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## **Data Structures:**

## 1. Binary Search Tree –

```
class Node(object):
 def __init__(self, d):
  self.data = d
  self.left = None
  self.right = None
 def insert(self, d):
  if self.data == d:
     return False
  elif d < self.data:
    if self.left:
     return self.left.insert(d)
    else:
     self.left = Node(d)
     return True
  else:
     if self.right:
      return self.right.insert(d)
     else:
      self.right = Node(d)
      return True
 def find(self. d):
    if self.data == d:
     return True
    elif d < self.data and self.left:
     return self.left.find(d)
    elif d > self.data and self.right:
     return self.right.find(d)
    return False
 def preorder(self, l):
    l.append(self.data)
    if self.left:
     self.left.preorder(l)
    if self.right:
     self.right.preorder(l)
    return 1
 def postorder(self, 1):
    if self.left:
     self.left.postorder(l)
    if self.right:
     self.right.postorder(l)
    l.append(self.data)
    return 1
 def inorder(self, 1):
    if self.left:
     self.left.inorder(1)
    l.append(self.data)
    if self.right:
     self.right.inorder(1)
```

#### return 1

```
class BST(object):
 def __init__(self):
  self.root = None
 def insert(self, d):
  if self.root:
   return self.root.insert(d)
  else:
   self.root = Node(d)
   return True
 def find(self, d):
  if self.root:
   return self.root.find(d)
  else:
   return False
 def remove(self, d):
  if self.root == None:
   return False
  if self.root.data == d:
   if self.root.left is None and self.root.right is
None:
     self.root = None
     return True
   elif self.root.left and self.root.right is None:
     self.root = self.root.left
     return True
   elif self.root.left is None and self.root.right:
     self.root = self.root.right
     return True
   else:
     moveNode = self.root.right
     moveNodeParent = None
     while moveNode.left:
      moveNodeParent = moveNode
      moveNode = moveNode.left
     self.root.data = moveNode.data
     if moveNode.data < moveNodeParent.data:
      moveNodeParent.left = None
      moveNodeParent.right = None
     return True
  parent = None
  node = self.root
  while node and node.data != d:
   parent = node
   if d < node.data:
     node = node.left
   elif d > node.data:
     node = node.right
  if node == None or node.data != d:
   return False
```

```
elif node.left is None and node.right is None:
                                                        2. Linked List (Insert and delete) –
  if d < parent.data:
                                                        class Node:
   parent.left = None
                                                         def __init__(self, data):
  else:
                                                           self.data = data
   parent.right = None
                                                           self.next = None
  return True
 elif node.left and node.right is None:
                                                        class LinkedList:
  if d < parent.data:
                                                          def __init__(self):
   parent.left = node.left
                                                           self.head = None
  else:
                                                         def printList(self):
   parent.right = node.left
                                                           temp = self.head
  return True
                                                           while (temp):
 elif node.left is None and node.right:
                                                            print (temp.data,)
  if d < parent.data:
                                                            temp = temp.next
   parent.left = node.right
                                                          def insertFirst(self, new_data):
                                                           new_node = Node(new_data)
   parent.right = node.right
                                                           new_node.next = self.head
  return True
                                                           self.head = new node
 else:
                                                          def insertAfter(self, prev_node, new_data):
  moveNodeParent = node
                                                           if prev_node is None:
  moveNode = node.right
                                                            print "The given previous node must in
  while moveNode.left:
                                                        LinkedList."
   moveNodeParent = moveNode
                                                            return
   moveNode = moveNode.left
                                                           new_node = Node(new_data)
  node.data = moveNode.data
                                                           new_node.next = prev_node.next
  if moveNode.right:
                                                           prev_node.next = new_node
   if moveNode.data < moveNodeParent.data:
                                                          def append(self, new_data):
    moveNodeParent.left = moveNode.right
                                                            new_node = Node(new_data)
                                                            if self.head is None:
    moveNodeParent.right = moveNode.right
                                                             self.head = new_node
  else:
                                                             return
   if moveNode.data < moveNodeParent.data:
                                                            last = self.head
    moveNodeParent.left = None
                                                            while (last.next):
   else:
                                                             last = last.next
    moveNodeParent.right = None
                                                            last.next = new_node
  return True
                                                          def deleteNode(self, key):
def preorder(self):
                                                           temp = self.head
 if self.root:
                                                           if (temp is not None):
  return self.root.preorder([])
                                                            if (temp.data == key):
 else:
                                                             self.head = temp.next
  return []
                                                             temp = None
def postorder(self):
                                                             return
 if self.root:
                                                           while(temp is not None):
  return self.root.postorder([])
                                                            if temp.data == key:
 else:
                                                              break
  return []
                                                            prev = temp
def inorder(self):
                                                            temp = temp.next
 if self.root:
                                                           if(temp == None):
  return self.root.inorder([])
                                                            return
 else:
                                                           prev.next = temp.next
  return []
                                                           temp = None
```

