

COLUMBIA UNIVERSITY

**MECE 4510 EVOLUTIONARY COMPUTATION AND  
DESIGN AUTOMATION**

**Evolved robot**

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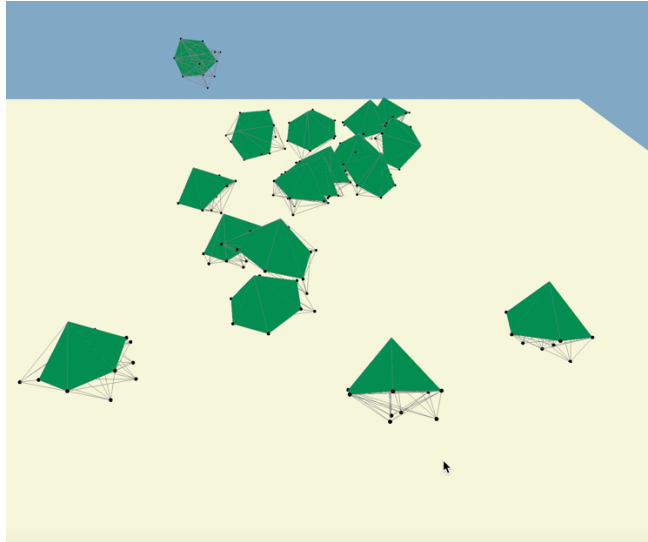
Instructor: Dr. Hod Lipson

Grace Hours Used: 20

Grace Hours Remaining: 126h

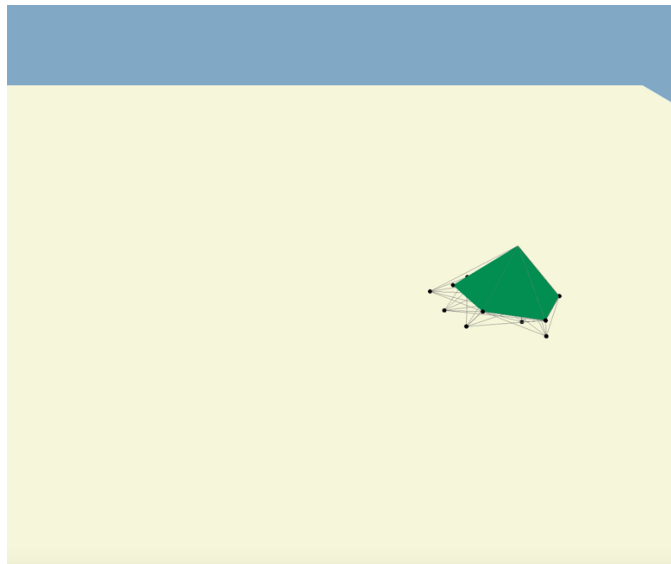
Dec 8, 2019

## Result

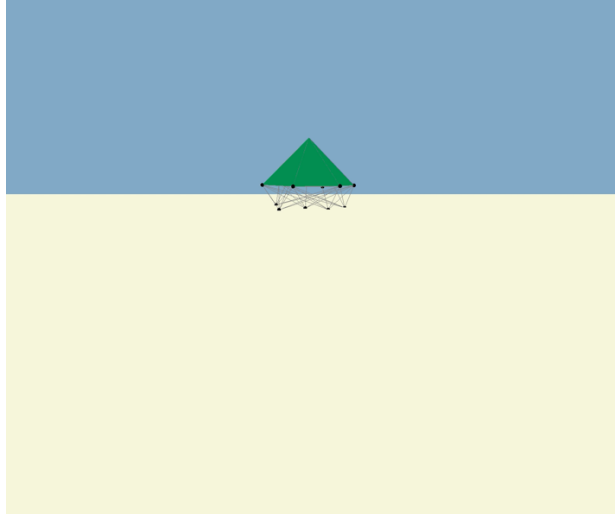


[https://youtu.be/hAcLQ7\\_2fcw](https://youtu.be/hAcLQ7_2fcw)<https://youtu.be/ppW31Lb8cPg>

the fast robot



<https://youtu.be/rpAglpyxgio>



<https://www.youtube.com/watch?v=oryK-FSM-dM>

## Method

### Description

In this phase, we should evolve a robot with a variable morphology. Unlike last phase of assignment 3, we change the number of feet of the robot. This base robot contains 13 masses and 72 springs, the picture as followed, just similar to last phase. We choose the all springs connected to each foot to evolve. And then after 20 second, we delete the worst robot and randomly create a new robot with different number of foot and different gene, and evolve them.

### Evolution

Like last phase of assignment 3, the population size is 20, the definition of fitness is the distance away from the initial position at x axis. Selection is keeping top 50% population by fitness to the next generation. Unlike last phase, crossover is choosing two parents from top 50% population and exchange the part of them even though their length is different. And then deleting the worst gene and robot, and adding a new gene and a new robot based on this new gene. The robot has randomly number of feet and randomly position of the feet. At last we mutate the whole generation with a small probability. Each generation we let the robot move for 20 second and then evolve them.

### Parameter

#### 1. simulation parameters

```
timeStep = 0.002;  
Nground = 50000;  
dampening = 1;  
frictionCoefficient = 0.5;  
generationT = 6s; // the time in one generation
```

#### 2. robot parameters

```
k = 9000; // spring constant to other spring that are not evolved  
mass = 2; // mass of one joint of robot  
length = 0.1;  
gravity = 9.81;
```

