

# **Fluid Mechanics I – Detailed Notes (Based on R.K. Bansal & CUSAT 2024 Syllabus)**

## **MODULE I – Properties of Fluids**

Fluid: A substance that deforms continuously when subjected to shear stress. The study of fluids in motion and at rest is essential for understanding flow in pipes, tanks, and marine systems.

### **1. Basic Properties:**

Density ( $\rho$ ) = mass/volume ( $\text{kg/m}^3$ ); Specific weight ( $\gamma$ ) =  $\rho g$  ( $\text{N/m}^3$ ); Specific gravity (S) =  $\rho/\rho_w$

Dynamic viscosity ( $\mu$ ):  $\tau = \mu (du/dy)$ ; Kinematic viscosity ( $\nu$ ) =  $\mu/\rho$  ( $\text{m}^2/\text{s}$ )

Compressibility ( $\beta$ ):  $-(1/V)(dV/dp)$ ; Surface tension ( $\sigma$ ): force per unit length; Capillarity:  $h = (4\sigma\cos\theta)/(pgd)$

Newton's law of viscosity  $\tau = \mu(du/dy)$ ; Non-Newtonian fluids deviate from this relation.

## MODULE II – Fluid Statics

Pressure variation in static fluid:  $dp/dz = -\rho g \rightarrow p = p_0 + \rho gh$ . Pascal's Law: Pressure at a point acts equally in all directions.

### Hydrostatic Forces:

On plane surfaces:  $F = \rho g A h_c$ ; Center of pressure  $h_{cp} = h_c + (I_G / (h_c A))$

On curved surfaces: Resolved into horizontal and vertical components; Vertical = weight of fluid above surface.

### Buoyancy and Stability:

Buoyant Force  $F_B = \rho g V_{displaced}$ . Center of Buoyancy (B) is centroid of displaced volume.

Metacentric height ( $GM$ ) =  $BM - BG$ ,  $BM = I/V$ . Stable if M above G.

Accelerated Fluids: Inclination  $\theta = \tan^{-1}(a_x/g)$ ; Rotational motion  $z = \omega^2 r^2/(2g)$ .

## MODULE III – Fluid Kinematics & Dynamics

**Types of Flow:** Steady/Unsteady, Uniform/Non-uniform, Laminar/Turbulent, Rotational/Irrotational.

**Flow lines:** Streamline, pathline, streakline.

**Continuity Equation:**  $\partial u / \partial x + \partial v / \partial y + \partial w / \partial z = 0$ . For steady 1D,  $A_1 V_1 = A_2 V_2$ .

**Bernoulli's Equation:**

From Euler's equation:  $dp/\rho g + V_1 dV_1 + g_1 dz = 0 \rightarrow (p/\rho g) + (V^2/2g) + z = \text{constant}$ .

Applications: Venturimeter, Orifice meter, Pitot tube, Weirs, Notches.

Momentum Equation:  $F = \rho(V_2 - V_1)$ . Used for jet impact and pipe bends.

Head Losses: Major  $h_f = f(L/D)(V^2/2g)$ ; Minor  $h_m = K(V^2/2g)$ .

## MODULE IV – Flow Measurement

**Venturimeter:**  $Q = Cd \left( A_1 A_2 / \sqrt{(A_1^2 - A_2^2)} \right) \sqrt{2gh}$ .

**Orifice Meter:**  $Q = Cd a \sqrt{2gh}$ .

**Pitot Tube:**  $V = C \sqrt{2gh}$ .

**Notches & Weirs:** Rectangular:  $Q = (2/3)Cd b \sqrt{2g} H^{3/2}$ ; Triangular (V-notch):  $Q = 1.417Cd H^{5/2}$ .

## MODULE V – Dimensional Analysis & Similitude

**Buckingham's  $\pi$  Theorem:** If a phenomenon depends on  $n$  variables with  $k$  fundamental dimensions, there are  $(n-k)$  dimensionless  $\Pi$  terms.

**Dimensionless Numbers:**

$Re = \rho VL/\mu$  (Inertia/Viscous);  $Fr = V/\sqrt{gL}$ ;  $We = \rho V^2 L/\sigma$ ;  $Eu = p/(\rho V^2)$ ;  $Ma = V/a$ .

**Similarity Laws:** Geometric (length ratios same), Kinematic (Re, Fr same), Dynamic (forces scale similarly).

## **Exam-Oriented Tips:**

**8-Mark Topics:** Bernoulli's derivation, Continuity eqn, Metacentric height, Venturimeter derivation.

**16-Mark Topics:** Flow through pipes (losses), Dimensional analysis using  $\pi$  theorem, Hydrostatic pressure on curved surface, Jet impact problems.

Ensure diagrams are labeled (lines plan, manometer, weir setup). Always show assumptions and stepwise derivation.