

## Mid Term Practice Quiz

1. Which of the following propositional formulas or set of propositional formulas are satisfiable? Choose all that apply.

- a.  $\{p \rightarrow q, q \rightarrow \neg p\}$
- b.  $\{p \rightarrow q, \neg p, \neg q\}$
- c.  $\{p \vee q, \neg p \wedge \neg q\}$
- d.  $\{p \rightarrow q, q, p \rightarrow \neg q\}$

2. Determine which of the following formulas are tautologies. Choose all that apply.

- a.  $[\neg p \wedge (p \vee q)] \rightarrow q$
- b.  $[(p \rightarrow q) \wedge (q \rightarrow r)] \rightarrow [p \rightarrow r]$
- c.  $(p \rightarrow q) \rightarrow (q \rightarrow p)$
- d.  $(p \rightarrow q) \wedge (q \rightarrow p)$

3. Is the following first-order formula satisfiable?

$$\forall x y (x \neq y)$$

- a. Unsatisfiable
- b. Satisfiable

4. What are the free variables in the following formula?

$$\exists x (P(x, y) \rightarrow \forall y P(y, x))$$

- a.  $y$
- b.  $x$
- c. Both  $x$  and  $y$
- d. No Free variable

5. Which is a stable model of the given program?

$$p \leftarrow \neg q$$

$$q \leftarrow \neg r$$

- a.  $\{p, q, r\}$
- b.  $\{p, q\}$
- c.  $\{p\}$
- d.  $\{q\}$

6. Every positive program has a model. True or False?

- a. True

b. False

7. What do you think is the number of stable models of the given program?

$\{p(1..3)\}. \{q(1..3)\}.$

- a. 8
- b. 16
- c. 32
- d. 64

8. How many rules are there in the given clingo program?

$\{p(l) : l = 1..7\}$

- a. 1
- b. 2
- c. 7
- d. 8

9. Select all the minimal models for the formula  $p \vee q$ , given the signature  $\{p, q\}$ .

- a.  $\{p\}$
- b.  $\{q\}$
- c.  $\{p, q\}$
- d. All of the above

10. Given the signature:  $\sigma \{a, b, P\}$ , which are the Herbrand interpretations for the given formula?

$P(a) \wedge \neg P(b) \wedge \exists x \neg P(x)$

- a.  $\emptyset$
- b.  $\{P(a)\}$
- c.  $\{P(b)\}$
- d.  $\{P(a), P(b)\}$