



M.Sc. In Electrical Energy Conversion and Power Systems



Industrial electronics in renewable energy generation systems

Unit 4.- Three-Phase converters

4.2 DC-AC conversion. The three-phase inverter

Semester 2 – Industrial electronics in renewable energy generation systems

Lecturer: Jorge García, garciajorge@uniovi.es



Unit 4.- Three-phase converters

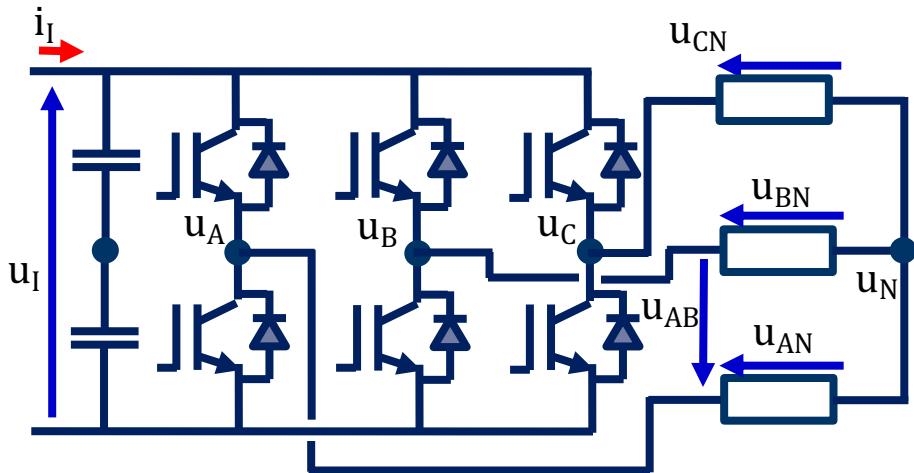
4.1	DC-AC conversion. The single-phase inverter General concepts in inverters. Characteristics and types Half-bridge square wave single-phase inverter Full-bridge square wave single-phase inverter Sine-waveform PWM modulation Output LC filter and harmonics analysis Input filter and DC-link current
4.2	DC-AC conversion. The three-phase inverter General concepts in inverters. 6-pulses inverter. Sine-waveform PWM modulation Output LC filter and harmonics analysis Input filter and DC-link current Effect of the dead-times. Limitations. Alternative modulations, 3rd harmonic injection, SVPWM.
4.3	AC-DC conversion. The three-phase controlled rectifier Reverse operation of the three-phase inverter Equivalent single-phase circuit Control of the filter current Main electrical magnitudes relations Evolution of waveforms



Three-Phase, Full-Bridge PWM Inverter

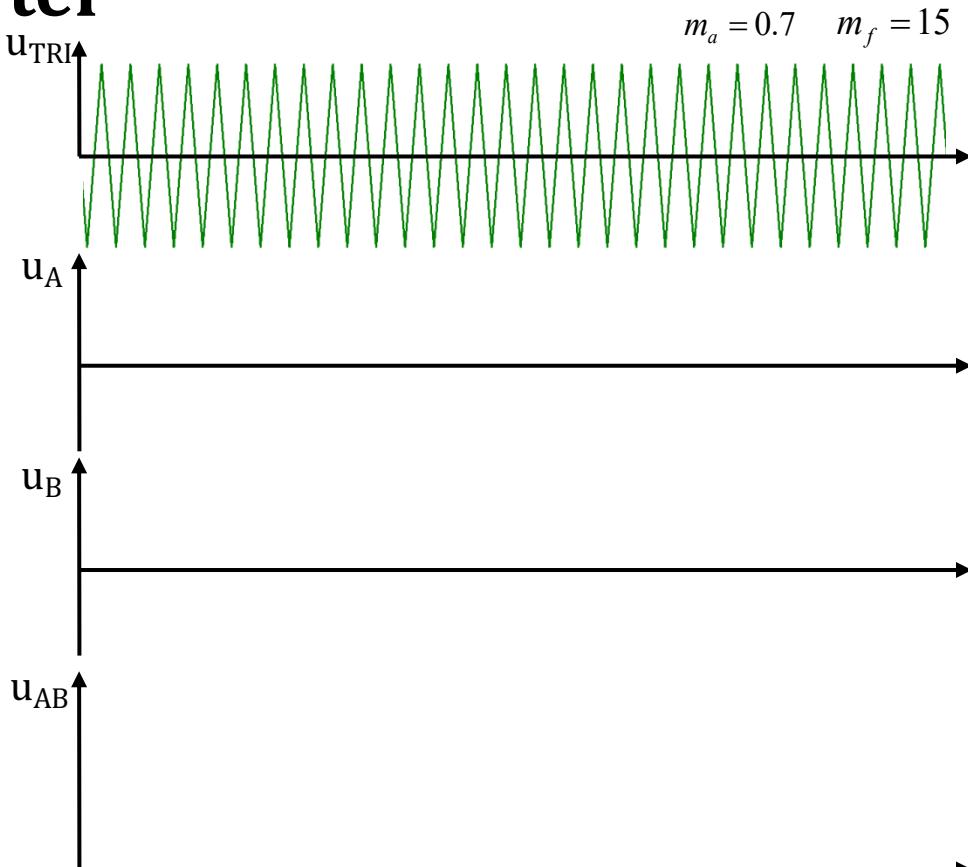


Three-Phase PWM Inverter



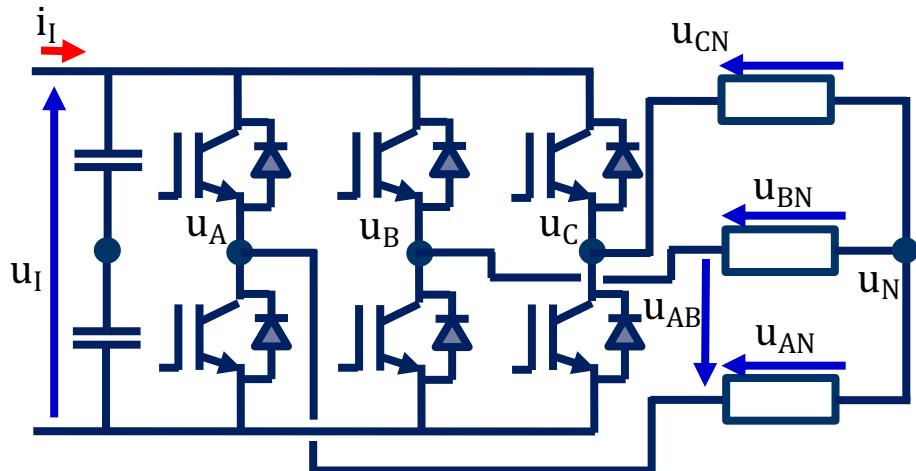
The Square Waveform Control (Six Step Operation) can be applied, but again PWM provides smaller harmonics

For PWM, the modulation ratios m_a and m_f can be defined





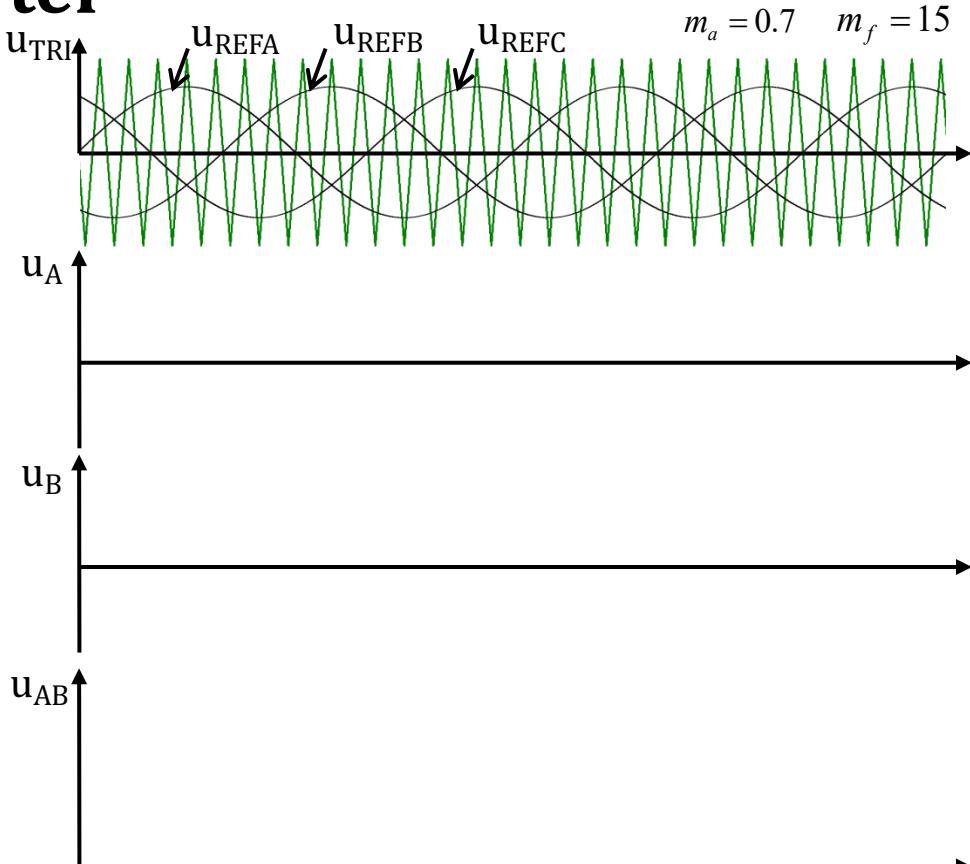
Three-Phase PWM Inverter



The Square Waveform Control can be applied, but again PWM provides smaller harmonics

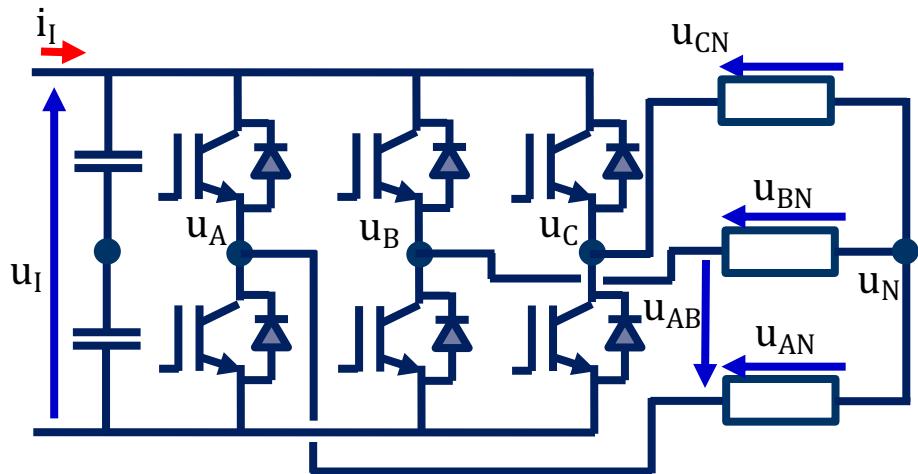
For PWM, the modulation ratios m_a and m_f can be defined

To minimize harmonics, m_f should be large, odd, and u_{REF} with opposite slope with respect to u_{TRI} . m_a should be < 1 (overmodulation is used in some applications, particularly in industrial drives).





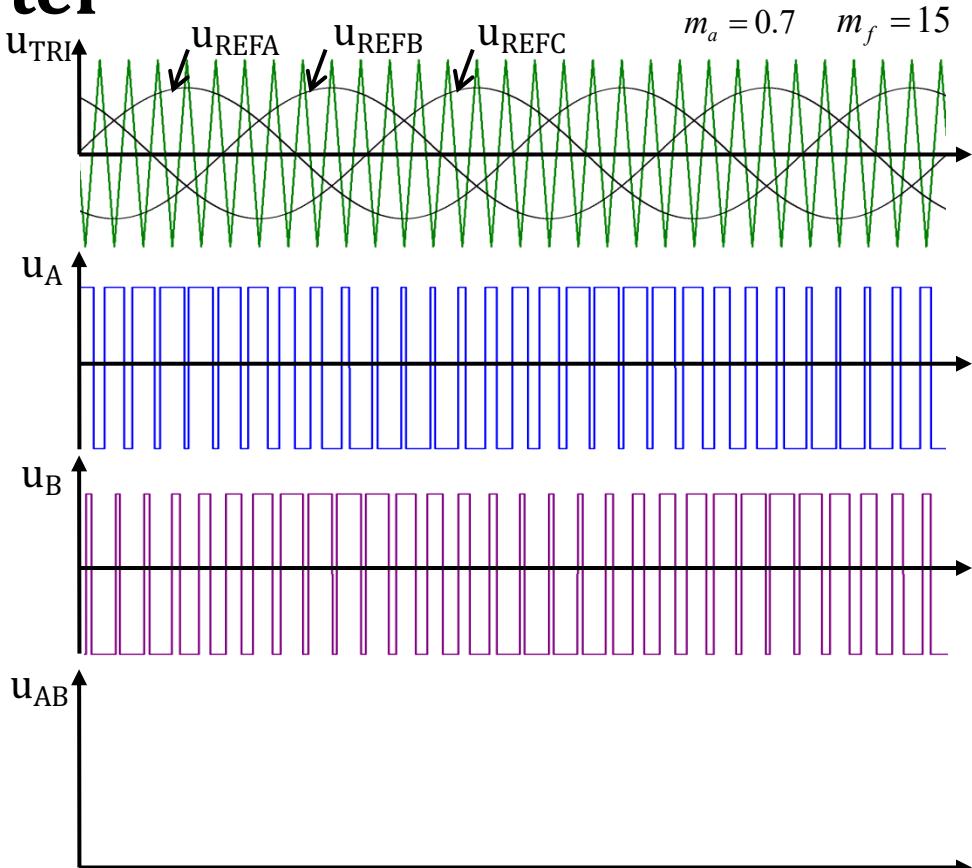
Three-Phase PWM Inverter



The Square Waveform Control can be applied, but again PWM provides smaller harmonics

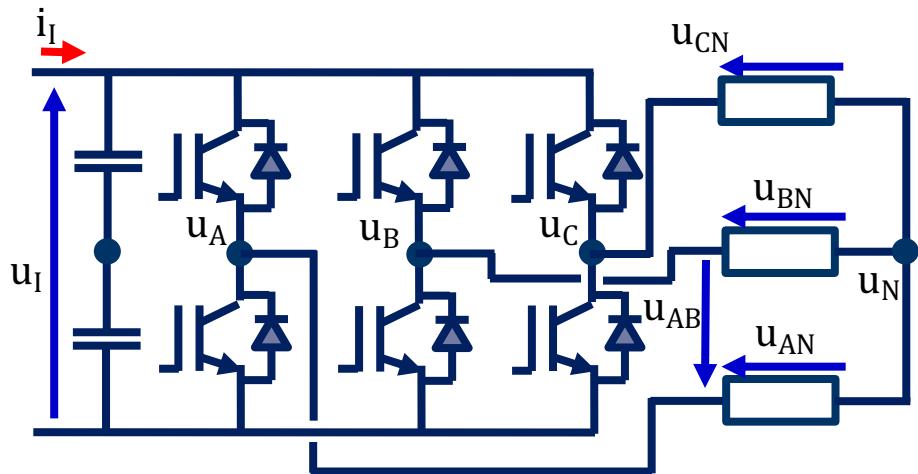
For PWM, the modulation ratios m_a and m_f can be defined

To minimize harmonics, m_f should be large, odd, and u_{REF} with opposite slope with respect to u_{TRI} . m_a should be < 1 (overmodulation is used in some applications, particularly in industrial drives).





Three-Phase PWM Inverter

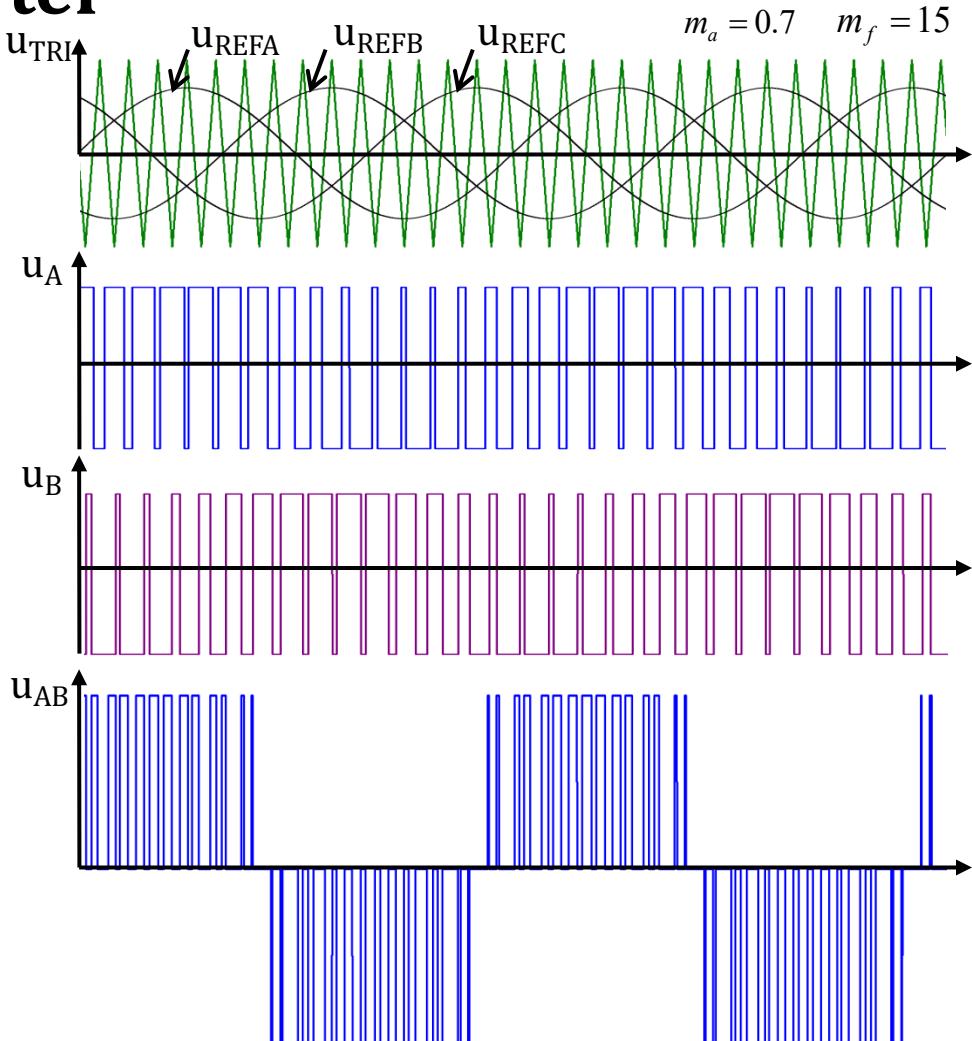


The Square Waveform Control can be applied, but again PWM provides smaller harmonics

For PWM, the modulation ratios m_a and m_f can be defined

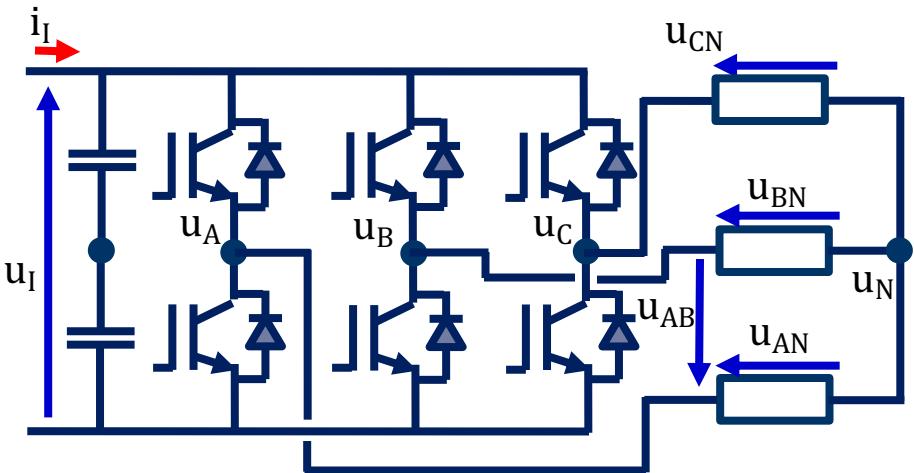
To minimize harmonics, m_f should be large, odd, and u_{REF} with opposite slope with respect to u_{TRI} . m_a should be < 1 (overmodulation is used in some applications, particularly in industrial drives).

u_A and u_B have a 120° lag, what yields to a UNIPOLAR scheme of the output line voltages





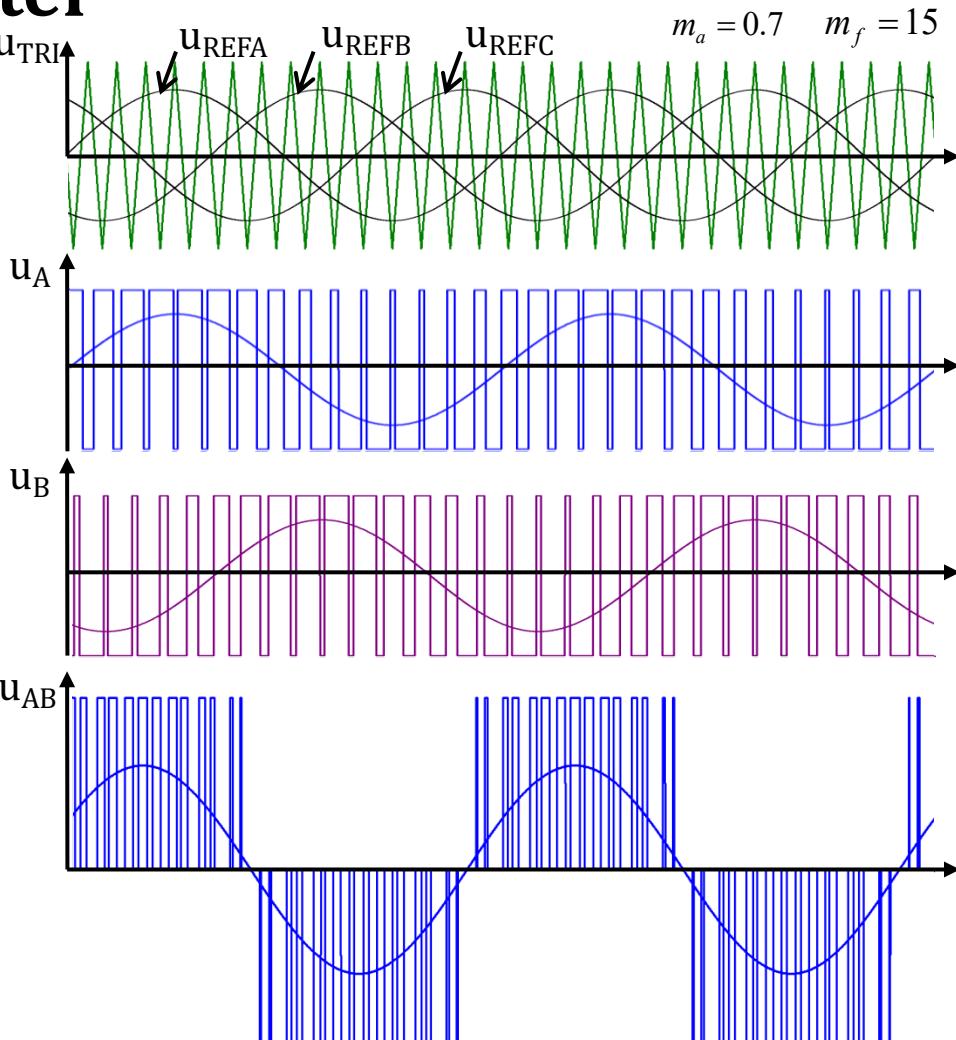
Three-Phase PWM Inverter



$$\begin{aligned} u_{CN}(t) &= u_C - u_N \\ u_{AN}(t) &= u_A - u_N \\ u_{BN}(t) &= u_B - u_N \end{aligned}$$

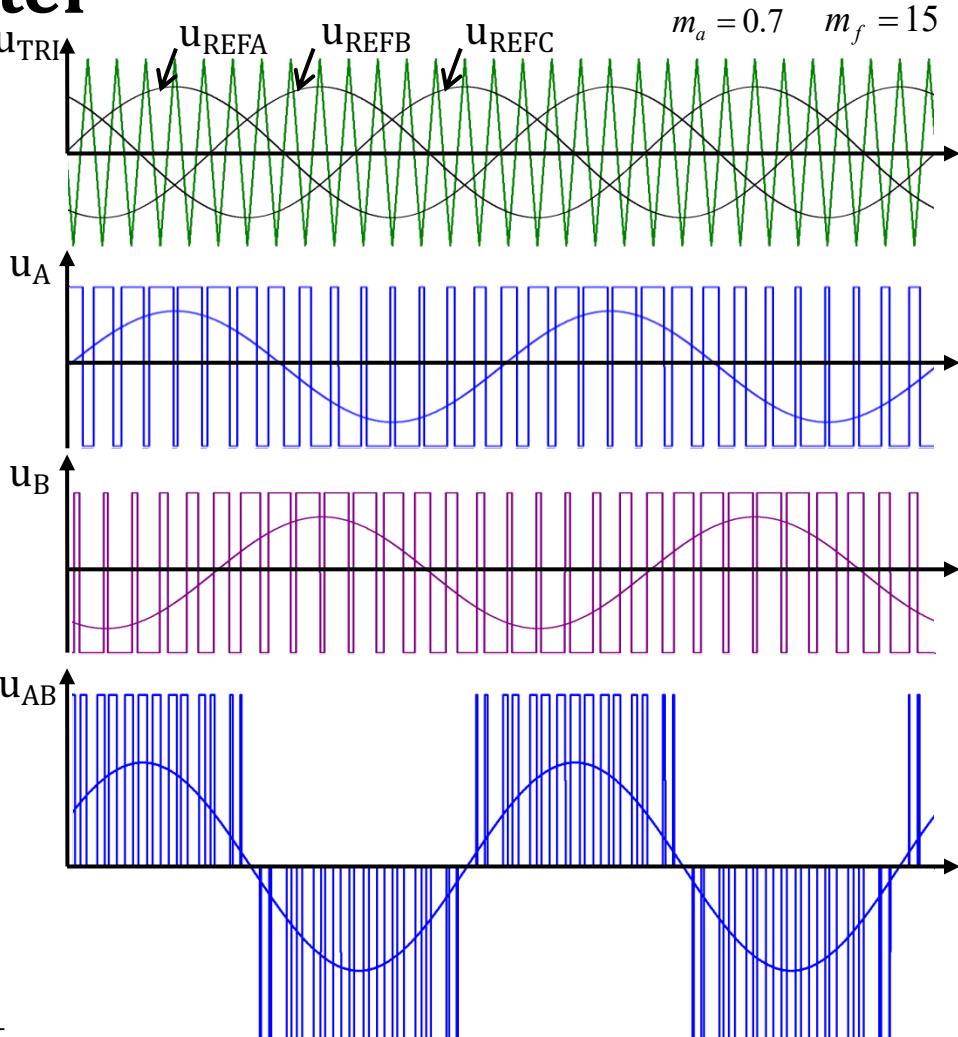
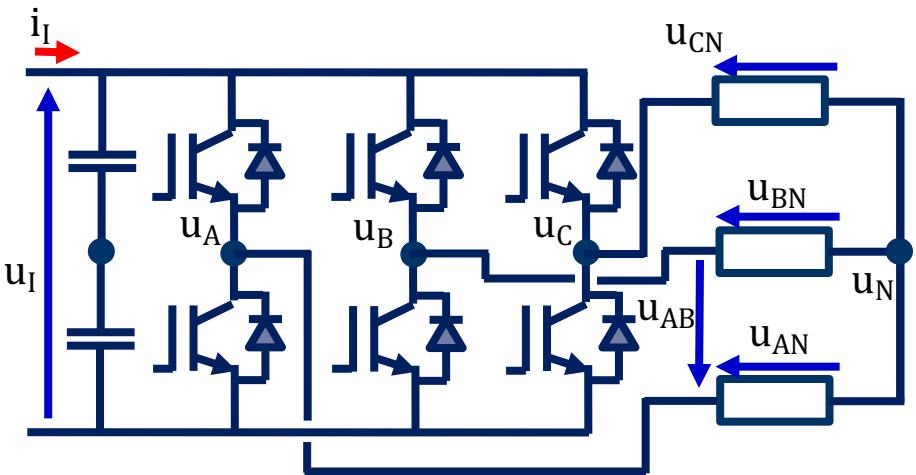
$$|u_{AN}(t)| = m_a \frac{U_I}{2}$$

$$u_{AN\langle RMS \rangle} = m_a \frac{U_I}{2\sqrt{2}}$$





Three-Phase PWM Inverter

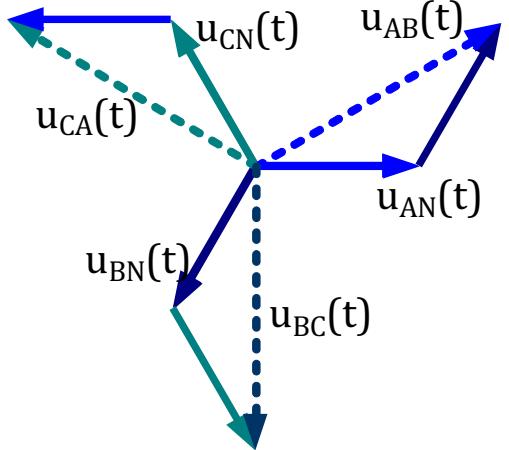


$$|u_{AN}(t)| = m_a \frac{U_I}{2}$$

$$u_{AN\langle RMS \rangle} = m_a \frac{U_I}{2\sqrt{2}}$$

$$|u_{AB}(t)| = \frac{m_a \cdot U_I}{2} \cdot \sqrt{3}$$

$$u_{AB\langle RMS \rangle} = m_a \frac{U_I \sqrt{3}}{2\sqrt{2}}$$





Three-Phase PWM Inverter

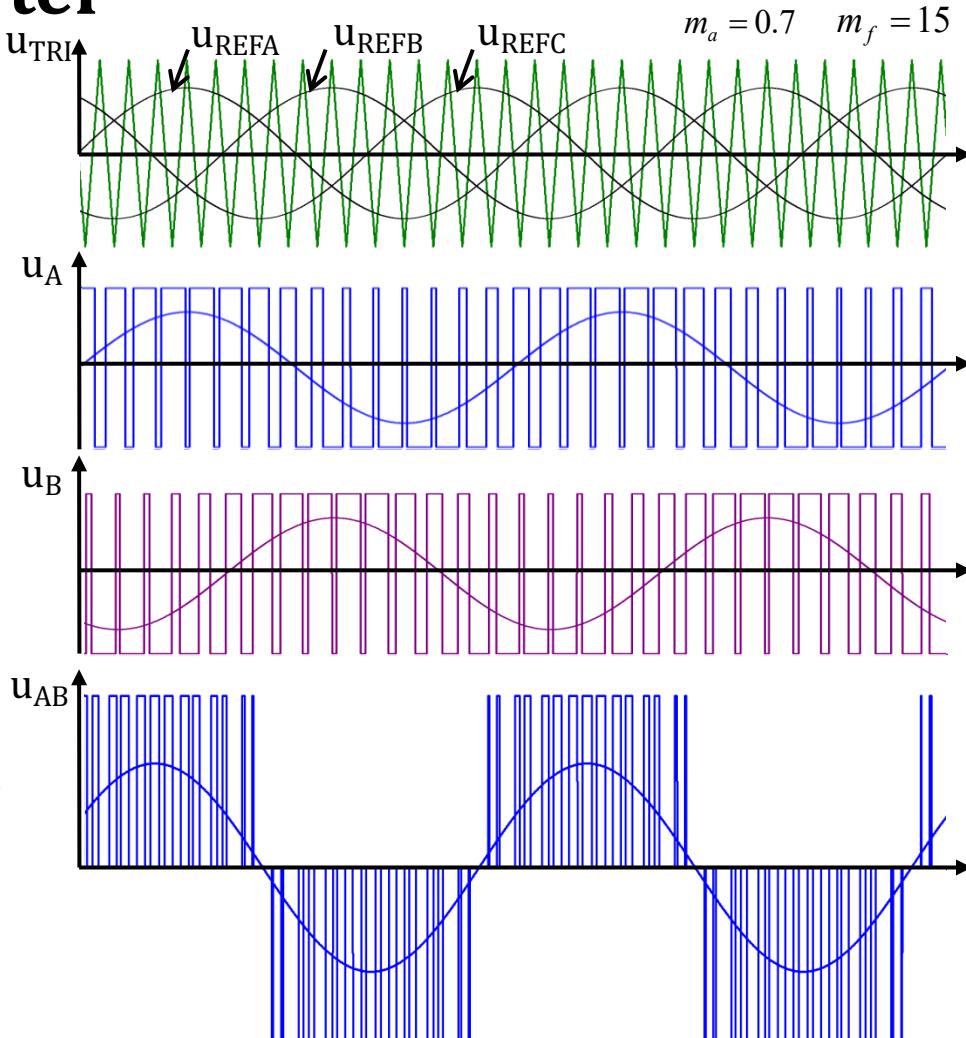
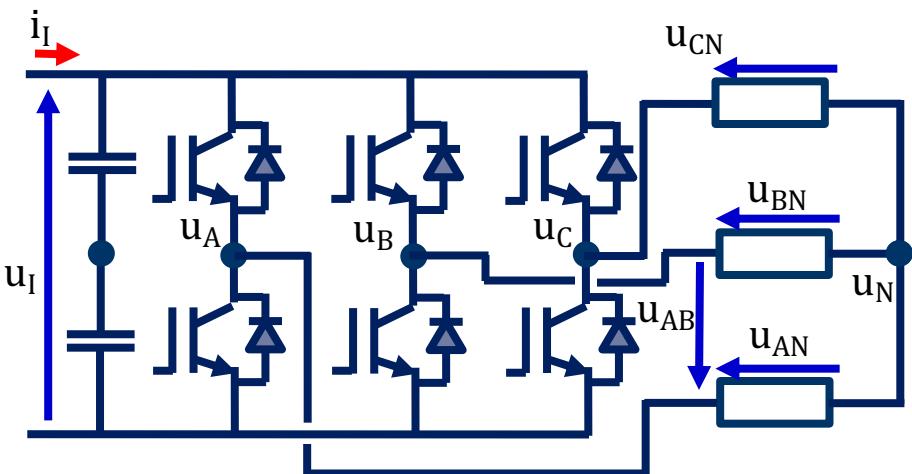


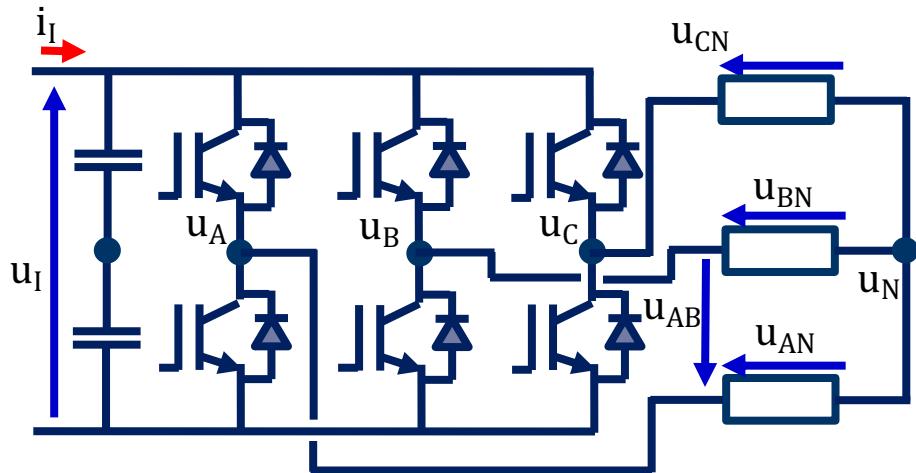
Table 8-2 Generalized Harmonics of v_{LL} for a Large and Odd m_f That Is a Multiple of 3.

