Caterwaul By Example

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Chapter 1

List of Primes

It's rare that you actually need to generate a list of primes in production code, but this problem makes a good programming language example. The goal here is to write a web page that ends up showing the user a list of primes below 10,000.

1.1 Preparing the HTML

The first step, assuming that we want to iterate rapidly, is to create a basic HTML document that loads Caterwaul and our application source code:

```
Listing 1.1 examples/primes/index.html

1 <!doctype html>
2 <html>
3 <head>
4 <script src='http://ajax.googleapis.com/ajax/libs/jquery/1.6.2/jquery.js'></script>
5 <script src='http://caterwauljs.org/build/caterwaul.js'></script>
6 <script src='http://caterwauljs.org/build/caterwaul.std.js'></script>
7 <script src='primes.js'></script>
8 </head>
9 <body></body>
10 </html>
```

Caterwaul's core and the std module don't depend on jQuery. I'm just including it here so that we can easily do things when the page is loaded.

1.2 Invoking Caterwaul

Caterwaul is a Javascript compiler written in Javascript. So to use it, you just hand your function to Caterwaul and run the function it gives you back. Here's an example of this behavior:

```
// Use an unconfigured caterwaul compiler; this has no effect:
var f = function (x) {return x + 1};
var g = caterwaul(f);

// Use all known Javascript extensions:
var f2 = function (x) {return y, where[y = x + 1]};
var c = caterwaul.js_all(); // Returns a configured compiler
var g2 = c(f2);
```

Most Javascript apps have a surrounding lexical closure to create a local scope, so you can save some space by transforming the function inline:

```
caterwaul.js_all()(function () {
    // app code
})();

// If using jQuery:
$(caterwaul.js_all()(function () {
    // app code
}));
```

We're using jQuery, so our app will look like the second function here.

1.3 Application code

Here's a Caterwaul app that computes our list of primes and shows it to the user:

```
Listing 1.2 examples/primes/primes-first.js
           $(caterwaul.js_all()(function () {
             var is_prime = function (x) {
               for (var i = 2; i * i <= x; ++i)
                 if (x % i === 0)
                   return false;
               return true;
             };
             var list = [];
        9
             for (var i = 2; i < 10000; ++i)
        10
               if (is_prime(i))
                 list.push(i);
        12
        14
             $('body').text(list.join(', '));
        15 }));
```

Caterwaul is a superset of Javascript, so this example behaves exactly as we'd expect. However, it doesn't look particularly special. Using Caterwaul idioms and refactoring a bit, we get this:¹

This code probably looks like voodoo, but it's actually not that complicated. There are two things happening here that aren't in regular Javascript. First, the where[] construct binds variables within an expression. Second, the seq modifier is deeply mysterious and somehow condenses five or six lines of code into two.

where[] is used when you want to locally bind something. For example:

```
alert(x) -where [x = 10];
alert(f(10)) -where [f(x) = x + 1];
```

This is translated into a local function scope that gets called immediately:

```
(function () {
  var x = 10;
  return alert(x);
})();

(function () {
  var f = function (x) {return x + 1};
  return alert(f(10));
})();
```

You'll notice that there's a little bit of magic going on to let you say f(x) = x + 1. This is not explicitly handled by where []; instead, Caterwaul has a macro that rewrites things that look like x(y) = z into x = x function (y) {return z}. Because this rule is applied globally, you can also use it to create methods or reassign existing functions:

```
jQuery.fn.size() = this.length;
```

Because it's recursive, you can create curried functions by providing multiple argument lists:

¹Thanks to Jeff Simpson for pointing out a bug here! I had previously written composite(n) = n[2, Math.sqrt(n)], which has an off-by-one error since it stops before reaching \sqrt{n} . It's necessary to use an inclusive upper bound to make sure that we get squares as well as other factors.

```
alert(f(1)(2)) -where [f(x)(y) = x + y];

// Is compiled to:
(function () {
  var f = function (x) {
    return function (y) {
     return x + y;
    };
  };
  return alert(f(1)(2));
})();
```