# 3. Fenwick Tree – def getsum(BITTree,i): i = i+1while i > 0: s += BITTree[i] i = i & (-i)return s def updatebit(BITTree, n, i, v): i += 1while $i \le n$ : BITTree[i] += vi += i & (-i)def construct(arr, n): BITTree = [0]\*(n+1)for i in range(n): updatebit(BITTree, n, i, arr[i]) return BITTree 4. Graph and functions – class Graph(object): def \_\_init\_\_(self, graph\_dict=None): #initializes a graph object if graph dict == None: graph\_dict = {} self.\_\_graph\_dict = graph\_dict def vertices(self): """ returns the vertices of a graph """ return list(self. graph dict.keys()) def edges(self): """ returns the edges of a graph """ return self. generate edges() def add vertex(self, vertex): """If the vertex "vertex" is not in self.\_\_graph\_dict, a key "vertex" with an empty list as a value is added to the dictionary. Otherwise nothing has to be done. if vertex not in self.\_\_graph\_dict: self.\_\_graph\_dict[vertex] = [] def add\_edge(self, edge): """assumes that edge is of type set, tuple or list between two vertices can be multiple edges!

edge = set(edge)

if edge:

vertex1 = edge.pop()

```
# not a loop
   vertex2 = edge.pop()
  else:
   # a loop
   vertex2 = vertex1
  if vertex1 in self.__graph_dict:
   self.__graph_dict[vertex1].append(vertex2)
  else:
   self.__graph_dict[vertex1] = [vertex2]
 def __generate_edges(self):
  """ A static method generating the edges of the
  graph "graph". Edges are represented as sets
  with one (a loop back to the vertex) or two
  vertices """
  edges = []
  for vertex in self.__graph_dict:
   for neighbour in self.__graph_dict[vertex]:
     if {neighbour, vertex} not in edges:
      edges.append({vertex, neighbour})
  return edges
 def __str__(self):
  res = "vertices: "
  for k in self.__graph_dict:
   res += str(k) + ""
  res += "\nedges: "
  for edge in self.__generate_edges():
   res += str(edge) + " "
  return res
 def find_isolated_vertices(self):
  """ returns a list of isolated vertices. """
  graph = self.__graph_dict
  isolated = []
  for vertex in graph:
   print(isolated, vertex)
   if not graph[vertex]:
     isolated += [vertex]
  return isolated
 def find_path(self, start_vertex, end_vertex,
path=[]):
  """find a path from start_vertex to end_vertex
  in graph """
  graph = self.__graph_dict
  path = path + [start_vertex]
  if start vertex == end vertex:
   return path
  if start_vertex not in graph:
   return None
  for vertex in graph[start_vertex]:
```

```
if vertex not in path:
                                                            def vertex_degree(self, vertex):
                                                              """ The degree of a vertex is the number of
     extended_path = self.find_path(vertex,
                                                           edges connecting
              end_vertex,
              path)
                                                             it, i.e. the number of adjacent vertices. Loops
     if extended_path:
                                                           are counted
      return extended_path
                                                              double, i.e. every occurence of vertex in the list
                                                             of adjacent vertices. """
  return None
                                                              adj_vertices = self.__graph_dict[vertex]
 def find_all_paths(self, start_vertex, end_vertex,
                                                              degree = len(adi_vertices) +
                                                           adj_vertices.count(vertex)
path=[]):
  """ind all paths from start_vertex to
                                                             return degree
  end_vertex in graph """
  graph = self.__graph_dict
                                                            def degree_sequence(self):
                                                              """ calculates the degree sequence """
  path = path + [start_vertex]
  if start_vertex == end_vertex:
                                                             seq = []
   return [path]
                                                             for vertex in self.__graph_dict:
  if start_vertex not in graph:
                                                               seq.append(self.vertex_degree(vertex))
   return []
                                                              seq.sort(reverse=True)
  paths = []
                                                             return tuple(seq)
  for vertex in graph[start_vertex]:
   if vertex not in path:
                                                            @staticmethod
     extended_paths = self.find_all_paths(vertex,
                                                            def is_degree_sequence(sequence):
