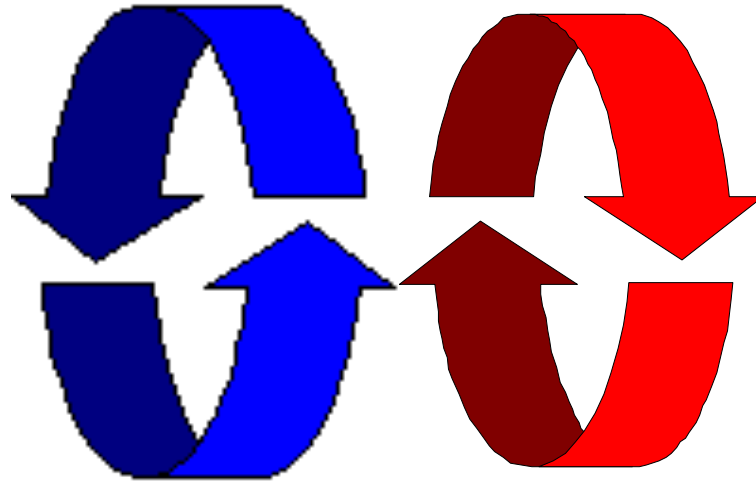


Concurrent Execution



Concurrent Execution

Concepts: processes - concurrent execution, interleaving.
process interaction.

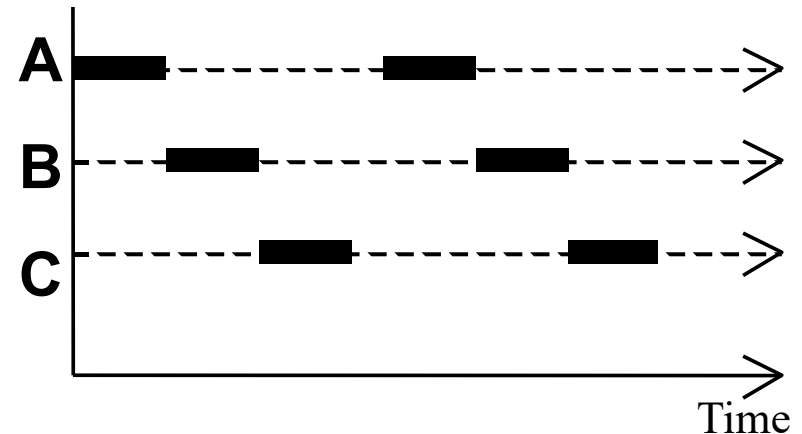
Models: parallel composition of asynchronous processes
- action interleaving
interaction - shared actions (synchronous)
process labelling, action re-labelling, hiding,
structure diagrams

Practice: Multithreaded Java programs.

Definitions

◆ (Pseudo) Concurrency

- *Logically* simultaneous processing. Does not imply multiple processing elements (PEs). Requires interleaved execution on a single PE.



◆ Parallelism

- *Physically* simultaneous processing. Involves multiple PEs and/or independent device operations.

Both **concurrency** and **parallelism** require controlled access to *shared resources*. We use the terms **parallel** and **concurrent** interchangeably and generally do not distinguish between real and pseudo-concurrent execution.

3.1 Modelling Concurrency

- ◆ How should we model process execution speed?
 - arbitrary speed
(we abstract away time)
- ◆ How do we model concurrency?
 - arbitrary relative order of actions from different processes
(interleaving but preserve each process's order)
- ◆ What is the result?
 - provides a general model independency of scheduling
(asynchronous model of execution)

Parallel Composition – Action Interleaving

If P and Q are processes then $(P || Q)$ represents the **concurrent execution** of P and Q . The **operator** $||$ is the **parallel composition operator**.

```
ITCH  = (scratch->STOP) .  
CONVERSE = (think->talk->STOP) .
```

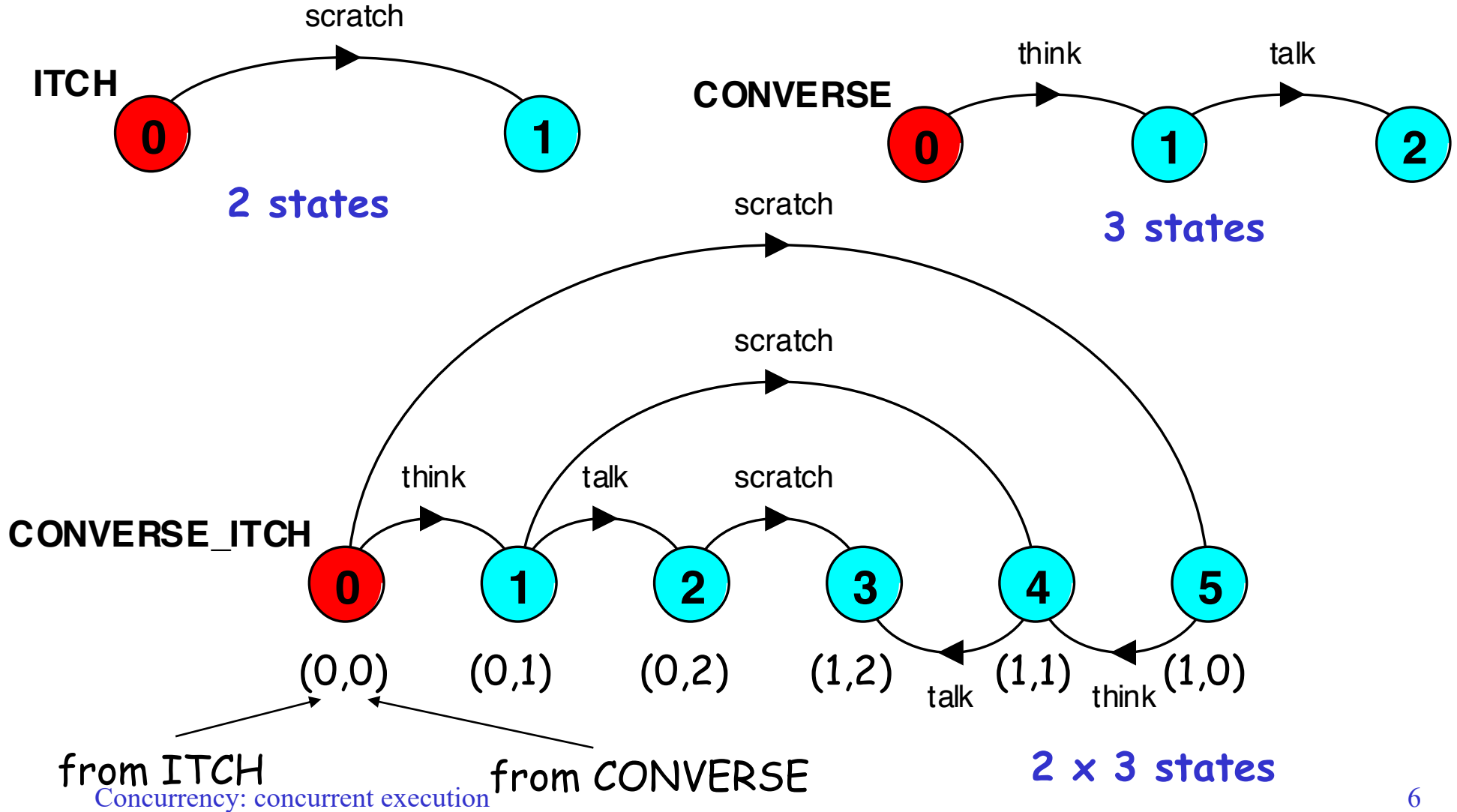
Disjoint
alphabets

```
|| CONVERSE_ITCH = (ITCH || CONVERSE) .
```

```
think→talk→scratch  
think→scratch→talk  
scratch→think→talk
```

Possible traces as
a result of **action**
interleaving.

Parallel Composition – Action Interleaving



Parallel Composition – Algebraic Laws

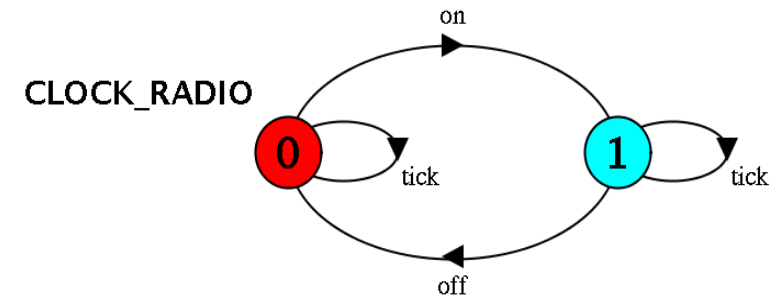
Commutative: $(P \mid \mid Q) = (Q \mid \mid P)$

Associative: $(P \mid \mid (Q \mid \mid R)) = ((P \mid \mid Q) \mid \mid R)$
 $= (P \mid \mid Q \mid \mid R) .$

Clock radio example:

$\text{CLOCK} = (\text{tick} \rightarrow \text{CLOCK}) .$
 $\text{RADIO} = (\text{on} \rightarrow \text{off} \rightarrow \text{RADIO}) .$

$\mid \mid \text{CLOCK_RADIO} = (\text{CLOCK} \mid \mid \text{RADIO}) .$



Modeling Interaction – Shared Actions

- If processes in a composition have **actions in common**, these **actions** are said to be **shared**.
- **Shared actions** is the way that **process interaction** is modelled. While **unshared actions** may be **arbitrarily** interleaved, a **shared action must be executed at the same time by all processes** that participate in the shared action.