A reasonable question is how where [] knows how much code should be able to see the variables you're binding. The answer has to do with its prefix: where is what's known as a modifier, and all modifiers have an accompanying operator that has a precedence. For example, in the expression $\mathbf{x} * \mathbf{y} - \mathbf{where}[\ldots]$ the where clause binds over the multiplication, since the minus has lower precedence. Writing it as $\mathbf{x} + \mathbf{y} / \mathbf{where}[\ldots]$ causes only \mathbf{y} to have access to the where variables.

seq is the macro that is more interesting in this prime-generator example. It's a mechanism that writes all different kinds of for loops. In this case we're using it in two places. The first time is in the composite() function, where we use it to detect factors:

```
composite(n) = ni[2, Math.sqrt(n)] | [n % x === 0] | seq
```

First, we use ni [] to generate an array of numbers between 2 and Math.sqrt(n), inclusive. ni [] (with square brackets) is a syntax form, not a function; so it won't collide with the variable n that we take as a parameter. The next piece, | [n % x === 0], has two parts. The pipe operator, which normally performs a bitwise-or, means "there exists" in sequence context. Its body, n % x === 0, is then evaluated for each element (seq calls the element x). So at this point we're asking, "does there exist an integer x for which n % x is zero?" We tack the | seq onto the end to cause the preceding expression (in this case, everything back to the =) to be interpreted by the seq macro. seq is a modifier just like where [], though seq doesn't take parameters.

The other use of seq is to retrieve all numbers that are not composite:

```
primes = n[2, 10000] %!composite -seq
```

n[] is doing the same thing as before. After it is %, which is the filter operator. So we're filtering down to only the elements which are not composite. The filter prefix is %, and the ! modifier negates the condition. Because there's already a function defined, I use that instead of writing out a block. I'm using a higher-precedence prefix for seq as a matter of convention; I default to using a minus unless there's a reason to use something else.

Chapter 2

This is Hideous!

```
o %k%~!f %v*!~[x /!g] -seq — valid Caterwaul code
```

A fair point. I certainly didn't design Caterwaul to look nice.¹

2.1 Linear edits

Seek time is a large burden for programmers, just as it is for mechanical hard drives. Programmers are extremely productive when they are able to type a continuous stream of text without jumping around. For instance, consider the amount of programmer-effort required to implement this edit:

```
// Update this function to log the square of the distance:
var distance = function (x1, x2, y1, y2) {
  var dx = x1 - x2;
  var dy = y1 - y2;
  return Math.sqrt(dx*dx + dy*dy);
};
```

This is a moderate-effort change. The expression dx*dx + dy*dy must be factored into a variable, then the variable must be typed twice, and logging code must be added. The steps probably look about like this:

 $^{^{1}}$ Otherwise it would be called something besides Caterwaul.

If you time yourself making this edit, I'm guessing it will take on the order of five or ten seconds. I doubt that it would ever become a one or two second edit even with practice. Now consider what this edit looks like using Caterwaul:

This edit can easily be made in about two seconds because it is mostly linear. This is really important! It isn't just about saving a few seconds here and there; every jump and every keystroke is a potential point of failure within the edit process. If, for example, you had ended up making this edit the first time (I've done things like this on many occasions without thinking):

```
var distance = function (x1, x2, y1, y2) {
  var dx = x1 - x2;
  var dy = y1 - y2;
  var d = dx*dx + dy*dy;
  console.log(d);
  return Math.sqrt(dx);
};
```

You might then be wondering why the function was returning bad results despite logging the right thing. It could easily turn into a 60 or 120-second bug-hunt. This is the kind of thing that saps productivity and demoralizes programmers, and this is exactly what Caterwaul was designed to overcome.

2.1.1 How Caterwaul does this

I thought a lot about this problem before deciding on the current notation. Infix operators are obviously a step in the right direction (the worst offender is Lisp, which requires at least one jump for every significant edit). These operators are organized by common-use precedence, since it was far more common to add products than to multiply sums, for instance. In a sense, this is a very ergonomic Huffman-style coding of common practice.