#### 3. evolutionary parameters

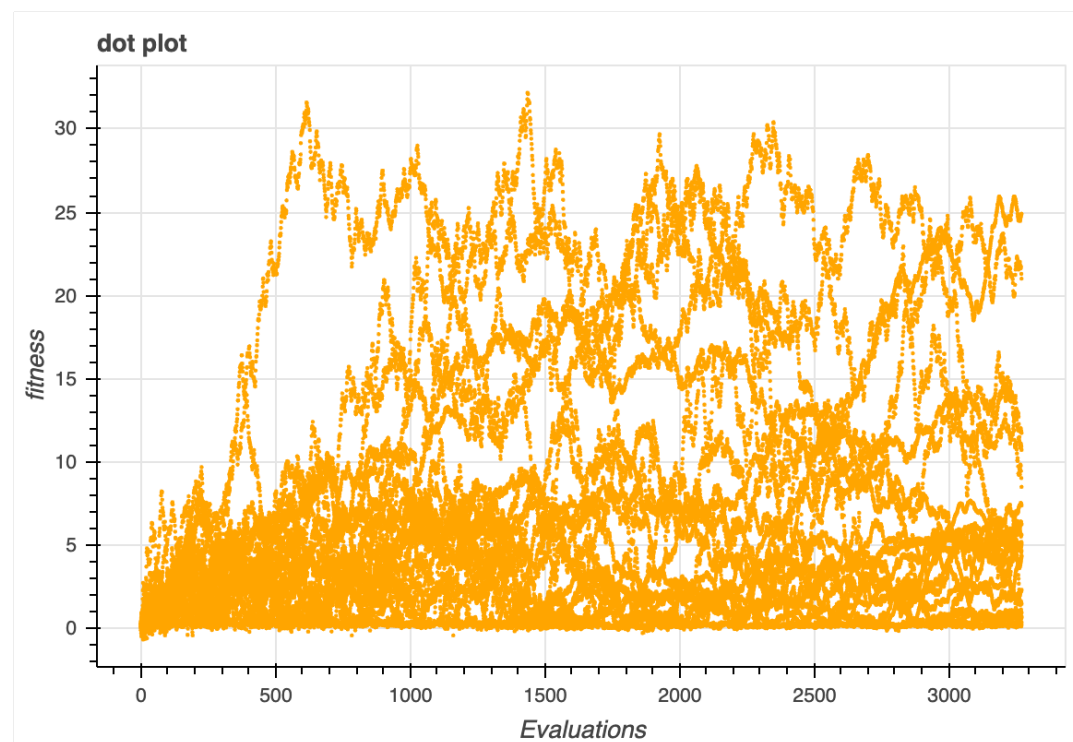
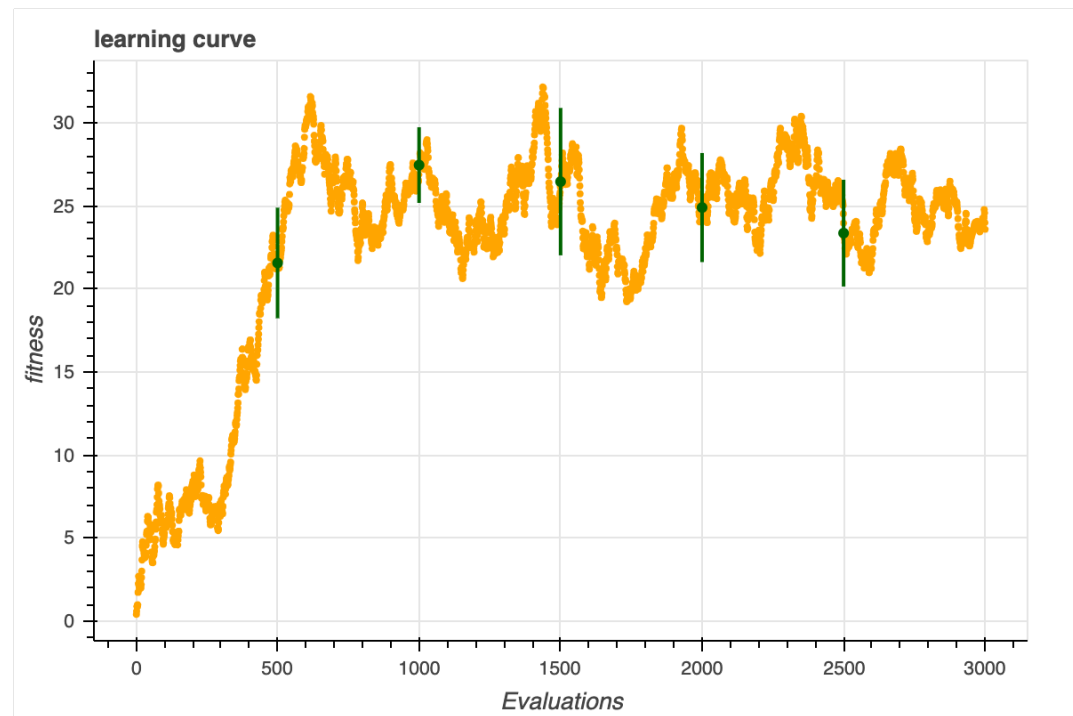
```
k : 600-5000; the range of evolved spring  
b: -1——1; the range of b  
c: -2PI——2PI; the range of c  
size = 20; //population size  
generation = 3000; // evaluation  
mutation probability = 0.5
```