MAKER = (make->**ready**->MAKER) .

USER = (**ready**->use->USER) .

|| MAKER_USER = (MAKER || USER) .

MAKER

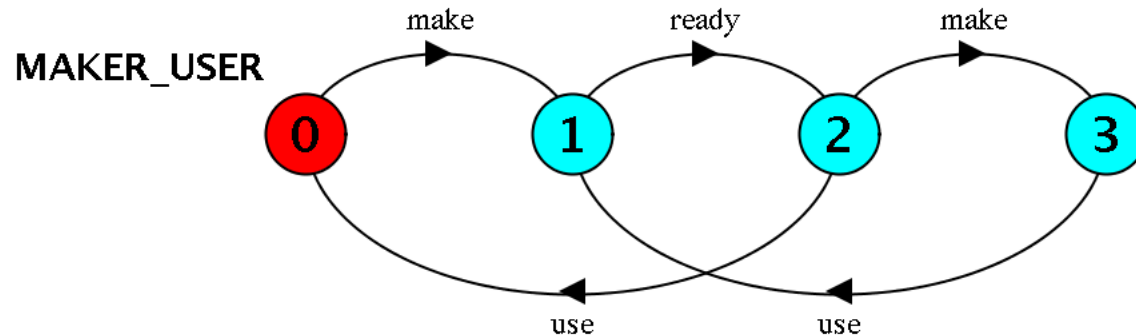
synchronizes
with USER
when **ready**.

Modeling Interaction – Shared Actions

```
MAKER = (make->ready->MAKER) .
```

```
USER = (ready->use->USER) .
```

```
||MAKER_USER = (MAKER || USER) .
```



make→ready→make→use→ready→ ...

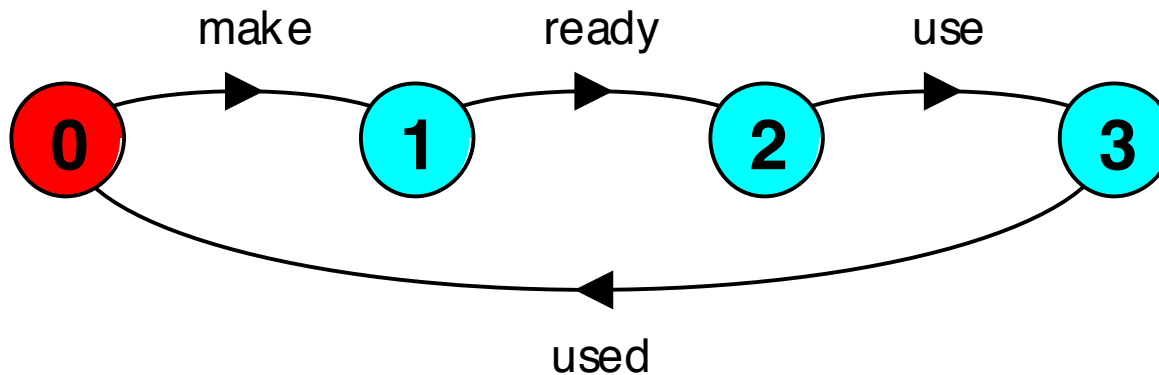
Modeling Interaction - Handshake

A **handshake** is an **action** (e.g., **used**) **acknowledged** by **another**:

MAKERv2 = (make->**ready**->**used**->MAKERv2) . 3 states

USERv2 = (**ready**->use->**used** ->USERv2) . 3 states

||MAKER_USERv2 = (MAKERv2 || USERv2) . 3 × 3
states?



4 states

Interaction
constrains
the overall
behaviour.

Modeling Interaction – Multiple Processes

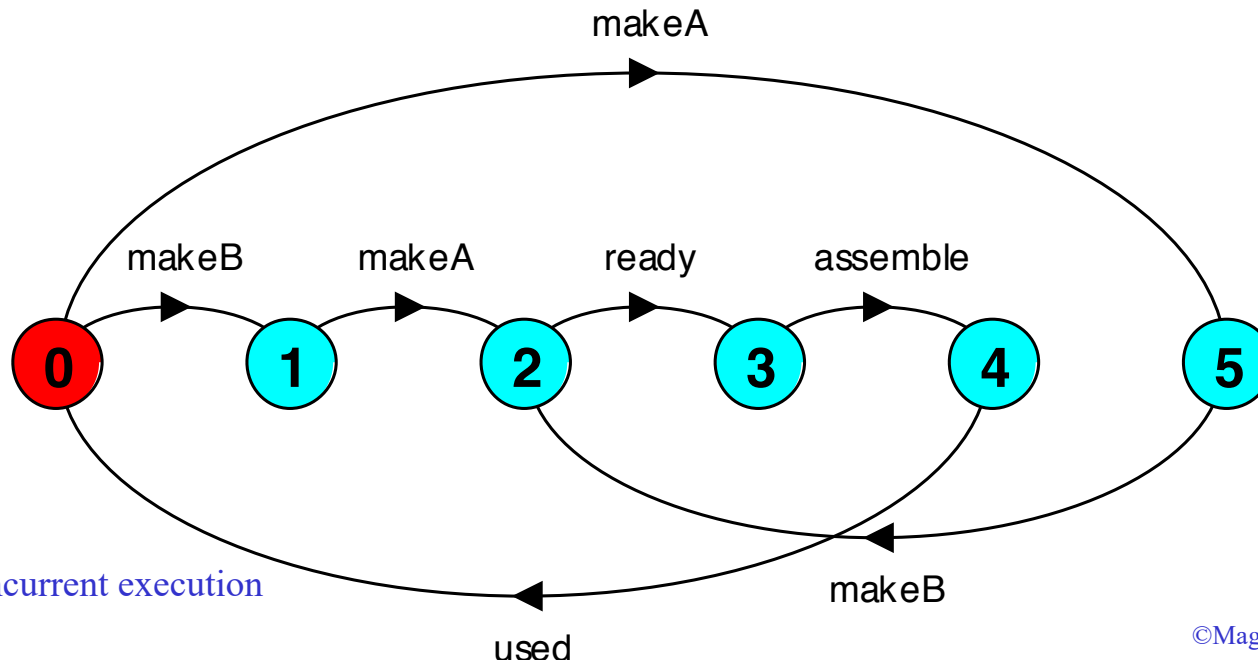
Multi-party **synchronization**:

MAKE_A = (makeA->**ready**->**used**->MAKE_A) .

MAKE_B = (makeB->**ready**->**used**->MAKE_B) .

ASSEMBLE = (**ready**->assemble->**used**->ASSEMBLE) .

|| FACTORY = (MAKE_A || MAKE_B || ASSEMBLE) .



Composite Processes

A **composite process** is a parallel composition of **primitive processes**. These composite processes can be used in the definition of further compositions.

$$|| \text{MAKERS} = (\text{MAKE_A} || \text{MAKE_B}) .$$
$$|| \text{FACTORY} = (\text{MAKERS} || \text{ASSEMBLE}) .$$

Substituting the definition for MAKERS in FACTORY and **applying the commutative and associative laws** for parallel composition results in the **original definition** for FACTORY in terms of **primitive processes**.

$$|| \text{FACTORY} = (\text{MAKE_A} || \text{MAKE_B} || \text{ASSEMBLE}) .$$

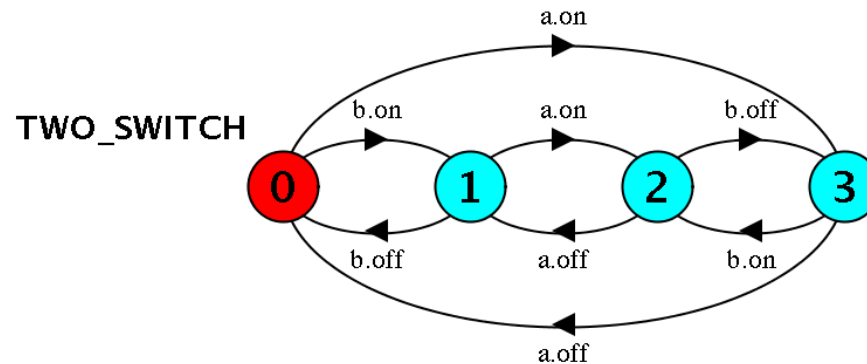
Process Instances and Labelling

- $a:P$: instance "a" of process P; prefixes each action in the alphabet of process P. (e.g., a.on)

- Two instances (a and b) of SWITCH process:

SWITCH = (on- \rightarrow off- \rightarrow SWITCH) .

|| TWO_SWITCH = (a:SWITCH || b:SWITCH) .



