.5} = 0.345$$

$$\text{From Fig 2 } \eta_f = 0.96$$

$$A_s = 120 \pi 0.018 = 6.79 \text{ m}^2$$

$$\frac{1}{UA} = \frac{1}{525 \times 6.79} + \frac{0.00175}{200 \times 6.79} + \frac{1}{23(7.6 + 0.96 \times 98.4)} \\ = 2.805 \times 10^{-4} + 1.2 \times 10^{-6} + 4.07 \times 10^{-4} \\ = 6.88 \times 10^{-4} \text{ K/W}$$

$$UA = 1453 \text{ W/K}$$

$$\text{Now air flow} = (0.85 \times 1 \times 3.1) = 2.635 \text{ m}^3/\text{s}$$

$$\text{At } 23^\circ\text{C } \rho = 1.18 \text{ kg/m}^3 \text{ (approx)}$$

$$m = 2.635 \times 1.18 = 3.11 \text{ kg/s}$$

$$\phi = 1453 \Delta \theta_m = 3.11 \times 1010 \times (\theta_{off} - 23)$$

$$\Delta \theta_m = [15 - (38 - \theta_{off})] / \ln [15 / (38 - \theta_{off})]$$

Simultaneous solution is required. $\Delta \theta_m$ must be less than 15 K so $\phi < 1453 \times 15 = 21795 \text{ W}$, Hence $\theta_{off} < 29.9^\circ\text{C}$

Try $\phi = 19000 \text{ W} \Rightarrow \Delta \theta_m = 13.1 \text{ K}$ and $\theta_{off} = 29.0^\circ\text{C}$