

Computing π

The German mathematician Leibniz discovered the rather remarkable fact that the mathematical constant π can be computed using the following mathematical relationship:

$$\pi/4 = 1 - (1/3) + (1/5) - (1/7) + (1/9) - (1/11) + \dots$$

The formula to the right of the equal sign represents an infinite series; each fraction represents a term in that series. If you start with 1, subtract one-third, add one-fifth, and so on, for each of the odd integers, you get a number that gets closer and closer to the value of $\pi/4$ as you go along.

For this computer assignment, you are to write a C++ program to get an approximate value for π for a given number of $N \geq 1$ terms in the above series. Your program should prompt and get the value of N from the stdin. Your program is supposed to work for any given value of N , but for a final run, use $N = 1,000,000$.

In addition to the `main()` routine, add the following subroutine in your program: `double add_terms (unsigned n)`: This routine adds the first N terms of the above series and returns the computed sum to the `main ()` routine.

Programming Notes:

- You are not allowed to use any I/O functions from the C library, such as `scanf` or `printf`. Instead, use the I/O functions from the C++ library, such as `cin` or `cout`.
- Name your source file as `prog1.cc` and your header file as `prog1.h`
- Guard the statements in your header file using the following format. (This is necessary because you don't want the statements in your header file are processed more than once.)

```
#ifndef H_PROG1 // should not be defined any place else
```

```
#define H_PROG1 // same const value as for ifndef directive above
```

```
// put all statements for your header file here
```

```
#endif
```

- Include all system header files that you need in your program in your header file. For example, to gain access the `iostream` library, which defines a set of I/O operations, insert the line: `#include` in your header file, and at the top of your file, insert your header file by the following line: `#include "prog1.h"`.