- An array of instances of the SWITCH process:

|| SWITCHES (N=3) = (forall [i:1..N] s[i]:SWITCH) .

|| SWITCHES (N=3) = (s[i:1..N]:SWITCH) .

Process Labelling by a Set of Instances

- $\{a_1, \dots, a_x\} :: P$ replaces every action label n in the alphabet of P process with the labels $a_1.n, \dots, a_x.n$.

Note: a_1, a_2, \dots, a_x : instances of process P

- Every transition ($n \rightarrow X$) in the definition of P is replaced with the transitions ($\{a_1.n, \dots, a_x.n\} \rightarrow X$).

Process prefixing is useful for modelling shared resources:

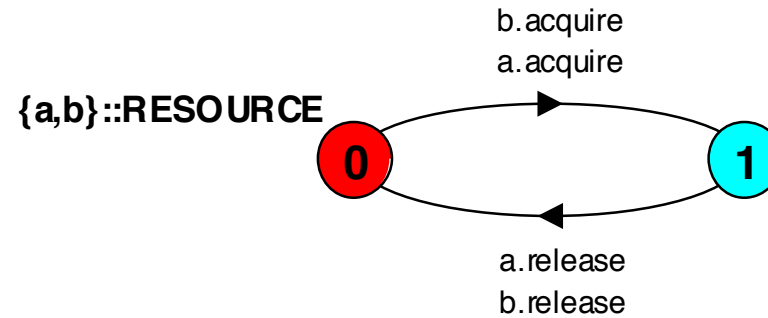
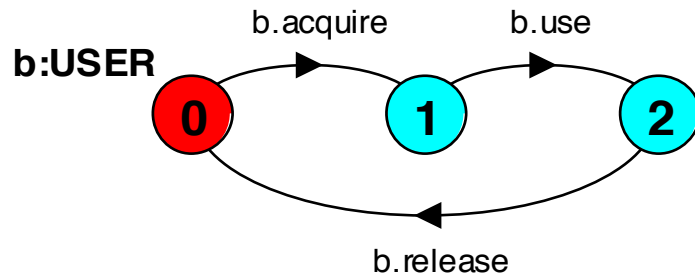
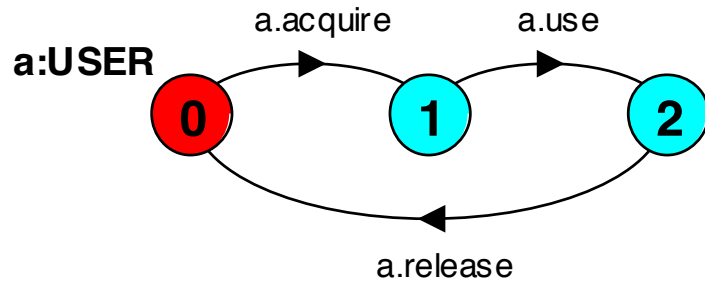
RESOURCE = (**acquire** \rightarrow **release** \rightarrow **RESOURCE**) .

USER = (**acquire** \rightarrow **use** \rightarrow **release** \rightarrow **USER**) .

RESOURCE_SHARE =
(**a** : **USER** || **b** : **USER** || {**a**, **b**} : **RESOURCE**) .

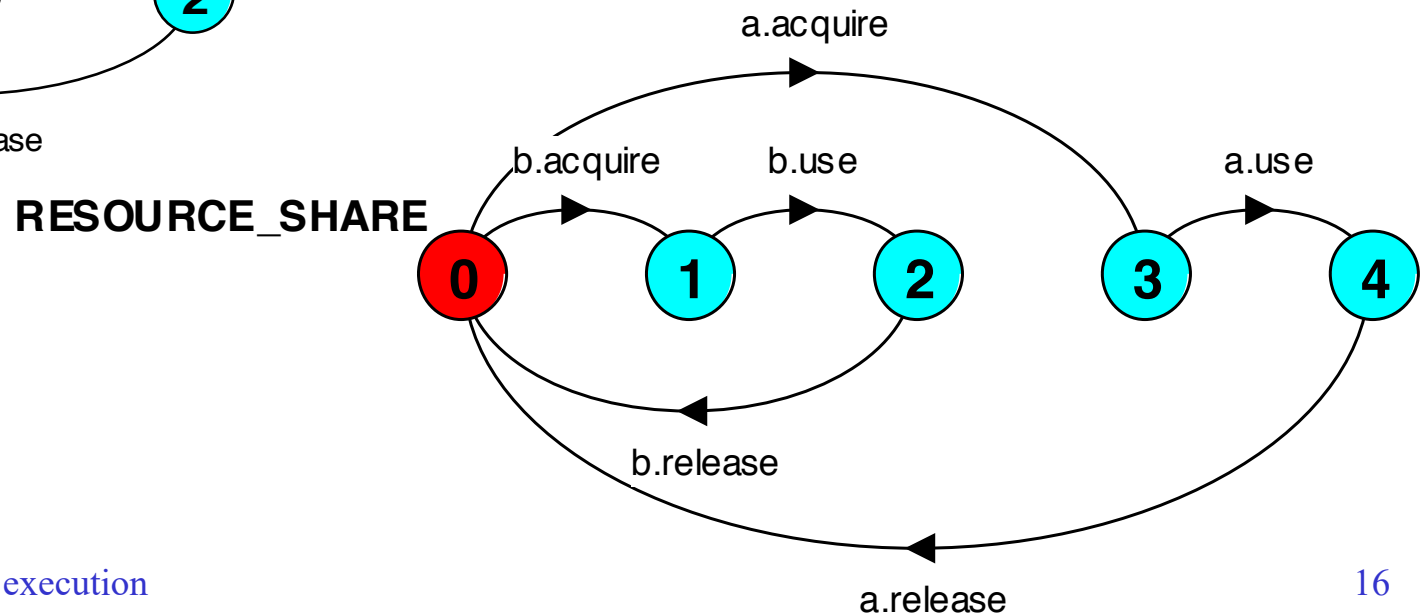
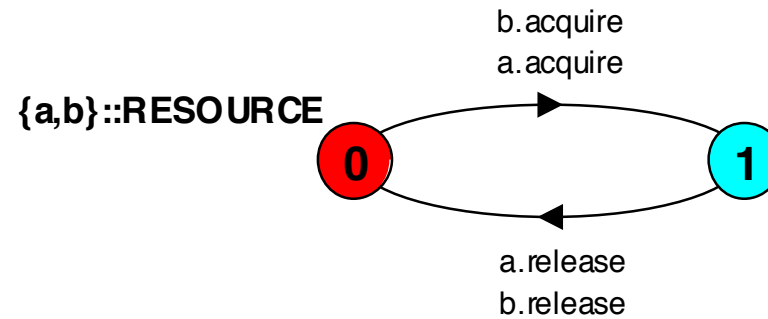
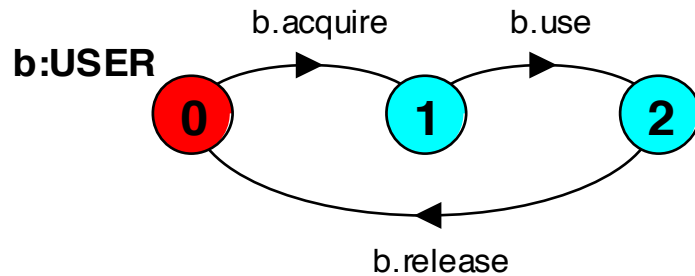
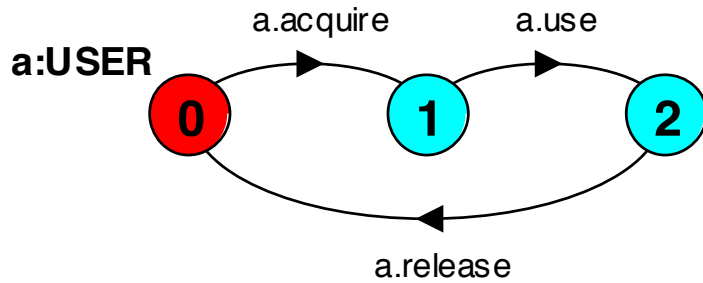
Instances: **a** and **b**

Process Prefix Labels for Shared Resources



How does the model ensure that the user that acquires the resource is the one to release it?

Process Prefix Labels for Shared Resources



Action Re-Labelling

- Re-labelling functions are applied to processes to change the names of action labels.
- The general form of the re-labelling function is:
$$/\{newlabel_1/oldlabel_1, \dots newlabel_n/oldlabel_n\}.$$
- Relabelling to ensure that composed processes synchronize on particular actions.

CLIENT = (**call**->**wait**->continue->**CLIENT**) .