$h \backslash m_a$	0.2	0.4	0.6	0.8	1.0
1	0.122	0.245	0.367	0.490	0.612
$m_f \pm 2$	0.010	0.037	0.080	0.135	0.195
$m_f \pm 4$				0.005	0.011
$2m_f \pm 1$	0.116	0.200	0.227	0.192	0.111
$2m_f \pm 5$				0.008	0.020
$3m_f \pm 2$	0.027	0.085	0.124	0.108	0.038
$3m_f \pm 4$		0.007	0.029	0.064	0.096
$4m_f \pm 1$	0.100	0.096	0.005	0.064	0.042
$4m_f \pm 5$			0.021	0.051	0.073
$4m_f \pm 7$				0.010	0.030

Note: $(V_{LL})_h/V_d$ are tabulated as a function of m_a where $(V_{LL})_h$ are the rms values of the harmonic voltages.



Three-Phase PWM Inverter

 u_{TRI}

THREE-PHASE PWM

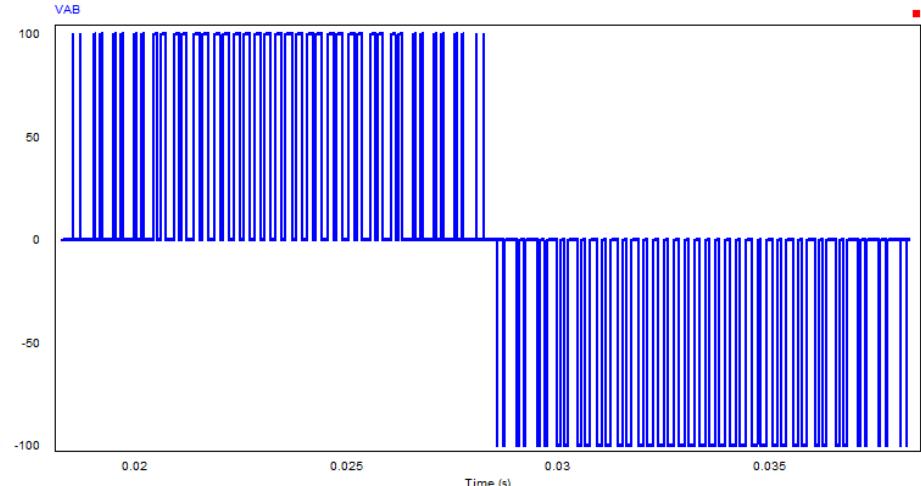
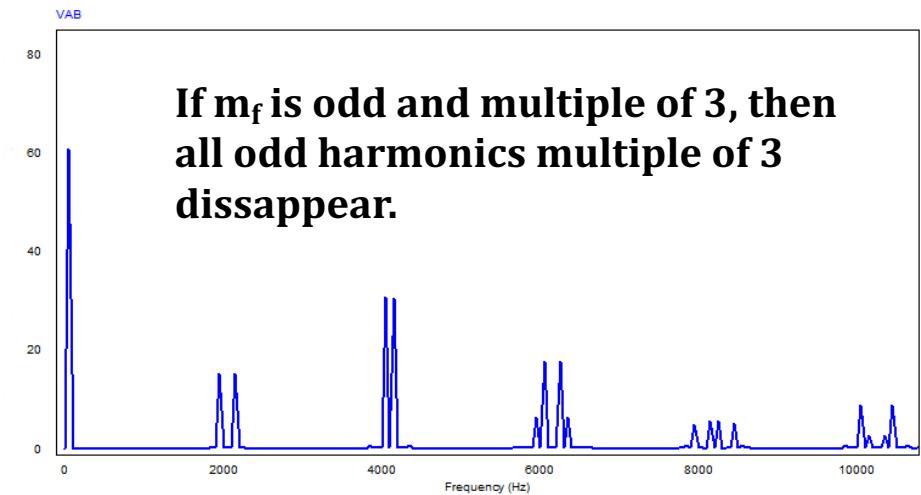


Table 8-2 Generalized Harmonics of v_{LL} for a Large and Odd m_f That Is a Multiple of 3.

m_a	0.2	0.4	0.6	0.8	1.0
1	0.122	0.245	0.367	0.490	0.612
$m_f \pm 2$	0.010	0.037	0.080	0.135	0.195
$m_f \pm 4$				0.005	0.011
$2m_f \pm 1$	0.116	0.200	0.227	0.192	0.111
$2m_f \pm 5$				0.008	0.020
$3m_f \pm 2$	0.027	0.085	0.124	0.108	0.038
$3m_f \pm 4$		0.007	0.029	0.064	0.096
$4m_f \pm 1$	0.100	0.096	0.005	0.064	0.042
$4m_f \pm 5$			0.021	0.051	0.073
$4m_f \pm 7$				0.010	0.030

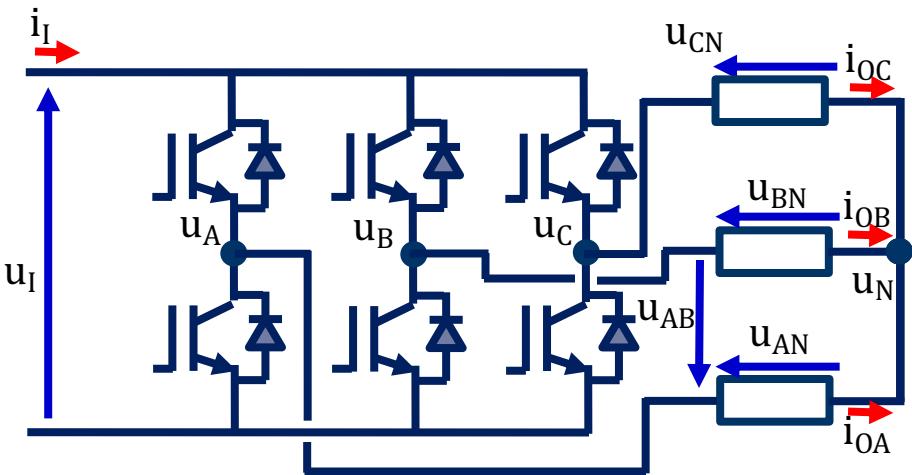
Note: $(V_{LL})_h/V_d$ are tabulated as a function of m_a where $(V_{LL})_h$ are the rms values of the harmonic voltages.

If m_f is odd and multiple of 3, then all odd harmonics multiple of 3 disappear.





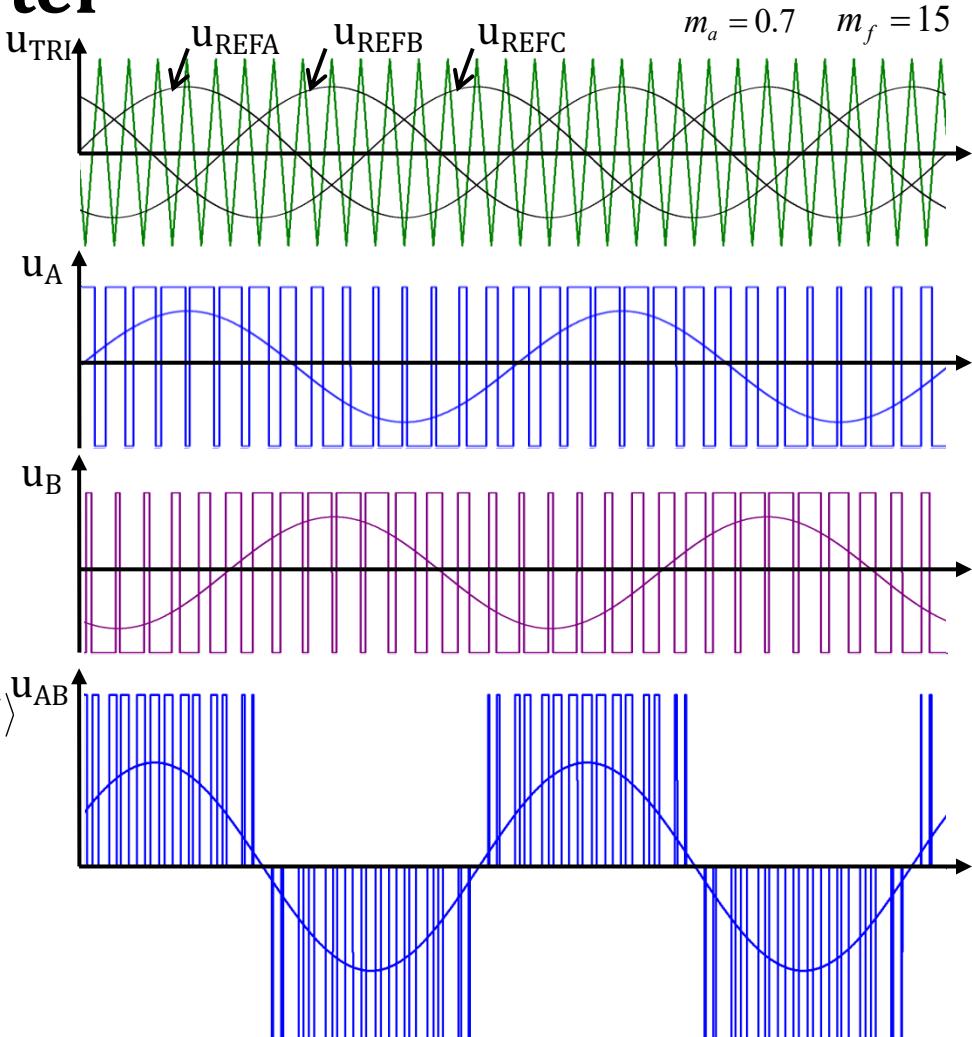
Three-Phase PWM Inverter



Size of components:

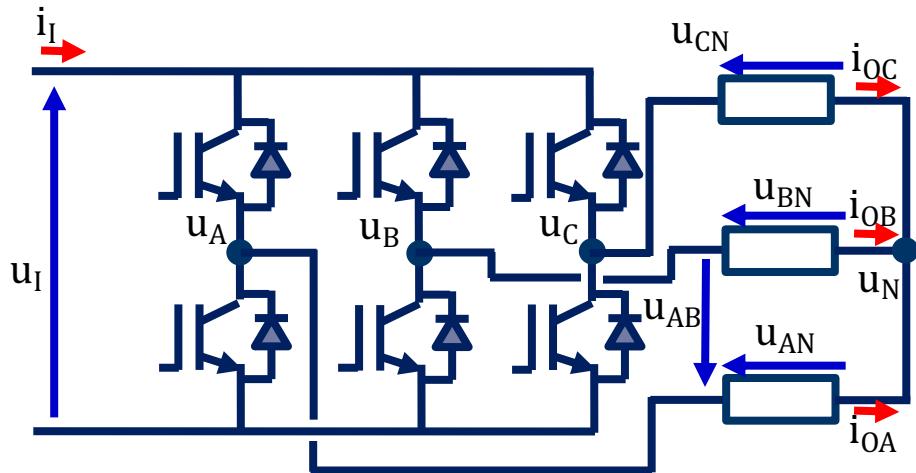
Voltage stress in Switches: $u_{CE\langle PEAK \rangle} = u_I$

Current stress in Switches: $i_{C\langle PEAK \rangle} = i_{O\langle PEAK \rangle}$





Three-Phase PWM Inverter

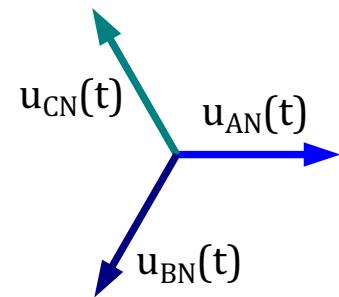


Input current:

$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t)$$

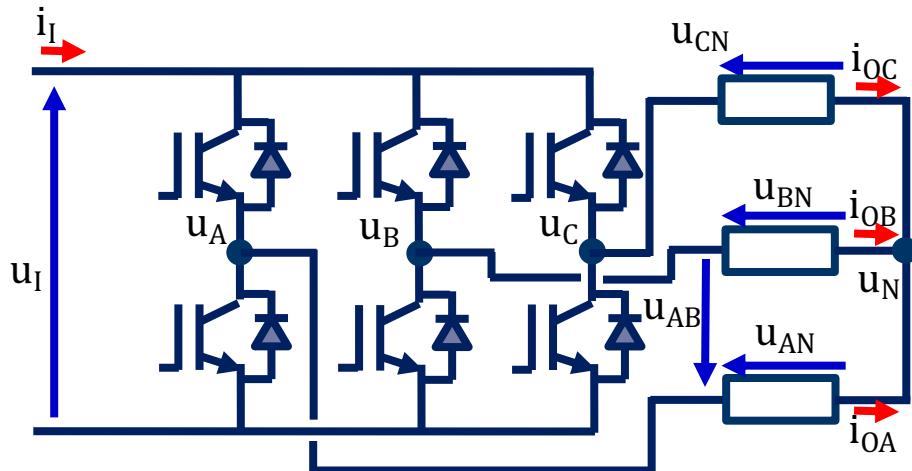
$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ)$$





Three-Phase PWM Inverter

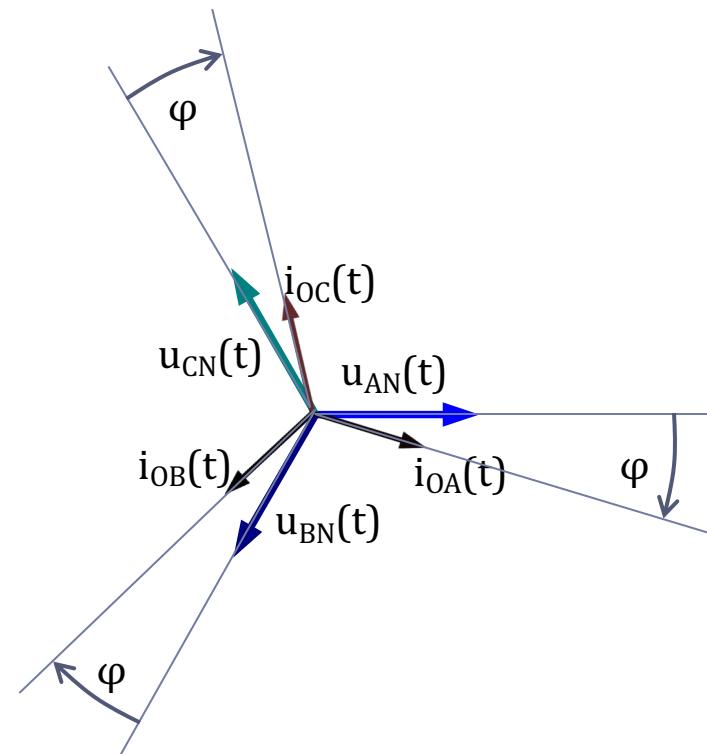


Input current:

$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t) \quad i_{OA}(t) = I_{OA} \cdot \sin(2\pi f_R t + \varphi)$$

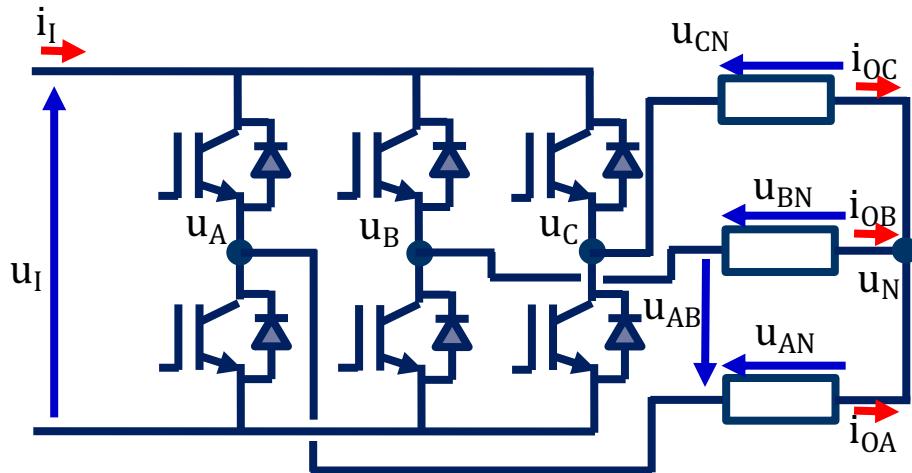
$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ) \quad i_{OB}(t) = I_{OB} \cdot \sin(2\pi f_R t + \varphi - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ) \quad i_{OC}(t) = I_{OC} \cdot \sin(2\pi f_R t + \varphi + 120^\circ)$$





Three-Phase PWM Inverter



Input current:

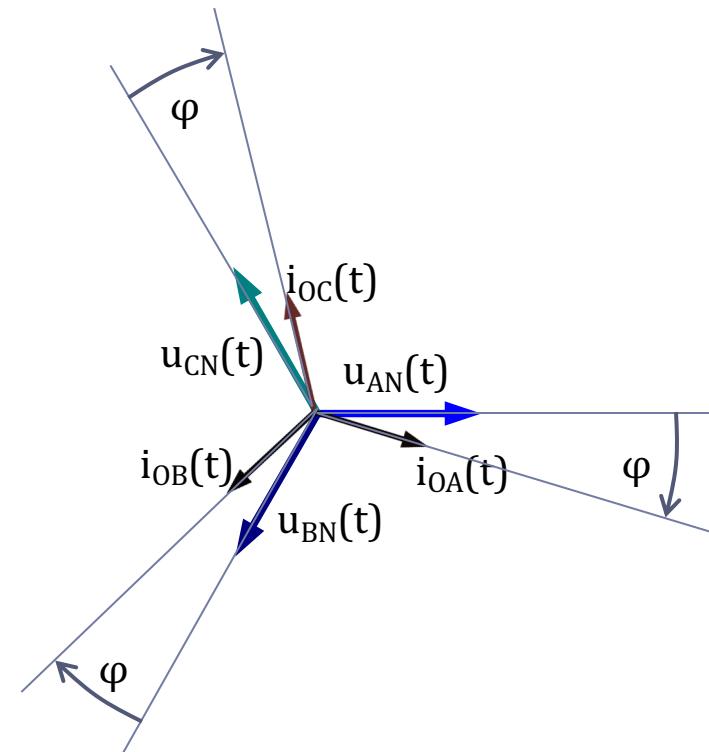
$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t) \quad i_{OA}(t) = I_{OA} \cdot \sin(2\pi f_R t + \varphi)$$

$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ) \quad i_{OB}(t) = I_{OB} \cdot \sin(2\pi f_R t + \varphi - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ) \quad i_{OC}(t) = I_{OC} \cdot \sin(2\pi f_R t + \varphi + 120^\circ)$$

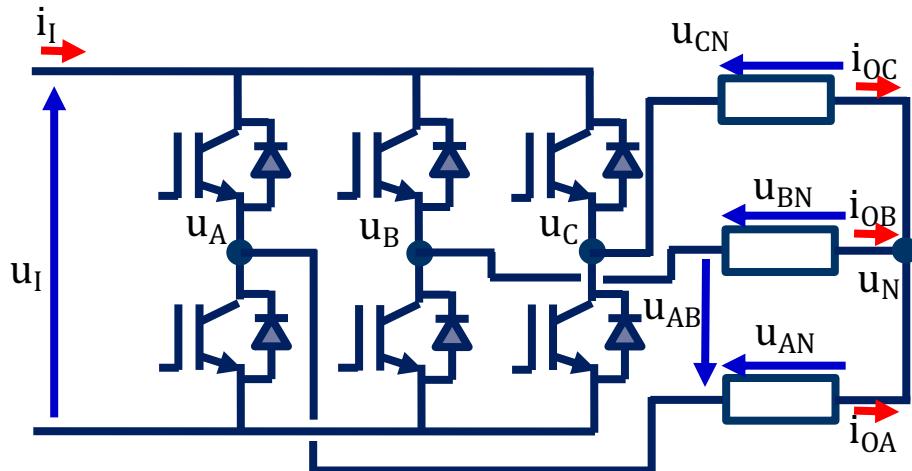
$$p_O(t) = u_{AN}(t) \cdot i_{OA}(t) + u_{BN}(t) \cdot i_{OB}(t) + u_{CN}(t) \cdot i_{OC}(t)$$

$$\begin{aligned} p_O(t) = U_{PN} I_{OP} & \left[\sin(2\pi f_R t) \sin(2\pi f_R t + \varphi) + \right. \\ & + \sin(2\pi f_R t - 120^\circ) \sin(2\pi f_R t + \varphi - 120^\circ) + \\ & \left. + \sin(2\pi f_R t + 120^\circ) \sin(2\pi f_R t + \varphi + 120^\circ) \right] = \dots = 3U_{PN} I_{OP} \cos \varphi \end{aligned}$$





Three-Phase PWM Inverter



Input current:

$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t) \quad i_{OA}(t) = I_{OA} \cdot \sin(2\pi f_R t + \varphi)$$

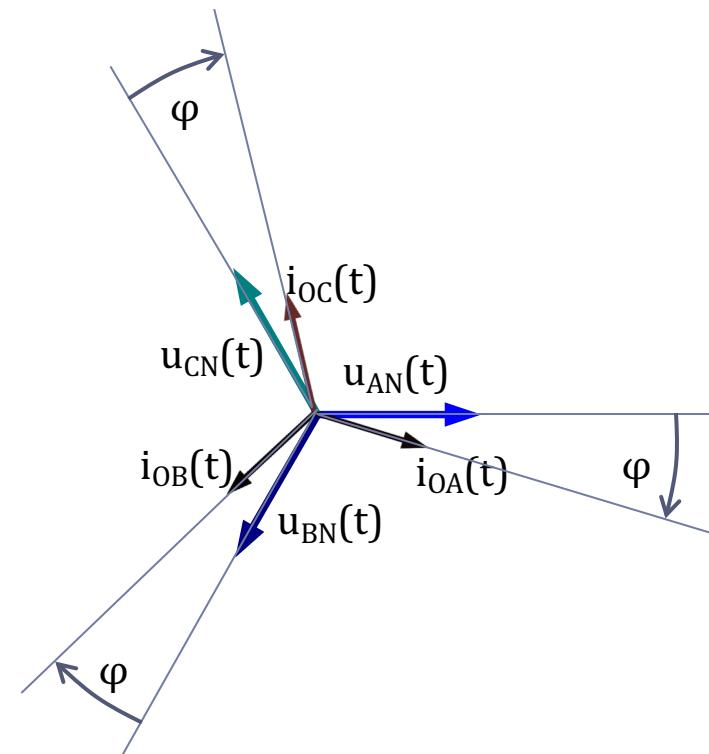
$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ) \quad i_{OB}(t) = I_{OB} \cdot \sin(2\pi f_R t + \varphi - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ) \quad i_{OC}(t) = I_{OC} \cdot \sin(2\pi f_R t + \varphi + 120^\circ)$$

$$p_O(t) = u_{AN}(t) \cdot i_{OA}(t) + u_{BN}(t) \cdot i_{OB}(t) + u_{CN}(t) \cdot i_{OC}(t)$$

$$\begin{aligned} p_O(t) = U_{PN} I_{OP} & \left[\sin(2\pi f_R t) \sin(2\pi f_R t + \varphi) + \right. \\ & + \sin(2\pi f_R t - 120^\circ) \sin(2\pi f_R t + \varphi - 120^\circ) + \\ & \left. + \sin(2\pi f_R t + 120^\circ) \sin(2\pi f_R t + \varphi + 120^\circ) \right] = \dots = 3U_{PN} I_{OP} \cos \varphi \end{aligned}$$

$$u_I(t) = U_I \quad p_I(t) = u_I(t) \cdot i_I(t)$$



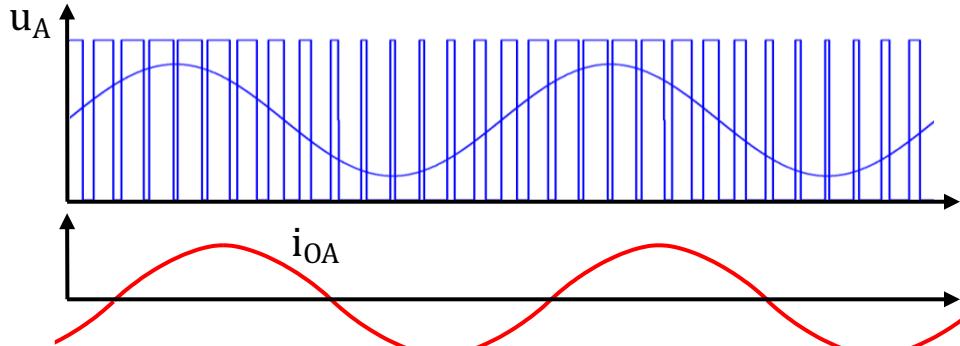
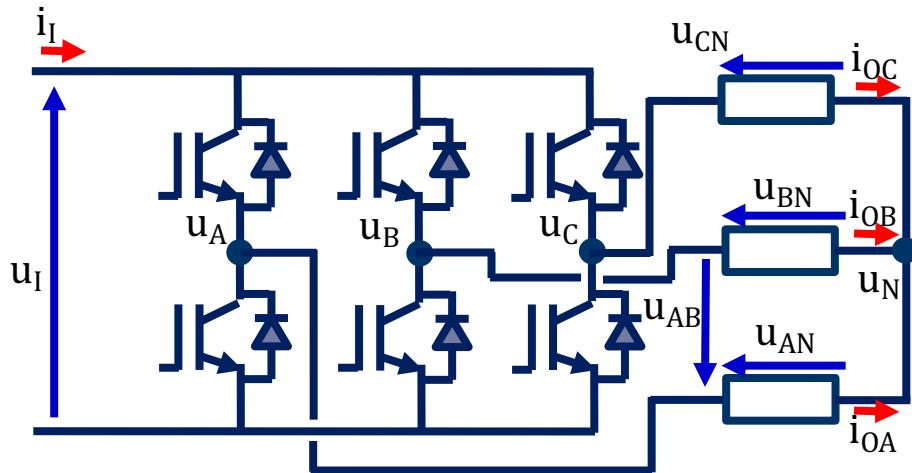
The filter has no effect at line frequencies!!!

$$p_I(t) = p_O(t)$$

$$i_I(t) = \frac{3U_{PN} I_{OP} \cos \varphi}{U_I}$$



Three-Phase PWM Inverter



Input current:

$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t) \quad i_{OA}(t) = I_{OA} \cdot \sin(2\pi f_R t + \varphi)$$

$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ) \quad i_{OB}(t) = I_{OB} \cdot \sin(2\pi f_R t + \varphi - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ) \quad i_{OC}(t) = I_{OC} \cdot \sin(2\pi f_R t + \varphi + 120^\circ)$$

$$p_O(t) = u_{AN}(t) \cdot i_{OA}(t) + u_{BN}(t) \cdot i_{OB}(t) + u_{CN}(t) \cdot i_{OC}(t)$$

$$\begin{aligned} p_O(t) = U_{PN} I_{OP} & \left[\sin(2\pi f_R t) \sin(2\pi f_R t + \varphi) + \right. \\ & + \sin(2\pi f_R t - 120^\circ) \sin(2\pi f_R t + \varphi - 120^\circ) + \\ & \left. + \sin(2\pi f_R t + 120^\circ) \sin(2\pi f_R t + \varphi + 120^\circ) \right] = \dots = 3U_{PN} I_{OP} \cos \varphi \end{aligned}$$

$$u_I(t) = U_I \quad p_I(t) = u_I(t) \cdot i_I(t)$$

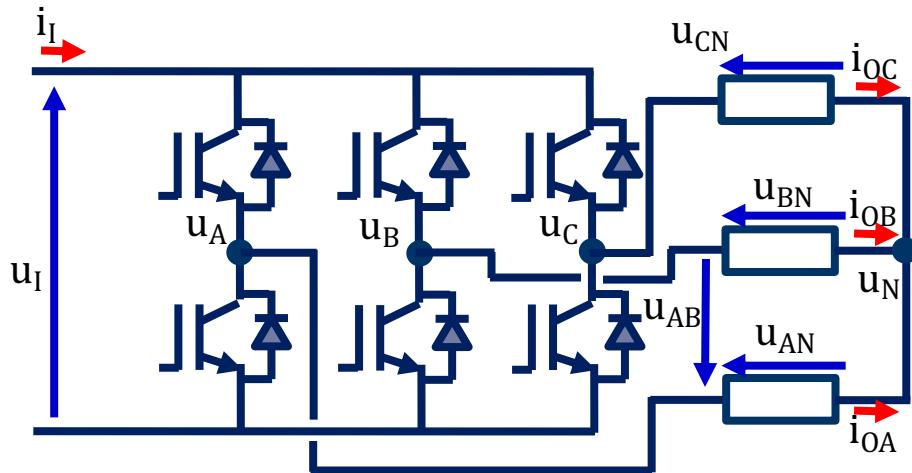
The filter has no effect at line frequencies!!!