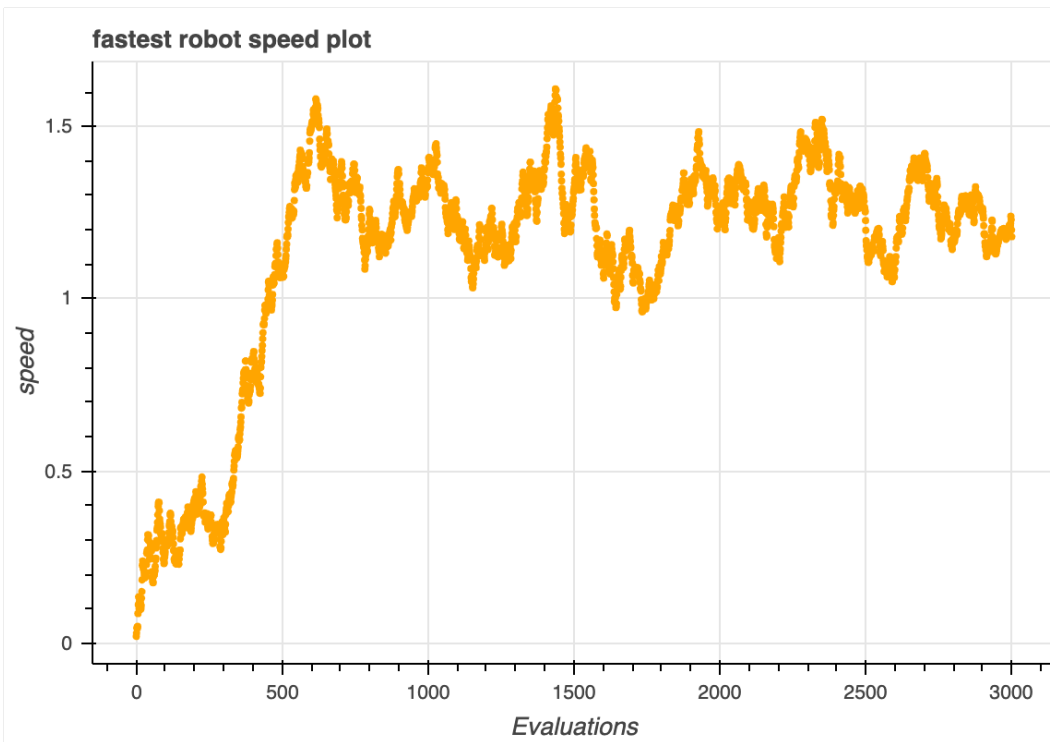
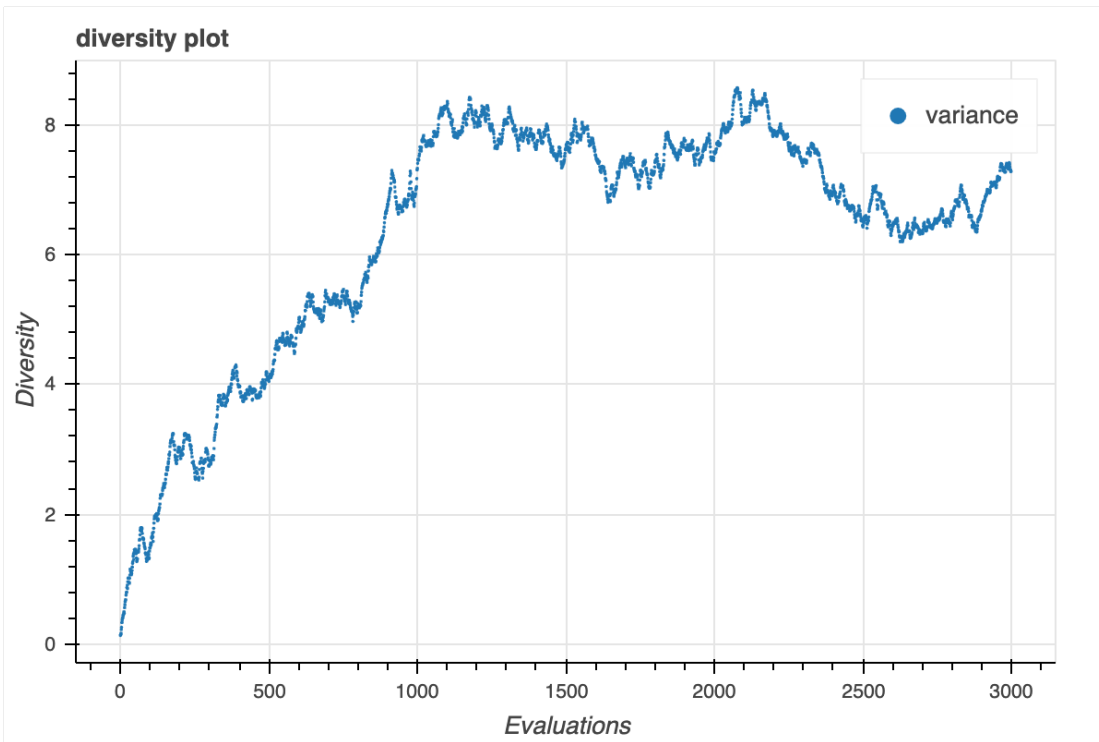
### Analysis

Compared to last phase of assignment, after lots of tempts to get a reasonable range of

parameters, we concluded that the shape of robot is important and all of the parameters play a significant role in the robot performance. Among three parameters ( $k$ ,  $b$ ,  $c$ ), it turns out that the  $k$  is the key of the robot. If the  $k$  is too large or too small, robots would be very unstable. So we choose a range of 600-5000.

## Performance





## Appendix

```
#include "HW3.h"

GLfloat worldRotation[16] = { 1,0,0,0,0,0,1,0,0,1,0,0,0,0,0,1 };

struct MASS
{
    double m;        // mass
    double p[3];     // 3D position
    double v[3];     // 3D velocity
    double a[3];     // 3D acceleration
};

struct SPRING
{
    double k;        // spring constant
    double L_0;     // rest length
    int m1;         // first mass connected
    int m2;         // second mass connected
};

struct GENE {
    double k;
    double b;
    double c;
};

//int num_foot = 2 + rand() % 6;

//ofstream outFile1("distance3.txt");
//ofstream outFile2("bestgene3.txt");
//ofstream outFile3("dot3.txt");

//struct Cube {
//    struct MASS cubemass[8];
//    struct SPRING cubespring[28];
//};

float L(MASS mass1, MASS mass2) {
    double length = sqrt(pow((mass1.p[0] - mass2.p[0]), 2) + pow((mass1.p[1] -
mass2.p[1]), 2) + pow((mass1.p[2] - mass2.p[2]), 2));

    return length;
}
```



```

//vector<MASS> joint = jointmass(mass, length, 0, 0, 0.01);
//
//
//vector<SPRING> spring = cubespring(length, k);


GLuint tex;
GLUquadric* sphere;
void make_tex(void)
{
    unsigned char data[256][256][3];
    for (int y = 0; y < 255; y++) {
        for (int x = 0; x < 255; x++) {
            unsigned char* p = data[y][x];
            p[0] = p[1] = p[2] = (x ^ y) & 8 ? 255 : 0;
        }
    }
    glGenTextures(1, &tex);
    glBindTexture(GL_TEXTURE_2D, tex);
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, 256, 256, 0, GL_RGB, GL_UNSIGNED_BYTE, (const
GLvoid*)data);
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_LINEAR);
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_LINEAR);
}

void init(void)
{
    glEnable(GL_DEPTH_TEST);
    make_tex();
    sphere = gluNewQuadric();
    glEnable(GL_TEXTURE_2D);
}

class Robot {
private:
    vector<GENE> walkgene;

public:
    vector<MASS> joint;
    vector<SPRING> spring;
    int mass_num;
    int num_sp;
}