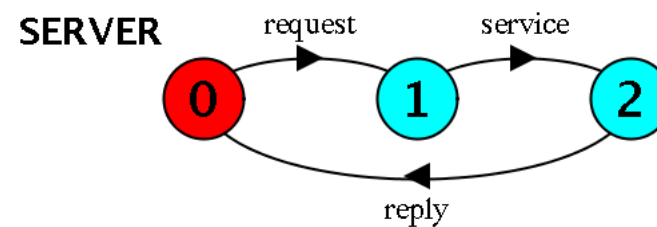
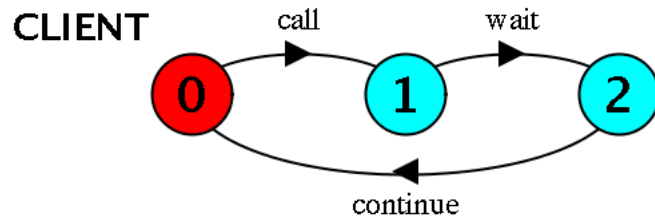
SERVER = (**request**->service->**reply**->**SERVER**) .

Note that both *newlabel* and *oldlabel* can be sets of labels.

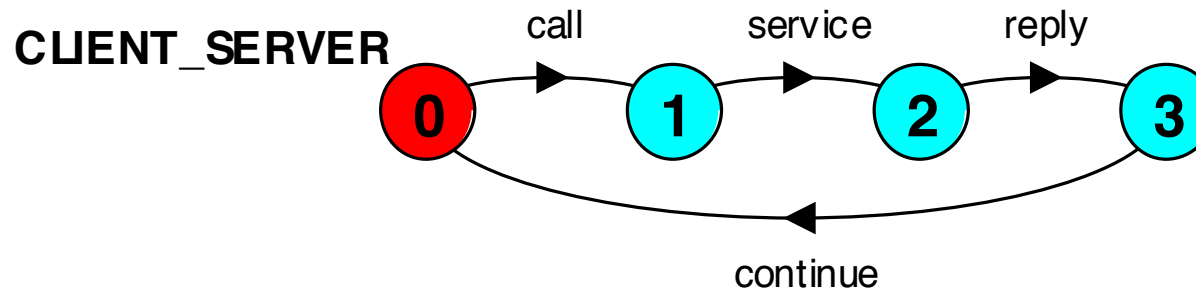
action re-labelling

CLIENT = (**call**->**wait**->continue->CLIENT) .

SERVER = (**request**->service->**reply**->SERVER) .



||CLIENT_SERVER = (CLIENT || SERVER)
/ {**call/request**, **reply/wait**} .



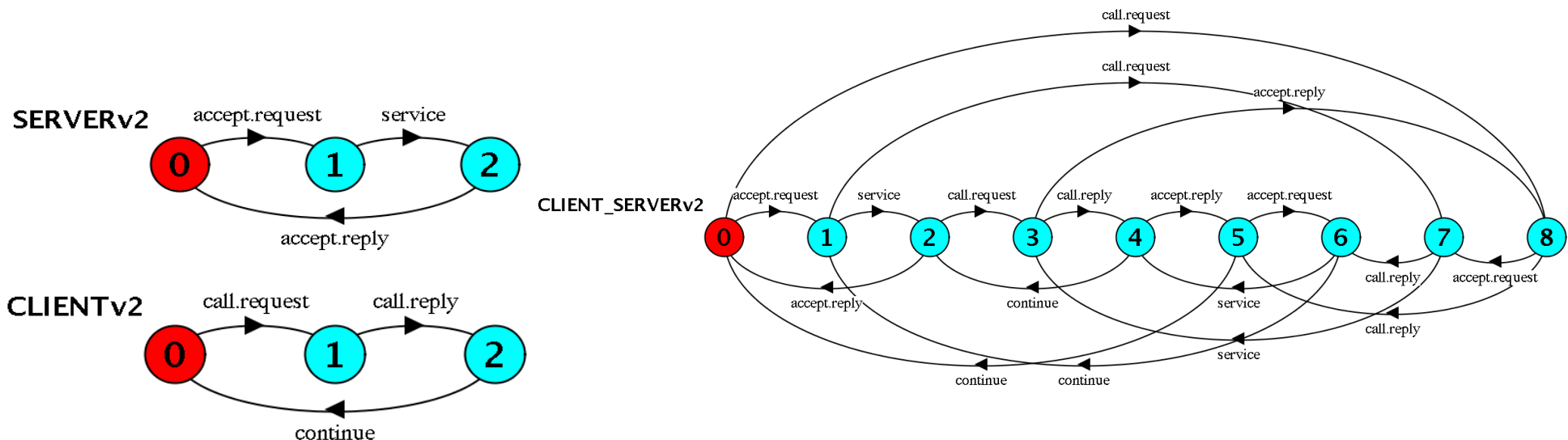
Action Re-Labeling – Prefix Labels

An alternative client server system: **qualified** or **prefixed labels**:

```
SERVERv2 = (accept.request  
            ->service->accept.reply->SERVERv2) .
```

```
CLIENTv2 = (call.request  
            ->call.reply->continue->CLIENTv2) .
```

```
||CLIENT_SERVERv2 = (CLIENTv2 || SERVERv2) .
```



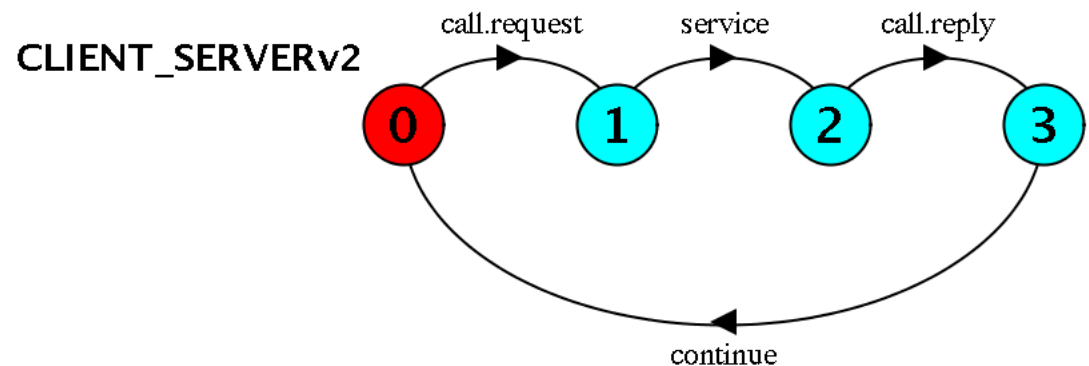
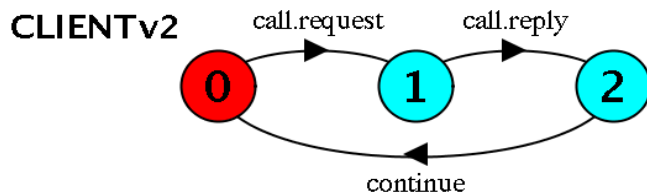
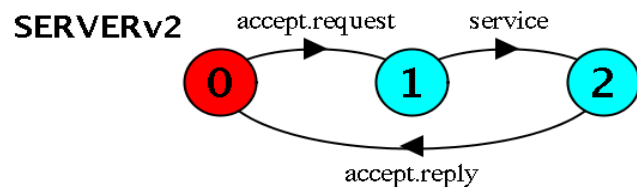
Action Re-Labeling – Prefix Labels

An alternative client server system: **qualified** or **prefixed labels**:

```
SERVERv2 = (accept.request  
            ->service->accept.reply->SERVERv2) .
```

```
CLIENTv2 = (call.request  
            ->call.reply->continue->CLIENTv2) .
```

```
||CLIENT_SERVERv2 = (CLIENTv2 || SERVERv2)  
                    /{call/accept} .
```



Action Hiding - Abstraction to Reduce Complexity

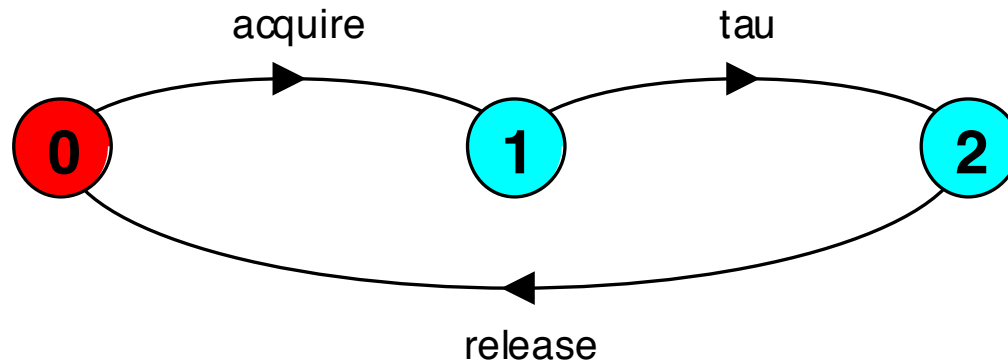
- When applied to a process P , the hiding operator $\backslash\{a1..ax\}$ removes the action names $a1..ax$ from the alphabet of P and makes these concealed actions "silent".
- These silent actions are labelled τ . Silent actions in different processes are not shared.
- Sometimes it is more convenient to specify the set of labels to be exposed....using $@\{a1..ax\}$

