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Regular Expressions and Finite State Au-4.1 Stochastic POS Tagging 1.1 Finite State Automaton

Formal definition: (Q, Σ , q_0 , F, $\delta(q,i)$) where:

- O: set of states σ : input alphabet

 q_0 : the start state

F: the set of final state

 $\delta(q,i)$: transition function between the states

1.2 Deterministic Finite State Automaton

Accepts an input string if we run out of input and it is in an accepting sta Exactly one transition for a given symbol from one state to another

1.3 Non-Deterministic Finite State Automaton

Accepts an input string if there is at least some path to an accepting sta that exhaust the input string

Could have more than one transition for the same input symbol or transiti to another empty state through an empty symbol L.4 Convert from NFSA to DFSA

Keep track of all states that can be transitioned from NFSA A state in converted DFSA denotes a combination of states in NFSA

Words, Spelling Errors and Edit Distance

Porter Stemming Algorithm

ATIONAL -> ATE

ING -> ϵ SSES -> SS

2.2 Bayesian Classification

$$c \triangleq argmax_{c \in C} P(c|o) = argmax_{c \in C} \frac{P(o|c).P(c)}{P(o)} = argmax_{c \in C} P(o|c).P(c)$$
 where $P(o|c)$ is the likelihood and $P(c)$ is the prior

2.3 Minimum Edit Distance

| tunction MIN-EDIT-DISTANCE(source, target) returns min-distance |
|--|
| m ← LENGTH(source) |
| n ← LENGTH(target) |
| Create a matrix distance[m + 1, n + 1] |
| $distance[0, 0] \leftarrow 0$ |
| for each row i from 1 to m do |
| distance[i, 0] ← distance[i – 1, 0] + del-cost(source _i) |
| for each column j from 1 to n do |
| distance[0, j] ← distance[0, j − 1] + ins-cost(target _i) |
| for each row i from 1 to m do |

for each column i from 1 to n do

distanceli, il ← MIN(distanceli – 1, il + del-cost(source.) distance[i - 1, j - 1] + subst-cost(source, target,), distanceli, i - 11 + ins-cost(target.))

3 N-grams

3.1 N-gram approximation

 $P(w_k|w_1,...,w_{k-1}) \approx P(w_k|w_{k-(n-1)},...,w_{k-2},2_{k-1})$

MLE: $P(w_k|w_{k-(n-1)},...,w_{k-2},w_{k-1},w_k) =$ $C(w_{k-(n-1)},...,w_{k-2},w_{k-1},w_k)$ $C(w_{k-(n-1)},...,w_{k-2},w_{k-1})$

bigram: n = 2 and trigram: n = 3

 $PP = m(w_1,..,w_n)^{-\frac{1}{n}} = \frac{1}{\sqrt[n]{m(w_1,..,w_n)}}$ For bigrams, $m(w_1, ..., w_n) = \prod_{k=1} nP(w_k | w_{k-1})$

Weighted average number of choices a random variable has to make 5.4 Gradient Descent (weighted average branching factor of a language)

3.3 Smoothing

• Add k smoothing: $P(w|w_0) = \frac{C(w_0w) + k}{C(w_0) + kV}$

Discount: $\frac{C*(w_0w)}{C(w_0w)}$

 $C(w_0w)$ if $C(w_0 w) > 0$ Witten-Bell Smoothing: $P(w|w_0)$ if $C(w_0w) = 0$ $\overline{Z(w_0)(C(w_0)+T(w_0))}$ Kneser-Ney Smoothing for Bigram:

 $C(w_0w)-D$ if $C(w_0w) > 0$ $C(w_0)$ $\alpha(w).|\{w':C(w'w_0)>0\}$ if $C(w_0w) = 0$ $\sum_{w} |\{w' : C(w'w) > 0\}|$

3.4 Entropy

• $H(x) = -\sum_{x \in X} p(x) log_2 p(x)$

• Entropy for a language: $H(L) = \lim_{n \to \inf} \frac{-1}{n} \log_2 p(w_1, ..., w_n)$ • Cross Entropy: $H(p, m) = \lim_{n \to \inf} \frac{-1}{n} \sum_{w \in L} p(w_1, ..., w_n) \log_2 m(w_1, ..., w_n)$

Relation between Perplexity and Entropy:

Perplexity = $2^H = 2^{\frac{-1}{n}} \log_2 m(w_1,...,w_n) = m(w_1,...,w_n)^{\frac{1}{n}}$

POS Tagging

 $T = argmax_{t_1,...,t_T} \prod_{i=1}^{n-1} TP(t_i|t_{i-1}).P(w_i|t_i).P(</s>|t_T)$

Time Complexity: $O(T.N^T)$

4.2 Viterbi (Dynamic Programming)

 $v_t(j) = max_{i=1} Na_{ij}b_j(o(t))$ where a_{ij} is the transition probability, b_i is the **6.5** Cosine similarity observation likelihood of observation o(t)

Time Complexity: $O(N^2)$

4.3 Penn Treebank POS Tags

| 1 | | · ····· · · · · · · · · · · · · · · · | | | | |
|-----|-----------------------|---------------------------------------|------|-----------------------|------------|--|
| Tag | Description | Example | Tag | Description | Example | |
| CC | coordin. conjunction | and, but, or | SYM | symbol | +,%, & | |
| CD | cardinal number | one, two, three | TO | "to" | to | |
| DT | determiner | a, the | UH | interjection | ah, oops | |
| EX | existential 'there' | there | VB | verb, base form | eat | |
| FW | foreign word | mea culpa | VBD | verb, past tense | ate | |
| IN | preposition/sub-conj | of, in, by | VBG | verb, gerund | eating | |
| JJ | adjective | yellow | VBN | verb, past participle | eaten | |
| JJR | adj., comparative | bigger | VBP | verb, non-3sg pres | eat | |
| JJS | adj., superlative | wildest | VBZ | verb, 3sg pres | eats | |
| LS | list item marker | 1, 2, One | WDT | wh-determiner | which, the | |
| MD | modal | can, should | WP | wh-pronoun | what, who | |
| NN | noun, sing. or mass | llama | WP\$ | possessive wh- | whose | |
| NNS | noun, plural | llamas | WRB | wh-adverb | how, when | |
| NNF | proper noun, singular | IBM | \$ | dollar sign | \$ | |
| NNF | S proper noun, plural | Carolinas | # | pound sign | # | |
| PDT | predeterminer | all, both | ** | left quote | ' or " | |
| POS | possessive ending | 's | ** | right quote | ' or " | |
| PRP | personal pronoun | I, you, he | (| left parenthesis | [, (, {, < | |
| PRP | \$ possessive pronoun | your, one's |) | right parenthesis |],), }, > | |
| RB | adverb | quickly, never | , | comma | , | |
| RBR | adverb, comparative | faster | | sentence-final punc | .1? | |
| RBS | adverb, superlative | fastest | : | mid-sentence punc | : ; | |
| RP | particle | up, off | | | | |

Neural Networks Multi Laver Perceptron

$$\begin{split} NN_{MLP2}(x) &= (g^2(g^1(xW^1+b^1)W^2+b^2))W^3+b^3\\ h^1 &= g^1(xW^1+b^1)\\ h^2 &= g^2(xW^2+b^2)\\ v &= h^2W^3+b^3 \end{split}$$

5.2 Activation Functions

RELU(x) = g(x) = max(0, x)

Sigmoid: $\sigma(x) = \frac{1}{1+e^{-x}}$, $\sigma'(x) = \sigma(x)(1-\sigma(x))$

Tanh: $tanh(x) = \frac{e^{x} + e^{-x}}{e^{x} - e^{-x}}$, $tanh'(x) = 1 - (tanh(x))^2$

HardTanh: $hardtanh(x) = \begin{cases} -1 & x < -1 \\ 1 & x > 1 \\ x & \text{otherwise} \end{cases}$

5.3 Loss Functions

Cross Entropy Loss: $L_{logistic}(\hat{y}, y) = -ylog_2(\hat{y}) - (1 - y)log_2(1 - \hat{y})$ where **8**.1 $y \in \{0,1\}$ for binary classification

For multi class classification (C > 2), $L_{logistic}(\hat{y}, y) = \sum_{-i}^{C} t_i log_2(\hat{y}_t)$