Perhaps a less commonly recognized feature of infix operators is that you can easily determine how much code to grab with one continuous edit. For example, support I'm editing the code below and want to conditionalize the side effect on truthiness:

I don't want to use short-circuit logic, since this has far lower precedence than minus. I also don't want to use a minus, since it left-associates (meaning that any modifier I used would grab everything back to the foo() invocation). Rather, I need a / prefix, which will modify only the log expression:

The alternative to choosing an operator is to add explicit grouping. This, however, requires a jump and decreases readability, which I complain about in more detail in the next section:

2.2 Silly parentheses

```
... get)) add) button))))))))) - Lisp
```

Relying on operator precedence for grouping has another beneficial side effect: It reduces the infamous Lisp problem of trailing parentheses.

Parentheses and other grouping constructs are hard for humans to parse unless they have some other kind of reinforcement such as indentation or differentiated brackets. For example, this code requires a lot of effort to understand:

```
sum(product(join(x, y)), fix(z(t), z()), a(b(c), d, e))
```

I think this has something to do with our natural language being primarily infix: subject-verb-object. Infix is simple because there is an implicit limit to how much stuff you can group together. If you're adding stuff, all you have to worry about is multiplication and more addition. You don't have to count parentheses to keep track of when an expression ends.

So while parentheses and other explicit grouping constructs are more versatile and computationally pure, they can impose a lot of conceptual overhead. This, along with the ergonomic advantage of infix operators, was a large influence on Caterwaul's macro design.

2.3 Keystrokes

Some things are easier to type than others. For example, it's far easier to type a dot than it is to type a caret. Part of it is frequency of use, but another part of it is layout. Caterwaul is optimized to avoid using the shift key for common cases, since this is a large cause of typos (for me, anyway). This is why it uses / and - instead of * and +.

This is also why all of its identifiers use lowercase and generally avoid underscores. The shift key produces its own set of typos, including:

```
aNameWithcaps <- missed shift
aNAmeWithCaps <- doubled shift
```

There's another issue though. The shift key generally occupies the hand opposite of the one typing the character. So, for instance, typing a + or a * would use the right index/middle or ring/pinky along with the left pinky on the shift. However, most Caterwaul modifiers begin with a letter typed by the left hand:

```
where
se
re
seq
when
raise
rescue
given
delay
```

So it's useful to have the left hand available for the character immediately following the modifier operator. In this case, that means using unshifted variants of + and *, which, naturally enough, are - and /.

2.4 Aesthetics

Caterwaul won't win any beauty contests, but I've tried to make design choices that keep it visually out of the way. This is another reason I chose -, /, and | as modifier prefixes: they are all straight lines and don't introduce intersections into a stream of text.²

Also, Caterwaul gives you the flexibility to write code that looks very nice. Consider this numerical integration function, for instance:

The definition of integration is clearly visible, and the implementation details follow as an afterthought. Most Javascript code requires that the implementation details come first, followed by the high-level description at the end:

```
function integrate(f, a, b, h) {
  var sum = 0;
  for (var x = a; x < b; x += h)</pre>
```

²I have no idea whether this actually matters, but I noticed that I preferred operators with simple linear forms to operators with more complex forms.

```
sum += f(x) * h;
return sum;
}
```

This imperative definition is simpler, but at the cost of eliding the moments variable. We can do the same with the Caterwaul definition, though it loses some readability:

```
integrate(f, a, b, h) = n[a, b, h] / [0][x0 + f(x) * h] - seq
```

Chapter 3

Game of Life

This example is more interesting than the prime list because it makes use of Caterwaul's jQuery macros. These macros, along with the sequence library, can significantly change the way Javascript programs are structured. As a twist, this game of life is implemented on a toroidal map; that is, both the horizontal and vertical edges wrap around to the opposite side.

