## **READ ME**

This folder contains the formalisation of various results in the theory of free groups, which are described in the paper "Formalizing Free Groups in Isabelle/HOL: The Nielsen-Schreier Theorem and the Conjugacy Problem.

The following files are a part of the formalisation and contain original work by the author(s):

- 1. Cancellation.thy
- 2. Conjugacy.thy
- 3. Conjugacy\_Problem.thy
- 4. Distinct\_Inverse.thy
- 5. FreeGroupMain.thy
- 6. Freegroup\_with\_Basis.thy
- 7. Minimal.thy
- 8. NielsenScheier.thy
- 9. N\_Properties.thy
- 10. UniversalProperty.thy
- 11. Word\_Problem.thy

Following file, which is a part of an archive of formal proof distribution, has been added only for the purpose of the ease of the review by reviewers. It contains a truncated version of the original file. Author(s) **do not** make any claims of original

development with regards to the formalisations contained in the following file. It has been redistributed under the permissions granted by BSD license.

1. Generators.thy

The following files contain the Haskell code extracted from our formalisation, using Isabelle's code generation, for the Word Problem and Conjugacy Problem respectively.

- 1. WP.hs
- 2. CP.hs

The formal constructions provided in the paper can be found in the following files:

**Section 4.1**: All definitions are in FreeGroupMain.thy

**Section 4.2:** The definition reduce is in FreeGroupMain.thy, the word\_problem\_reduce can be found in Word\_Problem.thy

 $\begin{tabular}{ll} \textbf{Section 4.3:} is\_free group can be found in Free Group Main.thy. $\tt fg\_with\_basis.can be found in Free Group\_With\_Basis.thy \\ \end{tabular}$ 

**Section 4.4**: All the lemmas contained are in the file- UniversalProperty.thy. The definition <code>gen\_span</code> is contained in Generators.thy.

**Section 5**: All the results are in Conjugacy Problem.thy

**Section 6.1 and Section 6.2**: All the definitions and results are in N\_Properties.thy

**Section 6.3:** Definition of G, X and the lemma span\_X\_eq\_SG are in N\_Properties.thy Lemma N\_reduced\_X and Nielson\_Schreier are in Nielsen\_Schreier.thy

To run all the files in the formalization (along with their dependencies), one could simply run Nielsen\_Schreier.thy