

Practice Problems

1. Practice turning the following systems in augmented matrices, and use MATLAB to solve for their solution, if they have one.

$$\begin{aligned}x + 11y + z &= -15 \\x + 2z - 3y &= 33 \\5y + 12z - x + 2 &= 5\end{aligned}$$

$$\begin{aligned}3x - 8x - 1.3y - 2z &= 71 + z \\x - y + z &= 13 + y + 2.2z \\-9.1x + 2.8y + 82.3z &= 6.5 + 1.9x - 9.4y - 3.3z\end{aligned}$$

2. Find the magnitude of the following vectors: $\vec{a} = \begin{bmatrix} -1 \\ 3 \end{bmatrix}$, $\vec{b} = \begin{bmatrix} 2 \\ 4 \\ 1 \end{bmatrix}$,

$$\vec{c} = \begin{bmatrix} 0.5 \\ 2.4 \\ 10.2 \\ 8.7 \end{bmatrix}$$

3. Let $\vec{a} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$, $\vec{b} = \begin{bmatrix} -6 \\ 4 \end{bmatrix}$, $\vec{c} = \begin{bmatrix} 1 \\ -8 \end{bmatrix}$. Find \vec{v} if $\vec{v} = 2\vec{a} - 3\vec{b} + 4\vec{c}$

4. Find the unit vector of the following vectors: $\vec{x} = \begin{bmatrix} 1 \\ -8 \end{bmatrix}$, $\vec{y} = \begin{bmatrix} -3 \\ 6 \\ 7 \end{bmatrix}$,

$$\vec{z} = \begin{bmatrix} 10 \\ -2 \\ -8 \\ 2 \end{bmatrix}$$

5. Check whether the following pairs of vectors are orthogonal:

$$\vec{a} = \begin{bmatrix} 1 \\ 3 \end{bmatrix} \text{ and } \vec{b} = \begin{bmatrix} -4 \\ -6 \end{bmatrix}$$

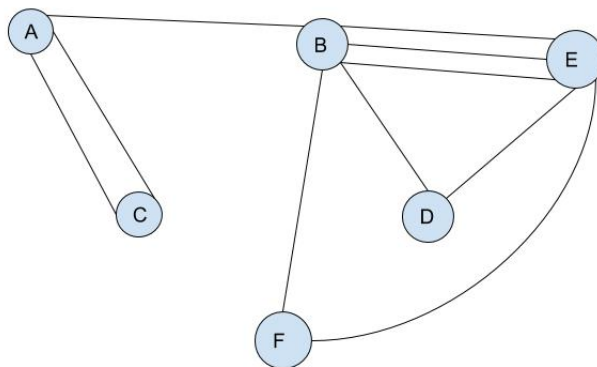
$$\vec{c} = \begin{bmatrix} 12 \\ 4 \\ -2 \end{bmatrix} \text{ and } \vec{d} = \begin{bmatrix} 1 \\ 1 \\ 8 \end{bmatrix}$$

$$\vec{e} = \begin{bmatrix} 6 \\ 6 \\ 6 \end{bmatrix} \text{ and } \vec{f} = \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix}$$

6. Find the transpose and inverse of the following matrix:

$$\mathbf{P} = \begin{pmatrix} 21 & -1 & 43 \\ 91 & -12 & 41 \\ 17 & -26 & -65 \end{pmatrix}$$

7. 6 towns, named A through F, have a series of roads connecting them. If you look at the picture, you can see that there are two roads connecting A and C, for example.



Create a matrix that displays how many roads connect each of the towns. Your matrix should look like

$$\left(\begin{array}{c|cccccc} & A & B & C & D & E & F \\ \hline A & 0 & 1 & 2 & 0 & 0 & 0 \\ B & & & & & & \\ C & & & & & & \\ D & & & & & & \\ E & & & & & & \\ F & & & & & & \end{array} \right)$$

The first row is filled out to demonstrate the solution. Fill in the rest of the spaces.