



Practice of Answer Set Programming Aggregates

Objectives



Objective

Use advanced constructs of aggregates in ASP for representing various knowledge.



Introduction

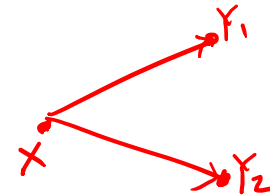
Aggregates: Counting

An aggregate is a function that can be applied to sets, such as `#count`, `#sum`, `#min`, `#max`

`#count{Y: edge(X,Y)}.`

`outdegree(X,N) :- vertex(X), N = #count{Y: edge(X,Y)}.`

`branching_vertex(X) :- vertex(X), #count{Y: edge(X,Y)} > 1.`



`#count{X,Y: edge(X,Y)}`

`num_edges(N) :- N = #count{X,Y: edge(X,Y)}.`

`#count{X,Y,Z: edge(X,Y), edge(Y,Z)}`

`num_length2_path(N) :- N = #count{X,Y,Z: edge(X,Y), edge(Y,Z)}.`



Aggregates : Counting, cont'd

The part of an aggregate expression to the left of the colon may include not only variables, but also more complex terms.

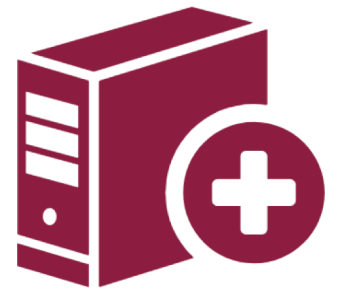
What is the value when $n=5, 10$?

$P(N):-$

$$\#count\{X*Y: X = 2..n, Y = 2..n, X*Y \leq n\} = N$$

$$n=5 : 2*2=4 \quad \{p(1)\}$$

$$n=10 : \begin{matrix} 2*2 & 2*3 & 2*4 & 2*5 & 3*3 \\ \#count\{ & 2 & 6 & 8 & 10 & 9 \} \end{matrix} = 5 \quad \{p(5)\}$$



calculates the number of composite numbers between 1 and n

Cardinality Constraints and Aggregates

$n \{ \text{in}(X) : \text{vertex}(X) \} n.$

(or equivalently, $\{ \text{in}(X) : \text{vertex}(X) \} = n.$

can be also rewritten with a choice rule and a constraint:

$\{ \text{in}(X) \} :- \text{vertex}(X).$

$:- \# \text{count}\{X : \text{in}(X)\} \neq n.$

Exercise. Find a similar transformation for the rule

$5 \{ p(X) : q(X) \} 7.$

$\{ p(X) \} :- q(X).$

$:- \# \text{count}\{X : p(X)\} < 5.$

$:- \# \text{count}\{X : p(X)\} > 7.$

Exercise

$p(a,1).$ $p(b,1).$ $p(b,2).$ $p(c,2).$

$q(N) \text{ :- } N = \#count\{A,X : p(A,X)\}.$

$r(N) \text{ :- } N = \#count\{A : p(A,X)\}.$

$s(N) \text{ :- } N = \#count\{X : p(A,X)\}.$

What is its stable model?

$\{ p(a,1), p(b,1), p(b,2), p(c,2) \}$

$q(4)$

$r(3)$

$s(2)$

Summation

- | If #sum is applied to an expression containing several terms to the left of the colon then the value of #sum can be described in terms of “weights.”
- | The weight of a tuple consisting of integers and symbolic constants is the first member of the tuple.
- | What #sum calculates in application to a set of tuples is the sum of the weights of all its elements that have integer weights.

$p(1, 10; 2, 20).$

$q(S) :- S = \#sum\{X, Y : p(X, Y)\}.$

$r(S) :- S = \#sum\{Y, X : p(X, Y)\}.$

$(X, Y) = (1, 10), (2, 20)$

$q(3)$

$\vdash(30)$

$(Y, X) = (10, 1), (20, 2)$

Exercise

What is the stable model of the program

$p(S) :- S = \#sum\{\underline{N*N}, N : N=-2..2\} .$ $\{ (4, -2), (1, -1), (0, 0), (1, 1), (4, 2) \}$ $p(10)$

$q(S) :- S = \#sum\{N*N : N=-2..2\} .$ $\{ 4, 1, 0 \}$ $q(5)$

Wrap-Up