                                                              """ Method returns True, if the sequence
                end_vertex,
                                                           "sequence" is a
                path)
     for p in extended_paths:
                                                              degree sequence, i.e. a non-increasing
      paths.append(p)
                                                           sequence.
                                                             Otherwise False is returned.
  return paths
 def is_connected(self,
                                                             # check if the sequence sequence is non-
      vertices_encountered = None,
                                                           increasing:
      start vertex=None):
                                                             return all(x \ge y for x, y in zip(sequence,
  """ determines if the graph is connected """
                                                           sequence[1:]))
  if vertices encountered is None:
                                                            def delta(self):
   vertices encountered = set()
                                                              """ the minimum degree of the vertices """
  gdict = self. graph dict
                                                             min = 1000000000
  vertices = list(gdict.keys()) # "list" necessary in
                                                              for vertex in self. graph dict:
Python 3
                                                               vertex_degree = self.vertex_degree(vertex)
                                                               if vertex degree < min:
  if not start vertex:
   # chosse a vertex from graph as a starting
                                                                min = vertex degree
point
                                                             return min
   start_vertex = vertices[0]
  vertices_encountered.add(start_vertex)
                                                            def Delta(self):
                                                             """ the maximum degree of the vertices """
  if len(vertices_encountered) != len(vertices):
   for vertex in gdict[start_vertex]:
                                                             max = 0
     if vertex not in vertices encountered:
                                                             for vertex in self.__graph_dict:
                                                               vertex_degree = self.vertex_degree(vertex)
      if self.is_connected(vertices_encountered,
                                                               if vertex_degree > max:
vertex):
       return True
                                                                max = vertex degree
  else:
                                                             return max
   return True
  return False
                                                            def density(self):
```

```
""" method to calculate the density of a graph
  g = self._graph_dict
  V = len(g.keys())
  E = len(self.edges())
  return 2.0 * E / (V * (V - 1))
 def diameter(self):
  """ calculates the diameter of the graph """
  v = self.vertices()
  pairs = [(v[i],v[j]) for i in range(len(v)) for j in
range(i+1, len(v)-1)]
  smallest_paths = []
  for (s,e) in pairs:
   paths = self.find_all_paths(s,e)
   smallest = sorted(paths, key=len)[0]
   smallest_paths.append(smallest)
  smallest_paths.sort(key=len)
  diameter = len(smallest_paths[-1]) - 1
  return diameter
5. Trie –
class TrieNode:
 # Trie node class
 def __init__(self):
  self.children = [None]*26
  #EndofWord condition check
  self.isEndOfWord = False
class Trie:
 def __init__(self):
  self.root = self.getNode()
 def getNode(self):
  # Returns new trie node (initialized to NULLs)
  return TrieNode()
 def _charToIndex(self,ch):
  # private helper function
  # Converts key current character into index
  # use only 'a' through 'z' and lower case
  return ord(ch)-ord('a')
 def insert(self,key):
  # If not present, inserts key into trie
  # If the key is prefix of trie node,
  # just marks leaf node
  pCrawl = self.root
  length = len(key)
  for level in range(length):
   index = self. charToIndex(key[level])
```

```
# if current character is not present
   if not pCrawl.children[index]:
     pCrawl.children[index] = self.getNode()
   pCrawl = pCrawl.children[index]
  # mark last node as leaf
  pCrawl.isEndOfWord = True
 def search(self, key):
  # Search key in the trie
  # Returns true if key presents
  # in trie, else false
  pCrawl = self.root
  length = len(key)
  for level in range(length):
   index = self._charToIndex(key[level])
   if not pCrawl.children[index]:
     return False
   pCrawl = pCrawl.children[index]
  return (pCrawl != None and
pCrawl.isEndOfWord)
```