3.1 HTML structure

Like other Caterwaul applications, this one is built on a minimal HTML file that pulls in various scripts.

```
Listing 3.1
           examples/game-of-life/index.html
        1 <!doctype html>
        2 <html>
             <head>
             <script src='http://ajax.googleapis.com/ajax/libs/jquery/1.6.2/jquery.js'></script>
             <script src='http://caterwauljs.org/build/caterwaul.js'></script>
             <script src='http://caterwauljs.org/build/caterwaul.std.js'></script>
             <script src='http://caterwauljs.org/build/caterwaul.ui.js'></script>
             <script src='life.js'></script>
             <link rel='stylesheet' href='style.css'/>
             </head>
             <body></body>
        12 </html>
Listing 3.2 examples/game-of-life/style.css
        1 .cell
                          {background: #eee}
        2 .cell:hover
                          {background: #ccc}
        3 .cell.on
                          {background: #444}
        4 .cell.on:hover {background: #555}
```

.board {position: relative}

3.2 UI structure

One of the tricky things about the game of life is linking the cells together. This is especially true when, as is the case here, we use the DOM as a data model (thus removing the usual layer of indirection that causes all sorts of synchronization bugs).

The key in this case is to build up arrays of elements first, establishing their visual position as a separate step. This avoids tricky reliance on DOM-level navigation and sibling checking. There are a couple of ways to represent the elements. One is to use a single long array and use modular access, but I'm going to use multiple nested arrays to illustrate some less commonly used features of the sequence library.

Above the board, which is contained within a single <div>, is a button to step the simulation.

3.3 Javascript code

Normally I write Caterwaul with 192-column wrapping. This makes it easier to write multiple layers of where[] modifiers without running out of horizontal space. (This, in turn, keeps the left margin relatively clean by moving lower-level details off to the right.) However, this code is wrapped at under 100 columns to be readable in the PDF.

```
examples/game-of-life/life.js
Listing 3.3
           $(caterwaul.jquery(caterwaul.js_all())(function () {
             $('body').append(top_button_row, board.div)
             -where [
                               = life_board(30, 30),
               board
               interval
                               = null.
               run_or_stop()
                              = interval ? stop_running() -se- $(this).text('Run') :
                                             start_running() -se- $(this).text('Stop'),
               start_running() = interval = setInterval(board.step, 100),
               stop_running() = clearInterval(interval) -se [interval = null],
               top_button_row = jquery in div(
                                   button.step('Step') /click(board.step),
                                   button.run('Run')
                                                      /click(run_or_stop))]
        12
             -where [
               life_board(x, y)
                                   = {cells: cells,
        14
                                              div_for(cells),
                                      div:
                                      step: step_function(cells)}
                                      -where [cells = cells_for(x, y)],
```

```
18
                            = n[x] *[n[y] *y[cell_for(x, y)]] -seq,
       cells_for(x, y)
19
       cell_for(x, y)
                            = jquery in div.cell *!x(x) *!y(y) %position(x, y)
20
                                                                %invert_on_click,
       position(x, y)(e)
                            = e.css({position: 'absolute',
22
                                     left: x * 12, width: 10,
23
                                     top: y * 12, height: 10}),
24
       invert_on_click(e) = e.mousedown($(this).toggleClass('on') -given.e),
26
       div_for(cs)
                            = jquery [div.board]
27
                              -se- cs *!~[x *![it.append(x)]] /seq,
28
       step_function(cs)() =
         cs *!~[x *!update] -seq
30
         -where [
           new_state(x, y) = on(x, y) ? count(x, y) -re [it >= 2 && it <= 3] :
                                          count(x, y) === 3,
           count(x, y)
                            = adjacent(x, y) /[x + x0] -seq,
34
           adjacent(x, y) = ni[x - 1, x + 1] *^{-1}xn[ni[y - 1, y + 1]
                                yn[x !== xn || y !== yn]
                                *yn[+on(xn, yn)]] -seq,
           cell(x, y)
                            = cs[wrap(x, cs)] -re- it[wrap(y, it)],
38
           wrap(x, xs)
                            = (x + xs.length) % xs.length,
39
                            = cell(x, y).hasClass('on'),
           on(x, y)
40
41
           new_states
                            = cs *^[x *y[new_state(xi, yi)]] -seq,
42
43
           update(cell)
                            = cell.toggleClass('on',
                                new_states[cell.data('x')][cell.data('y')])]]}));
44
```