Softmax loss: $L_{softmax}(\hat{y}, y) = \frac{e^{\hat{y}[\hat{t}]}}{\sum_{j} e^{\hat{y}[\hat{t}]}}$, squishes range of values to (0, 1), a probability $\hat{x}_{j} = \hat{x}_{j} = \hat{y}_{j} = \hat{y}_{j} = \hat{y}_{j}$

probability distribution Squared (quadratic) loss: $L_{squared}(y/hat, y) = 0.5 * (\hat{y} - y)^2$

 $w_i = w_i - \alpha \frac{\delta L}{w_i} \frac{\delta L}{w_m} = \sum_{i=1}^{N} N \frac{\delta L}{\delta x_i} \frac{\delta x_i}{\delta w_m}$

Word Embeddings

6.1 Word2Vec

$$\begin{split} s(w,c) &= w.c \\ P(+|t,c) &= \frac{1}{1+e^{-t.c}} \\ P(-|t,c) &= 1 - P(+|t,c) = \frac{e^{-t.c}}{1+e^{-t.c}} \end{split}$$

6.2 Choosing noise words

 $P_{\alpha}(w) = \frac{count(w)^{\alpha}}{\sum_{w}' count(w')^{\alpha}}$ where count is the unigram frequency. In practice, \$alpha\$ value of 0.75 works quite well.

Maximize objective function: $\textstyle \sum_{(w,c)\in D} log_2 P(+|t,c) + \sum_{(w,c)\in D} log_2 P(-|t,c)$

6.3 CBOW

 $c = \sum_{i} c_{i}$

 $c = \angle_{1} c_{i}$ $log P(+|w, c_{1:k}) = log \frac{1}{1 + e^{(\sum_{i=1...k} w. c_{i})}}$

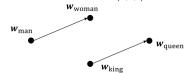
6.4 Skip-gram

 $P(+|w,c_{1..k}) = \prod_{i=1}^{k} \frac{1}{1+e^{-w.c_i}}$

 $P(+|w,c_{1..k}) = \sum_{i=1}^{k} log \frac{1}{1+e^{-w.c_i}}$

 $sim_{COS}(u, v) = \frac{\mathbf{u}.\mathbf{v}}{\|\|\mathbf{u}\|\|_2 \|\|\mathbf{v}\|\|_2}$

 $analogy(m: w->k:?) = argmax_{v \in V\{m,w,k\}}cos(v,k-m+w)$



CNN

7.1 Why is it used?

Identify informative ngrams Consider local ordering patterns

.2 Process

Apply non linear learned function (filter) over each k-word sliding window Apply I filters to get I-dimensional vector

Combine vectors from different windows using pooling into single 1 dimensional vector Feed single 1-dimensional vector into neural network for prediction

7.3 Convolution

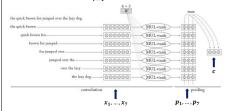
Narrow convolution (no padding): m = n - (k - 1)

Wide convolution (padding k - 1 to each side): m = n + (k - 1)

7.4 Pooling

Max pooling: $c_j = \max_{1 < i < m} p_{i[j]} \forall j \in [1, l]$

Average pooling: $\frac{1}{m}\sum_{i=1}^{m} p_i$



Narrow convolution, n = 9, d = 2, k = 3, l = 3, m = 7

RNN Why is it used?

Capture subtle patterns and regularities in sequences Model non-Markovian dependencies

$$RNN^{4}(x_{1:n}:s_{0}) = y_{1..n}$$

$$s_{i} = R(s_{i-1}, x_{i})$$

$$y_{i} = o(s_{i})$$

$$y_{1} \qquad y_{2} \qquad y_{3} \qquad y_{4} \qquad y_{5}$$

$$s_{0} \longrightarrow R, O \qquad s_{1} \longrightarrow R, O \qquad s_{4} \longrightarrow R, O \longrightarrow s_{5}$$

$$x_{1} \qquad x_{2} \qquad x_{3} \qquad x_{4} \longrightarrow s_{5}$$

Recursive view:



8.3 Elman RNN

Sensitive to the order of the words $y_i = O_R NN(s_i)$

$$x_i \in R^{d_X}, S_i \in R^{d_S}, W \in R^{(d_X + d_S).d_S}, b \in R_S^d$$

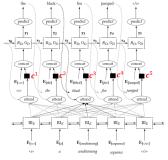
8.4 CBOW RNN

Does not take into account order of words

count order of words
$$s_i = R_{CBOW}(s_{i-1}, x_i) = s_{i-1} + x_i$$

 $y_i = O_{CBOW}(s_i)$

Seq2Seq



10 Grammars 10.1 CFG

 $G = (N, \Sigma, P, S)$

N - terminal symbols

Σ - non-terminal symbols

P - a -> A where a∈ N, A∈ (Σ ∪ N)*

10.2 CNF

A -> BC or A -> a No epsilon

10.3 Equivalence Strong equivalence: L(G1) = L(G2) and same phrase structure

Weak equivalence: L(G1) = L(G2) but different phrase structures

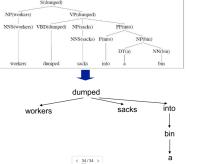
10.4 Convert to CNF

Copy all conforming rules to the new grammar unchanged Convert terminals within rules to dummy non-terminals

Convert unit-productions Binarize all rules and add to new grammar

10.5 Converting Phrase Structure to Untyped Dependency

Find the head (head child is underlined) and pass it up the tree



Top down parsing: Goal directed, begin from start symbol and then derive parse tree for the given sentence consisting of terminals

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Bottom up parsing: Data directed, start form the terminals in a sentence and derive parse tree by tracing up to the start symbol.

10.7 Ambiguity

- Attachment Ambiguity: Ambiguity on how a verb phrase is split up based on the rules in the CFG (VP -> V NP PP or VP -> V PP for example)
- Coordination Ambiguity: Ambiguity depending on how the Noun Phrase is
- · Noun Phrase Bracketing Ambiguity: Ambiguity depends on how the Noun Phrase is split

10.8 Parsing Algorithms

10.8.1 CKY algorithm



- · Bottom-up dynamic programming
- Grammar must be in CNF
- Time Complexity: $O(n^3)$, Space Complexity: $O(n^2)$
- Probabilistic version: most probable parse stored based on taking the max imum of probabilities calculated using the assigned probabilities for each production in the Grammar for regular CKY

10.8.2 Earley Algorithm

- Top-down dynamic programming
- Grammar need not be in CNF
- Scan sentence from left to right
- Predictor: Create new states from original states using grammar (e.g. Given S -> .VP [0, 0], add VP -> .Verb [0, 0] and VP -> .Verb NP [0, 0])
- Scanner: Use predicted POS to incorporate the next word (e.g. Given the state VP -> .Verb NP [0, 0], add Verb -> book. [0, 1])
- Completer: Find and advanced previously created states looking for non terminal at this position (e.g. Given stated NP -> Det Nominal.[1, 3] and VP
- -> Verb.NP [0, 1] and add the new state VP -> Verb NP. [0, 3]) Time Complexity: $O(n^3)$ maximum but tends to perform better, Space Com
- plexity: O(n)

11 Statistical Parsing

11.1 PCFG

• $P(T,S) = \prod_{t \in T} p(r(n))$ where r(n) represents the rules of CFG applicable to the parse trees

• T(S) = argmaxP(T)

11.2 Parse Tree Scoring

- stree(T) = σ(i,i,l)∈T s(i,j,l)
- Feed sentence through bidirectional LSTM and then a Dense NN and score based on loss
- Dynamic Programming:

$$s_{best}(i,j) = max_{l}[s(i,j,l)]ifj - i = 1$$

 $s_{best}(i,j) = max_{l}[s(i,j,1)] + max_{k}[s_{best}(i,k) + s_{best}(k,j)] \label{eq:sbest}$

Best scored tree: $T \triangleq argmax_T[s_{tree}(T)]$

12 Semantics

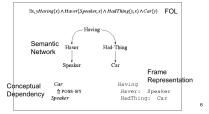
12.1 First Order Logic

FOL

Formula -> AtomicFormula Formula Connective Formula Quantifier Variable . . . Formula ¬ Formula (Formula) AtomicFormula → Predicate(Term,...) Term → Function(Term,...) Constant Variable Connective $\rightarrow \land |\lor| \Rightarrow$ Quantifier → ∀ | ∃ Constant → A | VegetarianFood | Maharani·· Predicate → Serves | Near | $Function \rightarrow LocationOf \mid CuisineOf \mid \cdots$

12.2 Meaning Representation in First-Order Logic Meaning Representation

Sentence: I have a car.



12.3 Syntax Driven Semantic Analysis