```

```

int num_foot;
vector<double> original;
double initl[3] = { 0,0,0 };
Robot(double x, double y, double z, int num, vector<GENE> newGene)
{
    mass_num = 7 + num;
    num_foot = num;
    num_sp = 21+ 6 * num_foot;
    initl[0] = x;
    initl[1] = y;
    initl[2] = z;
    walkgene = newGene;
    joint = jointmass(x, y, z, num);
    cubespring(walkgene);
}

vector<MASS> jointmass(double x, double y, double z, int num)
{
    vector<MASS> joint(7 + num);
    double subtle = length / 2;
    joint[0] = { mass, {x + 1.5 * length,y + length * sqrt(3) / 2, z + 1.5 * length},
{0,0,0}, {0,0,0} };
    joint[1] = { mass, {x + length ,y + sqrt(3) * length,z + 0.5 * length}, {0,0,0},
{0,0,0} };
    joint[2] = { mass, {x + 2 * length ,y + sqrt(3) * length ,z + 0.5 * length},
{0,0,0}, {0,0,0} };
    joint[3] = { mass, {x + length / 2,y + length / 2 * sqrt(3),z + 0.5 * length},
{0,0,0}, {0,0,0} };
    joint[4] = { mass, {x + length / 2 + 2 * length ,y + length / 2 * sqrt(3),z + 0.5
* length}, {0,0,0}, {0,0,0} };
    joint[5] = { mass, {x + length,y,z + 0.5 * length}, {0,0,0}, {0,0,0} };
    joint[6] = { mass, {x + 2 * length ,y ,z + 0.5 * length}, {0,0,0}, {0,0,0} };
    for (int i = 7; i < 7 + num; i++) {
        double a = -length + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (2 * length)));
        double b = -length + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (2 * length)));
        joint[i] = { mass, {joint[0].p[0] + a ,joint[0].p[1] + b, z}, {0,0,0},
{0,0,0} };
    }
    //joint[7] = { mass, {x + 1.5 * length ,y + length * 3 * sqrt(3) / 2 - subtle,z},
{0,0,0}, {0,0,0} };
    //joint[8] = { mass, {x + subtle ,y + sqrt(3) * length - subtle ,z}, {0,0,0},

```

```

{0,0,0} };

    //joint[9] = { mass, {x + 3 * length - subtle,y + sqrt(3) * length - subtle,z },
{0,0,0}, {0,0,0} };

    //joint[10] = { mass, {x + subtle ,y + subtle ,z }, {0,0,0}, {0,0,0} };
    //joint[11] = { mass, {x + 3 * length - subtle, y + subtle ,z}, {0,0,0}, {0,0,0} };
    //joint[12] = { mass, {x + 1.5 * length,y - length * sqrt(3) / 2 + subtle, z},
{0,0,0}, {0,0,0} };

    return joint;
}

void cubespring(vector<GENE> walkgene)
{

    int pointer = 0;
    for (int i = 0; i < 6; i++) {
        for (int j = i + 1; j < 7; j++) {
            original.push_back(L(joint[i], joint[j]));
            spring.push_back({ walkgene[pointer].k,L(joint[i],joint[j]),i,j });
//            cout << spring[i * j].k << endl;
            pointer++;
        }
    }

    for (int i = 7; i < 7 + num_foot; i++) {
        for (int j = 0; j < 6; j++) {
            original.push_back(L(joint[i], joint[j]));
            spring.push_back({ walkgene[pointer].k,L(joint[i],joint[j]),i,j });
            pointer++;
        }
    }

}

void drawcube()
{

    glPushMatrix();
    glMultMatrixf(worldRotation);

    glBegin(GL_TRIANGLES);
    glColor3f(R,G,B);
    glVertex3f(GLfloat(joint[0].p[0]),          GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));

```

```

        glVertex3f(GLfloat(joint[1].p[0]),
GLfloat(joint[1].p[1]),
GLfloat(joint[1].p[2]));

        glVertex3f(GLfloat(joint[2].p[0]),
GLfloat(joint[2].p[1]),
GLfloat(joint[2].p[2]));

        glEnd();

        glBegin(GL_TRIANGLES);
        glColor3f(R,G,B);
        glVertex3f(GLfloat(joint[0].p[0]),
GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));
        glVertex3f(GLfloat(joint[1].p[0]),
GLfloat(joint[1].p[1]),
GLfloat(joint[1].p[2]));
        glVertex3f(GLfloat(joint[3].p[0]),
GLfloat(joint[3].p[1]),
GLfloat(joint[3].p[2]));
        glEnd();

        glBegin(GL_TRIANGLES);
        glColor3f(R,G,B);
        glVertex3f(GLfloat(joint[0].p[0]),
GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));
        glVertex3f(GLfloat(joint[5].p[0]),
GLfloat(joint[5].p[1]),
GLfloat(joint[5].p[2]));
        glVertex3f(GLfloat(joint[3].p[0]),
GLfloat(joint[3].p[1]),
GLfloat(joint[3].p[2]));
        glEnd();

        glBegin(GL_TRIANGLES);
        glColor3f(R,G,B);
        glVertex3f(GLfloat(joint[0].p[0]),
GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));
        glVertex3f(GLfloat(joint[5].p[0]),
GLfloat(joint[5].p[1]),
GLfloat(joint[5].p[2]));
        glVertex3f(GLfloat(joint[6].p[0]),
GLfloat(joint[6].p[1]),
GLfloat(joint[6].p[2]));
        glEnd();

        glBegin(GL_TRIANGLES);
        glColor3f(R,G,B);
        glVertex3f(GLfloat(joint[0].p[0]),
GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));
        glVertex3f(GLfloat(joint[4].p[0]),
GLfloat(joint[4].p[1]),
GLfloat(joint[4].p[2]));
        glVertex3f(GLfloat(joint[6].p[0]),
GLfloat(joint[6].p[1]),
GLfloat(joint[6].p[2]));

```

```

    glEnd();

    glBegin(GL_TRIANGLES);
    glColor3f(R,G,B);
    glVertex3f(GLfloat(joint[0].p[0]),          GLfloat(joint[0].p[1]),
GLfloat(joint[0].p[2]));
    glVertex3f(GLfloat(joint[4].p[0]),          GLfloat(joint[4].p[1]),
GLfloat(joint[4].p[2]));
    glVertex3f(GLfloat(joint[2].p[0]),          GLfloat(joint[2].p[1]),
GLfloat(joint[2].p[2]));
    glEnd();
    glPopMatrix();

//
GLUquadric* quad[mass_num];
for (int i = 1; i < mass_num; i++) {

    glColor3f(R1,G1, B1);
    quad[i] = gluNewQuadric();
    glPushMatrix();
    glMultMatrixf(worldRotation);
    glTranslated(joint[i].p[0], joint[i].p[1], joint[i].p[2]);

    gluSphere(quad[i], 1.0 / 250, 10, 10);
    //          if (i == 6) { gluSphere(quad[i], 1.0 / 100, 10, 10); }
    glPopMatrix();

}

for (int i = 0; i < num_sp; i++) {
    int a = spring[i].m1;
    int b = spring[i].m2;

    glColor3f(0.5, 0.5, 0.5);
    glPushMatrix();
    glMultMatrixf(worldRotation);
    glBegin(GL_LINES);
    glLineWidth(20);
    glVertex3f(joint[a].p[0], joint[a].p[1], joint[a].p[2]);
    glVertex3f(joint[b].p[0], joint[b].p[1], joint[b].p[2]);
    glEnd();
    glPopMatrix();
}