Action Hiding

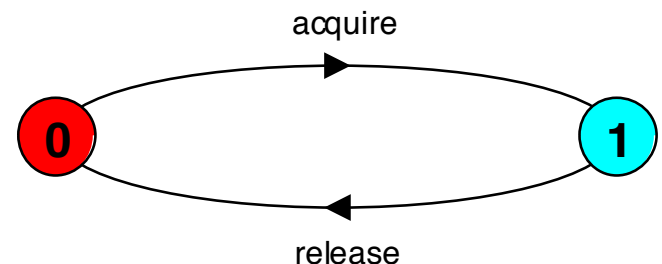
The following definitions are equivalent:

$\text{USER} = (\text{acquire} \rightarrow \text{use} \rightarrow \text{release} \rightarrow \text{USER})$
 $\backslash \{\text{use}\}.$

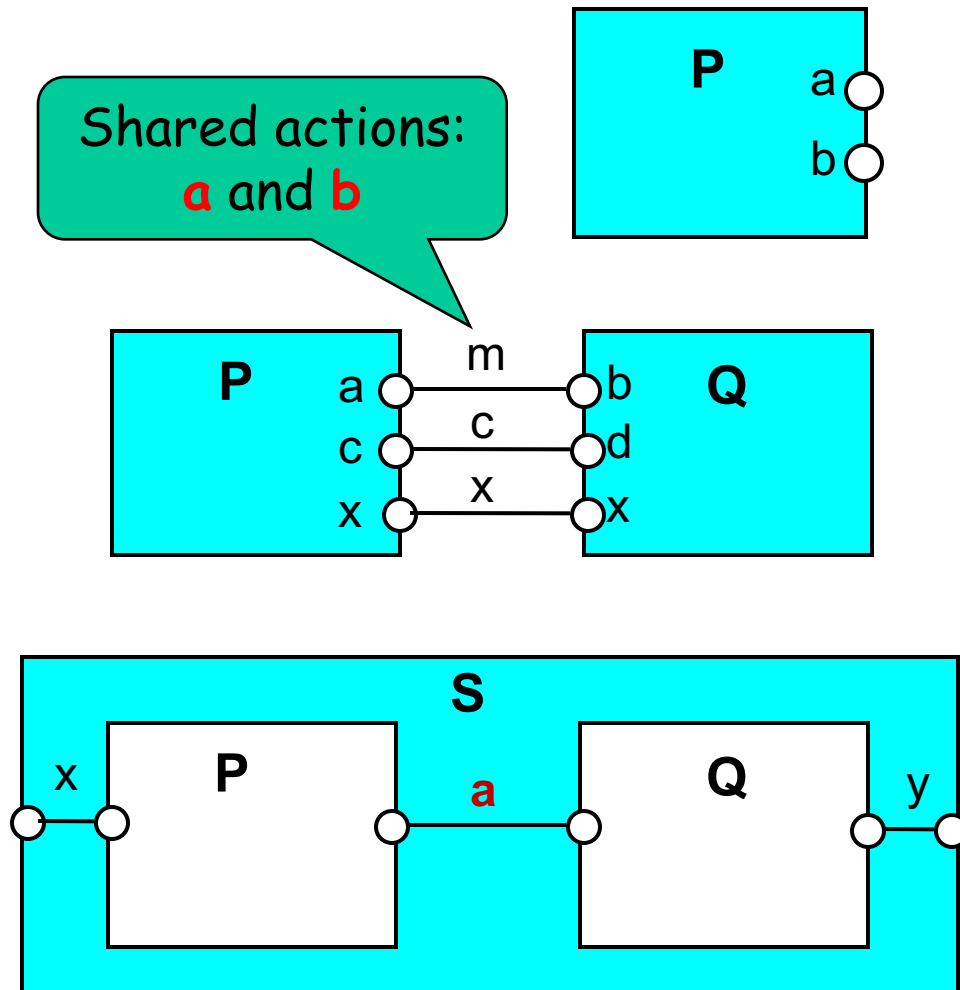
$\text{USER} = (\text{acquire} \rightarrow \text{use} \rightarrow \text{release} \rightarrow \text{USER})$
 $@ \{\text{acquire}, \text{release}\}.$



Minimization removes **hidden tau actions** to produce an LTS with **equivalent observable behavior**.



Structure Diagrams – Systems as **Interacting Processes**



Process **P** with
alphabet **{a,b}**.

Parallel Composition
 $(P || Q) / \{m/a, m/b, c/d\}$

Composite process
 $||S = (P || Q) @ \{x,y\}$

a : shared action between
P and **Q**

Concurrency: concurrent execution

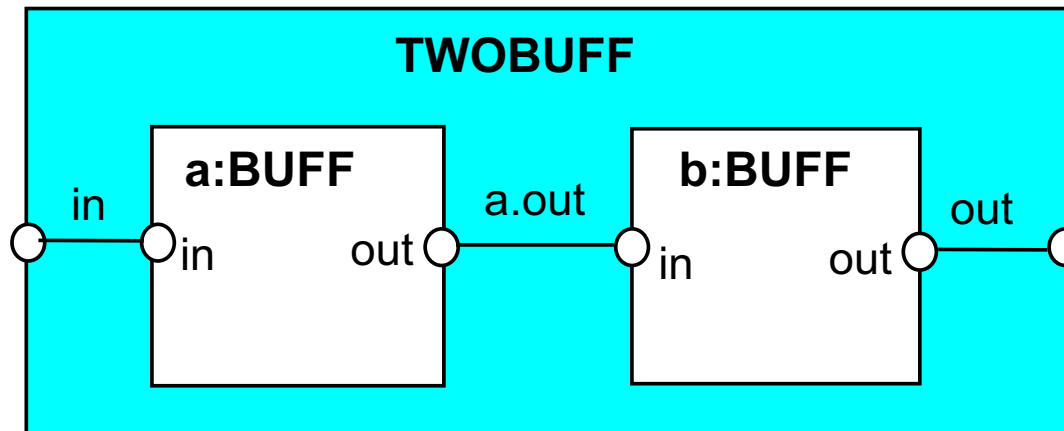
Structure Diagrams

We use **structure diagrams** to capture the **structure of a model** expressed by the **static combinators**: *parallel composition*, *relabeling* and *hiding*.

range $T = 0..3$

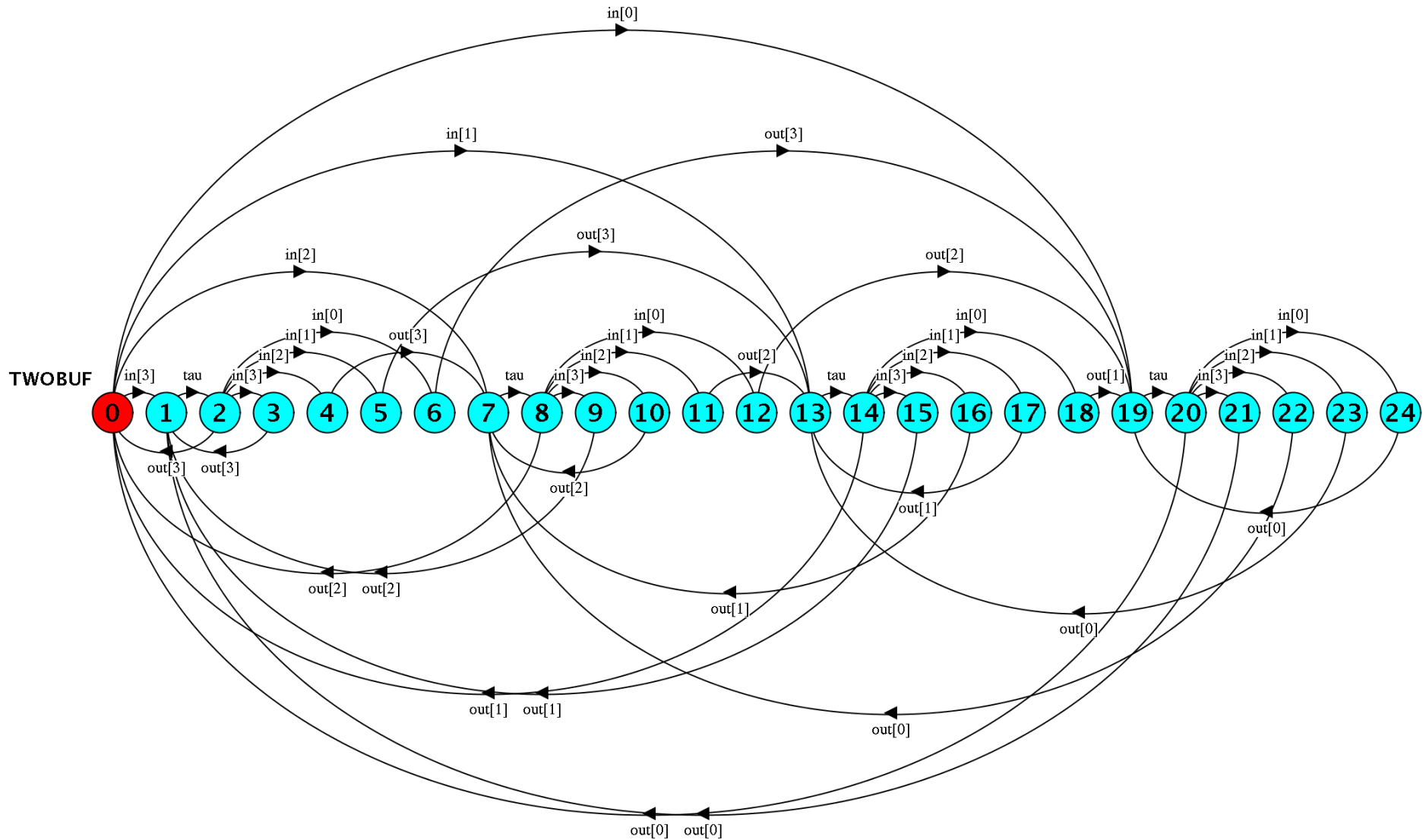
$\text{BUFF} = (\text{in}[i:T] \rightarrow \text{out}[i] \rightarrow \text{BUFF}) .$