## **String algorithms:**

## 1. **KMP Algorithm** –

```
def KMPSearch(pat, txt):
 M = len(pat)
 N = len(txt)
 # create lps[] that will hold the longest prefix
suffix
 # values for pattern
 lps = [0]*M
j = 0 \# index for pat[]
 # Preprocess the pattern (calculate lps[] array)
 computeLPSArray(pat, M, lps)
 i = 0 \# index for txt
 while i < N:
  if pat[i] == txt[i]:
   i += 1
   i += 1
  if i == M:
   print "Found pattern at index " + str(i-j)
   j = lps[j-1]
  # mismatch after j matches
  elif i < N and pat[j] != txt[i]:
   # Do not match lps[0..lps[j-1]] characters,
   # they will match anyway
   if i != 0:
    j = lps[j-1]
   else:
```

```
i += 1
                                                            return(ans)
def computeLPSArray(pat, M, lps):
 len = 0
                                                           def dfs(graph,start):
 lps[0]
                                                            n=len(graph)
                                                            visited=[False]*n
 i = 1
 # the loop calculates lps[i] for i = 1 to M-1
                                                            stack=[start]
 while i < M:
                                                            ans=[]
  if pat[i] == pat[len]:
   len += 1
                                                            while(stack!=[]):
   lps[i] = len
                                                             node=stack.pop()
   i += 1
                                                             ans.append(node)
  else:
                                                             visited[node]=True
                                                             for i in graph[node]:
   if len != 0:
     len = lps[len-1]
                                                              if(visited[i]==False):
   else:
                                                                stack.append(i)
     lps[i] = 0
    i += 1
                                                            return(ans)
Graph algorithms:
                                                          2. Prim's Algorithm (Adjacency Matrix) -
1. BFS and DFS –
                                                          import sys
def Graph():
                                                           class Graph():
 graph={}
                                                            def __init__(self, vertices):
 return(graph)
def addPath(n1,n2,graph):
                                                             self.V = vertices
                                                             self.graph = [[0 for column in range(vertices)]
 trv:
  graph[n1].append(n2)
                                                                 for row in range(vertices)]
 except:
  graph[n1]=[n2]
                                                            def printMST(self, parent):
 #Uncomment Below lines if Graph is Undirected
                                                             print "Edge \tWeight"
                                                             for i in range(1, self.V):
  graph[n2].append(n1)
                                                              print parent[i], "-", i, "\t", self.graph[i][
 except:
                                                           parent[i]]
  graph[n2]=[n1]"
                                                            # A utility function to find the vertex with
                                                            # minimum distance value, from the set of
 return(graph)
                                                          vertices
def bfs(graph,start):
                                                            # not yet included in shortest path tree
 n=len(graph)
                                                            def minKey(self, key, mstSet):
 visited=[False]*n
 queue=[start]
                                                             # Initilaize min value
 ans=[]
                                                             min = sys.maxint
 while(queue!=[]):
                                                             for v in range(self.V):
  node=queue.pop(0)
                                                              if key[v] < min and mstSet[v] == False:
  ans.append(node)
                                                                min = key[v]
  visited[node]=True
                                                                min index = v
  for i in graph[node]:
   if(visited[i]==False):
                                                             return min index
```