3.4 What's going on here?

This code is reasonably well front-loaded, so I'll explain the code from the top down

First off, there are two separate where[] blocks operating at the top level. This is totally ok because all of the operators used to modify things are left-associative. This means that the syntax tree will end up parsing like this:

```
($('body').append(...) -where [...]) -where [...]
```

This wouldn't be possible if - were right-associative; in that case, you'd have:

```
$('body').append(...) -(where [...] -where [...])
```

¹Meaning that higher-level things precede lower-level ones.

Caterwaul always follows Javascript's precedence and associativity, and it's helpful to be familiar with the nuances of Javascript's grammar when writing Caterwaul code.

3.4.1 UI code

The first part sets up the UI and appends it to the body:

This is all grouped into a single where[] block because it's all UI-related. Grouping things like this limits the amount of interaction that can happen between any two components.

An English-like description of each function and variable would be something like this:

- board The model for the simulation. This provides a UI, step function, and nested cell arrays.
- interval The interval timer used to run the simulation. When the simulation is running, this will hold the result of setInterval(); otherwise it will be null.
- run_or_stop() If the simulation is running, then stop it and set the button text to Run. Otherwise, start the simulation and set the button text to Stop.
- start_running() Creates and stores an interval timer that steps the simulation every 100ms.
- stop_running() Stops the (presumably running) interval timer and clears the interval variable to indicate that nothing is running.
- top_button_row This is just a <div> that contains the two buttons. Each one has a click handler; the step button delegates directly to board.step() (which is safe because board.step doesn't rely on any parameters or the value of this), and the run button references run_or_stop directly.

3.4.2 Model code

The model is a little unusual in that it stores its data directly on DOM elements. I did it this way to keep the example simple; it's more difficult (though often more scalable and performant) to maintain a purely logical data structure and keep it synchronized with a view layer of DOM nodes. The exact structure used is this:

where m is the number of columns (!) and n is the number of rows. So the cells are stored in column-major order if you're looking at it from the user's point of view. I didn't have a particularly compelling reason to do it this way, other than the fact that it seems more intuitive to first iterate over x and then y. (The outer loop is over y when using row-major order.)

There are two major pieces of code for the model. The first is the board setup code:

```
life_board(x, y)
                   = {cells: cells,
                             div_for(cells),
                      div:
                      step: step_function(cells)}
                      -where [cells = cells_for(x, y)],
cells_for(x, y)
                   = n[x] *^{n[y]} *y[cell_for(x, y)]] -seq,
cell_for(x, y)
                   = jquery in div.cell *!x(x) *!y(y) %position(x, y)
                                                      %invert_on_click,
position(x, y)(e) = e.css({position: 'absolute',
                            left: x * 12, width: 10,
                            top: y * 12, height: 10}),
invert_on_click(e) = e.mousedown($(this).toggleClass('on') -given.e),
div_for(cs)
                   = jquery [div.board]
                      -se- cs *!~[x *![it.append(x)]] /seq
```

Here's what each variable/function does:

The div and step attributes aren't linked to the board object itself, but they are linked to the cell array. This is useful from an API design perspective: it lets users call the step method without setting the context. (Which is what we did by using the step() method as the click handler in the

previous section.) The simplest way to create unbound functions such as step_function is to use currying, and this is how step_function is defined.

cells_for(x, y) This constructs a column-major nested array of cell <div> elements. Each of these <div>s keeps track of its state by either having or not having the on class. Elements with the on class set are drawn with a dark background; this behavior is governed by the stylesheet. (This prevents the Javascript from knowing too much about the UI presentation.)

$$n[x] *^{[n[y] *y[cell_for(x, y)]] -seq}$$

The sequence comprehension is a bit gnarly, but here's what each piece of it means:

- n[x] Construct an array of numbers [0, 1, 2, ..., x 1].
- *~[...] Map over a block, and interpret the contents of the block in sequence context (that is, as if the -seq modifier had been applied to the body of the block). The * operator signifies mapping, and the ~ indicates sequence context.