$|| \text{TWOBUF} = (\text{a:BUFF} || \text{b:BUFF}) / \{\text{in}/\text{a.in}, \text{a.out}/\text{b.in}, \text{out}/\text{b.out}\} @ \{\text{in}, \text{out}\} .$

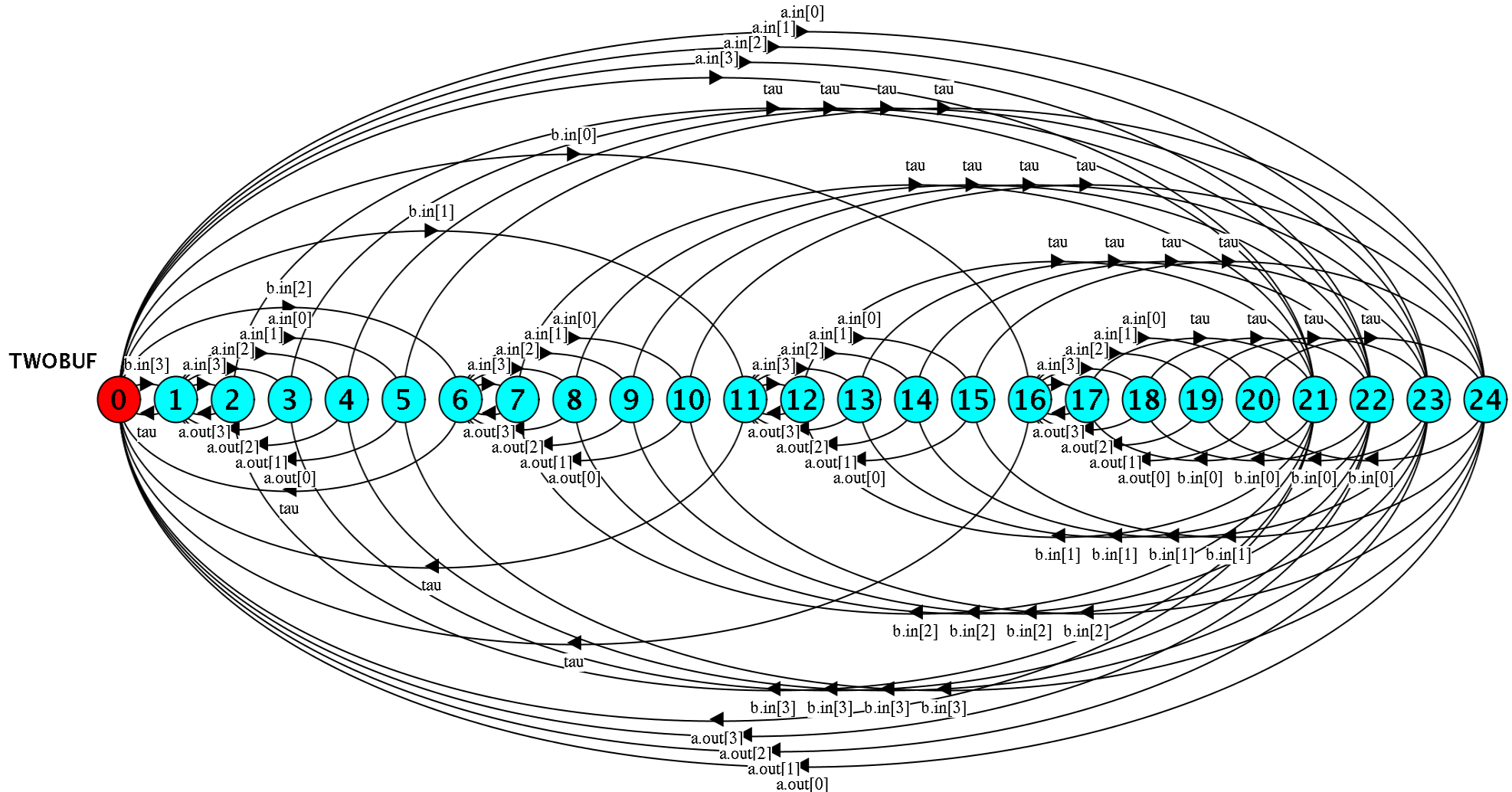


Labels **in**,
out, **a.out**
: $\text{in}[i:T]$,
 $\text{out}[i:T]$,
 $\text{a.out}[i:T]$

Structure Diagrams



Structure Diagrams



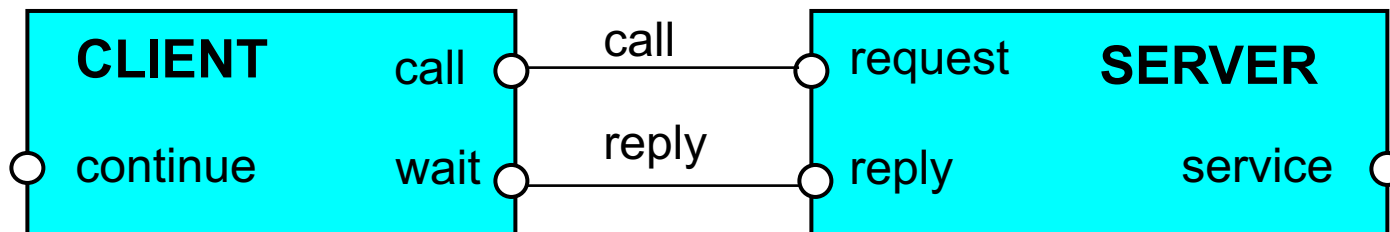
Structure Diagrams

CLIENT = (**call**->**wait**->continue->**CLIENT**) .

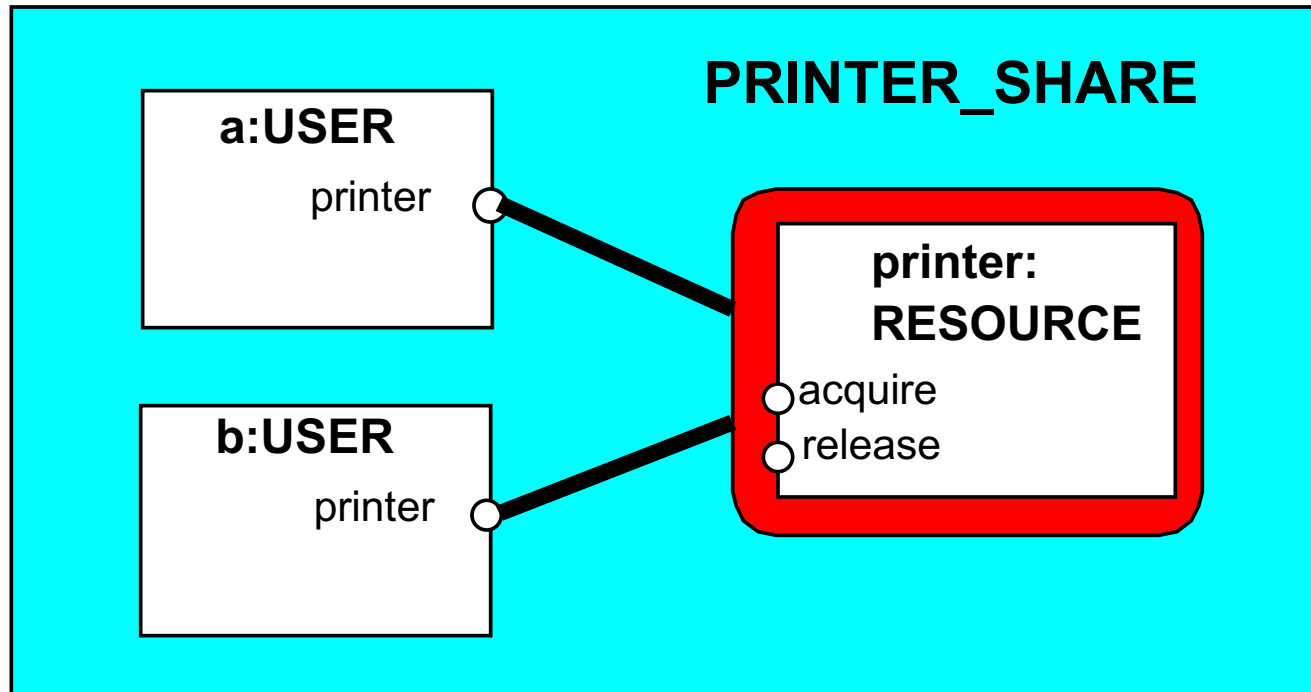
SERVER = (**request**->service->**reply**->**SERVER**) .