```

```

    }
}

void drawground()
{
    glPushMatrix();
    glColor3f(0.96078, 0.96078, 0.86274);
    glBegin(GL_QUADS);
    glNormal3f(0, 1, 0);
    glTexCoord2f(0.0, 0.0); glVertex3f(-1.5, +0.0, -1.5);
    glTexCoord2f(0.0, 1); glVertex3f(+1.5, +0.0, -1.5);
    glTexCoord2f(1, 1); glVertex3f(+1.5, +0.0, +1.5);
    glTexCoord2f(1, 0.0); glVertex3f(-1.5, +0.0, +1.5);
    glEnd();
    glPopMatrix();
    glDisable(GL_TEXTURE_2D);
    for (int i = 0; i < 10; i++) {
        for (int j = -9; j < 10; j++) {
            glColor3f(0, 1, 0);
            glPushMatrix();
            glMultMatrixf(worldRotation);
            glBegin(GL_LINES);
            glLineWidth(10);
            glVertex3f(-0.5 * i / 10, 0.02, 0.5 * j / 10);
            //
glV/Users/chiqu/class2019fall/EA/assignment3/HW3/HW3.cppvertex3f(0.5*i/10,    0.5*j/10,
0.01);

            glEnd();
            glPopMatrix();
        }
    }
}

void simulate() {
    vector<vector<double>> cForces(num_foot + 7, vector<double>(3));
    for (int i = 0; i < mass_num; i++) {
        cForces[i][0] = 0.0;
        cForces[i][1] = 0.0;
        cForces[i][2] = -joint[i].m * gravity;
    }

    for (int i = 0; i < num_sp; i++) {
        MASS mass1 = joint[spring[i].m1];
        MASS mass2 = joint[spring[i].m2];
    }
}

```

```

        //if (T < 1) {
//            if (i == 18 or i == 37 or i == 17 or i == 27 or i == 29 or i == 39 or i ==
46 or i == 48 or i == 54 or i == 56 or i == 62 or i == 64) {
//
//                spring[i].L_0 = original[i] * (1 + walkgene[i].b * sin(500 * T +
walkgene[i].c));
//                if (i > num_sp / 2) {
//                    spring[i].L_0 = original[i] * (1 + walkgene[i].b * cos(500 * T +
walkgene[i].c));
//                }}
            if (i > 21 && i < 21 + 6 * num_foot) {
                spring[i].L_0 = original[i] * (1 + walkgene[i].b * sin(500 * T +
walkgene[i].c));
            }

            double pd[3] = { mass2.p[0] - mass1.p[0], mass2.p[1] - mass1.p[1], mass2.p[2] -
mass1.p[2] };
            double new_L = L(mass1, mass2);
            double L_0 = spring[i].L_0;
            double force = spring[i].k * fabs(new_L - L_0);
            //springenergy += k * pow((new_L - L_0), 2) / 2;
            //cout <<i<<"---new_L---" <<new_L << endl;
            double norm_pd[3] = { pd[0] / new_L, pd[1] / new_L, pd[2] / new_L };
            //cout << i << "---force---" << force << endl;
            //compression
            if (new_L < spring[i].L_0) {
                cForces[spring[i].m1][0] -= norm_pd[0] * force;
                cForces[spring[i].m1][1] -= norm_pd[1] * force;
                cForces[spring[i].m1][2] -= norm_pd[2] * force;
                cForces[spring[i].m2][0] += norm_pd[0] * force;
                cForces[spring[i].m2][1] += norm_pd[1] * force;
                cForces[spring[i].m2][2] += norm_pd[2] * force;
            }

            //tension
            else {
                cForces[spring[i].m1][0] += norm_pd[0] * force;
                cForces[spring[i].m1][1] += norm_pd[1] * force;
                cForces[spring[i].m1][2] += norm_pd[2] * force;
                cForces[spring[i].m2][0] -= norm_pd[0] * force;
                cForces[spring[i].m2][1] -= norm_pd[1] * force;
                cForces[spring[i].m2][2] -= norm_pd[2] * force;
            }
        }
    }
}

```

```

//cout << T << "tan " << springenergy << endl;
for (int i = 0; i < mass_num; i++) {
    if (joint[i].p[2] <= 0) {
        cForces[i][2] -= Nground * joint[i].p[2];
        //cForces[i][2] -= joint[i].m*0.981;
        //groundenergy += Nground * pow(joint[i].p[2], 2) / 2;
        double Fh = sqrt(pow(cForces[i][0], 2) + pow(cForces[i][1], 2));
        double Fv = cForces[i][2];
        if (Fh < Fv * frictionCoefficient) {
            cForces[i][0] = 0;
            cForces[i][1] = 0;
            joint[i].v[0] = 0;
            joint[i].v[1] = 0;
        }
        else {
            double Fh_new = Fh - Fv * frictionCoefficient;
            cForces[i][0] = cForces[i][0] * Fh_new / Fh;
            cForces[i][1] = cForces[i][1] * Fh_new / Fh;
        }
    }
    //cout << T << " " << groundenergy << endl;
    for (int j = 0; j < 3; j++) {
        joint[i].a[j] = cForces[i][j] / joint[i].m;
        joint[i].v[j] += joint[i].a[j] * timeStep;
        joint[i].v[j] *= dampening;
        joint[i].p[j] += joint[i].v[j] * timeStep;
    }
    //cout << cube[i].p[j] << endl;
//gravityenergy
    //gravityenergy += joint[i].m * gravity * joint[i].p[2];
    //kinetic
    double norm_v = sqrt(pow(joint[i].v[0], 2) + pow(joint[i].v[1], 2) +
pow(joint[i].v[2], 2));
    //kineticenergy += joint[i].m * pow(norm_v, 2) / 2;

    //      cout << i << joint[i].p[2] << endl;
    //      cout << cForces[1][2] << endl;
}
//cout << "hhhhh"<< endl;

//cout << "wtfh" << endl;

drawground();