Because no variable was named, the block will receive x, xi, and xl as lexically-scoped variables. This inner x shadows the x passed into cells_for() within the context of the block.

The result of this inner block, which is an array of cells, will become a single entry in the final array returned by cells_for(). This outer map operation constructs the array of all columns (each column is constructed by the logic below).

- n[y] Construct an array of numbers [0, 1, 2, ..., y 1].
- *y[...] Map over another block, this time interpreted as a regular Javascript expression. The y immediately preceding the block causes the loop variables to be renamed to y, yi, and yl instead of the default x, xi, and xl. The inner y created for this block will shadow the one passed into cells_for().

This map operation constructs a column of cells.

- cell_for(x, y) Construct a single cell at the coordinates (x, y). Because this is the result of mapping, the cell will be added to the column array.
 - -seq This causes the entire preceding expression (in this case, everything back to the =, which has lower precedence than the on the front of seq) to be treated as a sequence comprehension. This is what causes * to be interpreted as a map operation, n[] to be interpreted as an array constructor, etc.

seq is a modifier just like jquery and where[], so it could be written
several different ways. I generally like to use - because it's a mediumprecedence operator that easily combines with things like -se- and
-re-.

cell_for(x, y) Constructs and returns a single cell, which is a jQuery-wrapped <div>. Each cell has some data associated with it. It has two jQuery data() properties to store its x and y coordinates, and it tracks its on/off state using the on CSS class.

jquery in div.cell *!x(x) *!y(y) %position(x, y) %invert_on_click

Here's what the jquery modifier is doing:

- jquery in Causes the following expression to be interpreted in jQuery context. This enables the transformations described below. in has the same precedence as <, >, <=, and >= and is left-associative. This means that all of the usual arithmetic operators will still be in jQuery context, but any relational or lower-precedence operators will escape.
- div.cell In jQuery context this constructs a <div> element with CSS class cell. Specifically, it expands to jQuery("<div>").addClass("cell").
- *!x(x) *!y(y) This looks a bit tricky, but there isn't anything particularly magical happening. The *! prefix, when interpreted by the jquery modifier, refers to a jQuery data property. So in general, things of the form a *!b(c) will expand to a.data("b", c), and that's exactly what's happening here. In this case, the resulting code is .data("x", x).data("y", y), which sets two data properties and returns the original jQuery selector.
- %position(x, y) This is interesting. First, it calls position() on the current x and
 y coordinates, then it calls that result on the current element. In
 general, a %b is expanded into b(a). Because applying position to
 (x, y) has higher precedence than the % operator, the resulting expansion is position(x, y)(...), where ... is the aforementioned
 element constructed by div.cell.
- %invert_on_click The same thing as %position(x, y), but this function isn't curried. %
 left associates, so the overall parse order is (... %position(x, y)) %invert_on_click.
 By the rule described above, then, the whole expansion would be
 invert_on_click(position(x, y)(...)). You can see this hap pening using the interactive shell on http://caterwauljs.org.
- position(x, y)(e) This is one of the functions used in the jQuery comprehension in the previous step. It's responsible for visually positioning each cell on the board. I've hard-coded some numbers here; basically, each cell is 10×10 pixels and has a 2-pixel margin.

Importantly, this function returns e (indirectly, since jQuery's css() method returns the original element when used as a setter). This matters because the jquery modifier lets you change the return value from a % function. For example, suppose we had written this:

 $position(x, y)(e) = e.css({...})$ -re- false

Then the jquery comprehension would end up passing false to invert_on_click, with unfortunate consequences. Generally, functions used with % should return the element they're given to avoid confusion.

invert_on_click(e) This function is generally unremarkable. The only interesting thing about it is that it uses an inline -given modifier, which converts its expression into a function. The .e on the end of given is a shorthand to indicate that e is the function's only parameter. (If we wanted a function that took multiple parameters, we'd write something like -given[e, x, y].)