$$p_I(t) = p_O(t)$$

$$i_I(t) = \frac{3U_{PN} I_{OP} \cos \varphi}{U_I}$$



Three-Phase PWM Inverter



Input current:

$$u_{AN}(t) = U_{PN} \cdot \sin(2\pi f_R t) \quad i_{OA}(t) = I_{OA} \cdot \sin(2\pi f_R t)$$

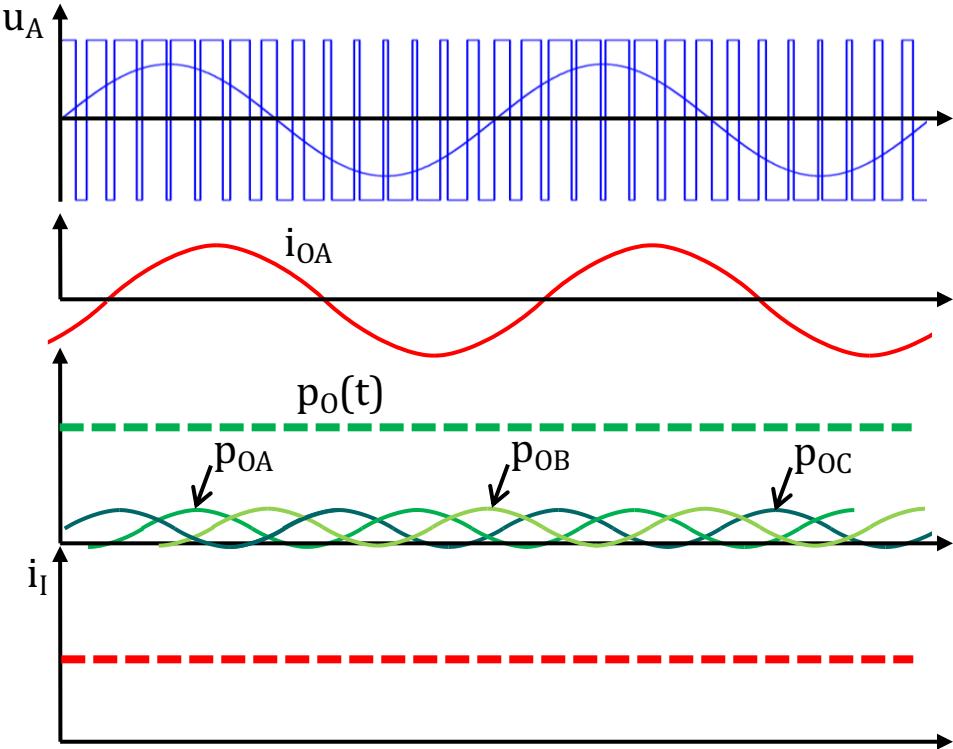
$$u_{BN}(t) = U_{PN} \cdot \sin(2\pi f_R t - 120^\circ) \quad i_{OB}(t) = I_{OB} \cdot \sin(2\pi f_R t - 120^\circ)$$

$$u_{CN}(t) = U_{PN} \cdot \sin(2\pi f_R t + 120^\circ) \quad i_{OC}(t) = I_{OC} \cdot \sin(2\pi f_R t + 120^\circ)$$

$$p_O(t) = u_{AN}(t) \cdot i_{OA}(t) + u_{BN}(t) \cdot i_{OB}(t) + u_{CN}(t) \cdot i_{OC}(t)$$

$$\begin{aligned} p_O(t) = U_{PN} I_{OP} & [\sin(2\pi f_R t) \sin(2\pi f_R t + \varphi) + \\ & + \sin(2\pi f_R t - 120^\circ) \sin(2\pi f_R t + \varphi - 120^\circ) + \\ & + \sin(2\pi f_R t + 120^\circ) \sin(2\pi f_R t + \varphi - 120^\circ)] = \dots = 3U_{PN} I_{OP} \cos \varphi \end{aligned}$$

$$u_I(t) = U_I \quad p_I(t) = u_I(t) \cdot i_I(t)$$



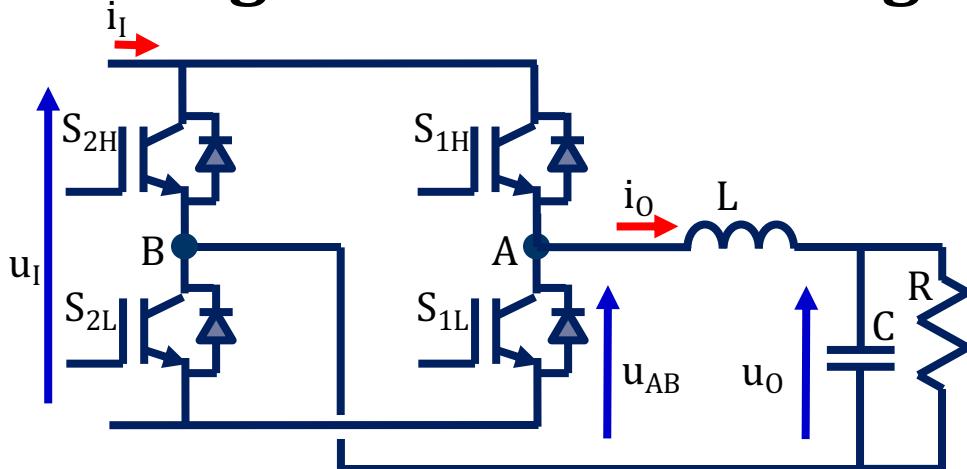
The filter has no effect at line frequencies!!!

$$p_I(t) = p_O(t)$$

$$i_I(t) = \frac{3U_{PN} I_{OP} \cos \varphi}{U_I}$$



Single-Phase Full-Bridge PWM Inverter



Size of components:

Voltage stress in Switches: $U_{CE\langle PEAK \rangle} = U_I$

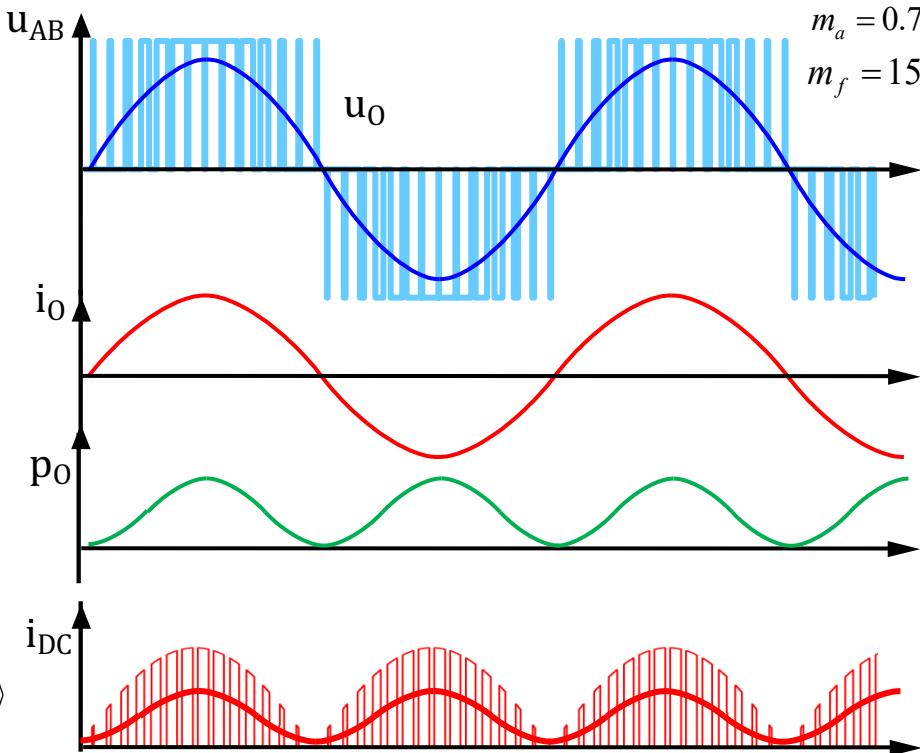
Current stress in Switches: $i_{C\langle PEAK \rangle} = i_{O\langle PEAK \rangle}$

Input current:

$$u_O(t) = \langle u_{AB}(t) \rangle_{T_S} = U_I \cdot m_a \cdot \sin(2\pi f_R t) \quad i_O(t) = \frac{U_I}{R} \cdot m_a \cdot \sin(2\pi f_R t)$$

$$p_O(t) = \frac{U_I^2}{R} \cdot m_a^2 \cdot \sin^2(2\pi f_R t) \quad p_O(t) = \frac{U_I^2}{R} \cdot m_a^2 \frac{1 - \cos(2\pi \cdot 2f_R \cdot t)}{2}$$

$$u_I(t) = U_I \quad p_I(t) = u_I(t) \cdot i_I(t)$$



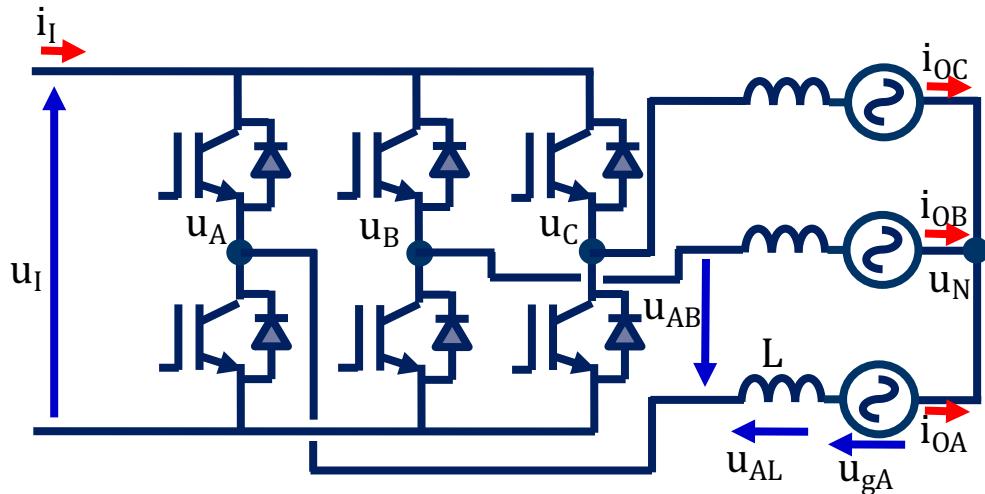
The filter has no effect at line frequencies!!!

$$p_I(t) = p_O(t)$$

$$i_I(t) = \frac{U_I}{R} \cdot m_a^2 \frac{1 - \cos(2\pi \cdot 2f_R \cdot t)}{2}$$

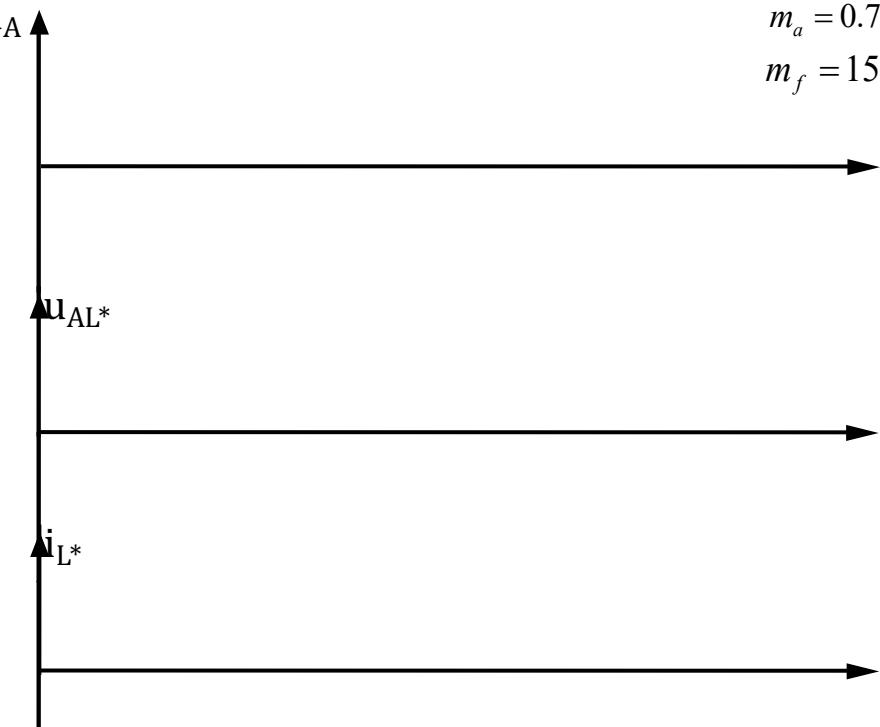


Three-Phase PWM Inverter



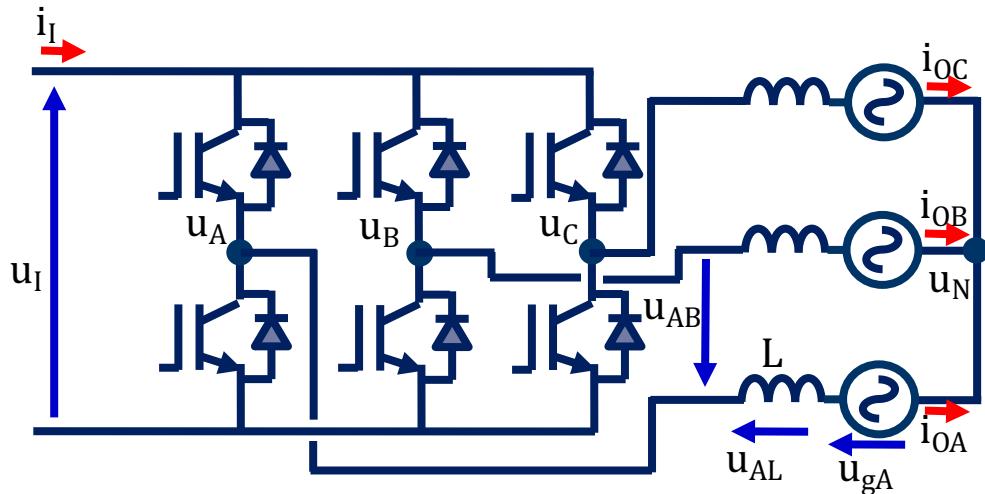
Output current ripple and switching frequency

Consider as a load an AC motor (or the grid line).





Three-Phase PWM Inverter

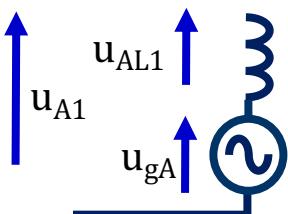


Output current ripple and switching frequency

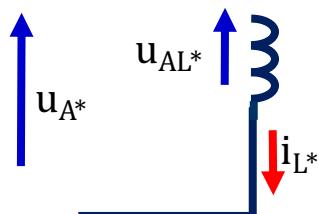
Consider as a load an AC motor (or the grid line).

Superposition:

1st harmonic:



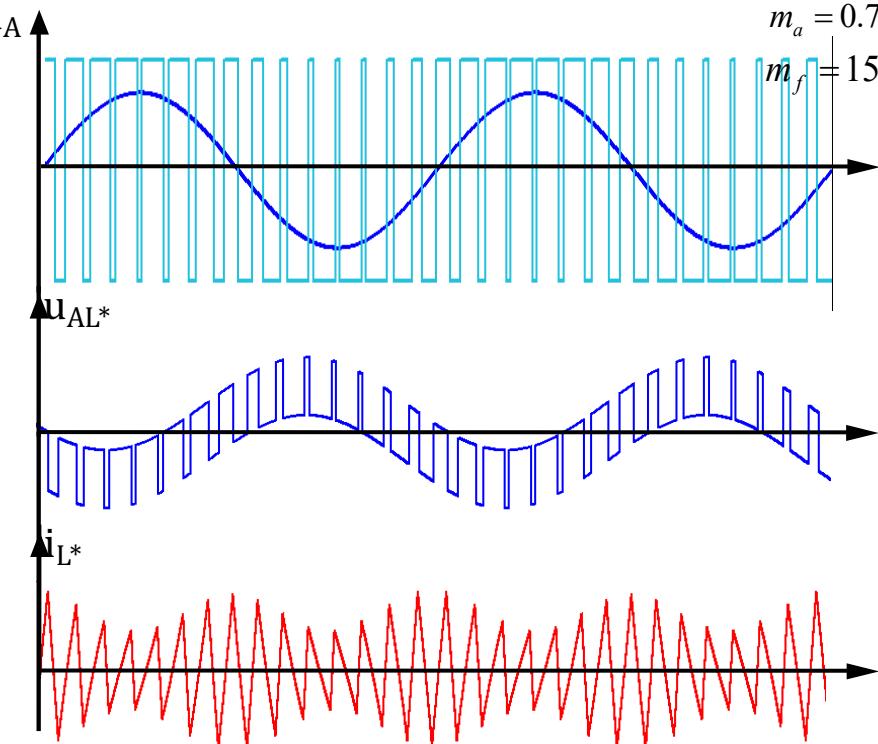
Rest of harmonics:



$$u_{A*}(t) = u_A - u_{A1}$$

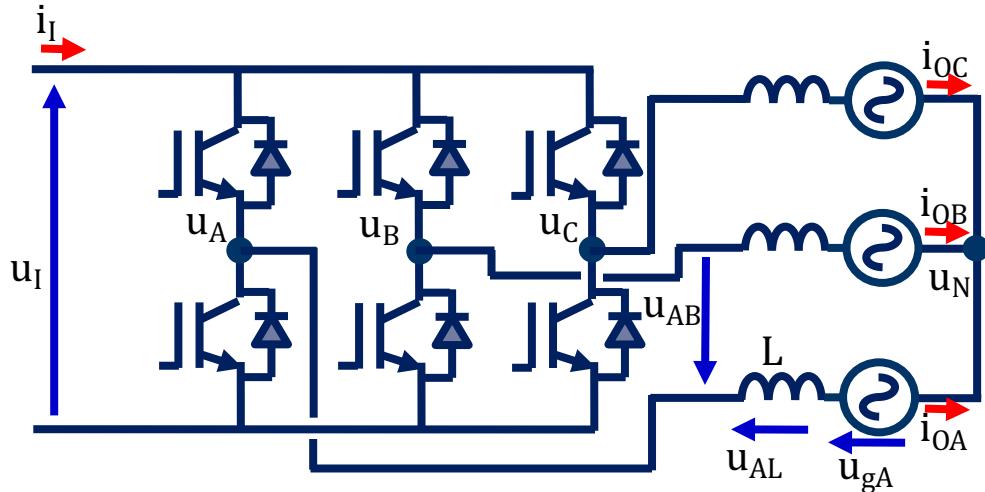
$$u_{AL*}(t) = L \cdot \frac{di_{L*}}{dt}$$

This current ripple implies losses (no active power delivered)





Three-Phase PWM Inverter

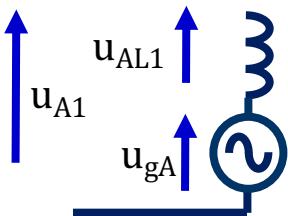


Output current ripple and switching frequency

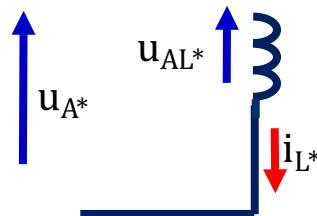
Consider as a load an AC motor (or the grid line).

Superposition:

1st harmonic:



Rest of harmonics:



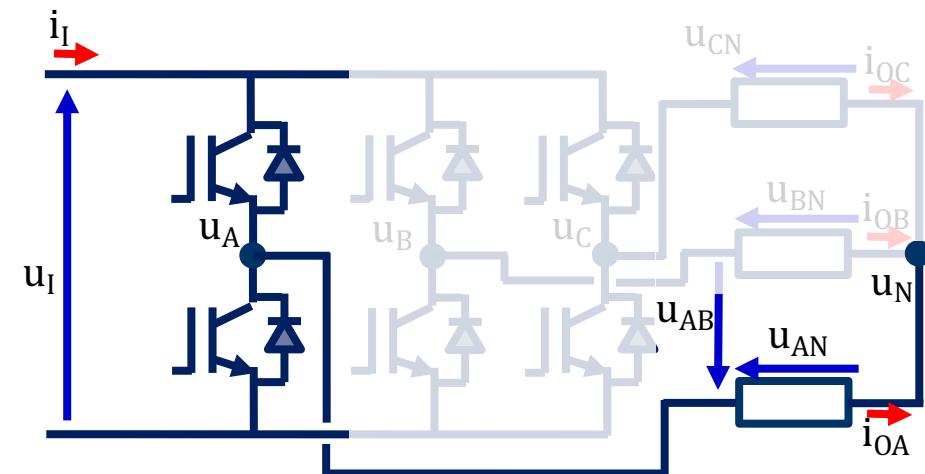
$$u_{A*}(t) = u_A - u_{A1}$$

$$u_{AL*}(t) = L \cdot \frac{di_{L*}}{dt}$$

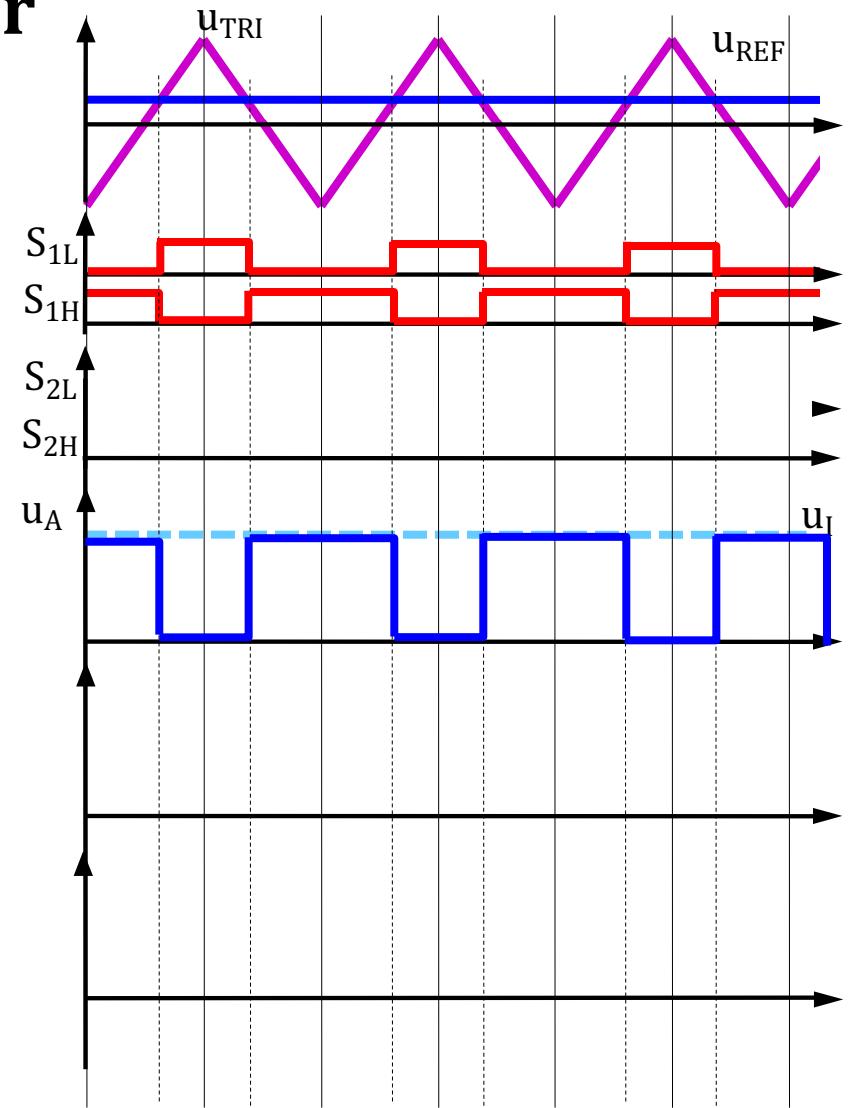
This current ripple implies losses (no active power delivered)



Three-Phase PWM Inverter

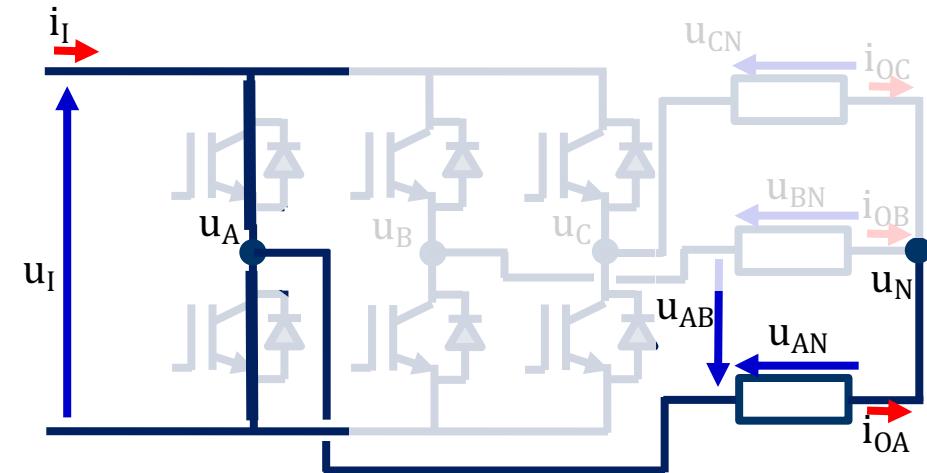


Need for Dead Times



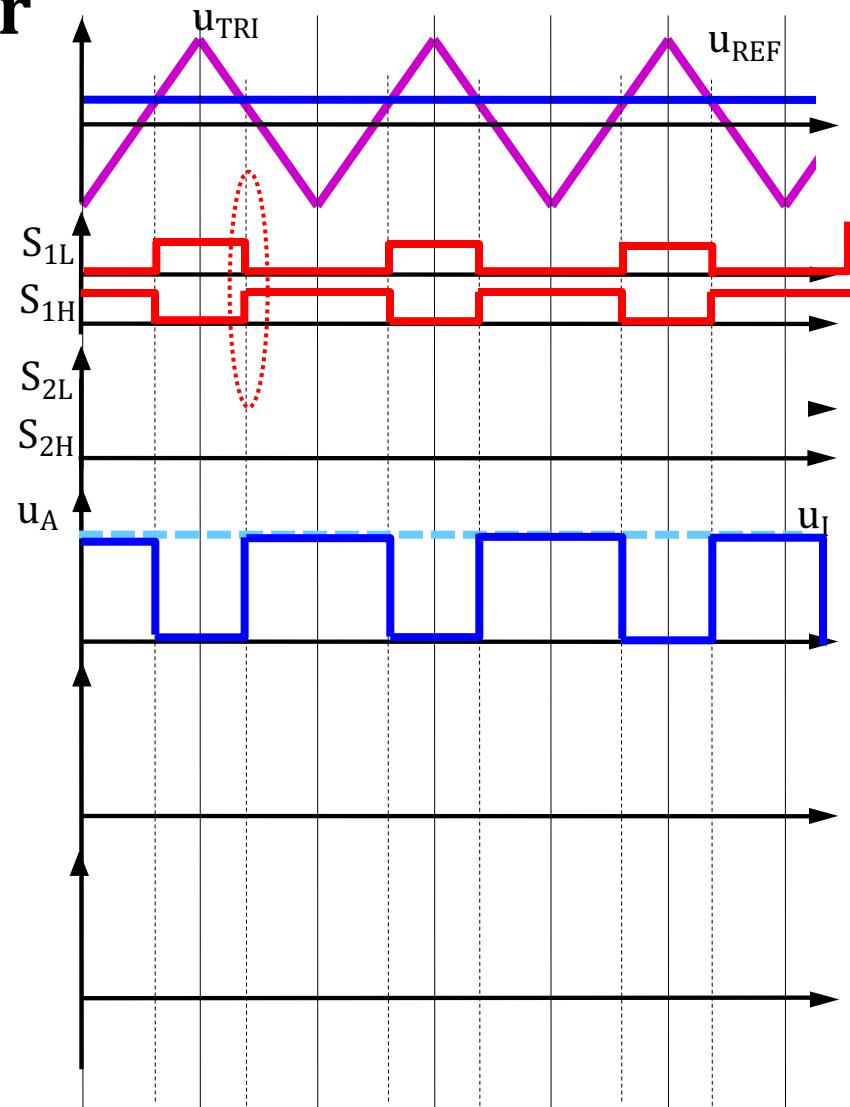


Three-Phase PWM Inverter



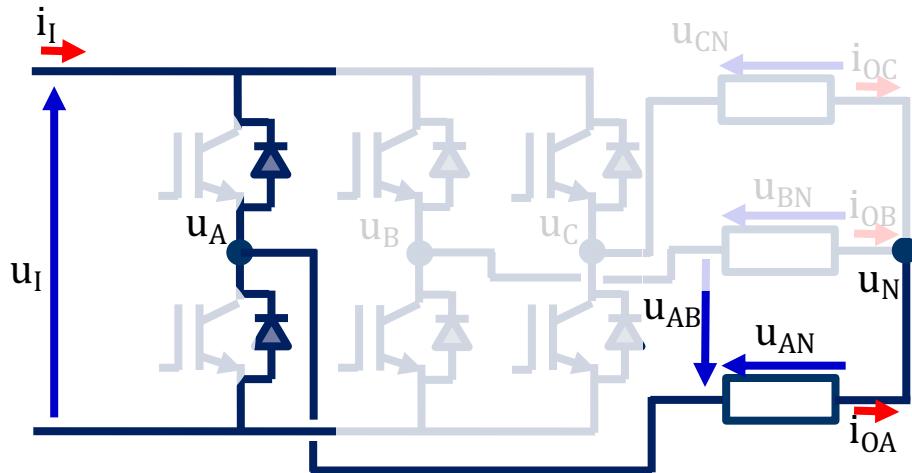
Need for Dead Times:

If both transistors in a leg are switched on simultaneously, a short circuit appears...