```



```

        T = T + timeStep;

    }

};

vector<vector<GENE>> populationGene;
vector<Robot> robot;
vector<double> totald2;
vector<vector<GENE>> newgenepop;
vector<vector<GENE>> nextpop;
vector<GENE> bestGene;
int populationsize = size;

vector<double> bestdistance;

//double maxdistance;
vector<vector<GENE>> bestgene;

vector<GENE> crossover(vector<GENE> p1, vector<GENE> p2) {
    if (p1.size() < p2.size()) {
        int crossposition = 7 + rand() % static_cast<int>(p1.size());

        vector<GENE> offspring = p1;
        //cout << "crossover" << endl;
        for (int i = 0; i < crossposition; i++) {
            offspring[i] = p2[i];
        }

        return offspring;
    }

    else {
        int crossposition = 7 + rand() % static_cast<int>(p2.size());
        vector<GENE> offspring = p2;
        //cout << "crossover" << endl;
        for (int i = 0; i < crossposition; i++) {
            offspring[i] = p1[i];
        }
    }
}

```

```

        return offspring;
    }
}

vector<vector<GENE>> genereateGene(int num_foot) {
    vector<vector<GENE>> populationGene1;
    for (int i = 0; i < populationsize; i++) {
        vector<GENE> temp;
        GENE temp_2;
        //      vector<GENE> temp_4 = {{9000,0,0},{900,0, 0},{9000,0, 0},{900,0, 0},{9000, 0,
0},{9000, 0, 0},{9000,0, 0},{9000, 0, 0},{9000, 0, 0},{9000, 0, 0},{9000, 0, 0},{9000,
0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {9000,0, 0},
        //      {9000, 0, 0},
        //      {9000, 0, 0},
        //      {1149.03, 0.89871, 1.59599},
        //      {3387.09, 0.0564407, 1.23423},
        //      {2002.62, 0.699834, -4.80743},
        //      {2914.94, 0.553911, 1.1057},
        //      {817.105, 0.321366, -3.82508},
        //      {4385, 0.813266, 0.71422},
        //      {1138.03, 0.402719, -0.0315316},
        //      {896.933, 0.0647815, 3.55796},
        //      {1613.19, 0.143684, 5.02053},
        //      {1201.31, 0.177645, 2.19434},
        //      {682.43, 0.771142, 1.13884},
        //      {1140.98, 0.416475, 2.54433},
        //      {1074.05, 0.766175,-5.02824},
        //      {2116.14, 0.297064, 3.23736},
        //      {2055.34, 0.0556062, 0.919644},
        //      {794.846, 0.637075, -2.20964},
        //      {2764.1, 0.367395, 3.83164},
        //      {1421.09, 0.473704, 0.641933},
        //      {2274.68, 0.883705, -0.953366},
        //      {1192.37, 0.17468, 4.34046},
        //      {1291.49, 0.273336, 5.86253},
        //      {1497.38, 0.0790328, -2.46469},

```

```

//      {2897.75, 0.861622, -2.79981},
//      {932.343, 0.309218, -5.87749},
//      {1368.84, 0.606336, 2.27619},
//      {963.681, 0.530644, 0.467611},
//      {870.933, 0.522875, 5.70392},
//      {4467.87, 0.359379, -5.15406},
//      {993.408, 0.668242, -4.40994}};

double k_1 = 9000;
double b_1 = 0;
double c_1 = 0;
int num_sp = 21 + 6 * num_foot;
for (int j = 0; j < num_sp; j++) {
//      double k_1 = 100 + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (1000 - 100)));
//      //      if (j == 18 or j == 37 or j == 17 or j == 27 or j == 29 or
j == 39 or j == 46 or j == 48 or j == 54 or j == 56 or j == 62 or j == 64) {
//      if (j < num_sp && j > 21) {
//      k_1 = 600 + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (5000 - 600)));
//      b_1 = static_cast <float> (rand()) / static_cast <float> (RAND_MAX /
1);
//      c_1 = -2 * M_PI + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (4 * M_PI)));
//      }
//      else {
//      k_1 = 9000;
//      b_1 = 0;
//      c_1 = 0;

k_1 = 9000;
b_1 = 0;
c_1 = 0;

temp_2 = { k_1, b_1, c_1 };

temp.push_back(temp_2);}
//      tempVec.push_back(k1);
//      tempVec.push_back(b1);
//      tempVec.push_back(c1);

populationGenel.push_back(temp);

}

```

```

        return populationGenel;
    }

vector<Robot> sortrobot(vector<Robot> robot, vector<double>totald){

    //    vector<int> Index;
    //        for (int i = 0; i < populationsize; i++) {
    //            cout<<"totald "<<totald[i]<<endl;
    //            double temp_min = totald[i];
    //            int pointer = i;
    //            for (int j = i; j < populationsize; j++) {
    //                if (totald[j] > temp_min) {
    //                    temp_min = totald[j];
    //                    pointer = j;
    //                }
    //            }
    //            sort(totald.begin(),totald.end());
    //            double a = *max_element (totald.begin(), totald.end());
    //            k = distance(totald,a);
    //            cout<<"pointer"<<pointer<<endl;
    //            Index.push_back(pointer);
    //        }
    vector<size_t> idx(totald.size());
    iota(idx.begin(), idx.end(), 0);

    // sort indexes based on comparing values in v
    sort(idx.begin(), idx.end(),
        [totald](size_t i1, size_t i2) {return totald[i1] > totald[i2];});

    vector<Robot> tempRobot;
    for(int i = 0; i<populationsize;i++){

        Robot tempp = robot[idx[i]];
        tempRobot.push_back(tempp);
    }

    return tempRobot;

}

```

```

vector<vector<GENE>> selection(vector<vector<GENE>> populationGene, vector<double>
totald) {
    vector<vector<GENE>> newgenepop;
    vector<size_t> idx(totald.size());
    iota(idx.begin(), idx.end(), 0);

    // sort indexes based on comparing values in v
    sort(idx.begin(), idx.end(),
        [totald](size_t i1, size_t i2) {return totald[i1] > totald[i2];});

    vector<size_t> Index = idx;
    //
    //     for (int i = 0; i < populationsize; i++) {
    //         double temp_min = totald[0];
    //         int pointer = 0;
    //         for (int j = i; j < populationsize; j++) {
    //             if (totald[j] > temp_min) {
    //                 temp_min = totald[j];
    //                 pointer = j;
    //             }
    //         }
    //         Index.push_back(pointer);
    //     }

    newgenepop.clear();
    newgenepop.shrink_to_fit();
    for (int i = 0; i < Index.size() / 2; i++) {
        newgenepop.push_back(populationGene[Index[i]]);
    }
    bestgene.push_back(populationGene[Index[0]]);
    bestdistance.push_back(totald[Index[0]]);
    cout << "best distance" << totald[Index[0]] << endl;
    evaluation++;
    //
    //     outFile1<<evaluation<< " "<< totald[Index[0]]<<endl;

    cout << "evaluation: " << evaluation << endl;
    //cout<<"worst"<<totald[index[-1]]<<endl;