CLIENT_SERVER = (**CLIENT** || **SERVER**)
/ {**call/request**, **reply/wait**} .

Structure diagram for **CLIENT_SERVER** ?



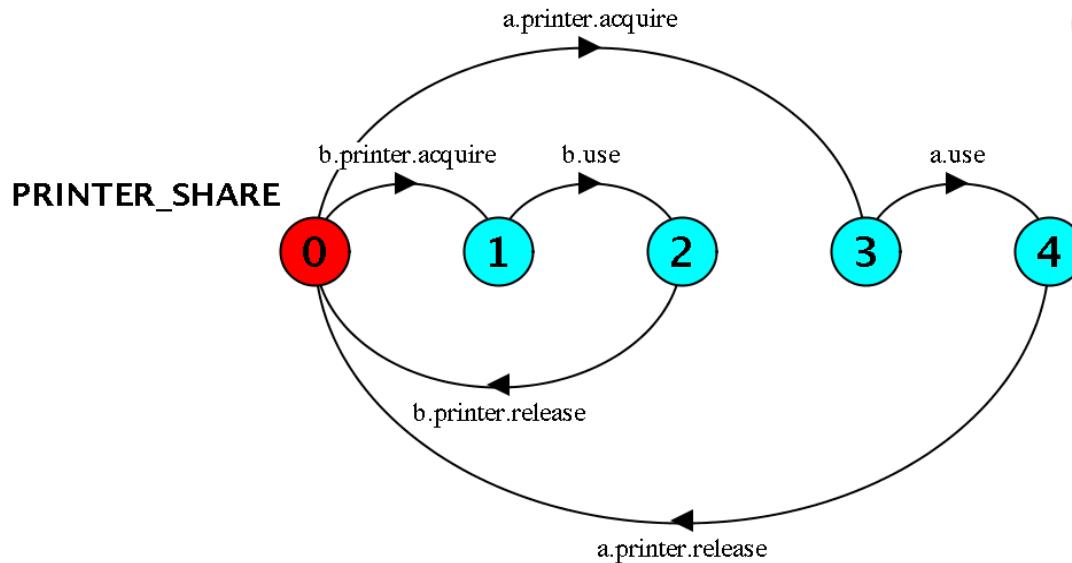
Structure Diagrams – Resource Sharing



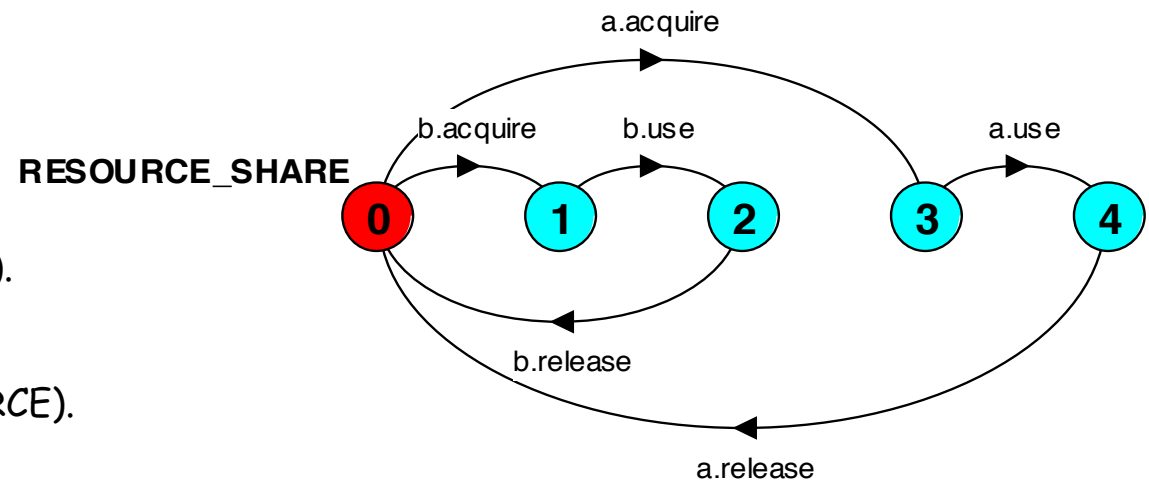
```
RESOURCE = (acquire->release->RESOURCE) .
USER =    (printer.acquire->use
           ->printer.release->USER) \ {use} .
```

```
|| PRINTER_SHARE
= (a:USER || b:USER || {a,b}::printer:RESOURCE) .
```

Structure Diagrams – Resource Sharing



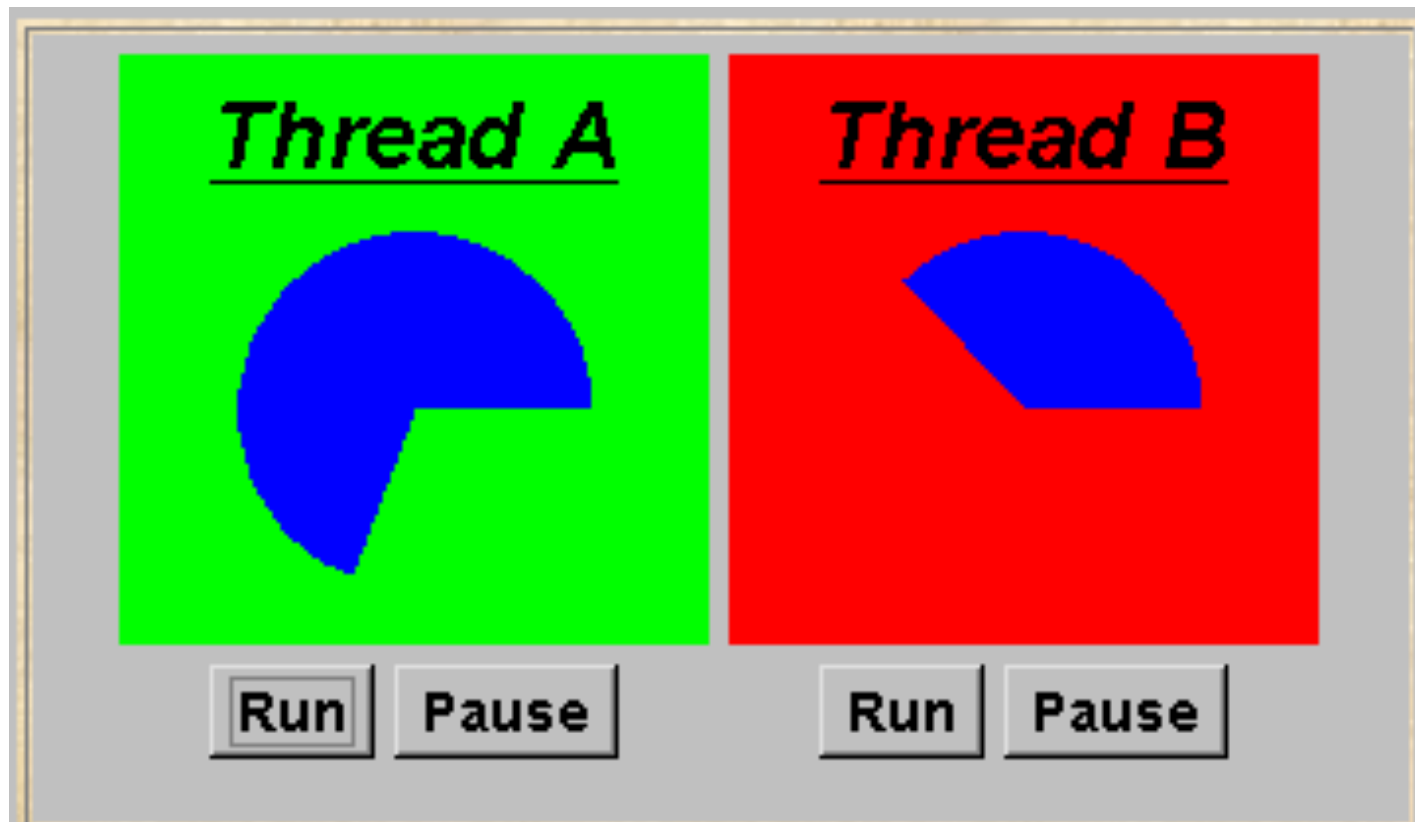
$\text{RESOURCE} = (\text{acquire} \rightarrow \text{release} \rightarrow \text{RESOURCE}).$
 $\text{USER} = (\text{printer.acquire} \rightarrow \text{use} \rightarrow \text{printer.release} \rightarrow \text{USER}).$
 $|| \text{PRINTER_SHARE} =$
 $(\text{a:USER} || \text{b:USER} || \{\text{a,b}\}::\text{printer:RESOURCE}).$



