

$$1) X = [0, 1, 2, 3, 4, 5], Y = [0, 0, 1, 2, 3]$$

a - permut aleatoare a lui  $x$ ,  $b, c$  - permut aliat indep a lui  $y$

a)  $P(\{a = [5, 1, 2, 3, 4, 0]\})$  b)  $P(\text{"c(1) - nr. min. 4"})$

c)  $Z$  - v.a. def astfel  $P(Z = -1) = P(\text{"c(1) - nr. par"})$ ,  $P(Z = 1) = P(\text{"c(1) - nr. impar"})$ ,  $E(Z) = ?$

d)  $P(\{b = [3, 1, 2, 0, 0]\} \cup \{c = [3, 0, 1, 2, 0]\})$

e)  $E$  adevar ca  $\{b = [0, 3, 1, 2, 0]\}$  si  $\{c = [3, 0, 1, 2, 0]\}$  nu au acceasi prob?

2)  $y_1, y_2, y_3, y_4, y_5$  - date st. p.  $Y$  dep de  $p \in (0, 0.5)$   
 $P(Y = -1) = 0.5 - p$ ,  $P(Y = 0) = p$ ,  $P(Y = 2) = 0.5$   
 met mom,  $E(Y) = 0.9$

3)  $U, T$  v.a. indep cu aceeasi  $f, \mathbb{R} \rightarrow [0, \infty)$   $f(u) = \begin{cases} 3u^2, & u \in [0, 1] \\ 0 & \end{cases}$

a)  $F_U(u)$ ,  $u \in [0, 1]$  si  $F_T(t)$ ,  $t \in [1, 3]$

b)  $P(U \leq \frac{1}{2}, T \leq \frac{3}{2})$

c)  $E(5U^2 - 4T)$