Three-Phase PWM Inverter



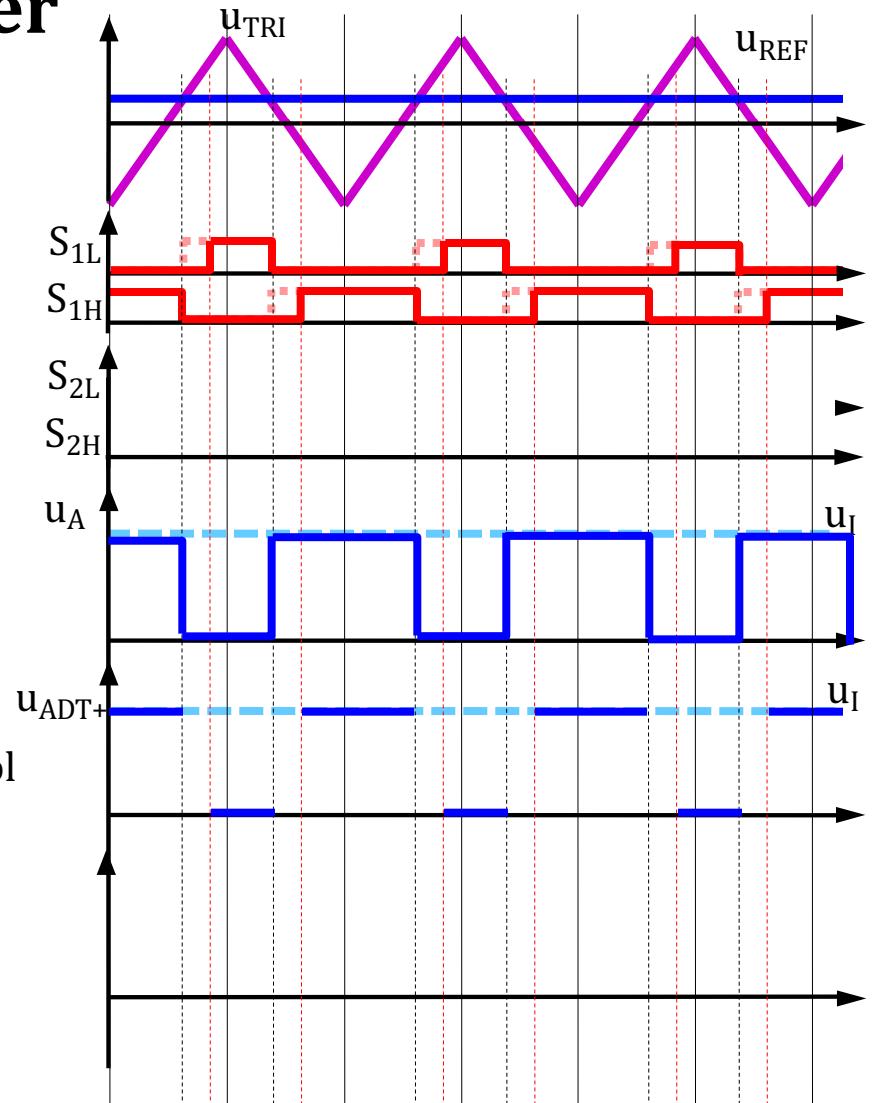
Need for Dead Times:

Dead times avoid these cross-conduction problems

Effect of Dead Times:

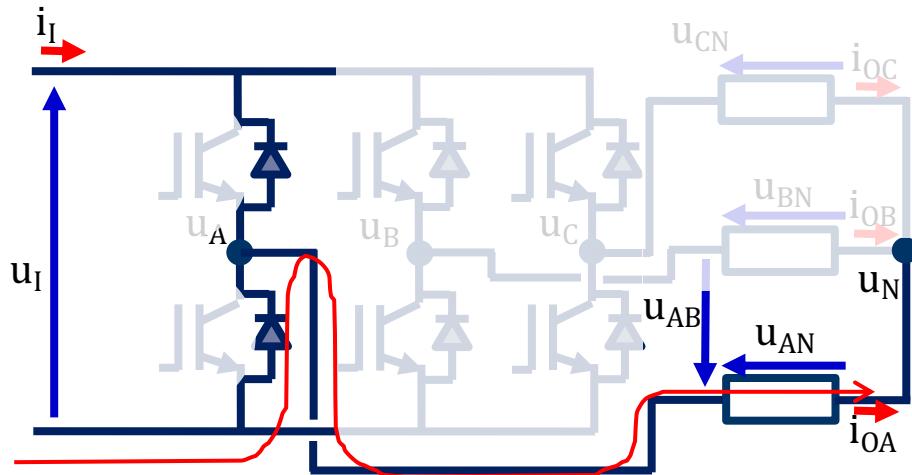
Consider a dead time at the rising edge of the control waveforms.

The voltage during the blank times depends on the direction of the line current i_{OA} !!!





Three-Phase PWM Inverter



Need for Dead Times:

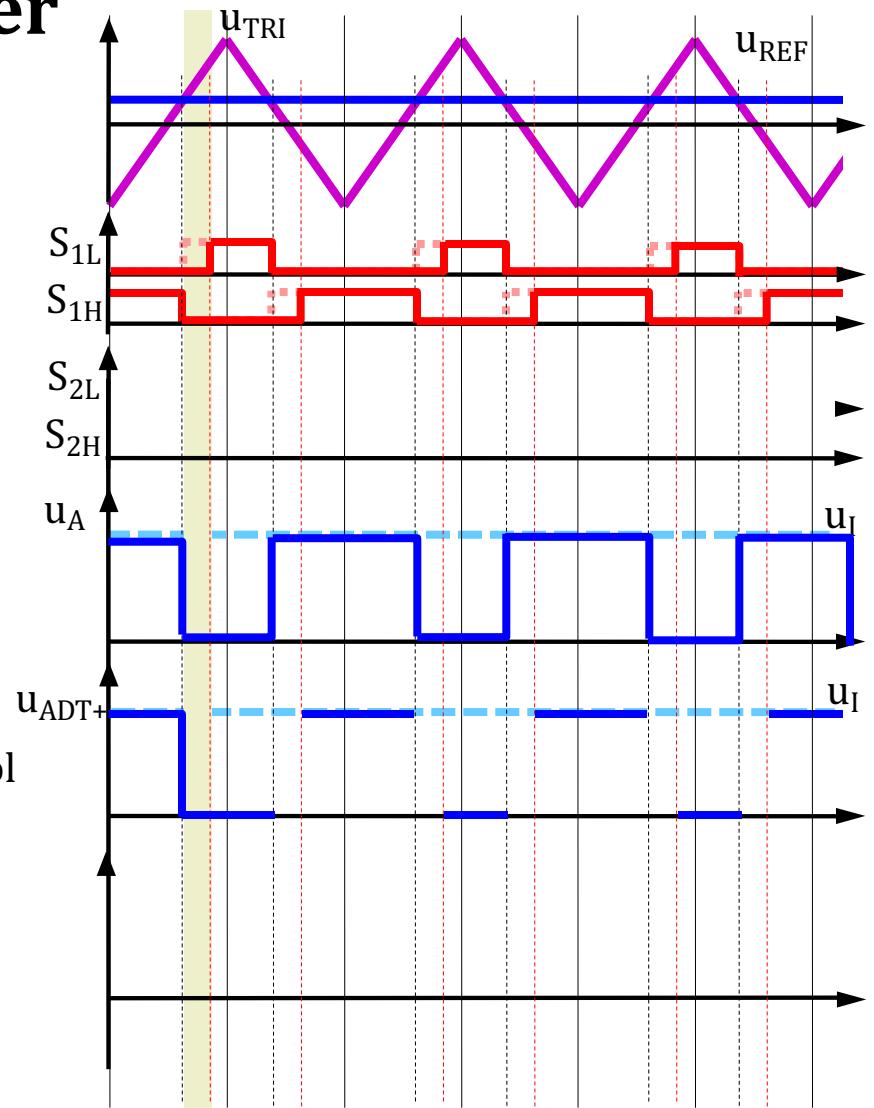
Dead times avoid these cross-conduction problems

Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

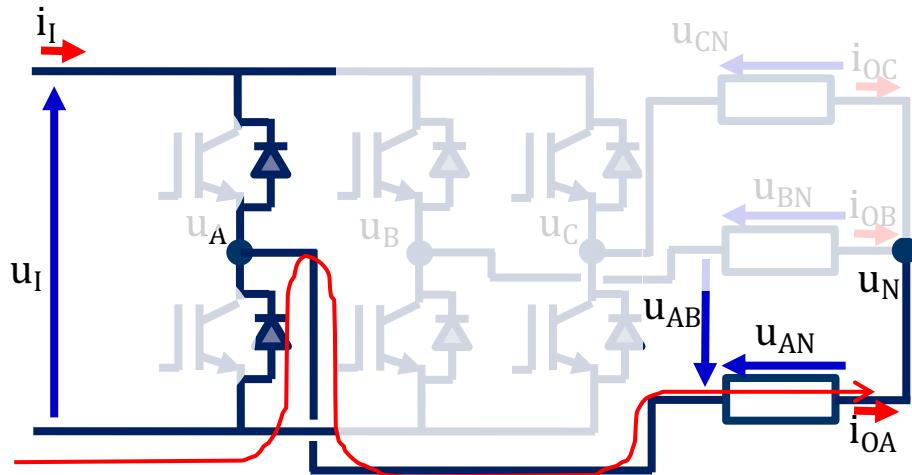
The voltage during the blank times depends on the direction of the line current i_{OA} !!!

Considering **POSITIVE** current:





Three-Phase PWM Inverter



Need for Dead Times:

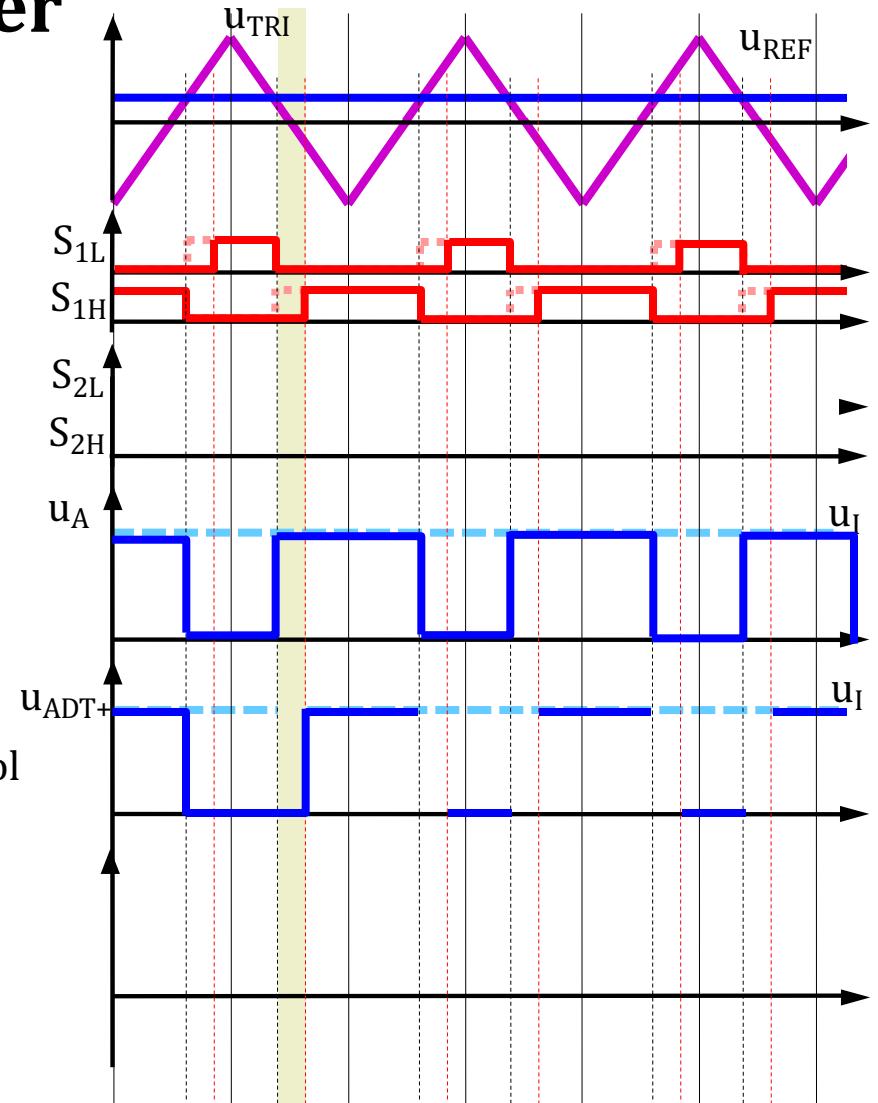
Dead times avoid these cross-conduction problems

Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

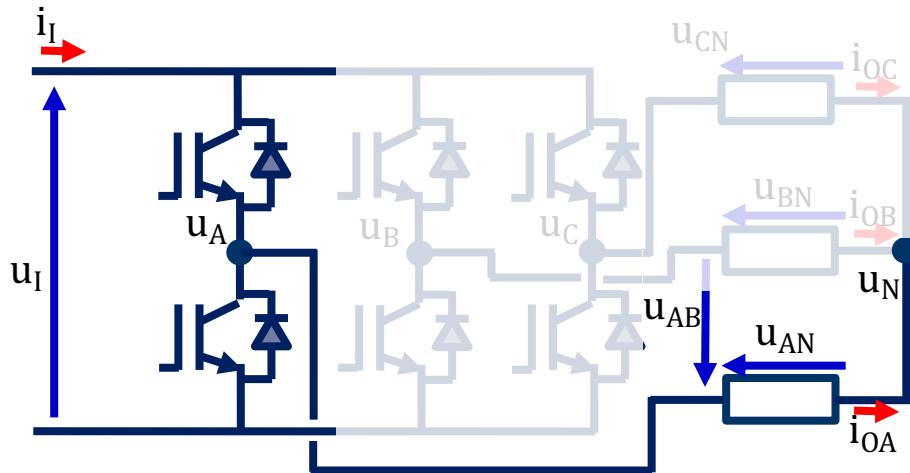
The voltage during the blank times depends on the direction of the line current i_{OA} !!!

Considering **POSITIVE** current:





Three-Phase PWM Inverter



Need for Dead Times:

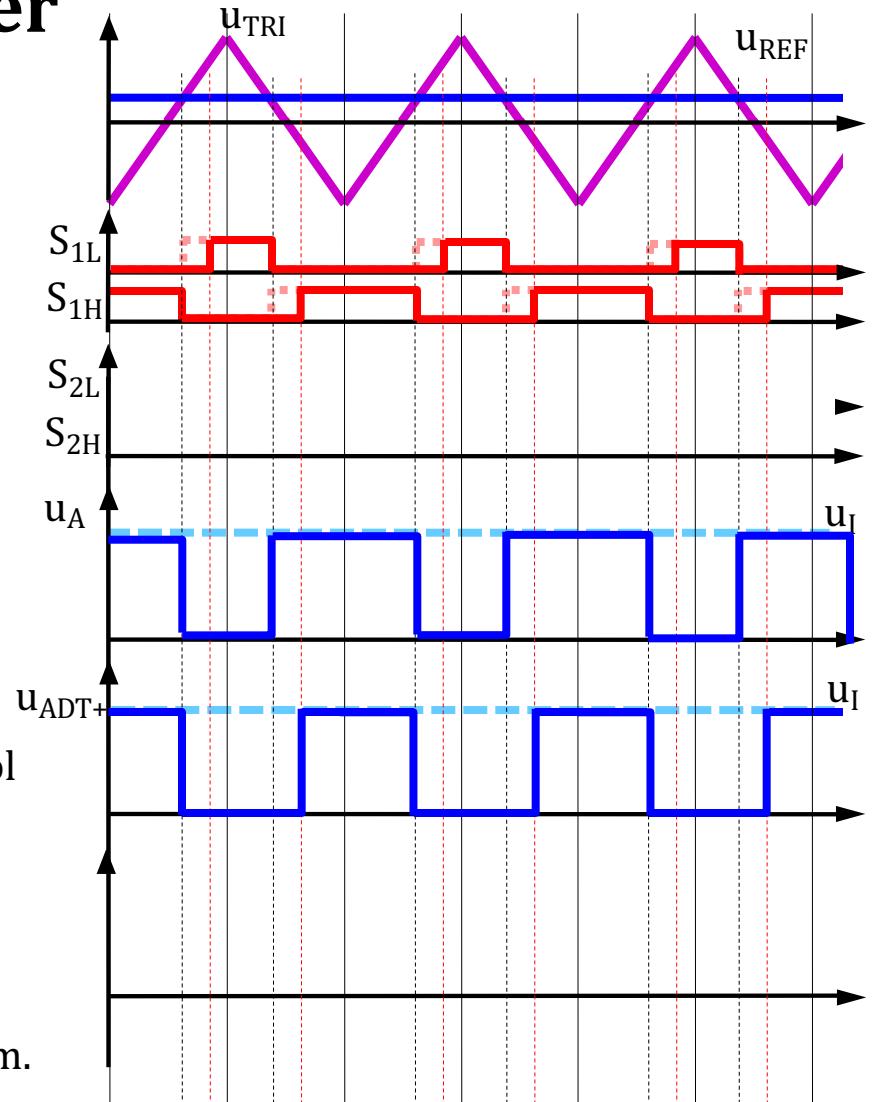
Dead times avoid these cross-conduction problems

Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

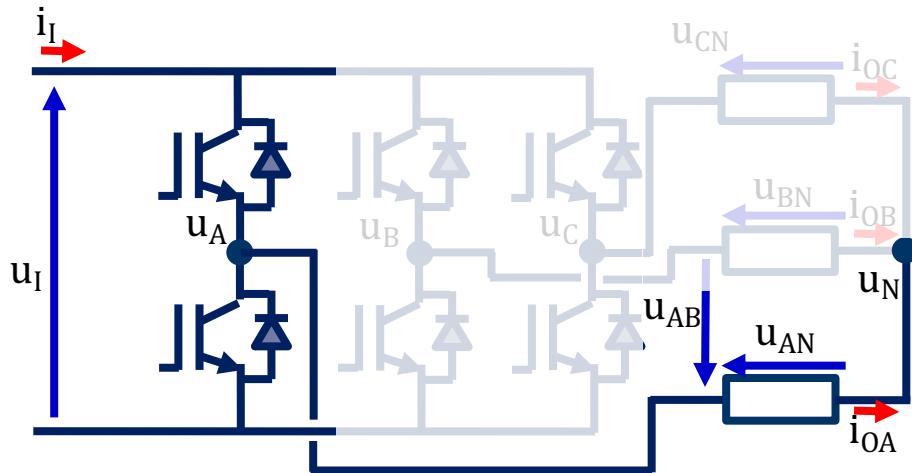
The voltage during the blank times depends on the direction of the line current i_{OA} !!!

Considering **POSITIVE** current: The output phase voltage is **smaller** than the ideal voltage waveform.





Three-Phase PWM Inverter



Need for Dead Times:

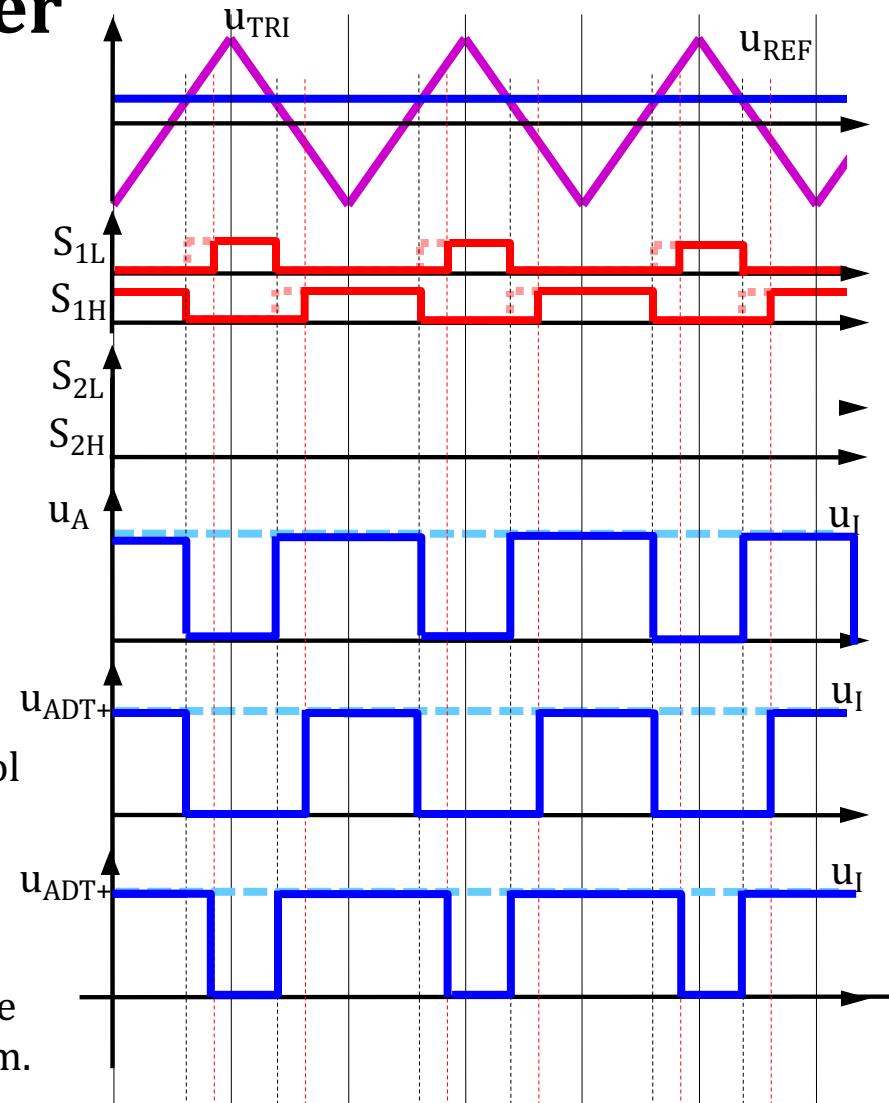
Dead times avoid these cross-conduction problems

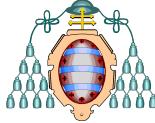
Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

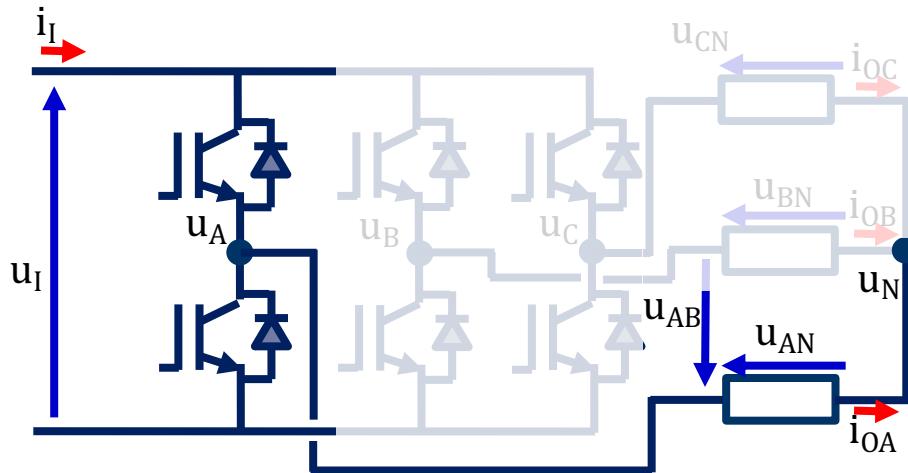
The voltage during the blank times depends on the direction of the line current i_{OA} !!!

Considering **NEGATIVE** current: The output phase voltage is **greater** than the ideal voltage waveform.





Three-Phase PWM Inverter



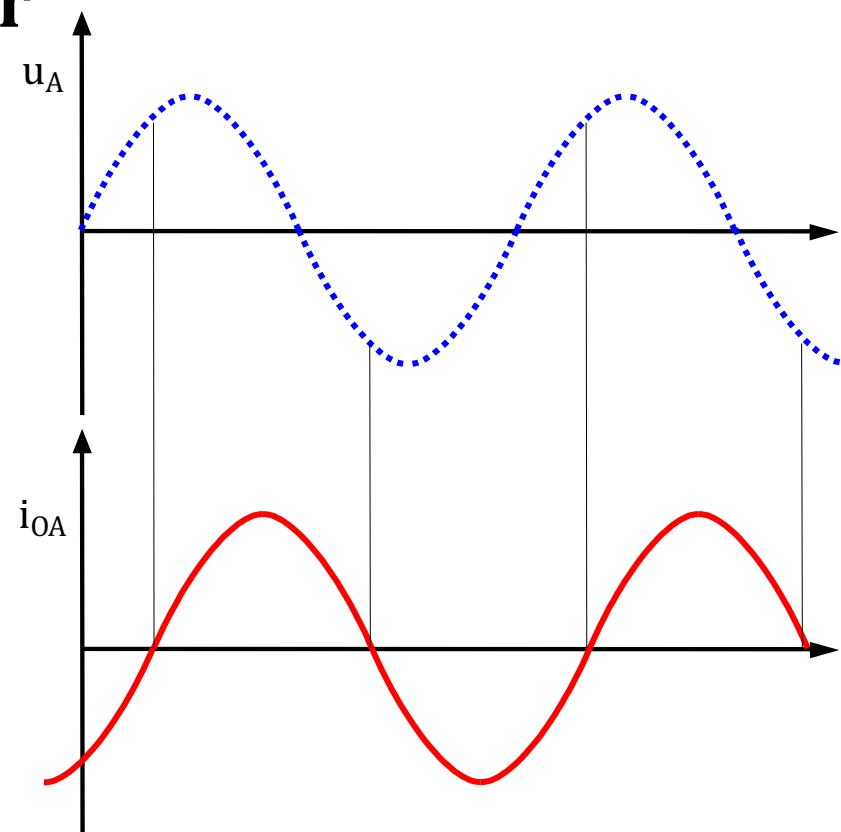
Need for Dead Times:

Dead times avoid these cross-conduction problems

Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

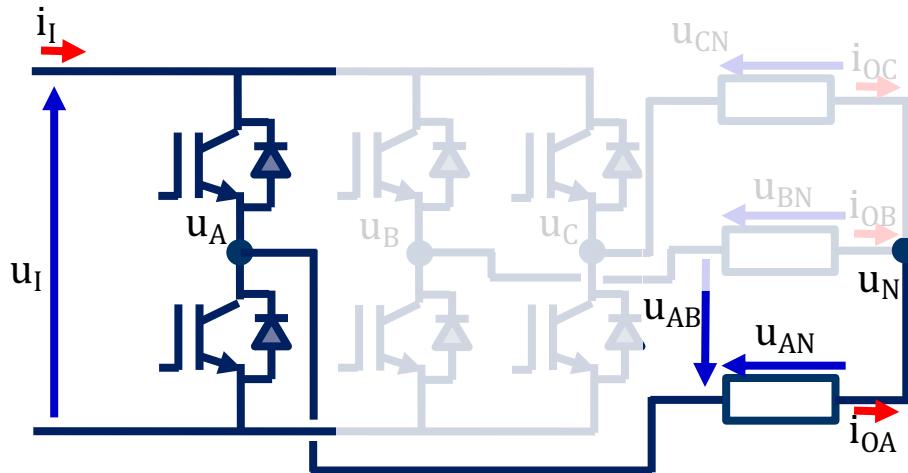
The voltage during the blank times depends on the u_{ADT+} direction of the line current i_{OA} !!!



The dead time implies a distortion in the output voltage waveform, that must be taken into account by the control stage.



Three-Phase PWM Inverter



Need for Dead Times:

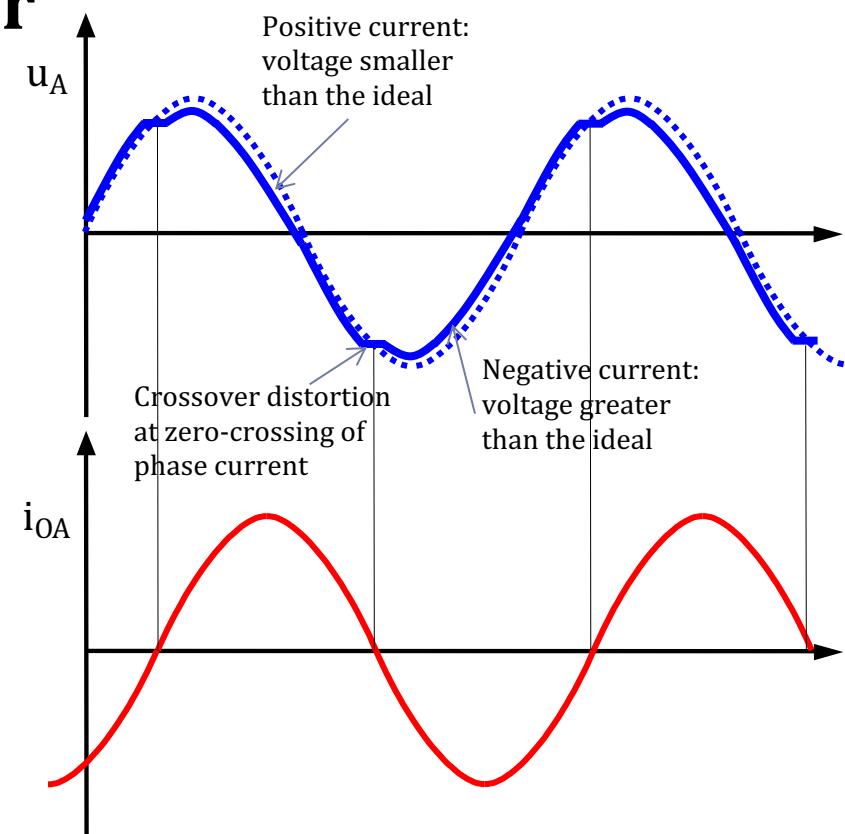
Dead times avoid these cross-conduction problems

Effect of Dead Times:

Consider a dead time at the rising edge of the control waveforms.

The voltage during the blank times depends on the u_{ADT+} direction of the line current i_{OA} !!!

The dead time implies a distortion in the output voltage waveform, that must be taken into account by the control stage.