queue.append(i)

```
def primMST(self):
                                                             # Initilaize min value
  key = [sys.maxint] * self.V
                                                             min = sys.maxint
  parent = [None] * self.V
  key[0] = 0
                                                             for v in range(self.V):
  mstSet = [False] * self.V
                                                               if key[v] < min and mstSet[v] == False:
                                                                min = key[v]
  parent[0] = -1
                                                                min_index = v
  for cout in range(self.V):
                                                             return min_index
   # Pick the minimum distance vertex from
                                                            # Function to construct and print MST for a
   # the set of vertices not yet processed.
                                                           graph
   u = self.minKey(key, mstSet)
                                                            # represented using adjacency matrix
                                                           representation
   # Put the minimum distance vertex in
                                                            def primMST(self):
   # the shortest path tree
                                                             key = [sys.maxint] * self.V
   mstSet[u] = True
                                                             parent = [None] * self.V
                                                             key[0] = 0
                                                             mstSet = [False] * self.V
   # Update dist value of the adjacent vertices
   # of the picked vertex only if the current
                                                             parent[0] = -1
   # distance is greater than new distance and
                                                             for cout in range(self.V):
   # the vertex in not in the shotest path tree
                                                              # Pick the minimum distance vertex from
   for v in range(self.V):
                                                              # the set of vertices not yet processed.
     if self.graph[u][v] > 0 and mstSet[v] == False
                                                               u = self.minKey(key, mstSet)
and key[v] > self.graph[u][v]:
       key[v] = self.graph[u][v]
                                                               # Put the minimum distance vertex in
                                                               # the shortest path tree
       parent[v] = u
                                                               mstSet[u] = True
  self.printMST(parent)
                                                               # Update dist value of the adjacent vertices
                                                               # of the picked vertex only if the current
3. Kruskal's Algorithm (Dictionary/List) –
                                                               # distance is greater than new distance and
                                                               # the vertex in not in the shotest path tree
import sys
                                                               for v in range(self.V):
class Graph():
                                                                if self.graph[u][v] > 0 and mstSet[v] == False
 def __init__(self, vertices):
                                                           and key[v] > self.graph[u][v]:
  self.V = vertices
                                                                  key[v] = self.graph[u][v]
  self.graph = [[0 for column in range(vertices)]
                                                                  parent[v] = u
      for row in range(vertices)]
                                                             self.printMST(parent)
 def printMST(self, parent):
  print "Edge \tWeight"
                                                           4. Dijkstra's Algorithm (Adjacency Matrix) –
  for i in range(1, self.V):
   print parent[i], "-", i, "\t", self.graph[i][
                                                           import sys
parent[i]]
                                                           class Graph():
 # A utility function to find the vertex with
 # minimum distance value, from the set of
                                                            def init (self, vertices):
vertices
                                                             self.V = vertices
 # not yet included in shortest path tree
                                                             self.graph = [[0 for column in range(vertices)]
 def minKey(self, key, mstSet):
                                                                 for row in range(vertices)]
```

```
def printSolution(self, dist):
  print "Vertex \tDistance from Source"
                                                               self.printSolution(dist)
  for node in range(self.V):
   print node, "\t", dist[node]
                                                            5. Strongly Connected components
                                                                (Adjacency List) -
 # A utility function to find the vertex with
 # minimum distance value, from the set of
                                                            from collections import defaultdict
vertices
 # not yet included in shortest path tree
                                                            class Graph:
 def minDistance(self, dist, sptSet):
                                                             def __init__(self,vertices):
                                                               self.V= vertices
  # Initialize minimum distance for next node
                                                               self.graph = defaultdict(list)
  min = sys.maxint
                                                             def addEdge(self,u,v):
                                                               self.graph[u].append(v)
  # Search not nearest vertex not in the
  # shortest path tree
  for v in range(self.V):
                                                             # A function used by DFS
   if dist[v] < min and sptSet[v] == False:
                                                             def DFSUtil(self,v,visited):
     min = dist[v]
                                                               for i in self.graph[v]:
     min index = v
                                                                if visited[i]==False:
                                                                 self.DFSUtil(i,visited)
  return min_index
                                                             def fillOrder(self,v,visited, stack):
 # Function that implements Dijkstra's single
                                                               for i in self.graph[v]:
                                                                if visited[i]==False:
source
                                                                 self.fillOrder(i, visited, stack)
 # shortest path algorithm for a graph represented
 # using adjacency matrix representation
                                                               stack = stack.append(v)
 def dijkstra(self, src):
                                                             # Function that returns reverse (or transpose) of
  dist = [sys.maxint] * self.V
                                                            this graph
  dist[src] = 0
                                                             def getTranspose(self):
  sptSet = [False] * self.V
                                                               g = Graph(self.V)
                                                               for i in self.graph:
  for cout in range(self.V):
                                                                for j in self.graph[i]:
                                                                 g.addEdge(j,i)
   # Pick the minimum distance vertex from
                                                              return g
   # the set of vertices not yet processed.
   # u is always equal to src in first iteration
                                                             # The main function that finds and prints all
   u = self.minDistance(dist, sptSet)
                                                            strongly connected components
                                                             def printSCCs(self):
   # Put the minimum distance vertex in the
                                                               stack = []
   # shotest path tree
                                                               # Mark all the vertices as not visited
   sptSet[u] = True
                                                               visited =[False]*(self.V)
                                                               for i in range(self.V):
   # Update dist value of the adjacent vertices
                                                                if visited[i]==False:
   # of the picked vertex only if the current
                                                                 self.fillOrder(i, visited, stack)
   # distance is greater than new distance and
   # the vertex in not in the shotest path tree
                                                               gr = self.getTranspose()
   for v in range(self.V):
                                                               visited =[False]*(self.V)
     if (self.graph[u][v] > 0 and sptSet[v] ==
False and dist[v] > dist[u] + self.graph[u][v]:
                                                               while stack:
       dist[v] = dist[u] + self.graph[u][v]
                                                                i = stack.pop()
```

```
if visited[i]==False:
     gr.DFSUtil(i, visited)
     print ("")
6. Connected components of a graph
   (Adjacency List) –
class Graph:
 def __init__(self,V):
  self.V = V
  self.adj = [[] for i in range(V)]
 def DFSUtil(self, temp, v, visited):
  visited[v] = True
  temp.append(v)
  for i in self.adj[v]:
   if visited[i] == False:
     temp = self.DFSUtil(temp, i, visited)
  return temp
 # method to add an undirected edge
 def addEdge(self, v, w):
  self.adj[v].append(w)
  self.adj[w].append(v)
 def connectedComponents(self):
  visited = []
  cc = \Pi
  for i in range(self.V):
   visited.append(False)
  for v in range(self.V):
   if visited[v] == False:
     temp = []
     cc.append(self.DFSUtil(temp, v, visited))
  return cc
7. Finding indegree and outdegree of all
   vertices in a graph (Adjacency List) –
def findInOutDegree(adjList, n):
 _{in} = [0] * n
 out = [0] * n
 for i in range(0, len(adjList)):
  List = adjList[i]
  # Out degree for ith vertex will be the count
  # of direct paths from i to other vertices
  out[i] = len(List)
  for j in range(0, len(List)):
   # Every vertex that has
```

