

Instructions: Use of a Non-Programmable Calculator is allowed.

Q1. Do as directed:

(6)

- (1.) What does probability mean?
 - (a) The total number of possible outcomes in an event
 - (b) The ratio of favourable outcomes to all outcomes
 - (c) The chance of an event happening (d) How certain an event will occur
- (2.) The standard deviation of the Binomial distribution is given by
 - (a) npq (b) $(npq)^2$ (c) $(npq)^{1/2}$ (d) 1
- (3.) A variable that can assume any value between two given points is called
 - (a) Continuous random variable (b) Discrete random variable
 - (c) Irregular random variable (d) Uncertain random variable
- (4.) Out of the following values, which one is not possible in probability?
 - a) $P(x) = 1$ b) $\sum x P(x) = 3$ c) $P(x) = 0.5$ d) $P(x) = -0.5$
- (5.) For two variables, X and Y, the maximum number of regression lines can be
 - (a) Three (b) Two (c) Four (d) One
- (6.) The rank correlation coefficient is always
 - (a) + 1 (b) - 1 (c) 0 (d) Between + 1 and - 1

Q2. Attempt Any Two:

(6)

- (a.) Define probability with different approaches to probability.
- (b.) An office has 12 clerks. The long-serving clerks feel that they should have a seniority increment based on length of service built into their salary structure. An assessment of their efficiency by their departmental manager and the personnel department produces a ranking of efficiency. This is shown below together with a ranking of their length of service.
Do the data support the clerks' claim for seniority increment

Length of service	1	2	3	4	5	6	7	8	9	10	11	12
Efficiency	2	3	5	1	9	10	11	12	8	7	6	4

- (c.) In a glass manufacturing process, it is known that on average 1 in every 1000 of the items produced has one or more bubbles. What is the probability that a random sample of 5000 will yield less than two times possessing bubbles?
- (d.) A card is drawn from a well-shuffled pack of playing cards. Find the probability that the card drawn is (a) either a heart or an honour or king (b) either an ace or a king or a queen.

Q3. Attempt Any Two:

(6)

- (a.) For an experiment of throwing a die twice, find the probability:
 - (i.) of the event of getting a total of 9, given that the die has shown up points between 4 and 6 (both inclusive)
 - (ii.) of the event of getting points between 4 and 6 (both inclusive), given that a total of 9 has already been obtained
- (b.) The owner of a small garment shop is hopeful that his sales are rising significantly week by week. Treating the sales for the previous six weeks as a typical example of this rising trend, he recorded them in Rs 1000's and analyzed the results

Week	1	2	3	4	5	6
Sales	2.69	2.62	2.80	2.70	2.75	2.81

Fit a linear regression equation to suggest to him the weekly rate at which his sales are rising and use this equation to estimate expected sales for the 7th week.

- (c.) A B. Tech graduate applies for a job in two firms X and Y. The probability of his being selected in firm X is 0.7 and being rejected at Y is 0.5. The probability of at least one of his applications being rejected is 0.6. What is the probability that he will be selected by one of the firms?
- (d.) A factory has three units A, B, and C. Unit A produces 50% of its products, and units B and C each produce 25% of the products. The percentage of defective items produced by A, B, and C units are 3%, 2%, and 1%, respectively. If an item is selected at random from the total production of the factory is found defective, what is the probability that it is produced by:
(a) Unit A (b) Unit B (c) Unit C

Q4. Attempt Any Two:

(6)

- (a.) Define continuous random variables with examples and write characteristics of Normal distribution.
- (b.) Assuming the probability of male birth as $\frac{1}{2}$, find the probability distribution of a number of boys out of 5 births. (a) Find the probability that a family of 5 children has (i) at least one boy (ii) at most 3 boys (b) Out of 960 families with 5 children each find the expected number of families with (i) and (ii) above
- (c.) Two random variables have the regression equations: $3x + 2y - 26 = 0$ and $6x + y - 31 = 0$ (a) Find the mean values of x and y and the coefficient of correlation between x and y. (b) If the variance of x is 25, then find the standard deviation of y from the data
- (d.) Ten entries are submitted for a competition. Three judges study each entry and list the ten in rank order. Their rankings are as follows:

Entry	A	B	C	D	E	F	G	H	I	J
Judge-1	9	3	7	5	1	6	2	4	10	8
Judge-2	9	1	10	4	3	8	5	2	7	6
Judge-3	6	3	8	7	2	4	1	5	9	10

Calculate the appropriate rank correlation to help you answer the following questions:

- (i) Which pair of judges agrees the most? (ii) Which pair of judges disagree the most?

Q5. Attempt Any Two:

(6)

- (a.) Define Discrete random variable with examples. Write characteristics of Binomial distribution.
- (b.) 52% of the students at a certain college are females. 5% of the students in this college are majoring in computer science. 2% of the students are women majoring in computer science. If a student is selected at random, find the conditional probability that (a) this student is female, given that the student is majoring in computer science; (b) this student is majoring in computer science, given that the student is female.
- (c.) The probability that an infection is cured by a particular antibiotic drug within five days is 0.75. Suppose four patients are treated by this antibiotic drug, what is the probability that: (a) No patient is cured (b) Exactly two patients are cured (c) At least two patients are cured
- (d.) The time it takes an international telephone operator to place an overseas phone call is normally distributed with a mean of 45 seconds and a standard deviation of 10 seconds. (a) What is the probability that my call will go through in less than 1 minute? (b) What is the probability that my call will get through in less than 40 seconds? (c) What is the probability that I will have to wait more than 70 seconds for my call to go through?