```

```

// for (int i=0;i<newgenepop[0].size(); i++){
//         outFile2<<i <<" "<< newgenepop[0][i].k << " " <<newgenepop[0][i].b<< " "
<<newgenepop[0][i].c << " ";
//     }
//
//     return newgenepop;
// }
vector<GENE> generateNewGene(int num_foot) {

    vector<GENE> temp;
    GENE temp_2;

//     double k_1 = 9000;
//     double b_1 = 0;
//     double c_1 = 0;
//     int num_sp = 21+ 6 * num_foot;
//
//     for (int j = 0; j < num_sp; j++) {
//         double k_1 = 100 + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (1000 - 100)));
//         //         if (j == 18 or j == 37 or j == 17 or j == 27 or j == 29 or
j == 39 or j == 46 or j == 48 or j == 54 or j == 56 or j == 62 or j == 64) {
//             if (j < num_sp && j > 21) {
//                 k_1 = 600 + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (5000 - 600)));
//                 b_1 = static_cast <float> (rand()) / static_cast <float> (RAND_MAX /
1);
//                 c_1 = -2 * M_PI + static_cast <float> (rand()) / (static_cast <float>
(RAND_MAX / (4 * M_PI)));
//             }
//             else {
//                 k_1 = 9000;
//                 b_1 = 0;
//                 c_1 = 0;
//             }

//         temp_2 = { k_1, b_1, c_1 };
//         temp.push_back(temp_2);

//     }

    return temp;
}
Robot getnewrobot(vector<GENE> gene, int num_foot){

```

```

//double x = -2 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX / 4));
double y = -1 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX / 2));
//    cout<<"getnewgenenene"<<gene[9].k<<endl;
Robot robot2(0, y, 0.1, num_foot, gene);

return robot2;
}

vector<GENE> mutation(vector<GENE> p1) {
    vector<int> list;
    for (int i = 21; i < p1.size(); i++) {
        list.push_back(i);
    }
    int i = 21 + rand() % static_cast<int>(p1.size() - 21);
    int il = list[i];
    vector<GENE> offspring = p1;
    GENE temp;
    temp.k = 600 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX / (1000
- 100)));
    temp.b = static_cast <float> (rand()) / static_cast <float> (RAND_MAX / 1);
    temp.c = -2 * M_PI + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX
/ (4 * M_PI)));

    offspring[i] = temp;
    list.clear();
    return offspring;
}

vector<vector<GENE>>    nextgeneration(vector<Robot>    robots,vector<vector<GENE>>
newgenepop) {
    vector<vector<GENE>> nextpop = newgenepop;
    vector<GENE> p3;
    for (int a = 0; a<int(newgenepop.size())-1; a++) {
        int i = rand() % static_cast<int>(newgenepop.size());
        int j = rand() % static_cast<int>(newgenepop.size());

        vector<GENE> p1 = nextpop[i];
        vector<GENE> p2 = newgenepop[j];
        if (p1.size() < p2.size()) {
            p1 = crossover(p1, p2);
            nextpop.push_back(p1);
        }
    }
}

```

```

        else {
            p2 = crossover(p1, p2);
            nextpop.push_back(p2);
        }

    }

    int num = 2 + static_cast<float>(rand()) / (static_cast<float>(RAND_MAX / 10));

    vector<GENE> temp3 = generateNewGene(num);
    nextpop.push_back(temp3);

    robots.pop_back();
    //nextpop[-1] = temp3;
    //    cout << "nextpop[-1].size(2222)" << nextpop[-1][5].k << endl;

    Robot a = getnewrobot(nextpop[9], num);
    robots.push_back(a);

    //    robots[-1] = getnewrobot(nextpop[-1], num);
    double r = static_cast<float>(rand()) / (static_cast<float>(RAND_MAX));
    if (r < 0.5) {
        vector<GENE> temp_off;
        int ra_ro = 1 + rand() % static_cast<int>(nextpop.size() - 1);
        temp_off = mutation(nextpop[ra_ro]);
        nextpop[ra_ro] = temp_off;
        cout << "mutationing" << endl;

    }

    for(int i =0; i<nextpop[0].size(); i++){
        //            outFile2<<evaluation<< " "<<i <<" "<< nextpop[0][i].k<<"
        "<<nextpop[0][i].b<<" "<<nextpop[0][i].c<<endl;
    }

    return nextpop;
}

//vector<Robot> getrobots(Robot a){
//    robots.pop_back();
//    robots.push_back(a);
//    return robots;

```



```

//}
//

vector<Robot> getinitalrobot(vector<vector<GENE>> nextpop, int num_foot) {
    vector<Robot> robots;
    for (int i = 0; i < populationsize; i++) {

        //double x = -2 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX
/ 4));
        double y = -1 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX /
2));
        //robots.push_back(ROBOT(0.0, 3.0*(i-populationSize/2), 0.0, populationGene[i]));
        //      int num = 2 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX
/ 8));

        Robot robot1(0, y, 0.1, num_foot, nextpop[i]);
        robots.push_back(robot1);

    }
    return robots;
}

double fitness(Robot r, int num_m) {
    // double fit = 0;
    double startpoint;
    double sumdis = 0;
    for (int i = 0; i < num_m-1; i++) {
//      fit += (r.joint[i].p[0] - r.initl[0]);
        sumdis += (r.joint[i].p[0] - r.initl[0]);

    }
    startpoint = sumdis / num_m;
    r.initl[0] = startpoint;
//      outFile3<< evaluation << " " << sumdis/(num_m-1) << endl;
        //cout<<"startpoint"<<startpoint<<endl;
    return sumdis / (num_m-1);
}

vector<double> totaldistance(vector<Robot> robots) {
    vector<double> totald;

```

```

    for (int i = 0; i < populationsize; i++) {
        double f = fitness(robots[i], robots[i].num_foot + 7);

        totald.push_back(f);
    }

    return totald;
}

```

```

void Print(const char* format, ...)
{
    char    buf[LEN];
    char* ch = buf;
    va_list args;
    // Turn the parameters into a character string
    va_start(args, format);
    vsnprintf(buf, LEN, format, args);
    va_end(args);
    // Display the characters one at a time at the current raster position
    while (*ch)
        glutBitmapCharacter(GLUT_BITMAP_HELVETICA_18, *ch++);
}

/*
 * OpenGL (GLUT) calls this routine to display the scene
 */