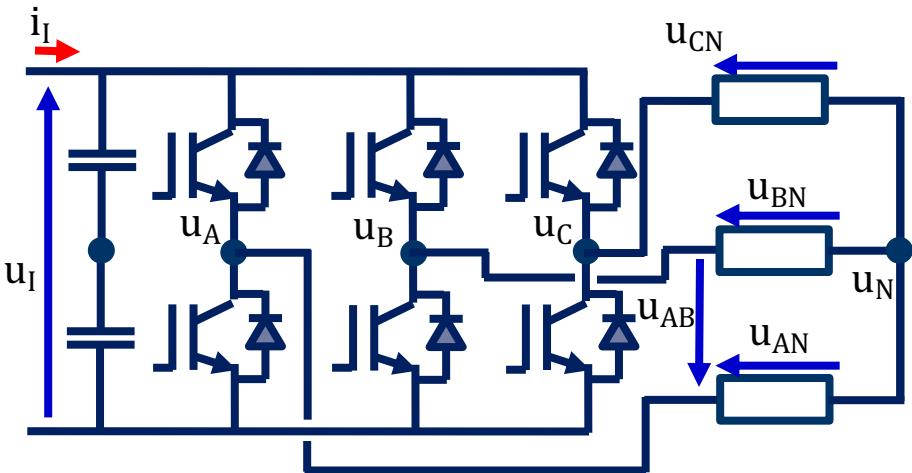




Limitations of the Sine-Triangle PWM Modulation



Three-Phase PWM Inverter



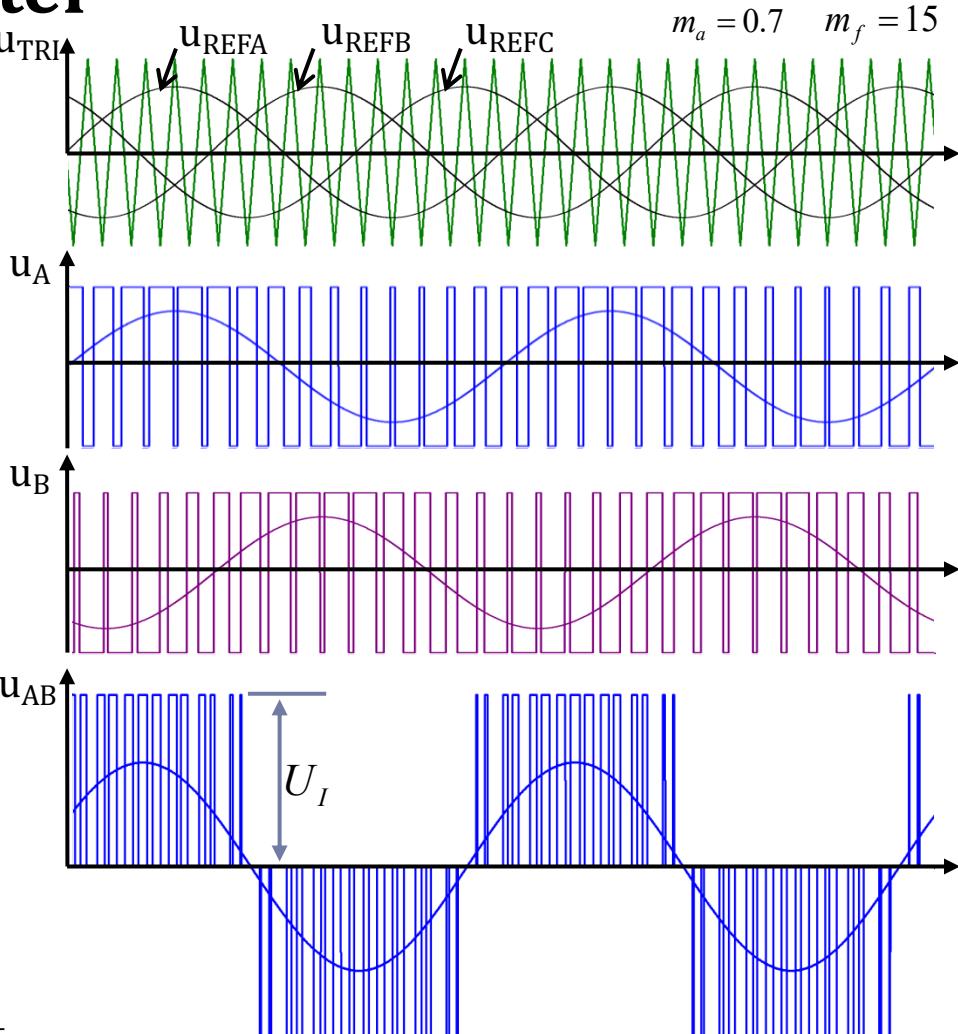
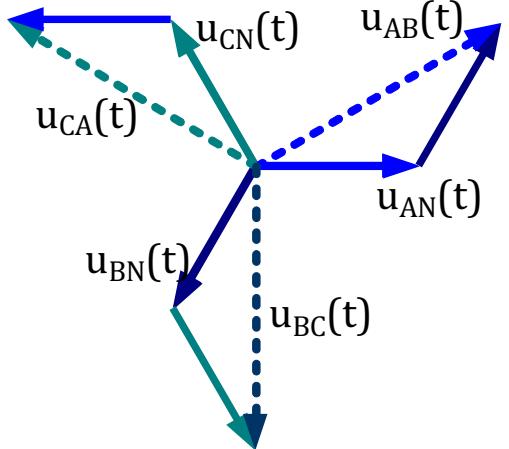
Which is the maximum output voltage reachable?

$$|u_{AN}(t)| = m_a \frac{U_I}{2}$$

$$u_{AN\langle RMS \rangle} = m_a \frac{U_I}{2\sqrt{2}}$$

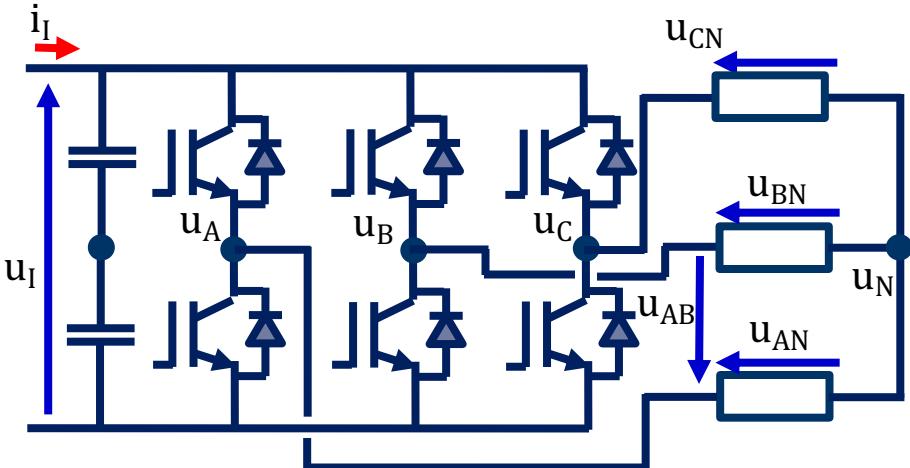
$$|u_{AB}(t)| = \frac{m_a \cdot U_I}{2} \cdot \sqrt{3}$$

$$u_{AB\langle RMS \rangle} = m_a \frac{U_I \sqrt{3}}{2\sqrt{2}}$$



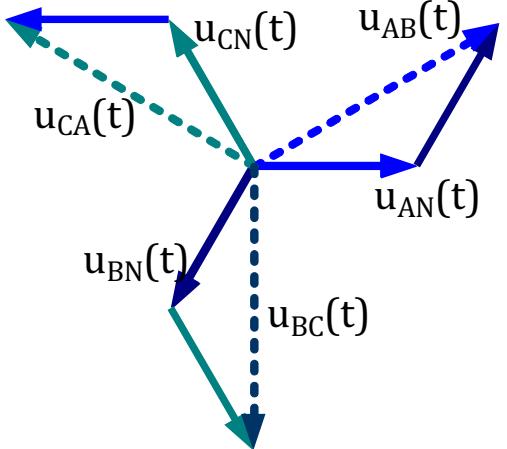


Three-Phase PWM Inverter



Which is the maximum output voltage reachable?

$$m_a = 1$$

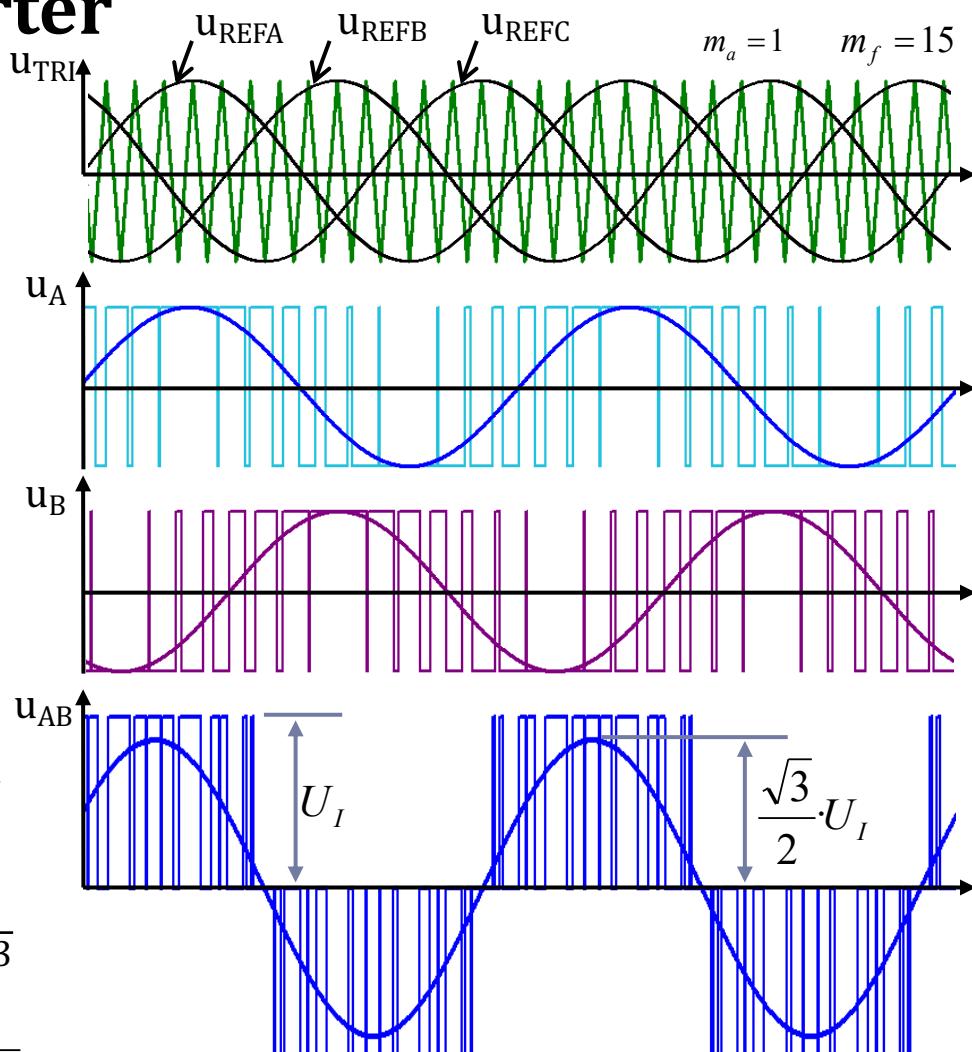


$$|u_{AN}(t)| = m_a \frac{U_I}{2}$$

$$u_{AN\langle RMS \rangle} = m_a \frac{U_I}{2\sqrt{2}}$$

$$|u_{AB}(t)| = \frac{m_a \cdot U_I}{2} \cdot \sqrt{3}$$

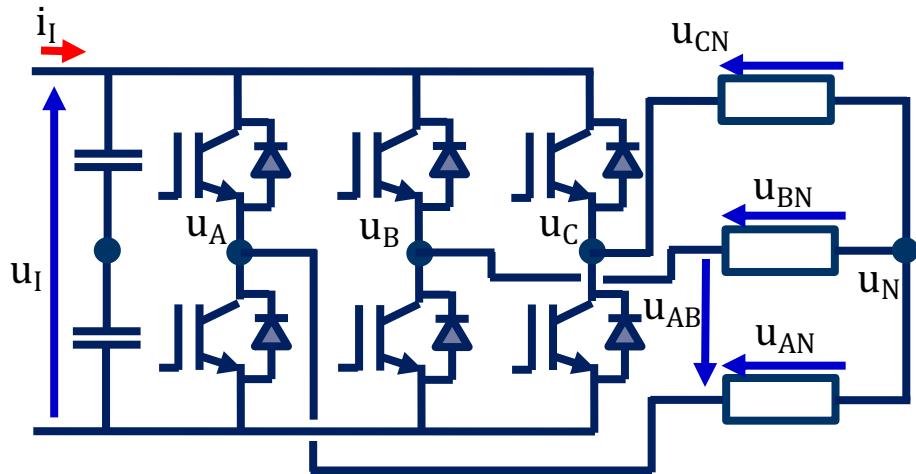
$$u_{AB\langle RMS \rangle} = m_a \frac{U_I \sqrt{3}}{2\sqrt{2}}$$



Is it possible to reach a higher line-to-line voltage?

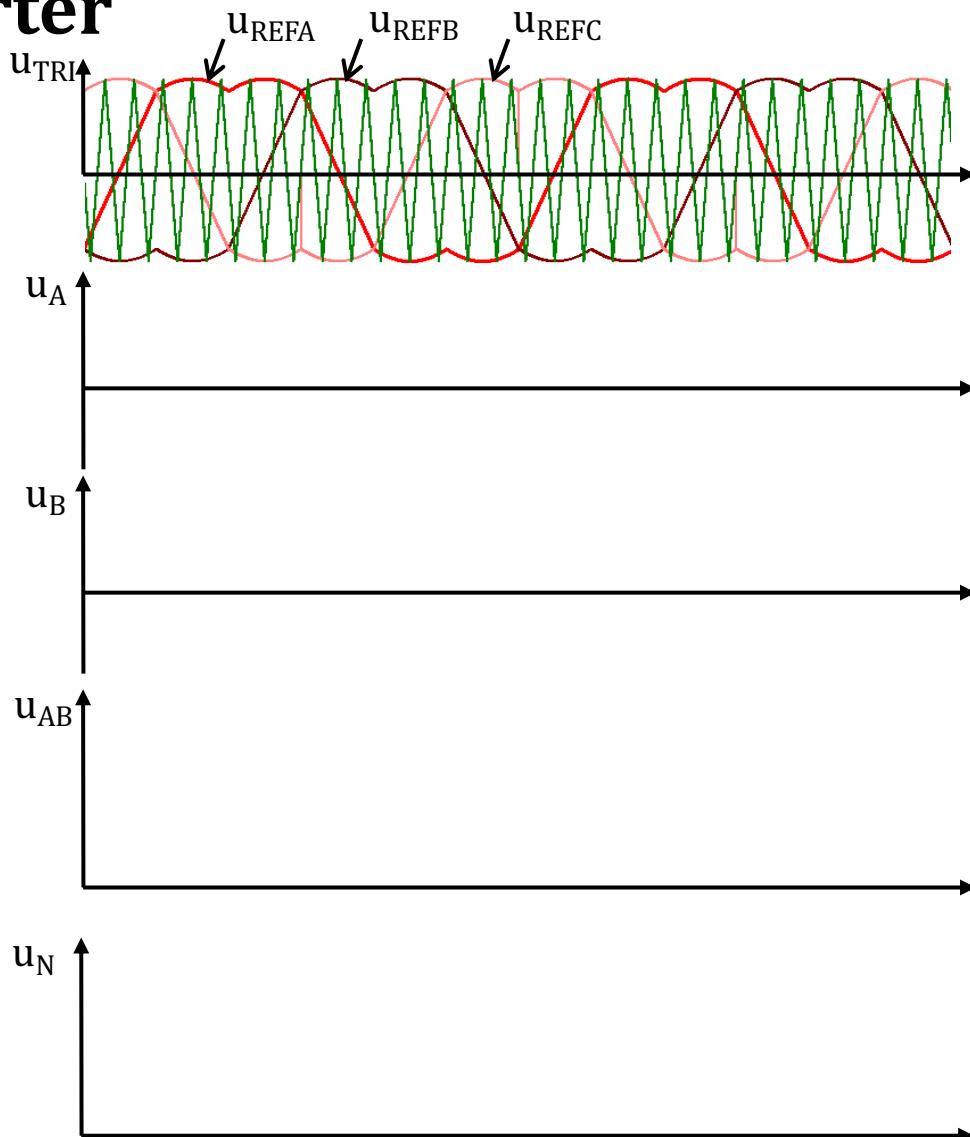


Three-Phase PWM Inverter



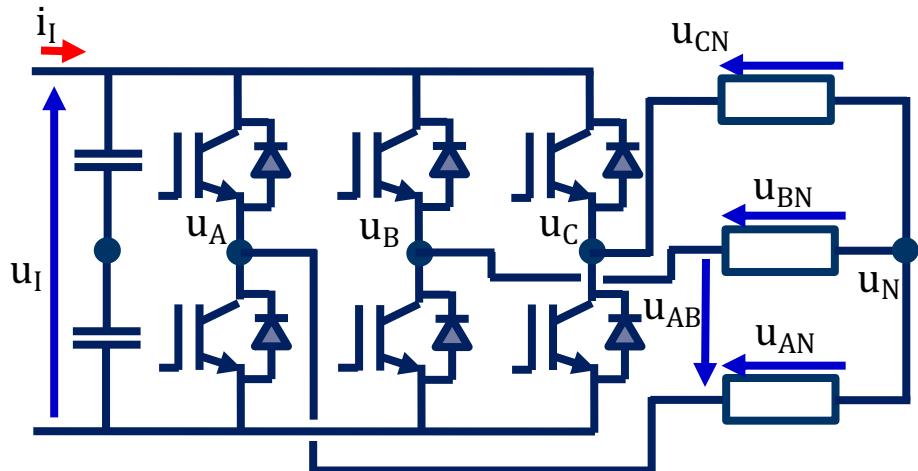
Which is the maximum output voltage?

Consider modulating waveforms different than pure sine waves.



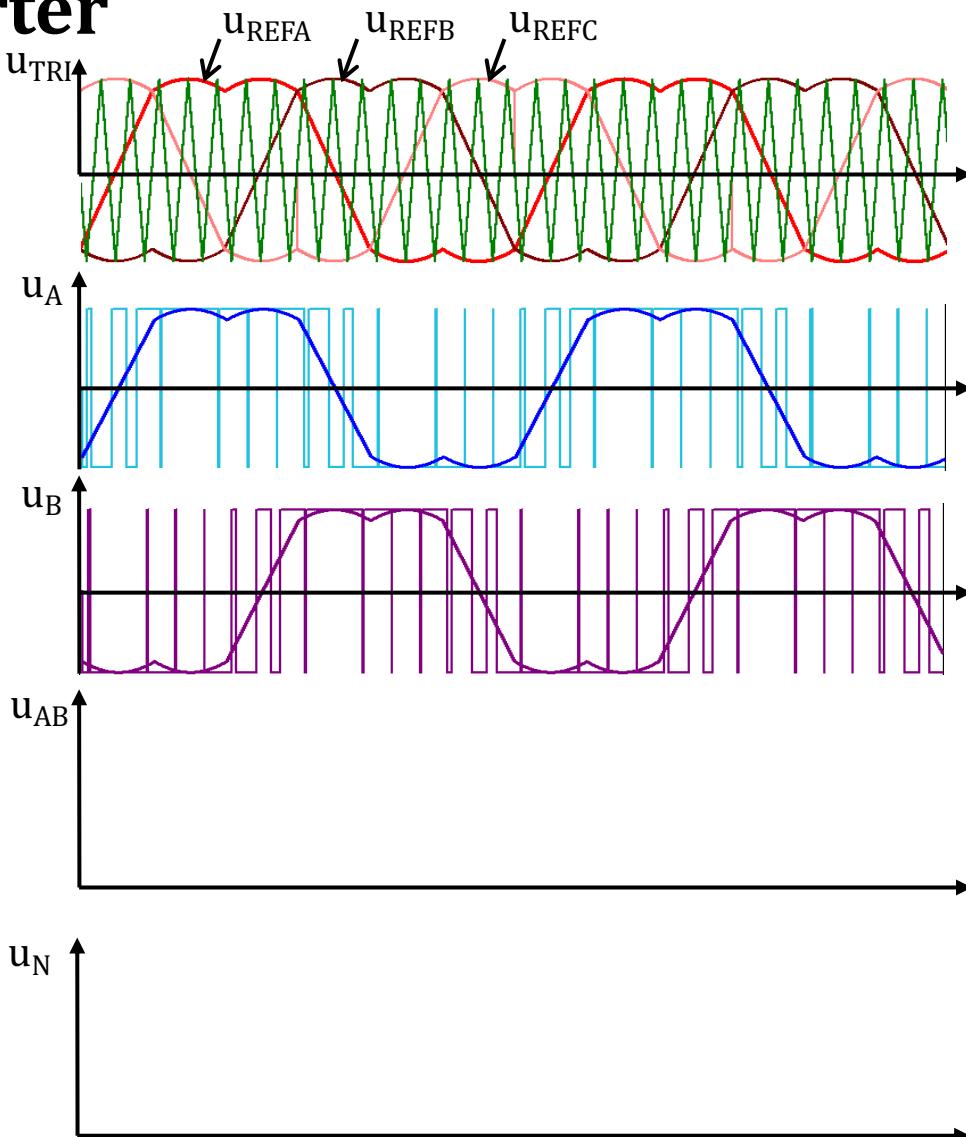


Three-Phase PWM Inverter



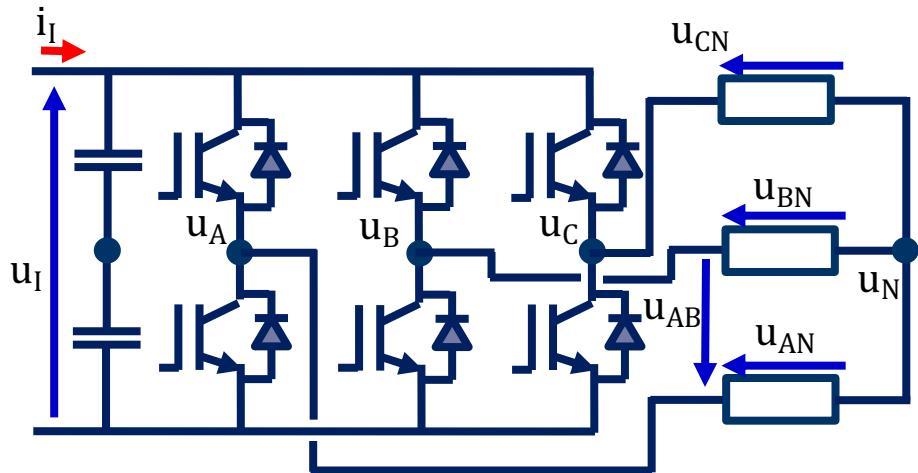
Which is the maximum output voltage?

Consider modulating waveforms different than pure sine waves.





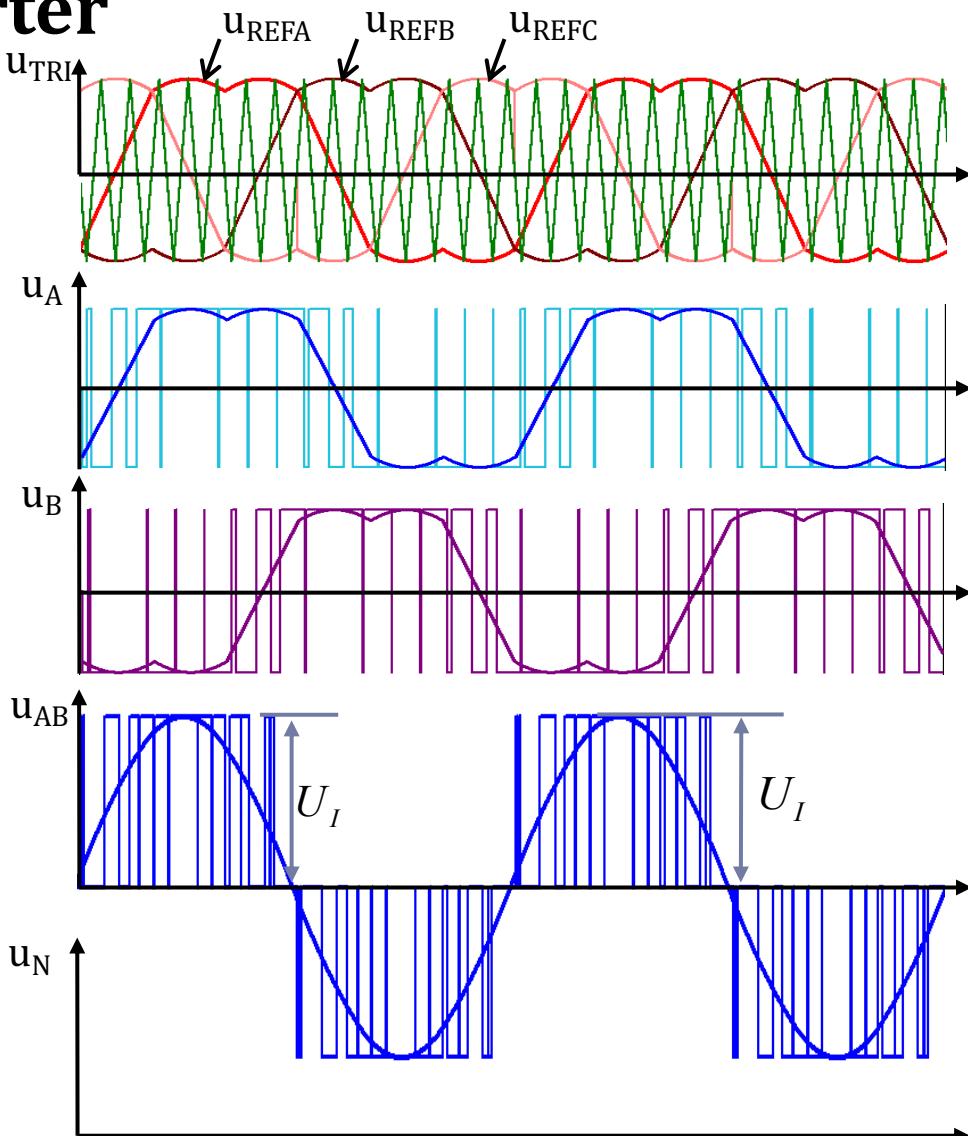
Three-Phase PWM Inverter



Which is the maximum output voltage?

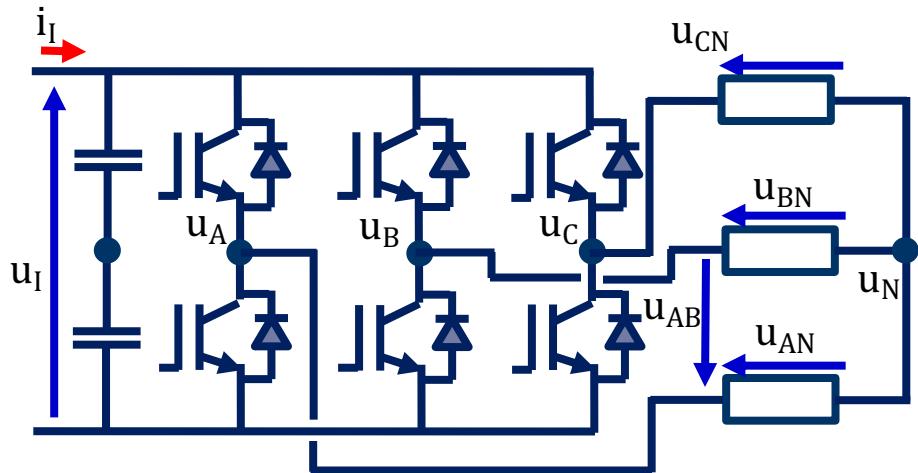
Consider modulating waveforms different than pure sine waves.

The line-to-line voltage is a pure sine waveform, with higher amplitude than with the sine-triangle modulation





Three-Phase PWM Inverter



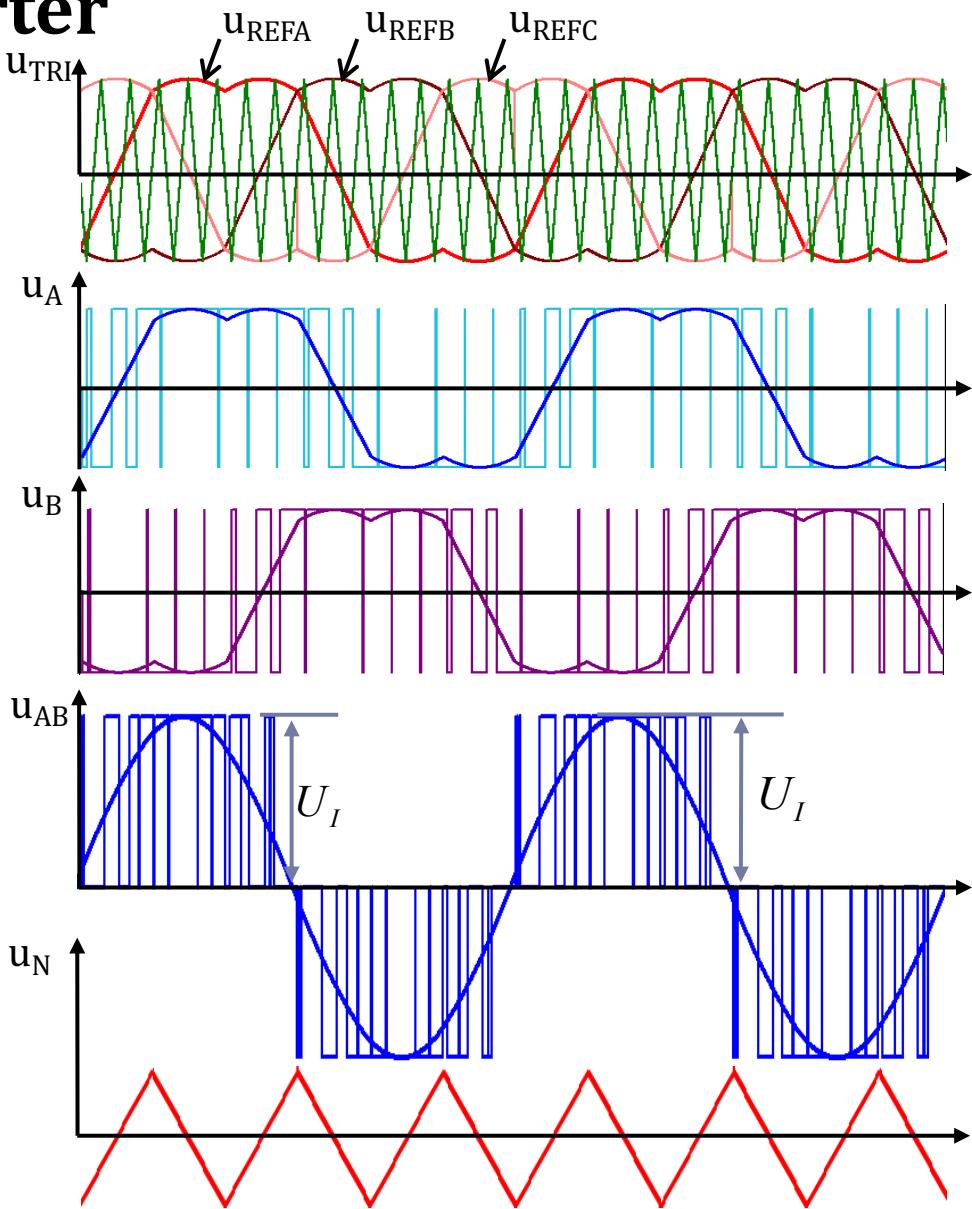
Which is the maximum output voltage?

Consider modulating waveforms different than pure sine waves.

The line-to-line voltage is a pure sine waveform, with higher amplitude than with the sine-triangle modulation

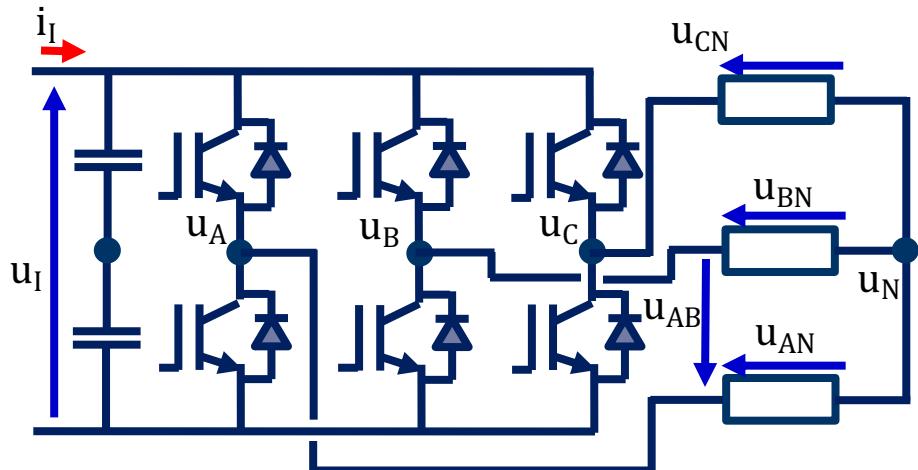
A voltage appears at the neutral point.

...but the phase-to neutral voltage is again a sinusoidal waveform!!!



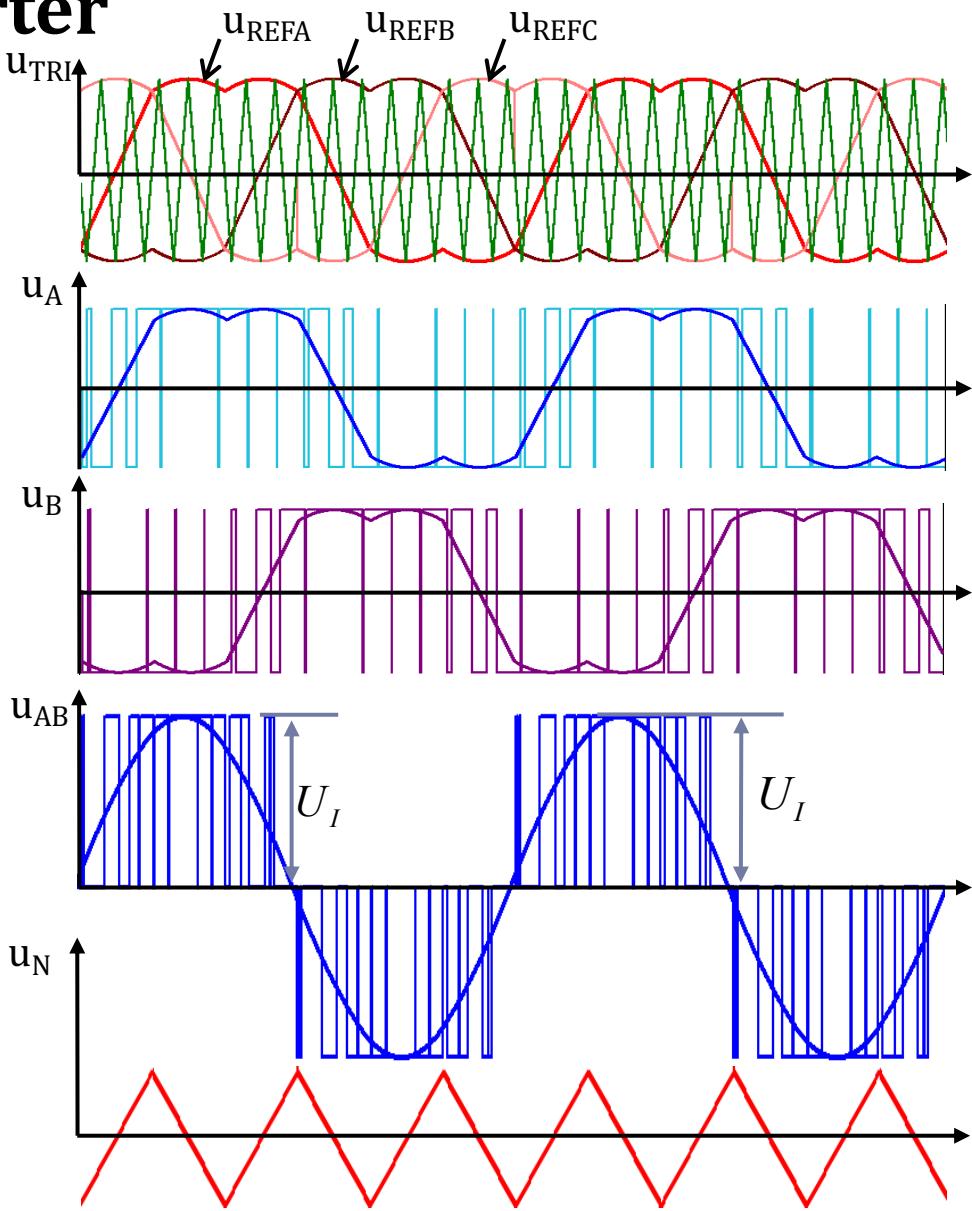


Three-Phase PWM Inverter



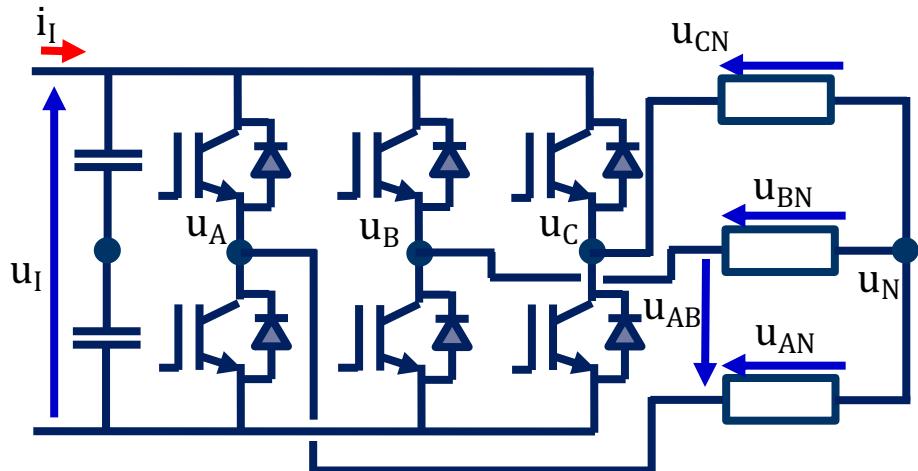
More complex modulation schemes can be implemented in the control of PWM inverters.