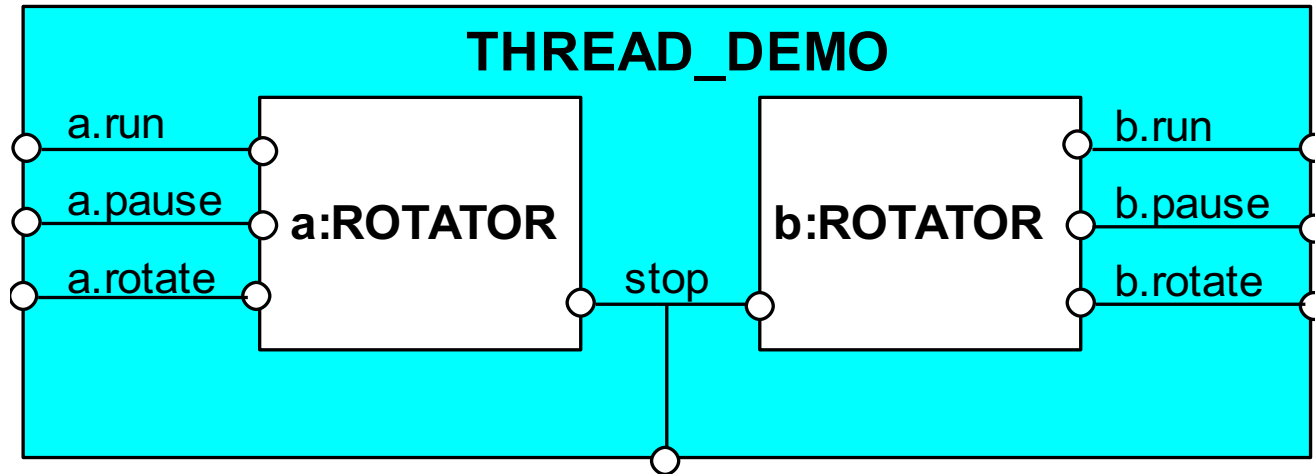
$\text{RESOURCE} = (\text{acquire} \rightarrow \text{release} \rightarrow \text{RESOURCE}).$
 $\text{USER} = (\text{acquire} \rightarrow \text{use} \rightarrow \text{release} \rightarrow \text{USER}).$
 $|| \text{RESOURCE_SHARE} =$
 $(\text{a:USER} || \text{b:USER} || \{\text{a,b}\}::\text{RESOURCE}).$

3.2 Multi-threaded Programs in Java

Concurrency in Java occurs when more than one thread is alive. ThreadDemo has **two threads** which rotate displays.



ThreadDemo model



```

ROTATOR = PAUSED ,
PAUSED  = (run->RUN | pause->PAUSED
           | interrupt->STOP) ,
RUN      = (pause->PAUSED | {run,rotate}->RUN
           | interrupt->STOP) .
    
```

```

|| THREAD_DEMO = (a:ROTATOR || b:ROTATOR)
    
```

```

/{stop/{a,b}.interrupt} .
    
```

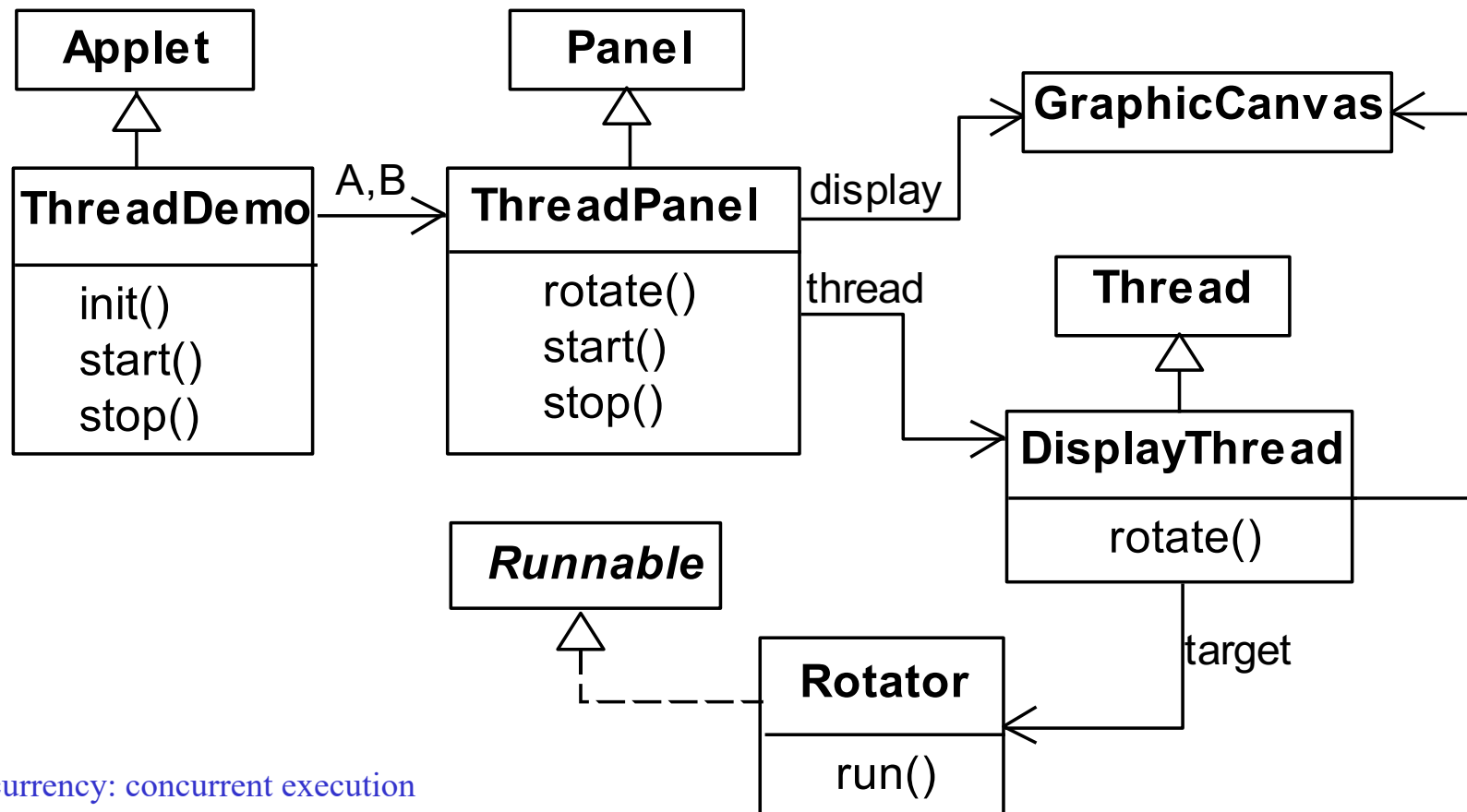
Input: run, pause, interrupt
Output: rotate

Concurrency: concurrent execution

ThreadDemo implementation in Java - class diagram

ThreadDemo creates two **ThreadPanel** displays when initialized.

ThreadPanel manages the **display** and **control** buttons, and delegates calls to **rotate()** to **DisplayThread**. **Rotator** implements the **Runnable** interface.



Rotator class

```
class Rotator implements Runnable {  
    public void run() {  
        try {  
            while(true) ThreadPanel.rotate();  
        } catch (InterruptedException e) {}  
    }  
}
```

Rotator implements the **Runnable** interface, calling **ThreadPanel.rotate()** to move the display.

run() finishes if an exception is raised by **Thread.interrupt()**.

ThreadPanel class

```
public class ThreadPanel extends Panel {  
    // construct display with title and segment color c  
    public ThreadPanel(String title, Color c) {...}  
  
    // rotate display of currently running thread 6 degrees  
    // return value not used in this example  
    public static boolean rotate()  
        throws InterruptedException {...}  
  
    // create a new thread with target r and start it running  
    public void start(Runnable r) {  
        thread = new DisplayThread(canvas, r, ...);  
        thread.start();  
    }  
  
    // stop the thread using Thread.interrupt()  
    public void stop() {thread.interrupt();}  
}
```

ThreadPanel
manages the display
and control buttons for
a thread.

Calls to **rotate()**
are delegated to
DisplayThread.

Threads are created by
the **start()** method,
and terminated by the
stop() method.

ThreadDemo class

```
public class ThreadDemo extends Applet {
    ThreadPanel A; ThreadPanel B;

    public void init() {
        A = new ThreadPanel("Thread A",Color.blue);
        B = new ThreadPanel("Thread B",Color.blue);
        add(A); add(B);
    }

    public void start() {
        A.start(new Rotator());
        B.start(new Rotator());
    }

    public void stop() {
        A.stop();
        B.stop();
    }
}
```

ThreadDemo creates two **ThreadPanel** displays when initialized and two threads when started.

ThreadPanel is used extensively in later demonstration programs.

Summary

◆ Concepts

- concurrent processes and process interaction

◆ Models

- **Asynchronous** (arbitrary speed) & **interleaving** (arbitrary order).
- **Parallel composition** as a finite state process with action interleaving.
- **Process interaction** by shared actions.
- Process labelling and action Relabelling and hiding.
- **Structure diagrams**

◆ Practice

- **Multiple threads** in Java.