```

```

void display()
{
    //drawground();
    double len = 0.2; // Length of axes
    // Erase the window and the depth buffer
    glClearColor(0.5372549, 0.6549019, 0.760784, 1.0);
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
    // Enable Z-buffering in OpenGL
    glEnable(GL_DEPTH_TEST);
}

```

```

// Undo previous transformations
glLoadIdentity();

// Eye position
double Ex = -1 * dim * Sin(th) * Cos(ph);
double Ey = +1 * dim * Sin(ph);
double Ez = +1 * dim * Cos(th) * Cos(ph);
gluLookAt(Ex, Ey, Ez, 0, 0, 0, 0, Cos(ph), 0);

//Simulate();

//      double y = -1 + static_cast <float> (rand()) / (static_cast <float> (RAND_MAX
/ 2));
//
//      Robot robot1(0, y, 0.1, 5, populationGene);
//
//      if (T >0) {

          for (int j = 0; j < populationsize; j++) {
//          cout<<robot[j].num_foot<<endl;
              if(j==0){
                  robot[j].simulate();

                  robot[j].drawcube();
              }
//          }

          }

//      else {
//          totald2 = totaldistance(robot);
//          newgenepop = selection(populationGene, totald2);
//          nextpop = nextgeneration(robot,newgenepop);
//          robot = sortrobot(robot, totald2);
//          robot.pop_back();
//          robot.push_back(getnewrobot(nextpop[9], int (nextpop[9].size()-21)/6));
//          populationGene = nextpop;
//          //cout<<"in loop evolve"<<endl;
//          T = 0;
//      }

//Draw axes
//glColor3f(1, 0, 0);
//      if (axes)
//      {

```

```

//      glBegin(GL_LINES);
//      glLineWidth(2);
//      glVertex3d(0.0, 0.0, 0.0);
//      glVertex3d(len, 0.0, 0.0);
//      glVertex3d(0.0, 0.0, 0.0);
//      glVertex3d(0.0, len, 0.0);
//      glVertex3d(0.0, 0.0, 0.0);
//      glVertex3d(0.0, 0.0, len);
//      glEnd();
//      // Label axes
//      glRasterPos3d(len, 0.0, 0.0);
//      Print("X");
//      glRasterPos3d(0.0, len, 0.0);
//      Print("Y");
//      glRasterPos3d(0.0, 0.0, len);
//      Print("Z");
//  }

// Render the scene
glFlush();
// Make the rendered scene visible
glutSwapBuffers();
}

void special(int key, int x, int y)
{
    // Right arrow key - increase angle by 5 degrees
    if (key == GLUT_KEY_RIGHT)
        th += 5;
    // Left arrow key - decrease angle by 5 degrees
    else if (key == GLUT_KEY_LEFT)
        th -= 5;
    // Up arrow key - increase elevation by 5 degrees
    else if (key == GLUT_KEY_UP)
    {
        if (ph + 5 < 90)
        {
            ph += 5;
        }
    }
    // Down arrow key - decrease elevation by 5 degrees
    else if (key == GLUT_KEY_DOWN)
    {
        if (ph - 5 > 0)

```

```

        {
            ph -= 5;
        }
    }
    // Keep angles to +/-360 degrees
    th %= 360;
    ph %= 360;
    // Tell GLUT it is necessary to redisplay the scene
    glutPostRedisplay();
}

```

```

void Project(double fov, double asp, double dim)
{
    // Tell OpenGL we want to manipulate the projection matrix
    glMatrixMode(GL_PROJECTION);
    // Undo previous transformations
    glLoadIdentity();
    // Perspective transformation
    if (fov)
        gluPerspective(fov, asp, dim / 16, 16 * dim);
    // Orthogonal transformation
    else
        glOrtho(-asp * dim, asp * dim, -dim, +dim, -dim, +dim);
    // Switch to manipulating the model matrix
    glMatrixMode(GL_MODELVIEW);
    // Undo previous transformations
    glLoadIdentity();
}

```

```

void key(unsigned char ch, int x, int y)
{
    // Exit on ESC
    if (ch == 27)
        exit(0);
    // Reset view angle
    else if (ch == '0')
        th = ph = 0;
    // Toggle axes
    else if (ch == 'a' || ch == 'A')
        axes = 1 - axes;
    // Change field of view angle
    else if (ch == '-' && ch > 1)

```

```

        fov++;
    else if (ch == '=' && ch < 179)
        fov--;
    // PageUp key - increase dim
    else if (ch == GLUT_KEY_PAGE_DOWN) {
        dim += 0.1;
    }
    // PageDown key - decrease dim
    else if (ch == GLUT_KEY_PAGE_UP && dim > 1) {
        dim -= 0.1;
    }
    // Keep angles to +/-360 degrees
    th %= 360;
    ph %= 360;
    // Reproject
    Project(fov, asp, dim);
    // Tell GLUT it is necessary to redisplay the scene
    glutPostRedisplay();
}

void reshape(int width, int height)
{
    // Ratio of the width to the height of the window
    asp = (height > 0) ? (double)width / height : 1;
    // Set the viewport to the entire window
    glViewport(0, 0, width, height);
    // Set projection
    Project(fov, asp, dim);
}

void idle()
{
    glutPostRedisplay();
}

int foot = 5;

int main(int argc, char* argv[])
{
    populationGene = genereateGene(foot);

    robot = getinitalrobot(populationGene,5);

```

```

//      Robot robot1 = getnewrobot(populationGene, 5);

// Initialize GLUT and process user parameters
glutInit(&argc, argv);
// double buffered, true color 600*600
glutInitWindowSize(1000, 800);
glutInitDisplayMode(GLUT_RGB | GLUT_DEPTH | GLUT_DOUBLE);
// create the window
glutCreateWindow("evolve");
// Tell GLUT to call "idle" when there is nothing else to do
glutIdleFunc(idle);
// Tell GLUT to call "display" when the scene should be drawn
glutDisplayFunc(display);
// Tell GLUT to call "reshape" when the window is resized
glutReshapeFunc(reshape);
// Tell GLUT to call "special" when an arrow key is pressed
glutSpecialFunc(special);
// Tell GLUT to call "key" when a key is pressed
glutKeyboardFunc(key);
init();

// Pass control to GLUT so it can interact with the user
glutMainLoop();

return 0;

};

```