The Space Vector Modulation (SVM) is an algorithm for the control of PWM inverters (mainly three-phase). The development of this technique provides inherently the adequate control waveforms for obtaining the desired output voltage waveforms.





Three-Phase PWM Inverter

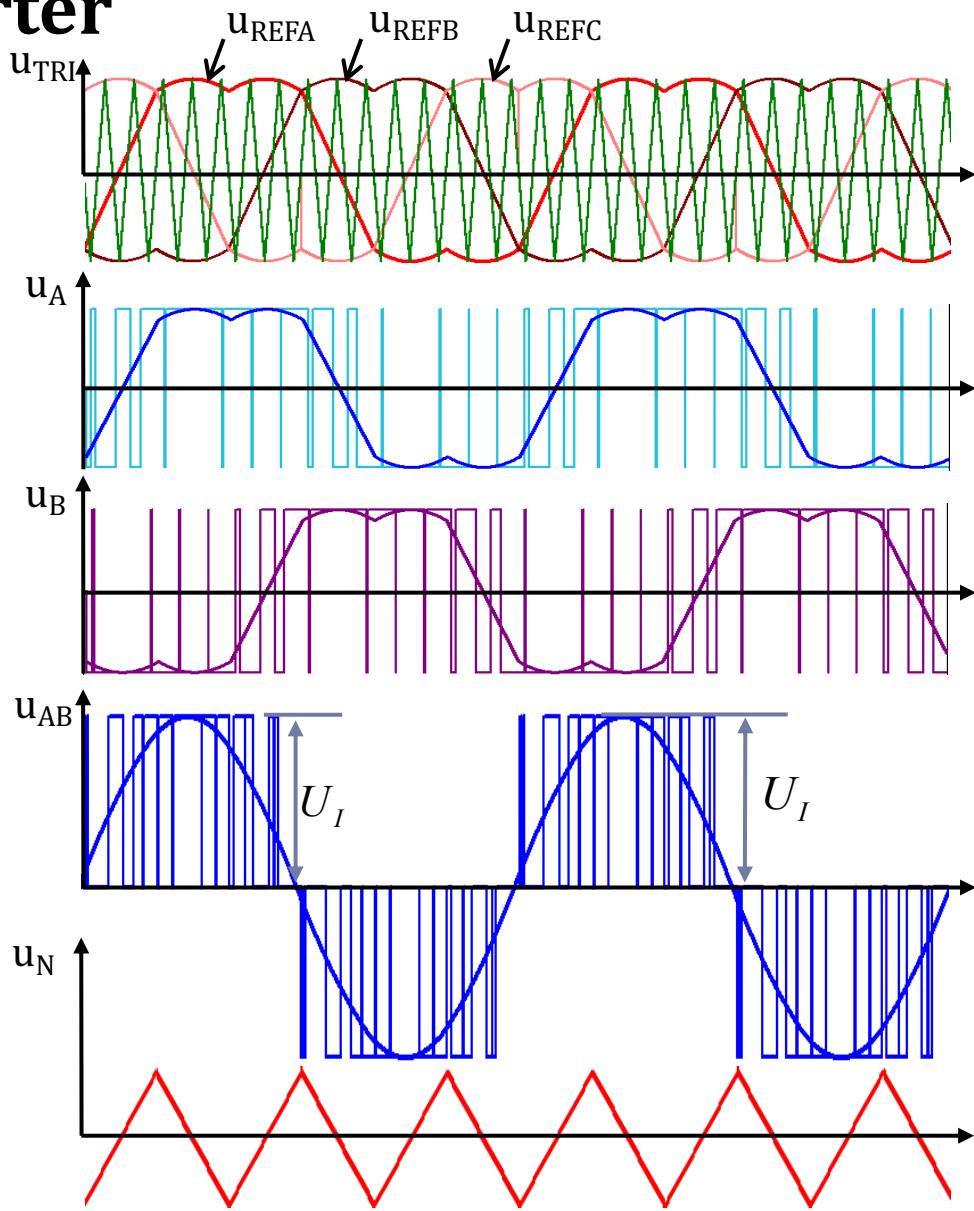


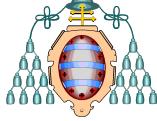
Task:

- Simulate a 3 phase inverter, with usual sine-triangle modulation.
- Try to increase the line-to-line voltage obtained beyond the maximum value possible with sine-triangle modulation only. Try to use different waveforms for modulation, try to add a voltage to the neutral, explore what happens with the 3rd harmonic...)

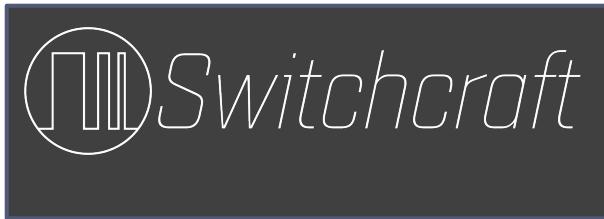
Input voltage: 3-phase system, 125 VRMS line to neutral, 60 Hz. Switching frequency=12kHz.

Load: Resistive balanced load, 5 ohms per phase.





Space Vector PWM



<https://www.switchcraft.org/>

SPACE VECTOR PWM INTRO

MAY 1, 2017

BY YNGVE SOLBAKKEN

<https://www.switchcraft.org/learning/2017/3/15/space-vector-pwm-intro>

VECTOR CONTROL FOR DUMMIES

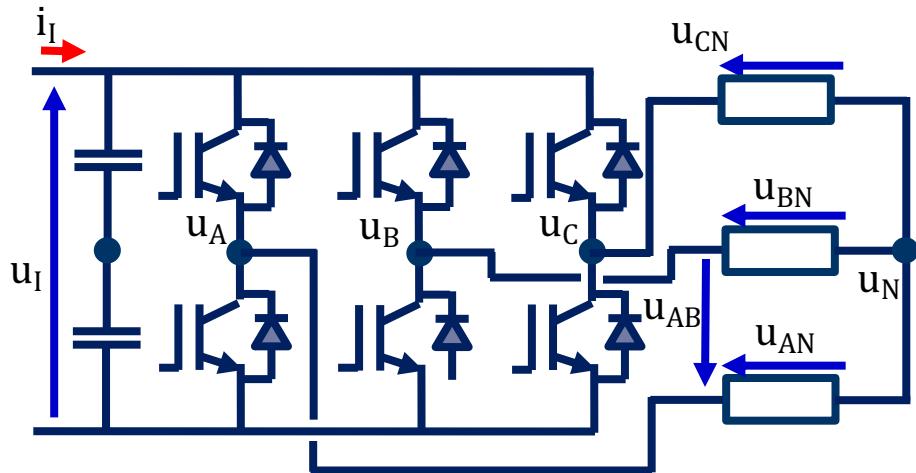
MAY 14, 2017

BY YNGVE SOLBAKKEN

<https://www.switchcraft.org/learning/2016/12/16/vector-control-for-dummies>

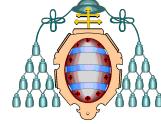


SV PWM

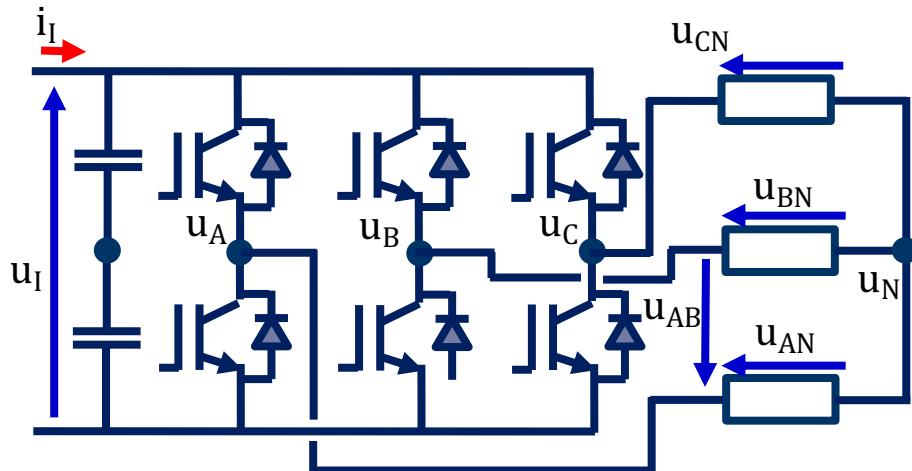


The three phased system is illustrated using two different, but equal forms:

- A vector diagram showing all three phases and their vector sum (*space vector*).
- An ordinary instantaneous sine wave representation, also showing the resultant space vector.

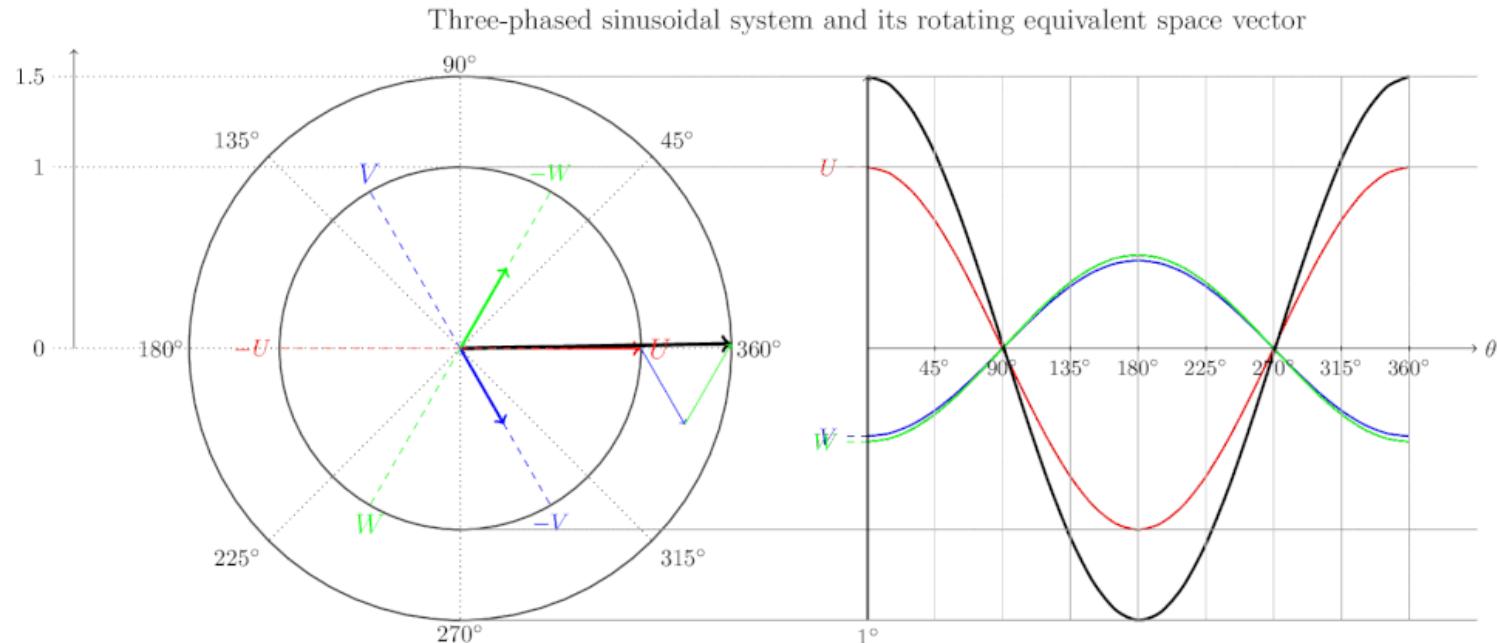


SV PWM



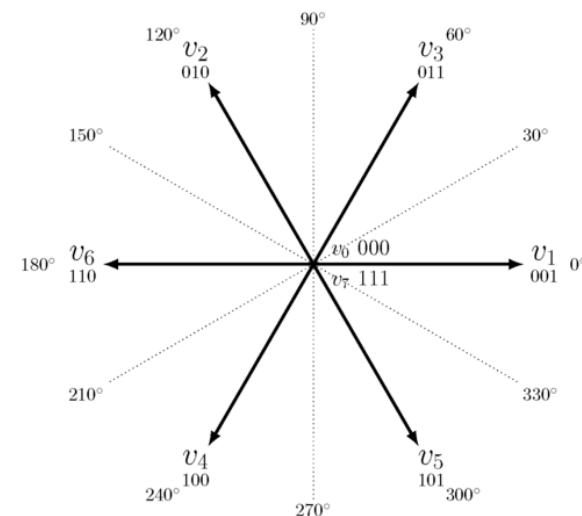
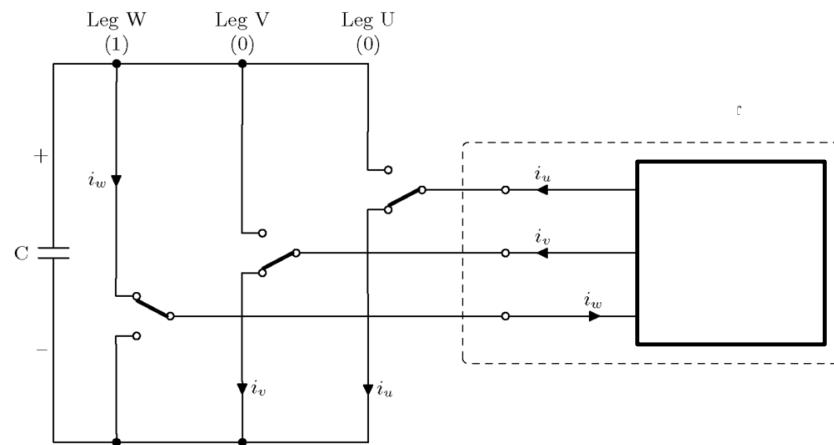
The three phased system is illustrated using two different, but equal forms:

- A vector diagram showing all three phases and their vector sum (*space vector*).
- An ordinary instantaneous sine wave representation, also showing the resultant space vector.

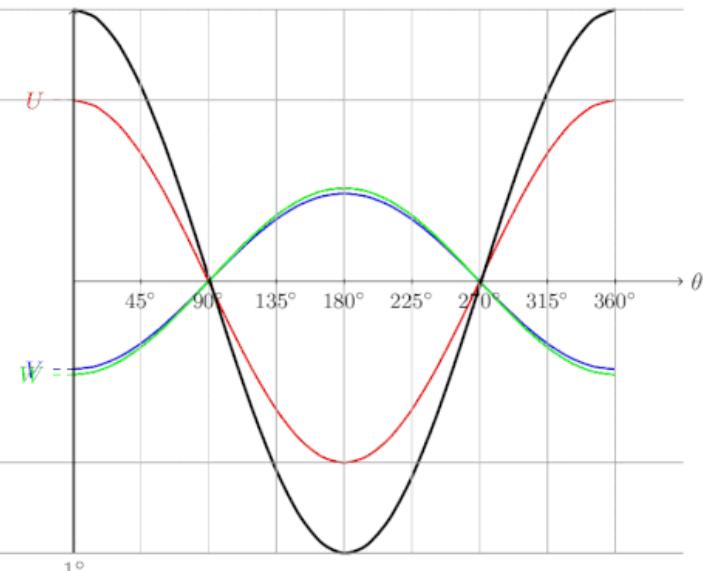
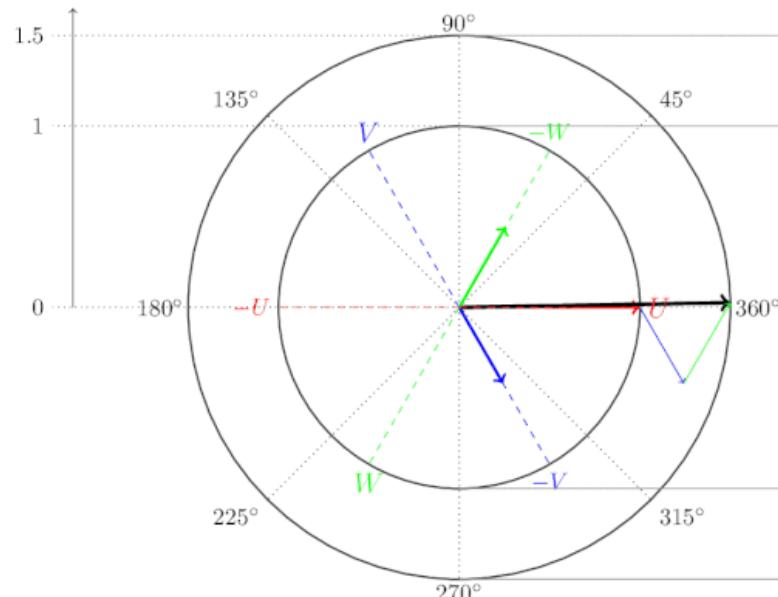




SV PWM



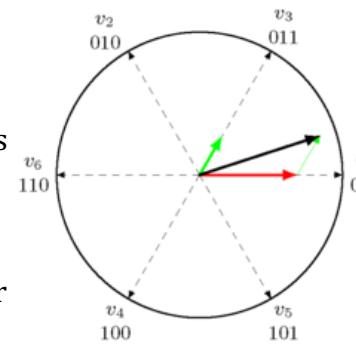
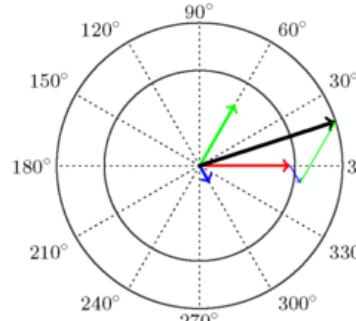
Three-phased sinusoidal system and its rotating equivalent space vector





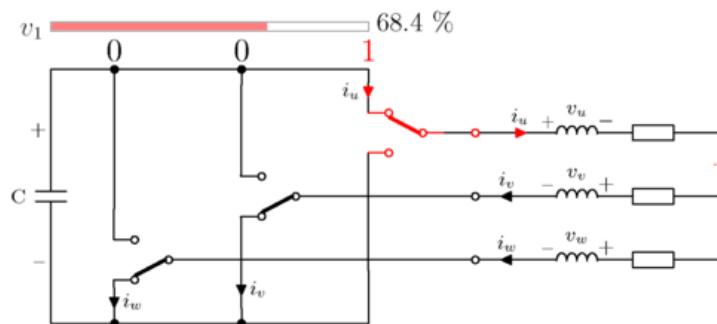
SV PWM

1) The 3 phase system forming the reference vector. It is assumed that the desired voltage reference is already available, e.g calculated by the reverse Clarke/Park transformation

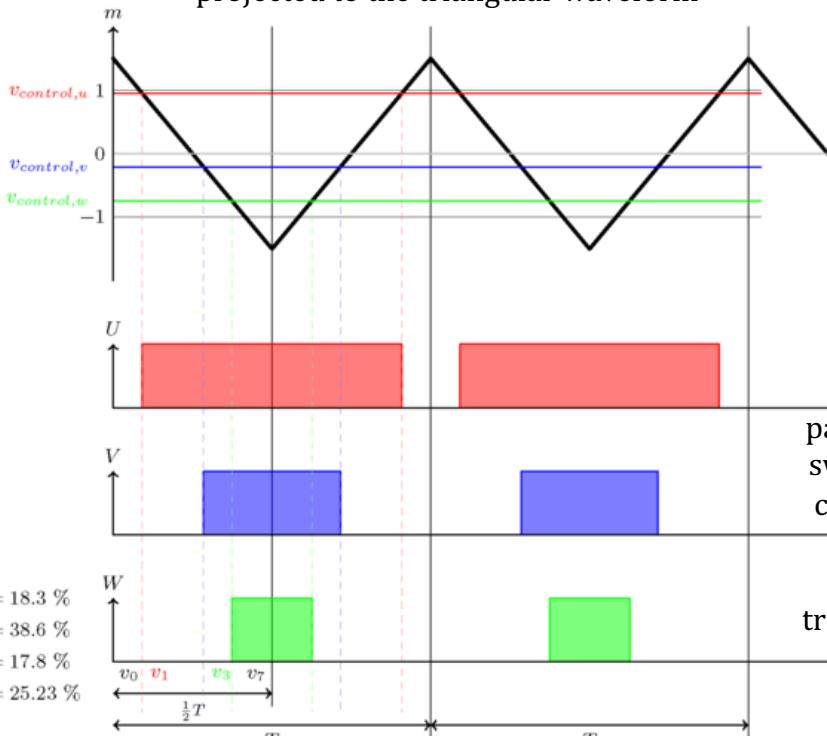


$$\begin{aligned}v_0 &= 18.3\% \\v_1 &= 38.6\% \\v_3 &= 17.8\% \\v_7 &= 25.23\%\end{aligned}$$

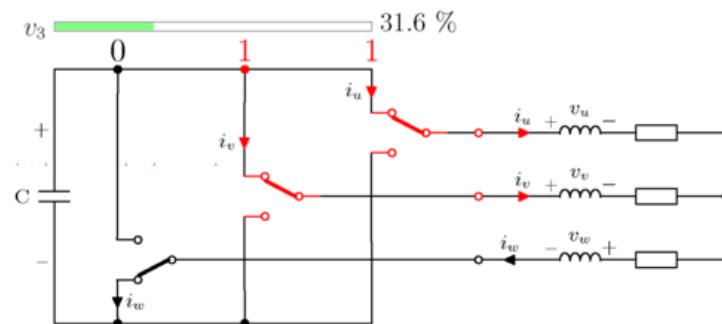
4) The switching pattern gives the space vector sequence:
000=>001=>011=>111 and viceversa,
 $\frac{s}{\varphi} = 1$
And also the time intervals for each vector. $x = 0.68419$
 $y = 0.31581$



2) The amplitudes of the 3 phase system voltages are projected to the triangular waveform



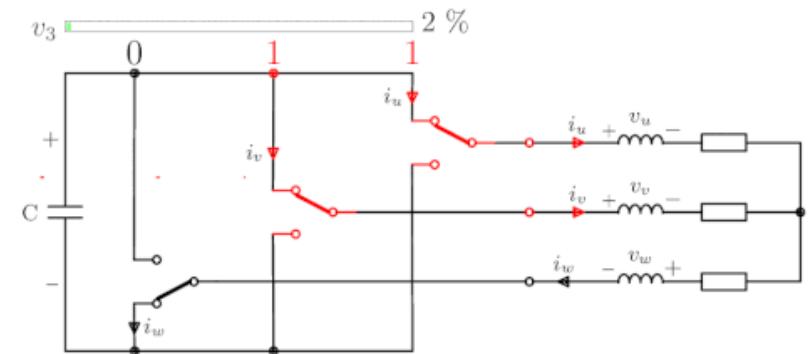
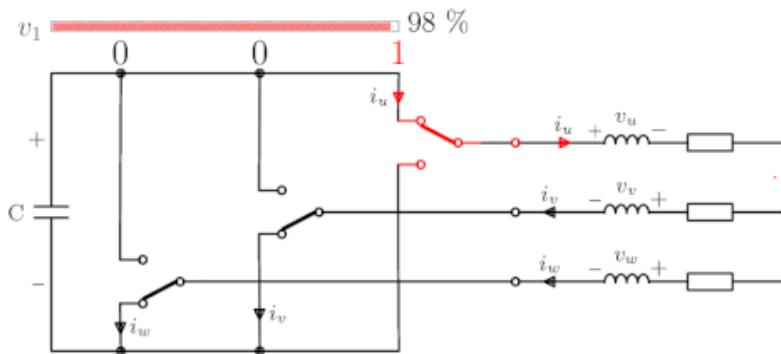
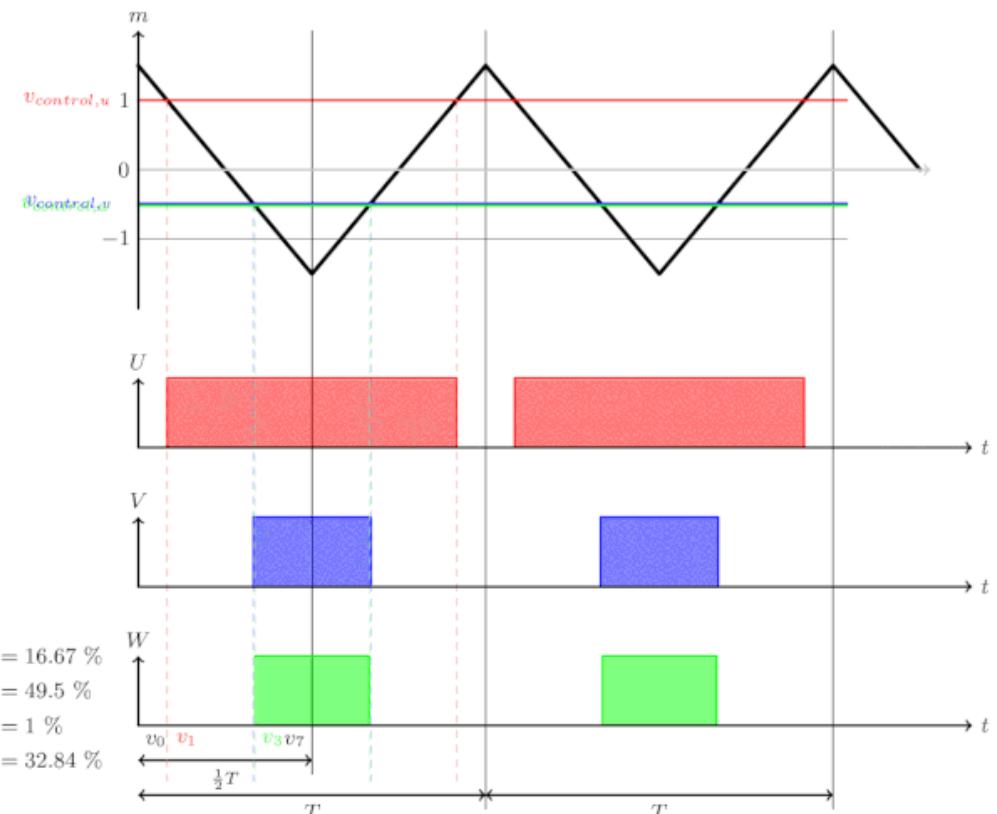
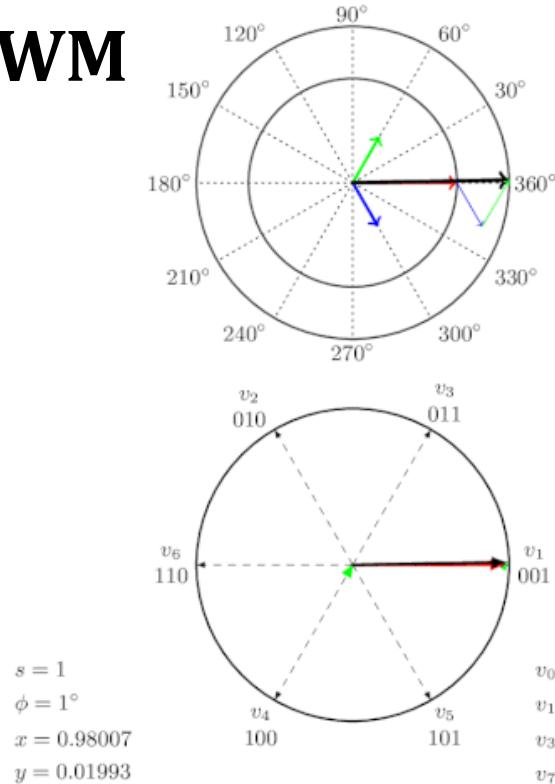
3) The switching pattern of the upper switches (lower are complementary) is generated by comparing to the triangular waveform





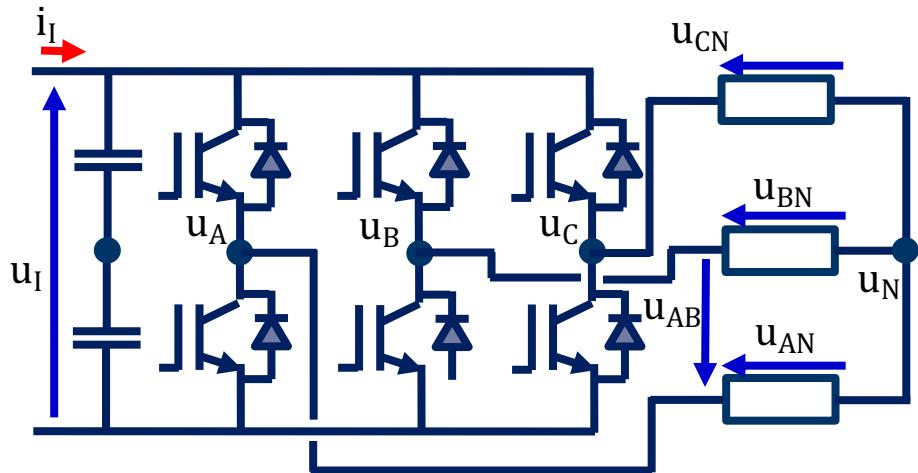
Industrial Electronics in renewable energy generation systems

SV PWM





SV PWM



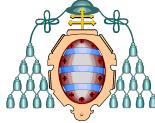
Conclusions:

- Every pattern starts and ends with a zero vector, and that between every transition, only one switch is being changed. This issue:
 - a) decreases switching losses (increases power density, simplifies cooling systems)
 - b) greatly reduces harmonics (THD)
- Easy to include 3rd harmonic injection, therefore:
 - a) higher voltage to the load/grid.
 - b) Greater DC-bus voltage utilization

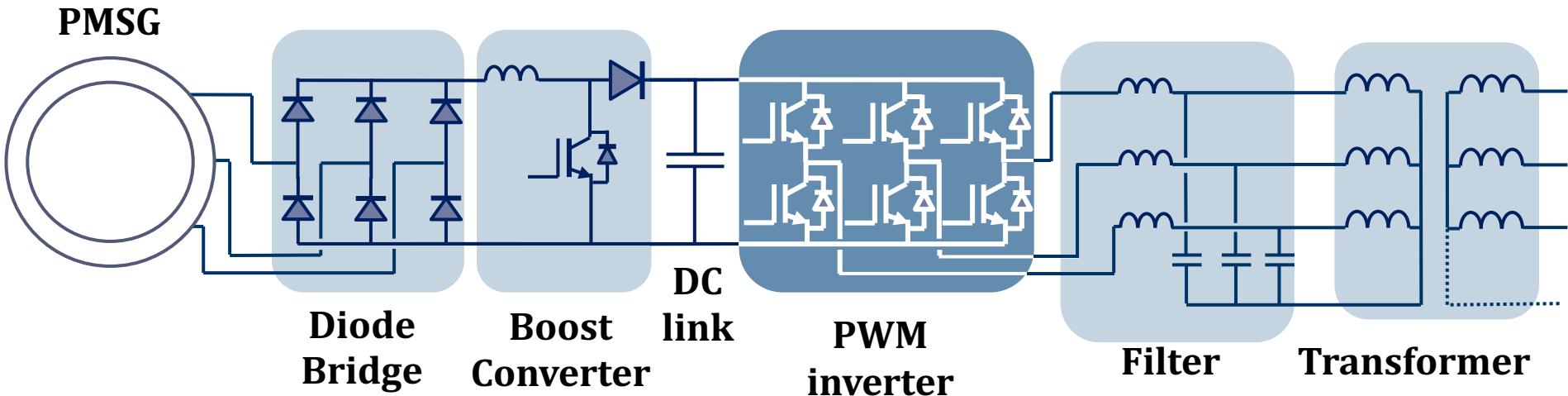
SVPWM is an advanced; computation intensive PWM method and possibly the best techniques for variable frequency drive application.



