

Let  $\lambda$  be the scale,  $\kappa$  be the shape factors of the Weibull distribution. Then the variance is given by

$$\sigma = \lambda^2[\Gamma(1 + 2/\kappa) - (\Gamma(1 + 1/\kappa))^2] \quad (1)$$

Equation (1) on its own shows increase of  $\lambda$  increase in the variance (when  $\lambda > 1$ ). For the original model, the parameters of larva generation 1 is given by:

$$(\kappa, \lambda) = (4.42486, 742.9410)$$

If we increase the scale by 10% and 20% we get

$$(\kappa_{10}, \lambda_{10}) = (4.42486, 817.2351)$$

and

$$(\kappa_{20}, \lambda_{20}) = (4.42486, 891.5292)$$

respectively. Computing the variance then would be easy.

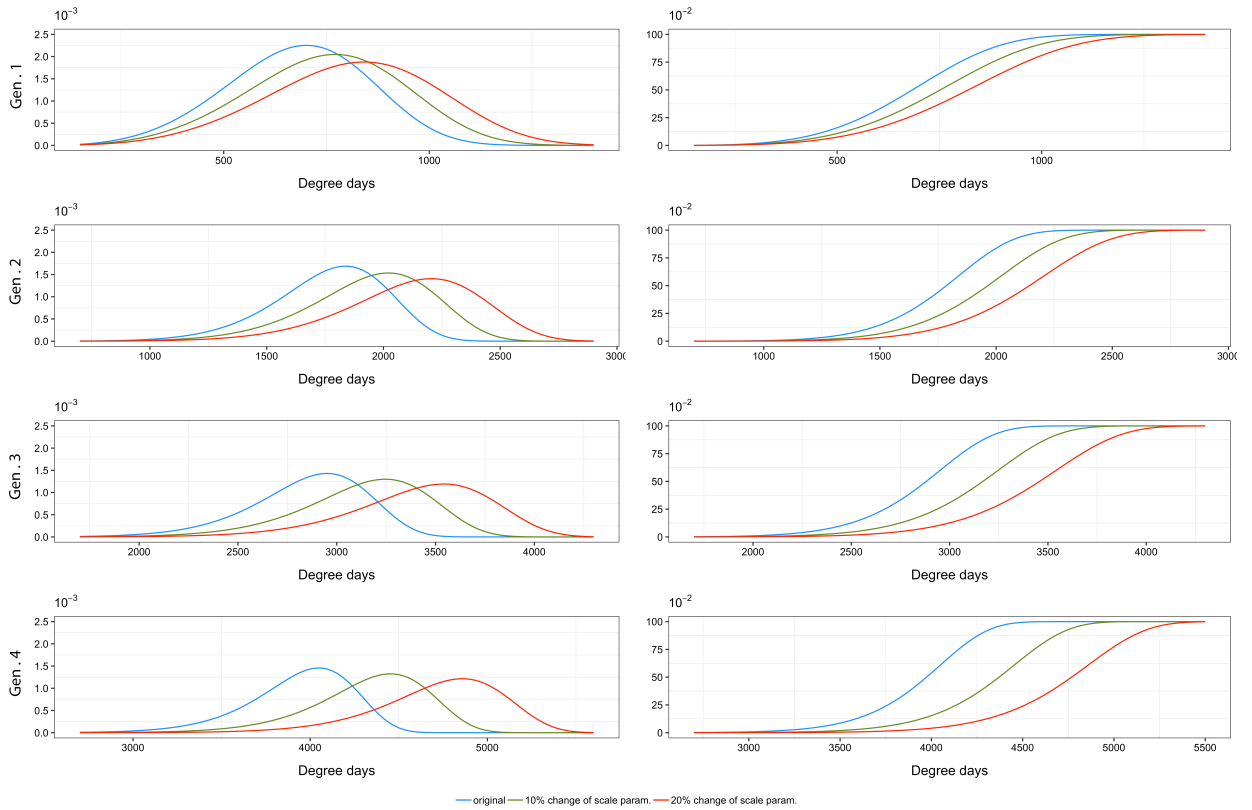


Figure 1: Weibull density and cumulative distributions.

Also, the lowered peaks show, the distributions are not just shifted.

# 1 Another take from cumulative function

The cumulative function of Weibull is given by

$$f(x, \lambda, \kappa) = 1 - \exp(-(x/\lambda)^\kappa)$$

hence,

$$f'(x, \lambda, \kappa) = \kappa/\lambda(x/\lambda)^{\kappa-1} - \exp(-(x/\lambda)^\kappa)$$

Using R and quantile function we can find the  $x$ 's for which cumulative probability is 0.5.

`qweibull(0.5, shape=shape, scale=scale_orig)` produces  $x = 683.8826$ .

`qweibull(0.5, shape=shape, scale=scale_10_percent)` produces  $x_{10} = 752.2708$ .

`qweibull(0.5, shape=shape, scale=scale_20_percent)` produces  $x_{20} = 820.6591$ .

Plugging the shape and scales with associated  $x$  into the derivative equation above we get

$$\left\{ \begin{array}{ll} f'(x, \lambda, \kappa_{orig}) & = 0.002242402 \\ f'(x_{10}, \lambda, \kappa_{10\_percent}) & = 0.002038547 \\ f'(x_{20}, \lambda, \kappa_{20\_percent}) & = 0.001868668 \end{array} \right. \quad (2)$$

Though, they are close, and visually may seem shifted, they are not.