

Homework-8

Question 1

You are given a picture with 5 point at the following (x, y) coordinates:

(1,3), (2,1), (2,5), (3,3), (3,5)

Apply the Hough Transform algorithm to search for circles in the parametric representation

$$(x - x_0)^2 + (y - y_0)^2 = r^2.$$

Quantize r^2 into three values: 2, 3, 4.

Quantize x_0 into four values: -1, 1, 3, 5.

Quantize y_0 into four values: -1, 1, 3, 5.

Follow these steps:

Initialization: Prepare and initialize to 0 the three dimensional accumulator space. You can visualize it (and write it in your notebook) as 3 two dimensional arrays. The first for $r^2 = 2$, the second for $r^2 = 3$, and the third for $r^2 = 4$.

Voting: for each point (x, y) of the five picture points
 for each possible value of x_0
 for each possible value of y_0
 {
 compute r^2 from the equation $r^2 = (x - x_0)^2 + (y - y_0)^2$
 If r^2 is in the range 2-4 vote by incrementing the corresponding cell
 }

(Notice that this requires calculating r^2 80 times.)

Choose a winner determine the cell with max number of votes.

- What are the values of the accumulator space after the voting phase?
- What is the most likely circle?

Question 2

You are given the following values of the camera calibration parameters:

$$f = 2, \quad u_0 = 0, \quad v_0 = 1$$

Compute the image location of the following 3D point:

$$X = 7, \quad Y = 13, \quad Z = 2$$

Answer:

Question 3

A point at the coordinates (u, v) in the picture is a projection of a 3D point X, Y, Z . Given that the camera calibration parameters f, u_0, v_0 , and that the 3D point X, Y, Z is on the plane

$$Z = aX + bY + c,$$

prove that:

$$X = \frac{c(u - u_0)}{f - a(u - u_0) - b(v - v_0)} = \frac{cx}{f - ax - by}, \quad Y = \frac{c(v - v_0)}{f - a(u - u_0) - b(v - v_0)} = \frac{cy}{f - ax - by}.$$

Compute Z as as an explicit function of $u, v, a, b, c, f, u_0, v_0$.

Answer