

...Question 3 continued

Useful equation:

$$\Delta T_i = \frac{\frac{1}{U_i}}{\frac{1}{U_1} + \frac{1}{U_2}} (T_s - T_2)$$

QUESTION 4 DRYING

Green tea extract is spray dried to produce instant tea. The tea extract is sprayed as a fine mist into the top of the spray dryer together with hot air at 90°C dry bulb temperature and 32°C wet bulb temperature. Assume all drying is by convection only.

The flow rate of tea extract into the dryer is 500 kg h⁻¹ and enters the dryer with a moisture content of 70% water. The instant tea powder exiting has a moisture content of 3.7% water, dry solid density of 650 kg m⁻³ and mean particle size of 300 µm. The critical moisture content for dried green tea extract is 1.5 kg water/kg dry solids.

- (a) Determine the time required to dry green tea extract to a moisture content of 1.5 kg water/kg dry solids. The mass transfer coefficient k_H , during the constant rate drying period, is 9.25 kg m⁻² s⁻¹.

[6 marks]

- (b) Estimate the time required in the spray dryer to dry the green tea extract to a final moisture content of 3.7% water if capillary drying dominates in the falling rate period. The equilibrium moisture content for the dried green tea extract powder is 0.002 kg water/kg dry solids.

[Note: If you did not find R_c in part (a) use 0.2 kg m⁻²s⁻¹.]

[4 marks]

Question 4 continued over...

... Question 4 continued

- (c) Calculate the flow rate of air required in the dryer to dry 500 kg h⁻¹ green tea extract solution to the final moisture content of 3.7% water if the exit air has a humidity of 0.015 kg kg⁻¹.

[4 marks]

- (d) Based on a flow rate of 500 kg h⁻¹, how much water is evaporated in the dryer (kg s⁻¹)?

[1 mark]

- (e) What is the exit temperature of the air leaving the dryer?

[1 mark]

- (f) If the dryer air is recycled back into the dryer, what impact will this have on the overall drying process?

[Note: No calculations required]

[2 marks]

- (g) Recommend operating conditions or procedures to ensure the required drying rate is maintained with recycling of dryer air.

[2 marks]

[Total: 20 marks]

A high temperature psychrometric chart is provided on page 14, if used, please attach it to your exam script.

Question 4 continued over...

Drying 2014

$$\theta_{air} = 90^\circ C$$

$$\theta_{wb} = 32^\circ C$$

$$m_i = 500 \text{ kg/h}^{-1} = 0.139 \text{ kg/s}$$

$$\text{moisture content}_i = 70\% \quad X_i = \frac{70}{100} = 2.3 \text{ kg/kg}$$

$$\text{moisture content}_o = 3.7\% \quad X_o = \frac{3.7}{96.3} = 0.038 \text{ kg/kg}$$

$$X_c = 1.2 \text{ kg/kg}$$

$$\rho_s = 650 \text{ kg/m}^3$$

$$\text{diameter} = 300 \mu\text{m}$$

$$(a) R_c = \frac{k_H A (H_s - H_{air})}{A} \quad k_H = 9.25 \text{ kg m}^{-2} \text{s}^{-1}$$

$$H_s = 0.030$$

$$H_{air} = 0.0075$$

$$R_c = 9.25 (0.03 - 0.0075) = 0.208 \text{ kg m}^{-2} \text{s}^{-1}$$

t_d to 1.5 kg/kg. constant rate

$$t_d = \frac{r \rho_s (X_1 - X_2)}{3R_c}$$

$$= \frac{150 \times 10^{-6} \times 650}{3 \times 0.208} (2.3 - 1.5) = 0.125 \text{ s}$$

(f) air recycled back into dryer

- humidity of air ↑

- rate of drying ↓

- drying time / time will increase to achieve same final moisture content

- air temperature after recycling back → ↓

(g) pass recycle air over heater to increase temperature
 purge some of the recycled moist air
 introduce make up air of low humidity to keep
 humidity ↓

(h) constant rate + falling rate drying

$$t_d = \frac{r_{ps} (X_i - X_e)}{3 R_c} + \frac{r_{ps} (X_e - X^*)}{3 R_c} \ln \left[\frac{\frac{X_e - X^*}{X_2 - X^*}}{\frac{X_c - X^*}{X_2 - X^*}} \right]$$

$$= \frac{150 \times 10^{-6} \times 650 (2.3 - 1.5)}{3 \times 0.208}$$

$$+ \frac{150 \times 10^{-6} \times 650 (1.5 - 0.002)}{3 \times 0.208} \ln \left[\frac{1.5 - 0.002}{0.038 - 0.002} \right]$$

$$= 0.125 + 0.00268 + 0.8726$$

$$= 0.875 \text{ s. approx. } 0.9975 = 1 \text{ s.}$$

$$(e) M_i \frac{1}{1+x_i} = M_o \frac{1}{1+x_o}$$

$$\text{Mass } 0.139 \times \frac{1}{1+2.3} = M_o \frac{1}{1+0.038}$$

$$M_o = 0.044 \text{ kg/s. } 158.4 \text{ kg/hr}$$

$$H_o = H_{Eo} = 0.0075$$

$$H_o = 0.015 \text{ kJ/kg}$$

$$M_i \frac{x_c}{1+x_i} + (F_{\text{make}}) H_{Ei} = M_o \frac{x_o}{1+x_o} + (F_{\text{make}}) H_o$$

$$M_i \frac{x_c}{1+x_i} - M_o \frac{x_o}{1+x_o} = (F_{\text{make}}) (H_o - H'_{Eo})$$

$$\left[0.139 \frac{23}{1+2.3} - 0.044 \frac{0.038}{1+0.038} \right] = (\cancel{F}) (0.015 - 0.0075)$$

$$0.0953 = F (0.0075)$$

$$F = 12.69 \text{ kg/s.}$$

$$12.7 \text{ kg/s.}$$

$$45,720 \text{ kg/hr.}$$

~~10~~

(d) mass H_2O exported = 0.0953 kg/s.
 343 kg/hr.

(e) exit air temperature = $70^\circ C$

PSYCHROMETRIC CHART

HIGH TEMPERATURES 1013.25 MILLIBARS