Like position(x, y), invert_on_click returns the element it modifies. That is, besides the fact that it is side-effecting, it behaves like the identity function.

3.4.3 Simulation code

This is the most complex bit of the program. It contains logic to count the neighbors of each cell, compute an array of new states, and update each cell to reflect its new state.

```
step_function(cs)() =
  cs *!~[x *!update] -seq
  -where [
    new_state(x, y) = on(x, y) ? count(x, y) -re [it >= 2 && it <= 3] :
                                 count(x, y) === 3,
    count(x, y) = adjacent(x, y) / [x + x0] - seq,
    adjacent(x, y) = ni[x - 1, x + 1] * [xn[ni[y - 1, y + 1]]
                        yn[x !== xn || y !== yn]
                        *yn[+on(xn, yn)]] -seq,
    cell(x, y)
                   = cs[wrap(x, cs)] -re- it[wrap(y, it)],
    wrap(x, xs)
                   = (x + xs.length) % xs.length,
    on(x, y)
                   = cell(x, y).hasClass('on'),
                   = cs *~[x *y[new_state(xi, yi)]] -seq,
    new_states
    update(cell)
                   = cell.toggleClass('on',
                        new_states[cell.data('x')][cell.data('y')])]
```

The first thing to notice is that this function is curried; it takes a cell array called cs, and expects to be invoked again before doing anything. This is an easy way to store temporary data using Caterwaul. I've curried this function because it ends up being invoked as the click handler of the step button. The click handler won't receive a reference to the board, so the function will need to have one already available. In this sense the function is behaving more like a callable object, and in fact currying can be a good substitute for immutable object-oriented data structures.

The other unusual thing about step_function is that it has a bunch of variables defined in a sub-where[]. These variables are re-created on each invocation of step_function()().

Like other functions, this one is front-loaded; here's a breakdown of what's happening.

cs *!~[x *!update] -seq This just runs through the two-dimensional array, calling update() on each cell <div>. Cells know their own coordinates, so we don't need to pass the array indexes into the update() function; it will obtain the coordinates directly from the cell object's data properties.

The sequence comprehension here consists of:

- cs *!~[...] A foreach operation on cs. This invokes the block, in sequence context due to the tilde, on each element of cs. Each element of cs is itself an array. The block's result isn't stored because it is used in a foreach rather than a map operation. (For this reason, foreach has less overhead than map.)
- x *!update This block takes x, which is one of the arrays in cs, and invokes
 update on each element. In this case, update appears where a block
 would normally go. seq handles this by turning it into this block:
 [update(x, x0, xi, x1)]. It's safe to use update() this way because it uses only its first parameter. It isn't safe to use a function
 such as Array.prototype.push in this context, however, as it will
 push each item you pass it (which probably isn't what you would
 want to do).
 - -seq Modifies the preceding expression by interpreting it in sequence context. It's ok to use here because of left-associativity.
- $new_state(x, y)$ Returns a boolean specifying whether the cell at position (x, y) will be activated in the next generation. The rules for this depend on the current state of the cell. If the cell is currently on and has 2 or 3 active neighbors, then it will remain activated. A cell that is currently off and has 3 active neighbors will become activated.

As might be expected, on(x, y) returns a boolean indicating whether the cell at (x, y) is presently activated.

The -re[] expression is being used to bind a temporary variable. This is useful when you don't want to go to the trouble of setting up a -where[] block or when you need to box up low-precedence operators such as &&. It's similar to the linguistic construct people would use when saying something like "if the neighbor count of (x, y) is at least 2 and it's at most 3, then ...", though Caterwaul's construct is a bit clunkier, requiring both uses to be referred to as it.

count(x, y) Returns the number of active neighbors of the cell at (x, y). This is done by
 retrieving the active-status of each adjacent cell (returned by adjacent(x,
 y)), and folding over addition. A less efficient but equivalent way to do it
 would be to use filtering: adjacent(x, y) %[x] -seq -re- it.length.
 Conceptually, I think folding communicates the intention more clearly.

adjacent(x, y) This is a fun one, and it's where most of the heavy lifting happens.