# an incoming edge from i

```
_{in[List[j]]} += 1
 print("Vertex\tIn\tOut")
 for k in range(0, n):
  print(str(k) + "\t" + str(_in[k]) +
       "\t" + str(out[k])
8. Topological Sort (Adjacency List) –
from collections import defaultdict
class Graph:
 def __init__(self,vertices):
  self.graph = defaultdict(list)
  self.V = vertices
 def addEdge(self,u,v):
  self.graph[u].append(v)
 def topologicalSortUtil(self,v,visited,stack):
  visited[v] = True
  for i in self.graph[v]:
    if visited[i] == False:
     self.topologicalSortUtil(i,visited,stack)
  stack.insert(0,v)
 def topologicalSort(self):
  visited = [False]*self.V
  stack =[]
  for i in range(self.V):
   if visited[i] == False:
     self.topologicalSortUtil(i,visited,stack)
  print (stack)
9. Floyd-Warshall Algorithm (Adjacency
   Matrix) -
import sys
V = int(input())
# Define infinity as the large enough value. This
value will be
# used for vertices not connected to each other.
INF = sys.maxsize
# Solves all pair shortest path via Floyd Warshall
Algorithm
def floydWarshall(graph):
 dist = map(lambda i : map(lambda j : j, i),
graph)
 for k in range(V):
  for i in range(V):
    for j in range(V):
     dist[i][j] = min(dist[i][j],
       dist[i][k] + dist[k][j]
```

```
printSolution(dist)
def printSolution(dist):
 for i in range(V):
  for j in range(V):
   if(dist[i][j] == INF):
     print ("%7s" %("INF"),)
   else:
     print ("%7d\t" %(dist[i][j]),)
   if j == V-1:
     print ("")
Dynamic Programming:
1. Longest increasing subsequence –
def CeilIndex(A, l, r, key):
 while (r - 1 > 1):
  m = 1 + (r - 1)//2
  if (A[m] >= key):
   r = m
  else:
   1 = m
 return r
def LongestIncreasingSubsequenceLength(A,
size):
 tailTable = [0 \text{ for i in range}(size + 1)]
 len = 0
 tailTable[0] = A[0]
 len = 1
 for i in range(1, size):
  if (A[i] < tailTable[0]):
   tailTable[0] = A[i]
  elif (A[i] > tailTable[len-1]):
   tailTable[len] = A[i]
   len+=1
  else:
   tailTable[CeilIndex(tailTable, -1, len-1, A[i])]
=A[i]
 return len
2. Longest increasing subarray –
def printLogestIncSubArr( arr, n) :
 m = 1
```

```
1 = 1
 maxIndex = 0
 for i in range(1, n):
  if (arr[i] > arr[i-1]):
   1 = 1 + 1
  else:
   if (m < 1):
     m = 1
     maxIndex = i - m
   l = 1
 if (m < 1):
  m = 1
  maxIndex = n - m
 for i in range(maxIndex, (m+maxIndex)):
  print(arr[i], end=" ")
3. Knapsack problem –
def knapSack(W, wt, val, n):
 K = [[0 \text{ for } x \text{ in } range(W+1)] \text{ for } x \text{ in }
range(n+1)
 # Build table K[][] in bottom up manner
 for i in range(n+1):
  for w in range(W+1):
    if i==0 or w==0:
     K[i][w] = 0
    elif wt[i-1] \le w:
     K[i][w] = max(val[i-1] + K[i-1][w-wt[i-1]],
K[i-1][w]
   else:
     K[i][w] = K[i-1][w]
 return K[n][W]
4. Maximum contiguous subarray:
from sys import maxsize
def maxSubArraySum(a,size):
 max\_so\_far = -maxsize - 1
 max\_ending\_here = 0
 start = 0
 end = 0
 s = 0
 for i in range(0,size):
  max\_ending\_here += a[i]
  if max so far < max ending here:
```

```
max_so_far = max_ending_here
start = s
end = i

if max_ending_here < 0:
    max_ending_here = 0
    s = i+1

print ("Maximum contiguous sum, max_so_far)
print ("Starting Index", start)
print ("Ending Index", end)</pre>
```