Consideration for dynamic analysis

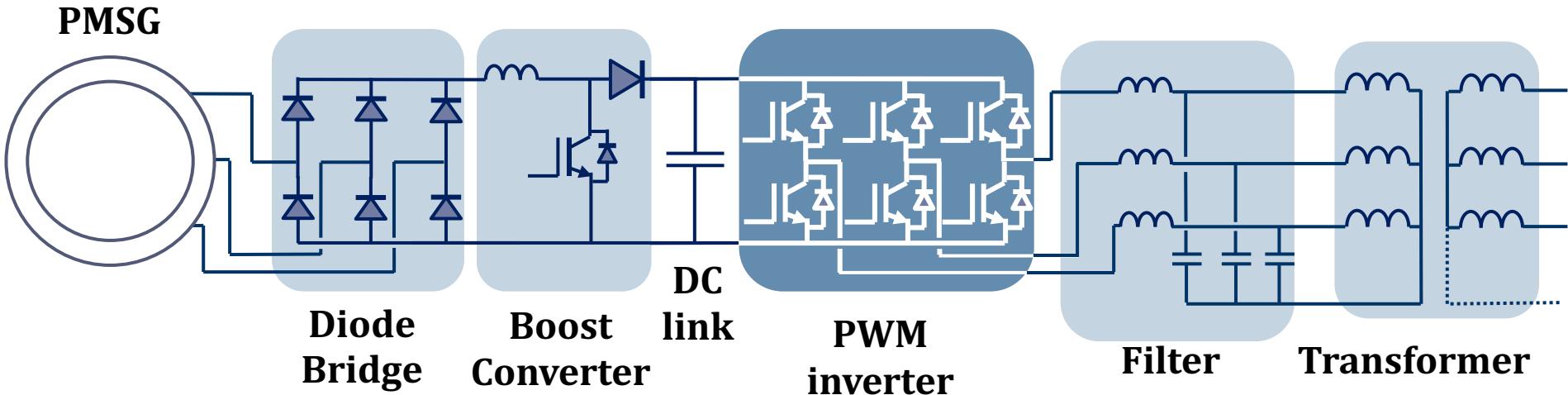


Three-Phase PWM Inverter





Three-Phase PWM Inverter

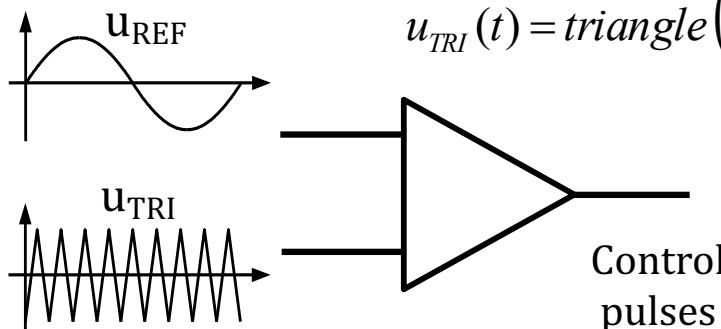


If we consider the filter/load as another block of the system, then **the Dynamic analysis of the PWM inverter is very simple:**

$$u_{REF}(t) = u_{REF \langle PEAK \rangle} \cdot \sin(2\pi \cdot f_R \cdot t)$$

$$u_{TRI}(t) = \text{triangle}\left(u_{TRI \langle PEAK \rangle}, T_S\right)$$

$$\langle u_{Phase}(t) \rangle_{T_S} = u_I \cdot m_a \cdot \sin(2\pi \cdot f_R \cdot t)$$



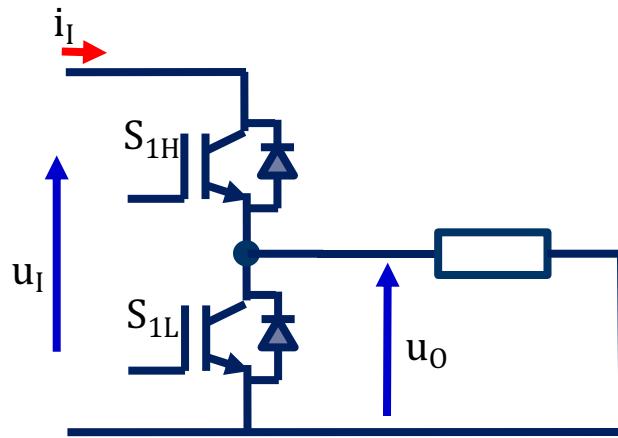
No elements that store energy: NO DYNAMICS
(Except for dead times, switching losses, etc...)



Derivation of the buck and boost converters

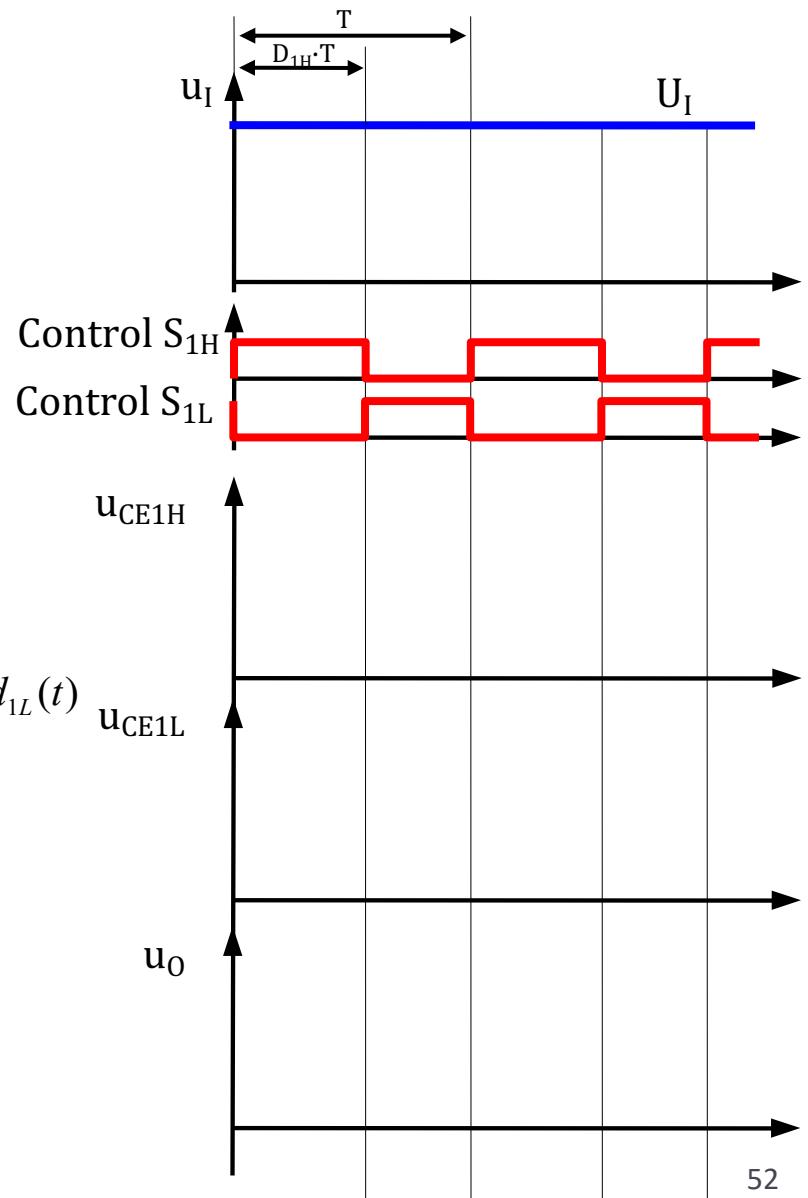


The PWM inverter: 1 leg



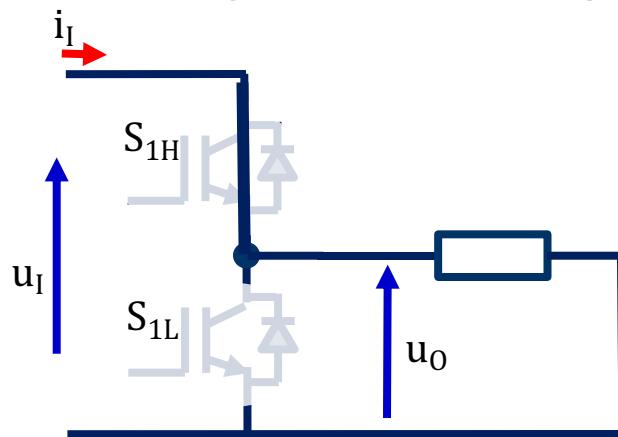
Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$





The PWM inverter: 1 leg

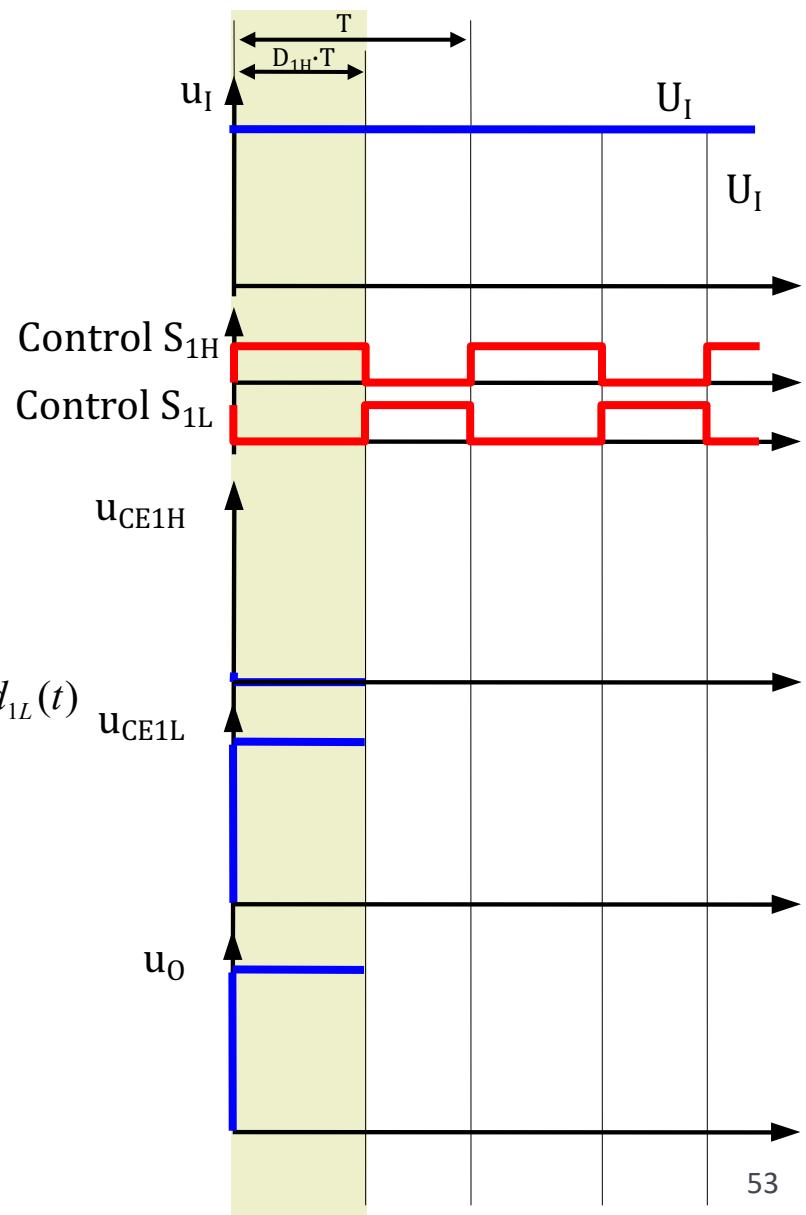


Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$

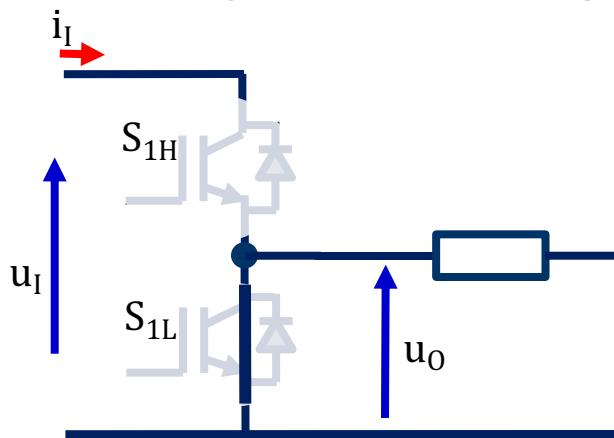
If Switch S_{1H} is ON $0 \leq t < d_{1H}(t) \cdot T$

$$u_O(t) = U_I$$





The PWM inverter: 1 leg

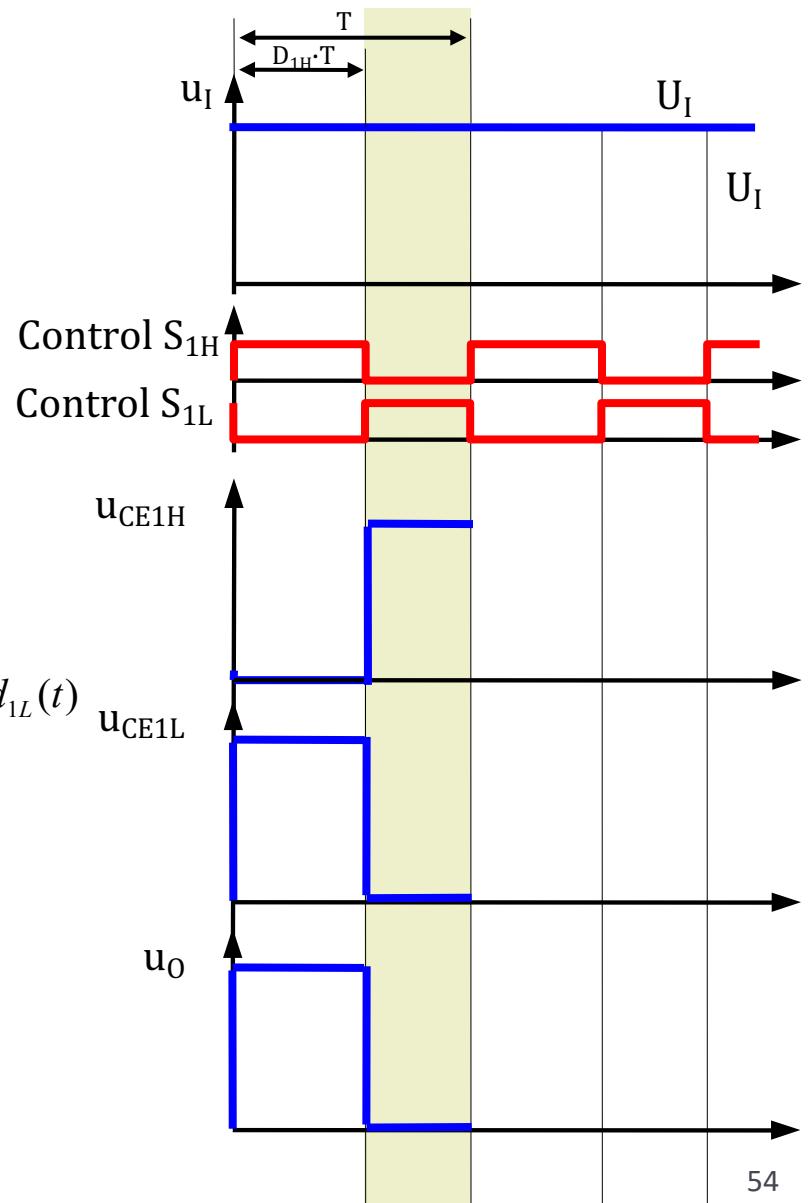


Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$

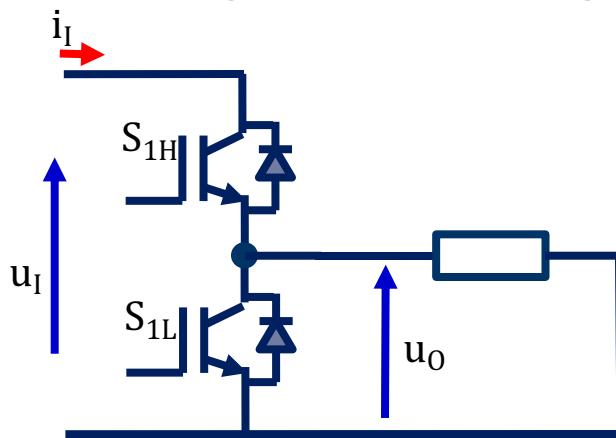
If Switch S_{1H} is OFF $d_{1H}(t) \cdot T \leq t < T$

$$u_O(t) = 0$$





The PWM inverter: 1 leg



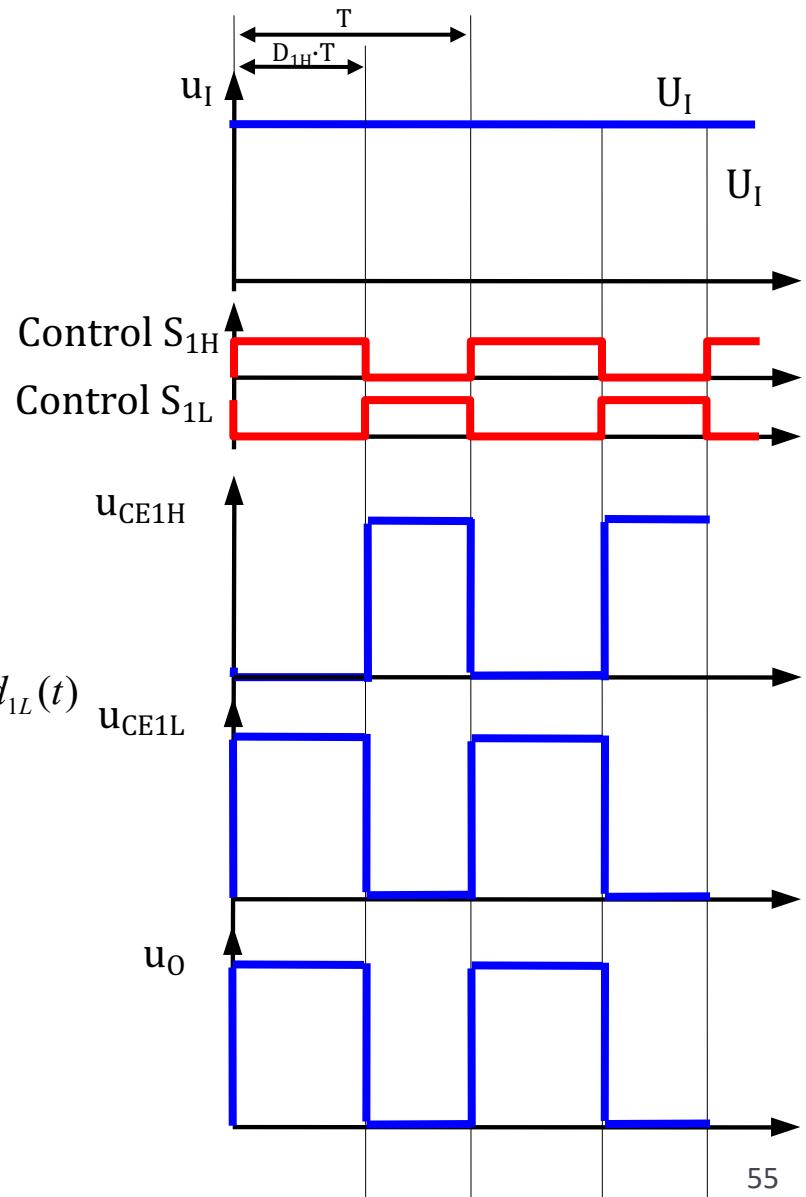
Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$

$$u_O(t) = \begin{cases} U_I & 0 \leq t < D_{1H} \cdot T \\ 0 & D_{1H} \cdot T \leq t < T \end{cases}$$

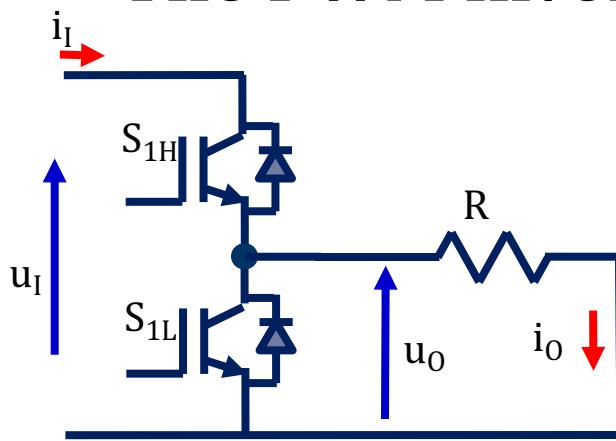
$$\langle x(t) \rangle_T = \frac{1}{T} \int_t^{t+T} x(\tau) d\tau \quad \text{Averaged value of } x(t) \text{ during a period } T$$

$$u_{O\langle AVG \rangle} = \langle u_O(t) \rangle_T = \frac{1}{T} \int_t^{t+T} u_O(\tau) d\tau = \dots = D_{1H} \cdot U_I$$





The PWM inverter: 1 leg

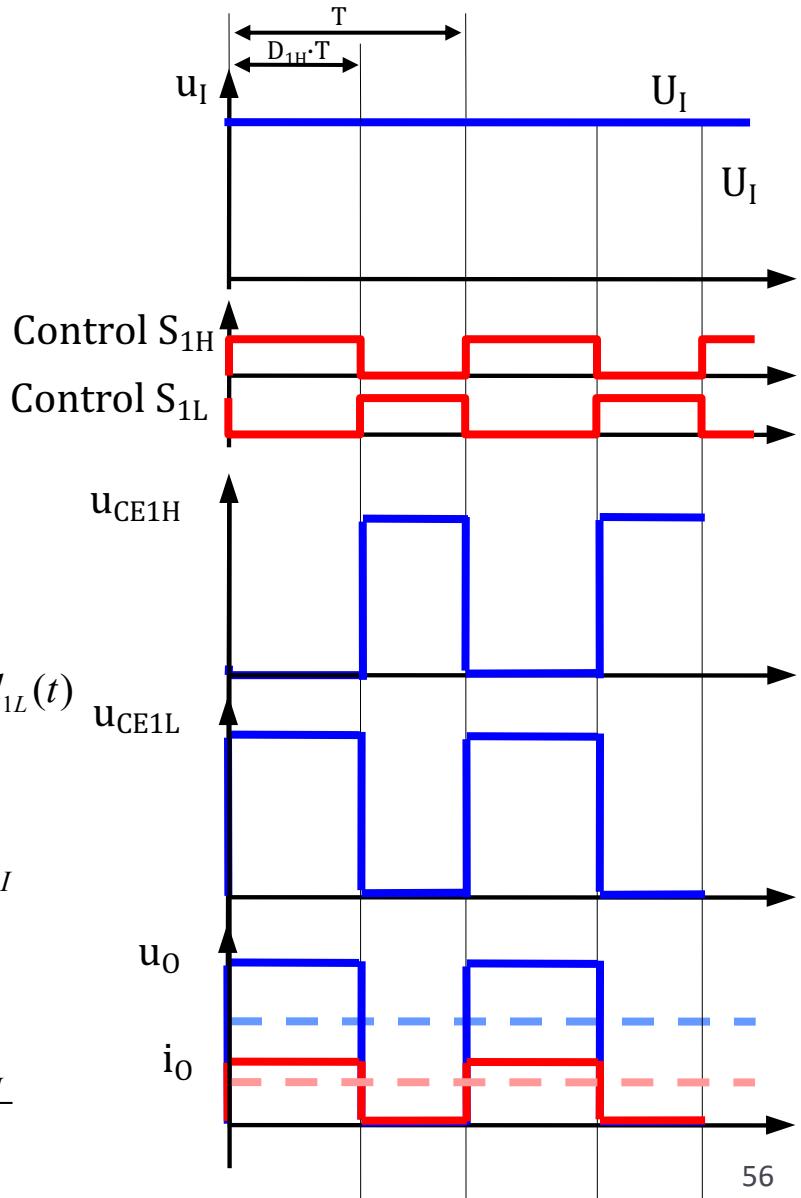


Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$
- Resistive load

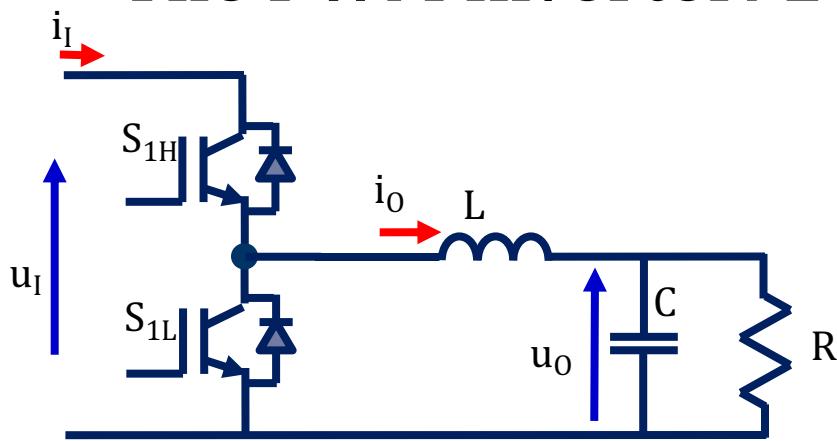
$$u_O(t) = \begin{cases} U_I & 0 \leq t < D_{1H} \cdot T \\ 0 & D_{1H} \cdot T \leq t < T \end{cases} \quad \langle u_O(t) \rangle_T = D_{1H} \cdot U_I$$

$$i_O(t) = \begin{cases} \frac{U_I}{R} & 0 \leq t < D_{1H} \cdot T \\ 0 & D_{1H} \cdot T \leq t < T \end{cases} \quad \langle i_O(t) \rangle_T = D_{1H} \cdot \frac{U_I}{R}$$





The PWM inverter: 1 leg

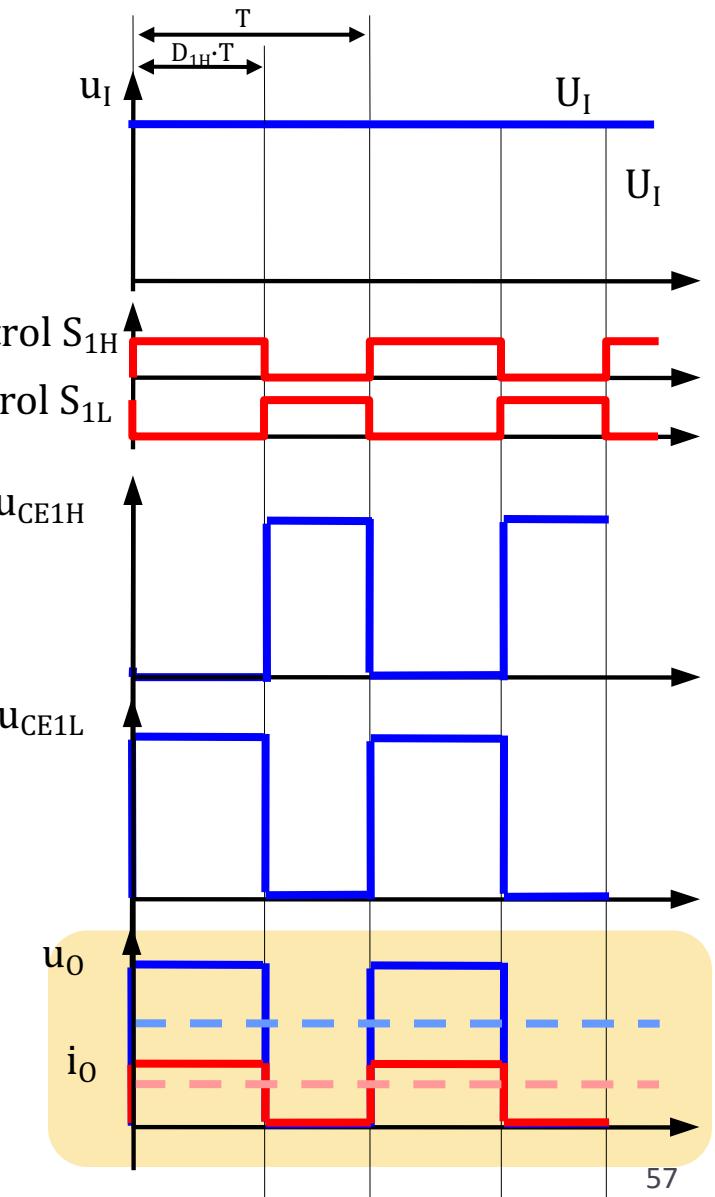


Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$
- LC filtered load ($L \uparrow\uparrow$, $C \uparrow\uparrow$)

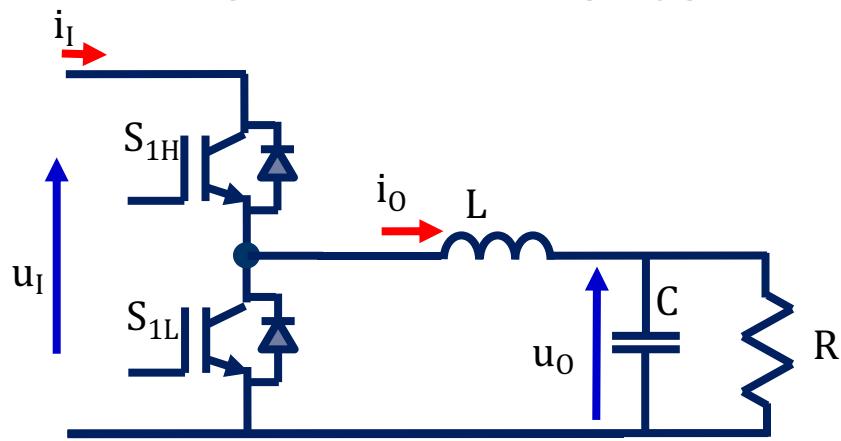
$$u_O(t) = \begin{cases} U_I & 0 \leq t < D_{1H} \cdot T \\ 0 & D_{1H} \cdot T \leq t < T \end{cases} \quad \langle u_O(t) \rangle_T = D_{1H} \cdot U_I$$

$$i_O(t) = \begin{cases} \frac{U_I}{R} & 0 \leq t < D_{1H} \cdot T \\ 0 & D_{1H} \cdot T \leq t < T \end{cases} \quad \langle i_O(t) \rangle_T = D_{1H} \cdot \frac{U_I}{R}$$





