

1) Problem One

- a) Is a function
- b) Is injective
- c) N/A

- 
- a) Is a function
  - b) Is surjective
  - c) N/A

- 
- a) Is a function
  - b) Is bijective
  - c)  $\{('y', 'b'), ('z', 'a'), ('x', 'c'), ('w', 'd')\}$

- 
- a) Is a function
  - b) Is injective
  - c) N/A

- 
- a) Is a function
  - b) Is injective
  - c) N/A

- 
- a) Is a function
  - b) Is surjective
  - c) N/A

- 
- a) Is a function
  - b) Is bijective
  - c)  $\{(1, 'b'), (4, 'a'), (2, 'd'), (3, 'c')\}$

- 
- a) Is a function
  - b) Is injective
  - c) N/A

- 
- a) Not a function
  - b) N/A
  - c) N/A

2) Problem Two

$662/414 = 1 \text{ R } 248$   
 $414/248 = 1 \text{ R } 166$   
 $248/166 = 1 \text{ R } 82$   
 $166/82 = 2 \text{ R } 2$   
 $82/2 = 41 \text{ R } 0$   
 $\gcd(414, 662) = 82$

-----

$14/6 = 2 \text{ R } 2$   
 $6/2 = 3 \text{ R } 0$   
 $\gcd(6, 14) = 6$

-----

$36/24 = 1 \text{ R } 12$   
 $24/12 = 2 \text{ R } 0$   
 $\gcd(24, 36) = 24$

-----

$42/12 = 3 \text{ R } 6$   
 $12/6 = 2 \text{ R } 0$   
 $\gcd(12, 42) = 12$

-----

$252/198 = 1 \text{ R } 54$   
 $198/54 = 3 \text{ R } 36$   
 $54/36 = 1 \text{ R } 18$   
 $36/18 = 2 \text{ R } 0$   
 $\gcd(252, 198) = 36$

-----  
3) Problem Three

$2 = 1 * 166 - 2 * 82$   
 $2 = 1 * 166 - 2 * (248 - 1 * 166)$   
 $2 = 3 * 166 - 2 * 248$   
 $2 = 3 * (414 - 1 * 248) - 2 * 248$   
 $2 = 3 * 414 - 5 * 248$   
 $2 = 3 * 414 - 5 * (662 - 1 * 414)$   
 $2 = 8 * 414 - 5 * 662$   
 $\gcd(414, 662) = (8 * 414) + (-5 * 662)$

-----  
 $2 = 1 * 14 - 2 * 6$   
 $\gcd(6, 14) = (-2 * 6) + (1 * 14)$

-----  
 $12 = 1 * 36 - 1 * 24$   
 $\gcd(24, 36) = (-1 * 24) + (1 * 36)$

-----  
 $6 = 1 * 42 - 3 * 12$   
 $\gcd(12, 42) = (-3 * 12) + (1 * 42)$

-----  
 $18 = 1 * 54 - 1 * 36$   
 $18 = 1 * 54 - 1 * (198 - 3 * 54)$   
 $18 = 4 * 54 - 1 * 198$   
 $18 = 4 * (252 - 1 * 198) - 1 * 198$   
 $18 = 4 * 252 - 5 * 198$   
 $\gcd(252, 198) = (4 * 252) + (-5 * 198)$

-----  
4) Problem Four

$q_0 = 1, q_1 = 1, q_2 = 1, q_3 = 2, q_4 = 41,$   
 $s_0 = 1, s_1 = 0, s_2 = s_0 - 1 * s_1 = 1, s_3 = s_1 - -1 * s_2 = -1, s_4 = s_2 - 2 * s_3 =$   
 $2, s_5 = s_3 - -5 * s_4 = -5,$   
 $t_0 = 0, t_1 = 1, t_2 = t_0 - -1 * t_1 = -1, t_3 = t_1 - 2 * t_2 = 2, t_4 = t_2 - -3 * t_3$   
 $= -3, t_5 = t_3 - 8 * t_4 = 8,$   
 $\gcd(414, 662) = (8 * 414) + (-5 * 662)$

-----  
 $q_0 = 2, q_1 = 3,$   
 $s_0 = 1, s_1 = 0, s_2 = s_0 - 1 * s_1 = 1,$   
 $t_0 = 0, t_1 = 1, t_2 = t_0 - -2 * t_1 = -2,$   
 $\gcd(6, 14) = (-2 * 6) + (1 * 14)$

-----  
 $q_0 = 1, q_1 = 2,$   
 $s_0 = 1, s_1 = 0, s_2 = s_0 - 1 * s_1 = 1,$   
 $t_0 = 0, t_1 = 1, t_2 = t_0 - -1 * t_1 = -1,$   
 $\gcd(24, 36) = (-1 * 24) + (1 * 36)$

-----  
 $q_0 = 3, q_1 = 2,$   
 $s_0 = 1, s_1 = 0, s_2 = s_0 - 1 * s_1 = 1,$   
 $t_0 = 0, t_1 = 1, t_2 = t_0 - -3 * t_1 = -3,$   
 $\gcd(12, 42) = (-3 * 12) + (1 * 42)$

-----  
 $q_0 = 1, q_1 = 3, q_2 = 1, q_3 = 2,$   
 $s_0 = 1, s_1 = 0, s_2 = s_0 - 1 * s_1 = 1, s_3 = s_1 - -3 * s_2 = -3, s_4 = s_2 - 4 * s_3 =$   
 $4,$   
 $t_0 = 0, t_1 = 1, t_2 = t_0 - -1 * t_1 = -1, t_3 = t_1 - 4 * t_2 = 4, t_4 = t_2 - -5 * t_3$   
 $= -5,$   
 $\gcd(252, 198) = (4 * 252) + (-5 * 198)$