## 5. Longest common subsequence –

```
def lcs(X, Y, m, n):
 L = [[0 \text{ for } x \text{ in } xrange(n+1)] \text{ for } x \text{ in }
xrange(m+1)
 for i in xrange(m+1):
  for j in xrange(n+1):
    if i == 0 or j == 0:
     L[i][j] = 0
    elif X[i-1] == Y[j-1]:
     L[i][j] = L[i-1][j-1] + 1
    else:
     L[i][j] = max(L[i-1][j], L[i][j-1])
 index = L[m][n]
 lcs = [""] * (index+1)
 lcs[index] = ""
 i = m
 j = n
 while i > 0 and j > 0:
  if X[i-1] == Y[j-1]:
    lcs[index-1] = X[i-1]
    i=1
   j-=1
    index=1
  elif L[i-1][j] > L[i][j-1]:
   i=1
  else:
    j-=1
 return ("".join(lcs))
```

## 6. Suffix array -

```
def suffix_array_best(s):
```

```
n = len(s)
k = 1
line = to_int_keys_best(s)
while max(line) < n - 1:

line = to_int_keys_best(
  [a * (n + 1) + b + 1
  for (a, b) in
  zip_longest(line, islice(line, k, None),
      fillvalue=-1)])
k <<= 1
return line</pre>
```

## **Greedy Algorithms:**

## 1. Activity selection:

```
def printMaxActivities(s , f ):
    n = len(f)
    i = 0
    print i,

for j in xrange(n):
    if s[j] >= f[i]:
    print j,
    i = j
```

#### **Searching Algorithms:**

## 1. Binary Search:

```
def binarySearch (arr, 1, r, x):
  if r >= 1:
    mid = 1 + (r - 1)/2
  if arr[mid] == x:
    return mid
  elif arr[mid] > x:
    return binarySearch(arr, 1, mid-1, x)
  else:
    return binarySearch(arr, mid + 1, r, x)
  else:
    # Element is not present in the array
  return -1
```

#### 2. Ternary Search:

```
def ternarySearch(l, r, key, ar):

if (r \ge 1):

mid1 = 1 + (r - 1) //3

mid2 = r - (r - 1) //3
```

## Math:

#### 1. Factors of a No:

from functools import reduce

```
\begin{array}{c} \text{def factors(n):} \\ \text{return set(reduce(list.\_add\_,} \\ & \quad ([i,\,n/\!/i] \text{ for } i \text{ in range}(1,\,\text{int}(n^{**}0.5)+1) \\ \text{if not } n~\%~i))) \end{array}
```

#### 2. GCD:

```
def GCD(arr):
    return(math.gcd(arr[0],arr[1]))
def gcdlist(arr):
    if len(arr) > 2:
        return reduce(lambda x,y: GCD([x,y]), arr)
    else:
        return(GCD(arr))
```

## 3. Sieve of Erastothenes:

```
MAX_SIZE = 1000001
isprime = [True] * MAX_SIZE
prime = []
SPF = [None] * (MAX_SIZE)
def manipulated_sieve(N):
isprime[0] = isprime[1] = False

for i in range(2, N):
   if isprime[i]==True:
    prime.append(i)
    SPF[i] = i
   i = 0
```

```
while (j < len(prime) and i * prime[j] < N and
prime[j] <= SPF[i]):
    isprime[i * prime[j]] = False
    SPF[i * prime[j]] = prime[j]
    j += 1</pre>
```

#### 4. Fast nCr Function:

```
import operator as op
from functools import reduce

def ncr(n, r):
    r = min(r, n-r)
    numer = reduce(op.mul, range(n, n-r, -1), 1)
    denom = reduce(op.mul, range(1, r+1), 1)
    return numer / denom
```

## 5. Pascal Triangle:

```
def pascal(n):
    line = [1]
    for k in range(n//2):
        line.append((line[k] * (n-k) // (k+1)))
    if(n%2==1):
        line=line+line[::-1]
    else:
        nline=line[:-1]
        line=line+nline[::-1]
    return line
```

#### 6. Wilson theorem:

A natural number p > 1 is a prime number if and only if

```
(p-1)! \equiv -1 \mod p (OR)
(p-1)! \equiv (p-1) \mod p
```