The PWM inverter: 1 leg

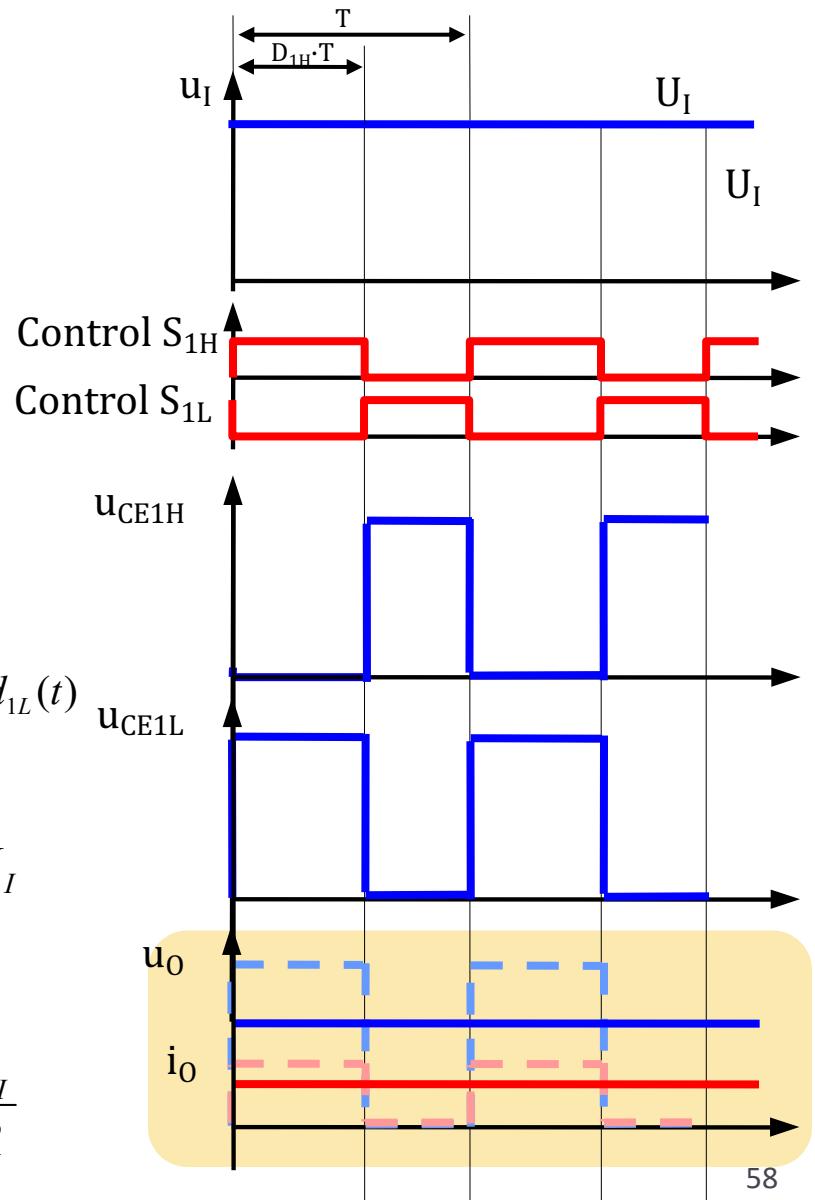


Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$
- LC filtered load ($L \uparrow\uparrow$, $C \uparrow\uparrow$)

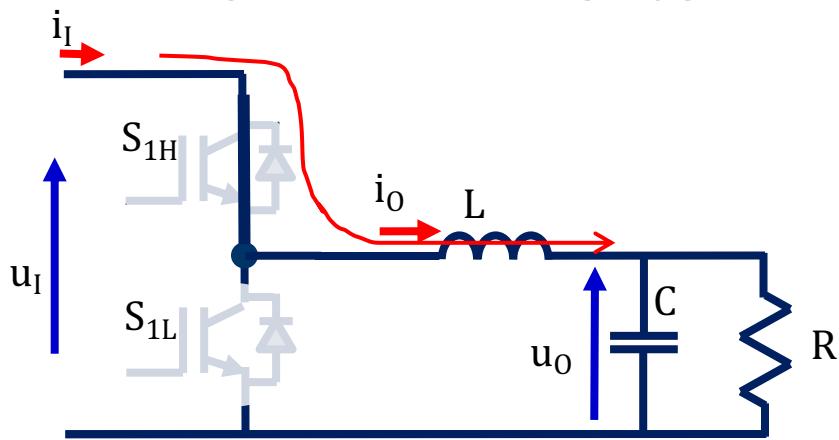
$$u_O(t) = D_{1H} \cdot U_I \quad (\text{ripple neglected}) \qquad \langle u_O(t) \rangle_T = D_{1H} \cdot U_I$$

$$i_O(t) \approx D_{1H} \frac{U_I}{R} \quad (\text{ripple neglected}) \qquad \langle i_O(t) \rangle_T = D_{1H} \cdot \frac{U_I}{R}$$





The PWM inverter: 1 leg



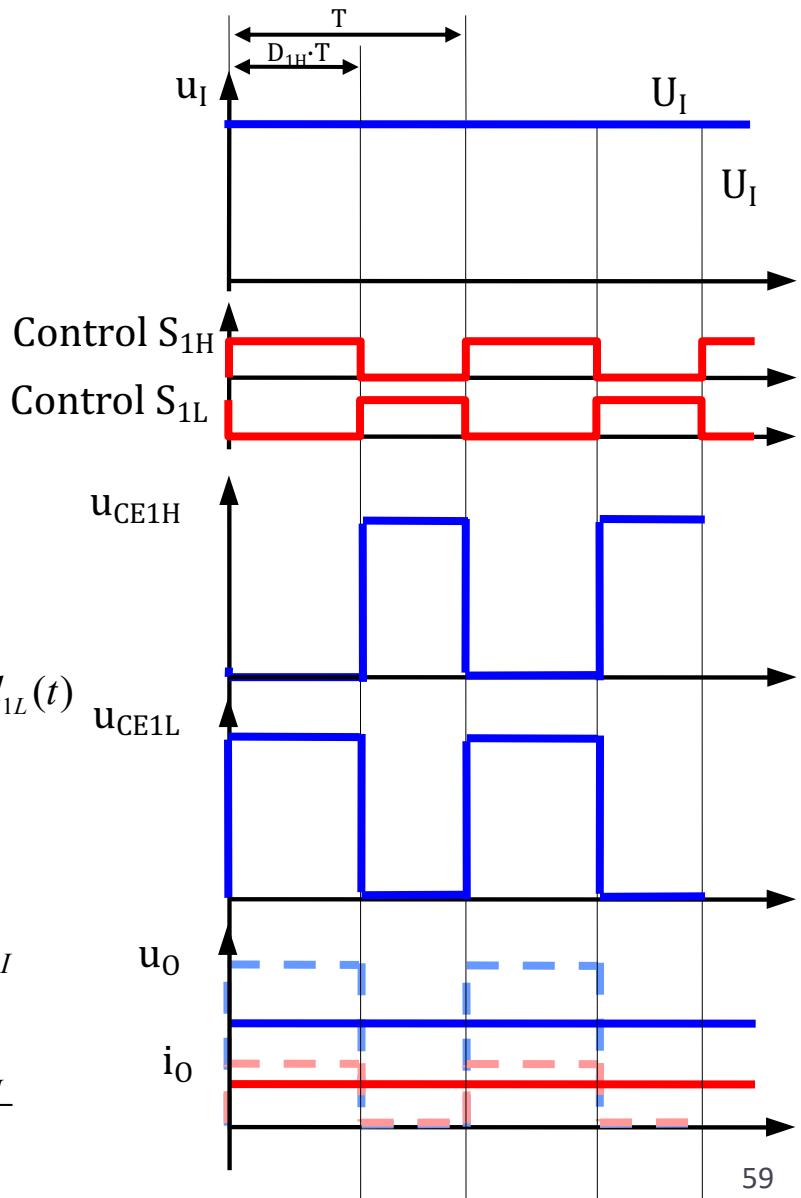
Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$
- LC filtered load ($L \uparrow\uparrow$, $C \uparrow\uparrow$)

If Switch S_{1H} is ON $0 \leq t < d_{1H}(t) \cdot T$

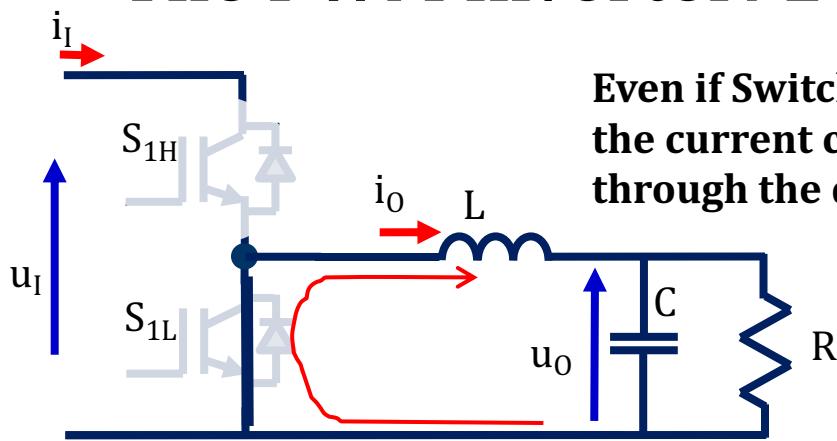
$$u_O(t) = D_{1H} \cdot U_I \quad (\text{ripple neglected}) \quad \langle u_O(t) \rangle_T = D_{1H} \cdot U_I$$

$$i_O(t) \approx D_{1H} \frac{U_I}{R} \quad (\text{ripple neglected}) \quad \langle i_O(t) \rangle_T = D_{1H} \cdot \frac{U_I}{R}$$





The PWM inverter: 1 leg



Consider only 1 leg. Also consider:

- Ideal switches (no losses)
- Complementary control of S_{1H} and S_{1L} $d_{1H}(t) = 1 - d_{1L}(t)$
- LC filtered load ($L \uparrow\uparrow$, $C \uparrow\uparrow$)

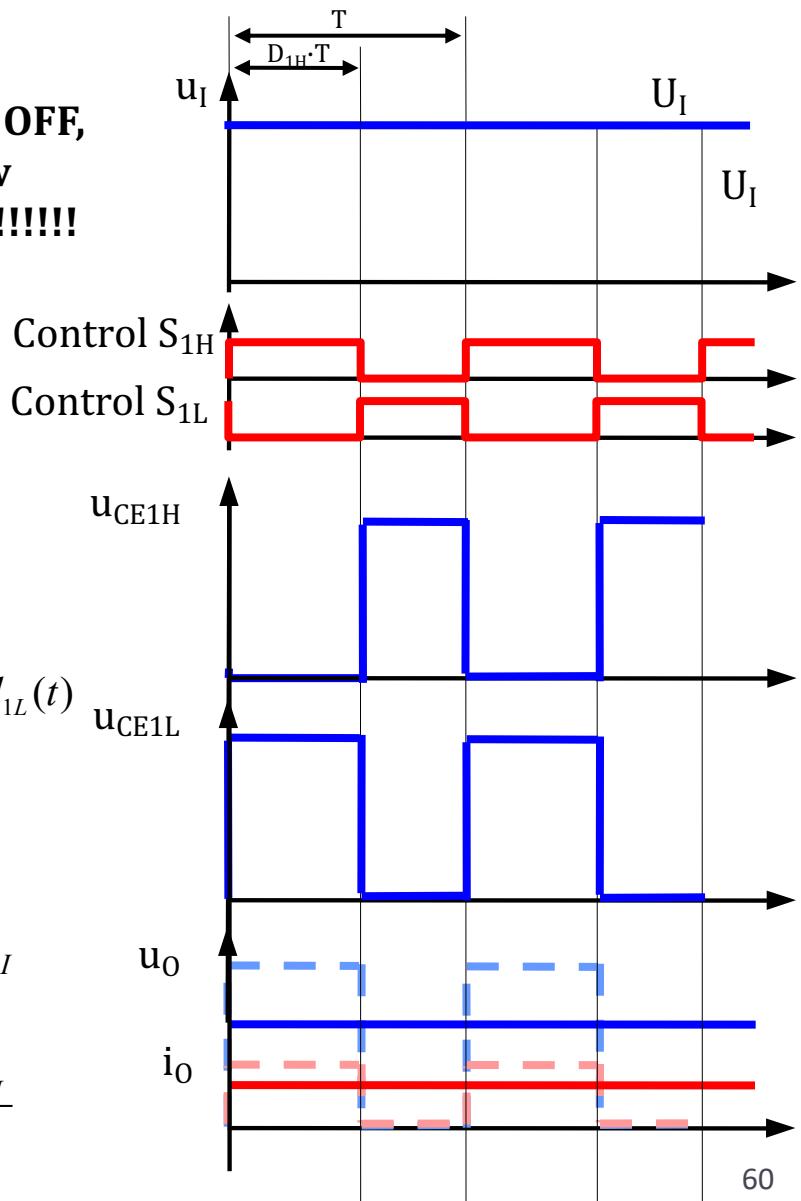
If Switch S_{1H} is OFF $d_{1H}(t) \cdot T \leq t < T$

$$u_O(t) = D_{1H} \cdot U_I \quad (\text{ripple neglected})$$

$$i_O(t) \approx D_{1H} \frac{U_I}{R} \quad (\text{ripple neglected})$$

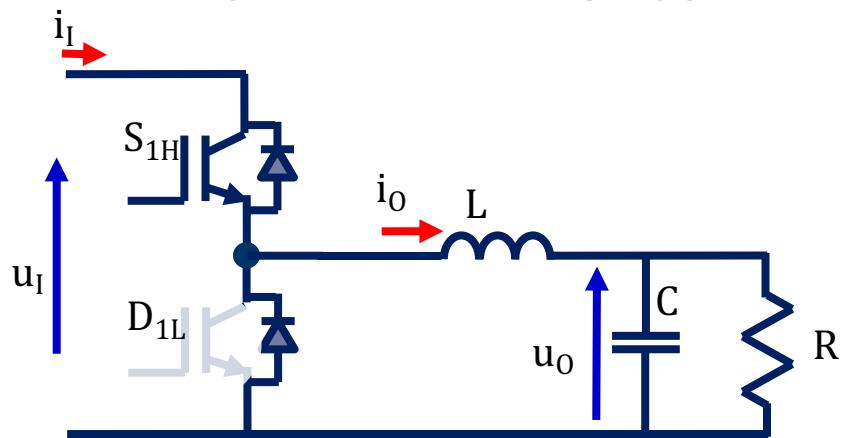
$$\langle u_O(t) \rangle_T = D_{1H} \cdot U_I$$

$$\langle i_O(t) \rangle_T = D_{1H} \cdot \frac{U_I}{R}$$



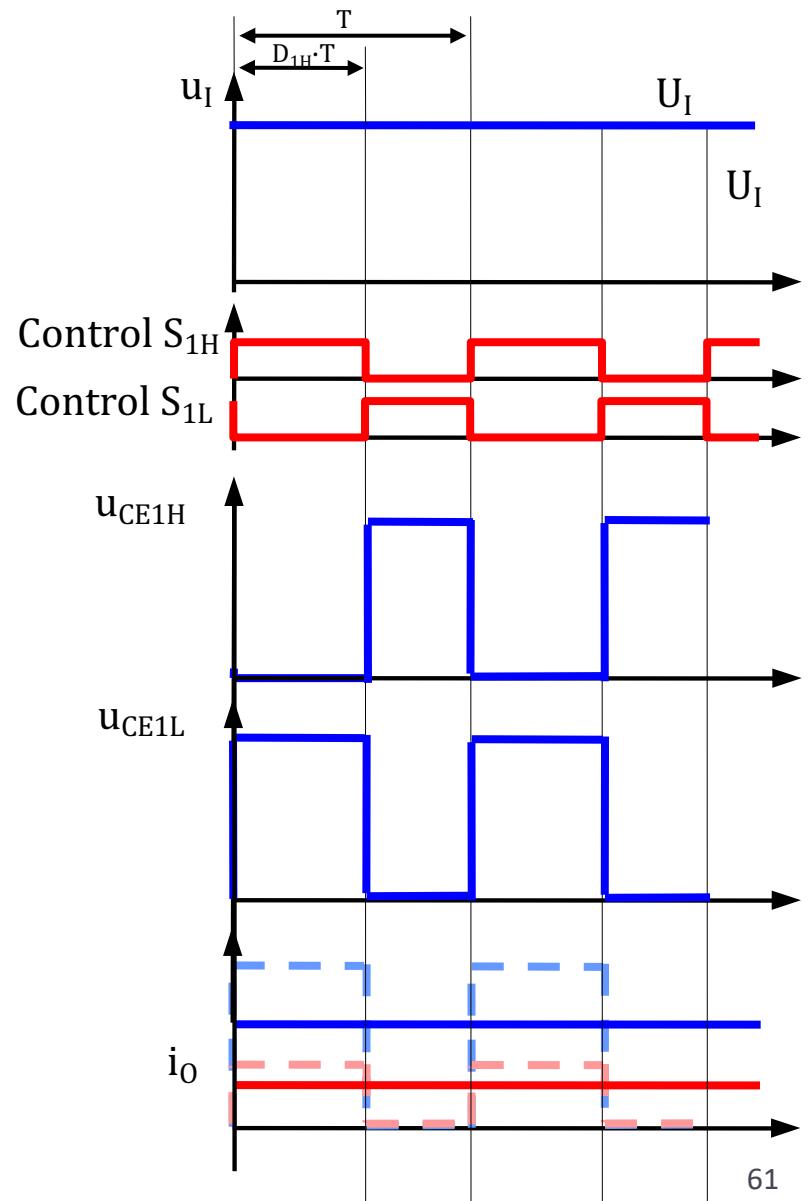


The PWM inverter: 1 leg



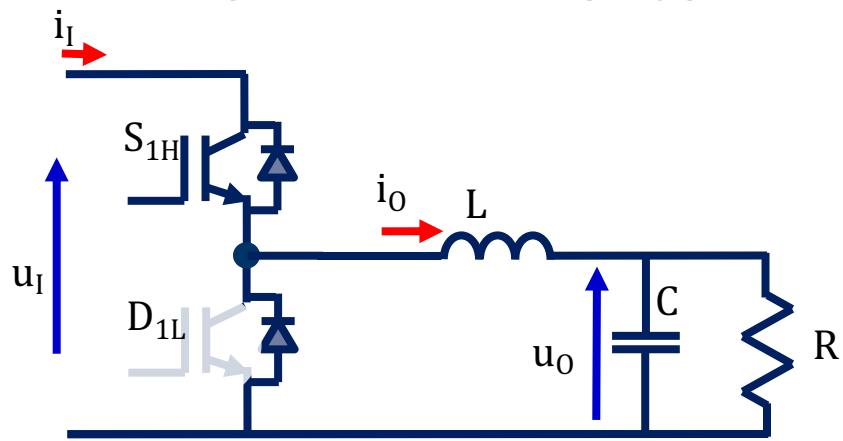
Thus, this converter (under these conditions) can be redrawn:

$$\langle u_O(t) \rangle_T = U_O = D_{1H} \cdot U_I \quad \Rightarrow \quad \frac{U_O}{U_I} = D_{1H}$$





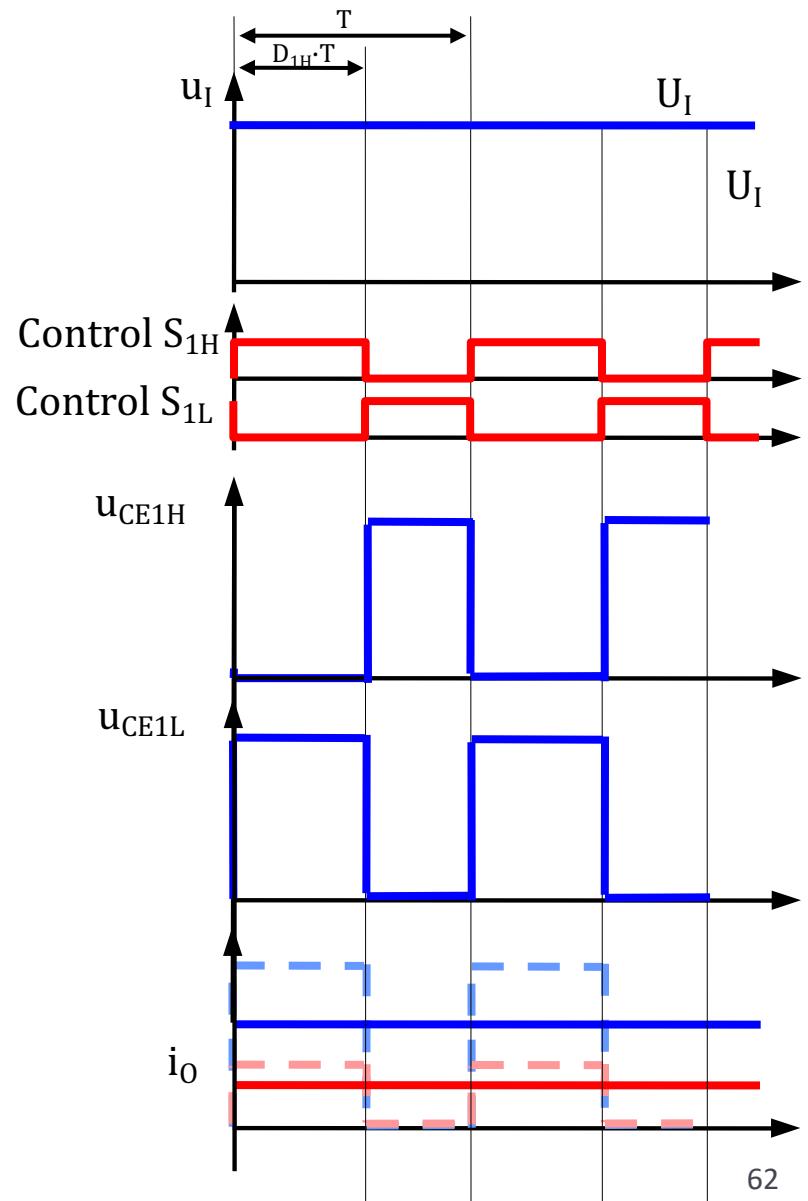
The PWM inverter: 1 leg



Thus, this converter (under these conditions) can be redrawn:

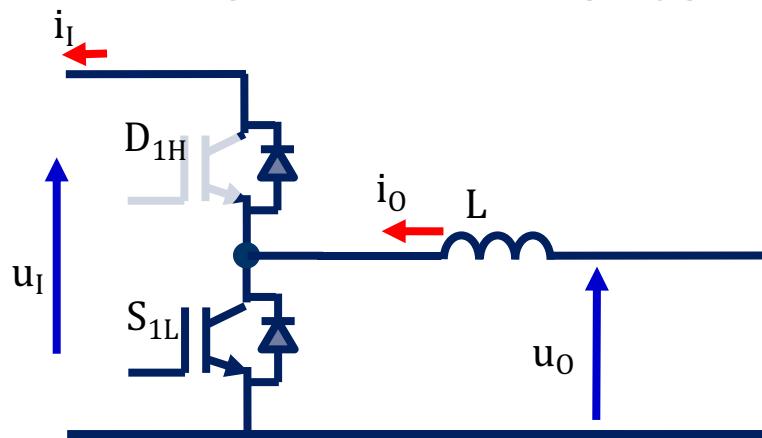
$$\langle u_O(t) \rangle_T = U_O = D_{1H} \cdot U_I \quad \Rightarrow \quad \frac{U_O}{U_I} = D_{1H}$$

... to find the **BUCK** converter in CCM!!!





The PWM inverter: 1 leg

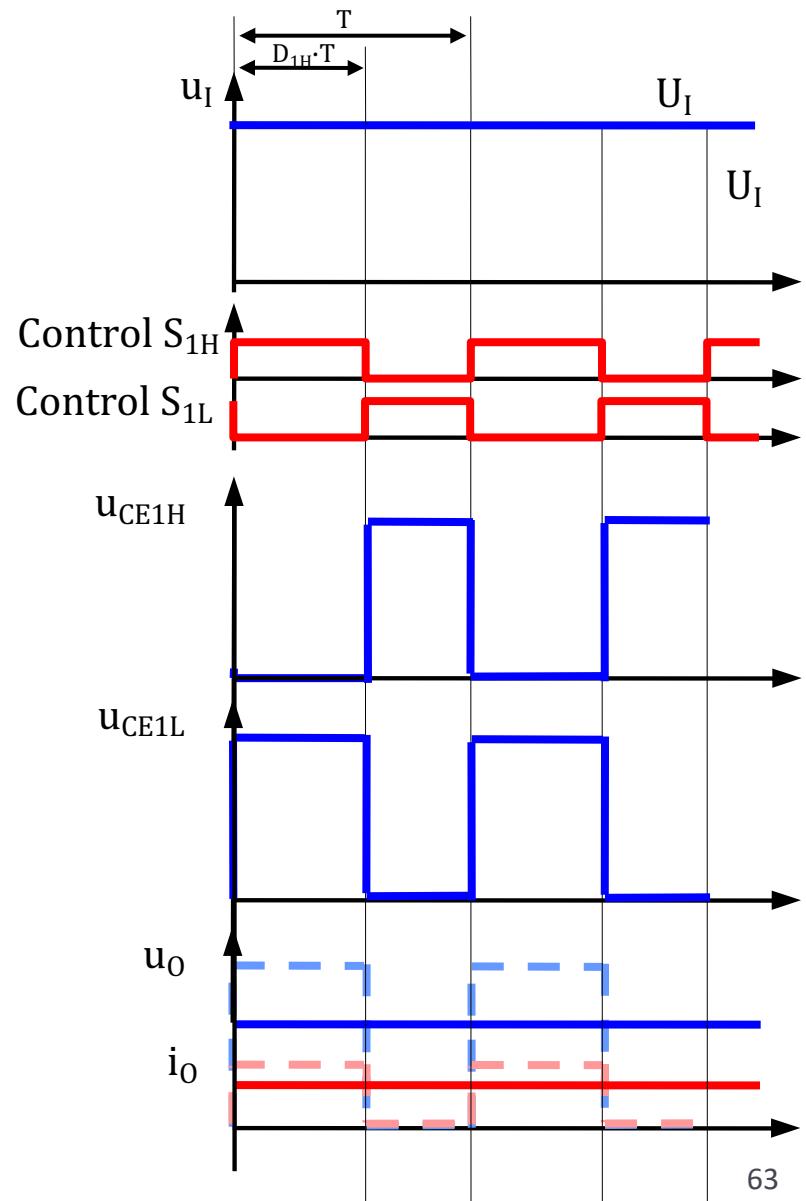


Thus, this converter (under these conditions) can be redrawn:

$$\langle u_O(t) \rangle_T = U_O = D_{1H} \cdot U_I \quad \Rightarrow \quad \frac{U_O}{U_I} = D_{1H}$$

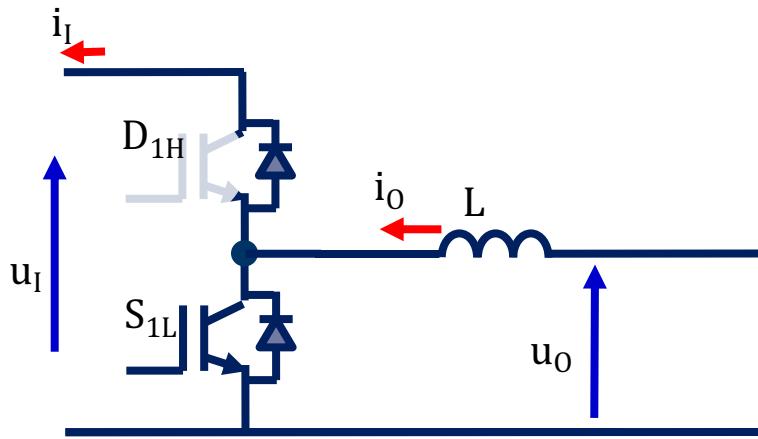
... to find the **BUCK** converter in CCM!!!

Furthermore, if we consider the bidirectional converter, (delivering power to u_I),





The PWM inverter: 1 leg



Thus, this converter (under these conditions) can be redrawn:

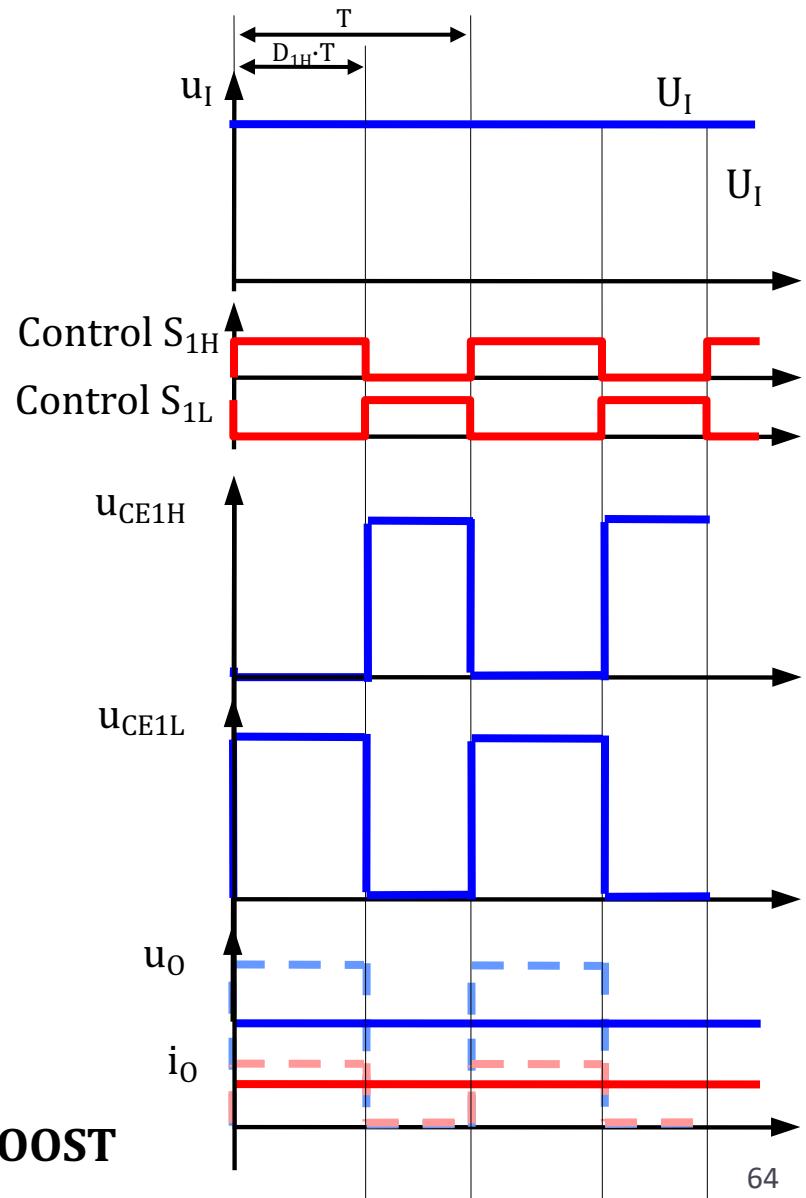
$$\langle u_o(t) \rangle_T = U_o = D_{1H} \cdot U_I \quad \Rightarrow \quad \frac{U_o}{U_I} = D_{1H}$$

... to find the **BUCK** converter in CCM!!!

Furthermore, if we consider the bidirectional converter, (delivering power to u_I),

$$\frac{U_I}{U_o} = \frac{1}{D_{1H}} = \frac{1}{1 - D_{1L}}$$

... then we have the **BOOST** converter in CCM!!!





References:

"Power Electronics Handbook, Second Edition: Devices, Circuits and Applications" *Editor: Muhammad H. Rashid, Ed. Elsevier Inc., 2007.*
ISBN-10: 0120884798

"Power Electronics: Converters, Applications and Design, 3rd edition". Mohan, Undeland, Robbins. John Wiley & Sons, Inc. 2003.
ISBN: 978-0-471-22693-2

"Fundamentals of Power Electronics" Second edition. Robert W. Erickson, Dragan Maksimovic, Ed. Springer Science + Business Media, LLC, 2001.
ISBN: 978-0-7923-7270-7

<https://www.switchcraft.org/learning/2017/3/15/space-vector-pwm-intro>