#### 7. Fermat's Little theorem:

```
a^{p-1} \equiv 1 \pmod{p}
OR
a^{p-1} \% p = 1
Here a is not divisible by p.
```

#### 8. Chinese Remainder theorem:

It states that there always exists a x that satisfies given congruence modulo. Used to find minimum x, when a list of numbers and their remainders when mod with x is given.

```
def inv(a, m):
 m0 = m
 x0 = 0
 x1 = 1
 if (m == 1):
  return 0
 while (a > 1):
  q = a // m
  t = m
 m = a \% m
  a = t
  t = x0
  x0 = x1 - q * x0
  x1 = t
 # Make x1 positive
 if (x1 < 0):
  x1 = x1 + m0
 return x1
def findMinX(num, rem, k) :
 prod = 1
 for i in range(0, k):
  prod = prod * num[i]
 result = 0
 for i in range(0,k):
  pp = prod // num[i]
  result = result + rem[i] * inv(pp, num[i]) * pp
 return result % prod
```

## 9. Euler Totient function (?(n)):

Finds the count of numbers in  $\{1,2,3...n\}$  that are relatively prime to n (i.e) the numbers whose GCD with n is 1.

```
Euler Theorem: a^{?(n)} \equiv 1 \pmod{n}
def phi(n):
 result = n
 p = 2
 while(p * p \le n):
  if (n \% p == 0):
    while (n % p == 0):
     n = int(n / p)
    result -= int(result / p)
  p += 1
```

```
14
 if (n > 1):
  result -= int(result / n)
 return result
10. Convex Hull (Graham's scan):
from functools import reduce
def convex_hull_graham(points):
 TURN LEFT, TURN RIGHT, TURN NONE =
(1, -1, 0)
 def cmp(a, b):
  return (a > b) - (a < b)
 def turn(p, q, r):
  return cmp((q[0] - p[0])*(r[1] - p[1]) - (r[0] -
p[0]*(q[1] - p[1]), 0)
 def _keep_left(hull, r):
  while (len(hull) > 1 \text{ and } turn(hull[-2], hull[-1],
r) != TURN_LEFT):
   hull.pop()
  if not len(hull) or hull[-1] != r:
   hull.append(r)
  return hull
 points = sorted(points)
 l = reduce(_keep_left, points, [])
 u = reduce(_keep_left, reversed(points), [])
 return l.extend(u[i] for i in range(1, len(u) - 1))
or 1
11. Modular Exponentiation (Find x^y \% p):
def power(x, y, p):
 res = 1
 # Update x if it is more
 # than or equal to p
 x = x \% p
 while (y > 0):
  # If y is odd, multiply
  # x with result
  if ((y \& 1) == 1):
   res = (res * x) \% p
```

# y must be even now

# y = y/2

y = y >> 1

return res

x = (x \* x) % p

#### 12. Fast Fibonacci:

```
def _fib(n):
    if n == 0:
        return (0, 1)
    else:
        a, b = _fib(n // 2)
        c = a * (b * 2 - a)
        d = a * a + b * b
        if n % 2 == 0:
        return (c, d)
    else:
        return (d, c + d)
```

## 13. Bit Manipulation techniques:

```
1. To multiply by 2^x : S = S < x

2. To divide by 2^x : S = S > x

3. To set jth bit : S = (1 < j)

4. To check jth bit : T = S & (1 < j) (If T = 0 not set else set)

5. To turn off jth bit : S = (1 < j)

6. To flip jth bit : S = (1 < j)

7. To get value of LSB: T = (S & (-S)) (Gives 2^p)

8. To turn on all bits S = (1 < n) - 1

in a set of size n:
```

#### Important packages to use -

- 1. Heapq
- 2. Itertools
- 3. Bisect
- 4. Counter (in collections)
- 5. Defaultdict
- 6. Functools (reduce and @lru cache)
- 7. Time (perf\_counter)

```
t1_start=perf_counter()
t1_stop=perf_counter()
#do something
elapsed_time=t1_start-t1_stop
```

- 8. Regex (Cheat Sheet)
- Matches the beginning of a line
- \$ Matches the end of the line
- . Matches any character
- \s Matches whitespace
- \S Matches any non-whitespace character
- Repeats a character zero or more times

- \*? Repeats a character zero or more times (non-greedy)
- + Repeats a character one or more times
- +? Repeats a character one or more times(non-greedy)
- [aeiou] Matches a single character in the listed set
- [^XYZ] Matches a single character not in the listed set
- [a-z0-9] The set of characters can include a range
- ( Indicates where string extraction is to start
- ) Indicates where string extraction is to end

## **Game Theory:**

- 1. If nim-sum is non-zero, player starting first wins
- 2. Mex: smallest non-negative number not present in a set.
- 3. Grundy=0 means game lost.
- 4. Grundy=mex (Minimum excludant) of all possible next states.
- 5. Sprague-Grundy theorem:

If a game consists of sub games (nim with multiple piles)

Calculate grundy number of each sub game (each pile)

Take xor of all grundy numbers:

If non-zero, player starting first wins.