

These problems will help you understand the Basic data structure (queues, stacks, ...etc.) and Quick-Union. This Homework should prepare you for Project as well.

Submitting Information:

- DO NOT post your code on Piazza
- Use the code I provided for each problem. DO NOT delete any function
- Submit your work on Canvas.
- DO NOT change the name of .java files.
- Put all the .java files in one zip file and name it <last_Name><first_initial>.zip for example ChandakA.zip for Name Aniket Chandak
- For theory answer, you are allowed to write your answer in word or handwritten on paper. You create pdf for your word/scanned copy of handwritten answer and put in the zip file
- The deadline is Tuesday, Feb 17th at 11:55PM
- Follow the guidelines in homework rubric

Problem 1. Give a counterexample that shows why this intuitive implementation of `union()` for quick-find is not correct:

```
public void union(int p, int q) {  
    if (connected(p, q)) return;  
    for (int i = 0; i < id.length; i++)  
        if (id[i] == id[p]) id[i] = id[q];  
    count--;  
}
```

Problem 2: Consider for union function, p is part of smaller tree and q is part of bigger tree. As per the weighted quick-union, we change the `id[root(p)]` to `id[root(q)]` to make a union. If we change `id[root(p)]` to q instead of `id[root(q)]`, would the resulting algorithm be still correct? Give reason for your answer. Also are there any performance consequences?

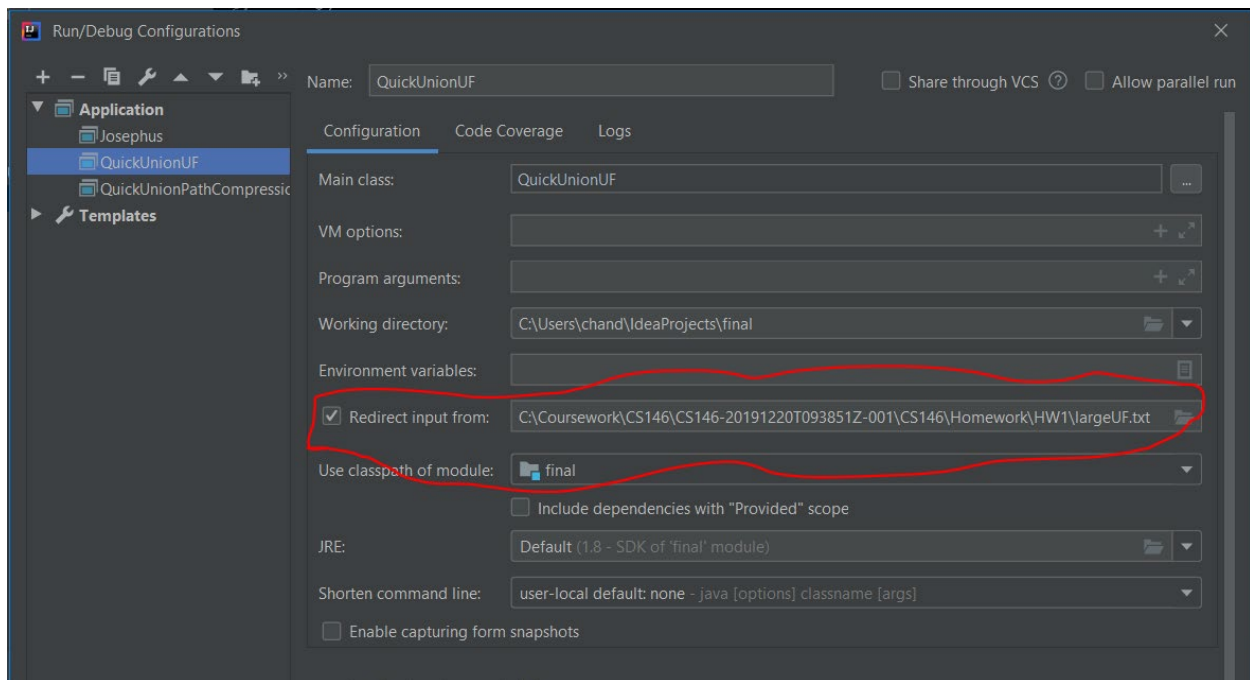
Problem 3: Two skeleton code are given for Quick-Union implementation, `QuickUnionUF.java` and `QuickUnionPathCompressionUF.java`. Add the missing code for functions in both programs. `QuickUnionUF.java` is normal implementation with no improvement whereas the other code should have improvement for path compression (Two pass). Three different inputs are provided to run a program `smallUF.txt`, `mediumUF.txt` and `LargeUF.txt`. You can test your implementation using any of the given input file.

Following command is example to run a code:

```
$ java QuickUnionUF < smallUF.txt
```

If you are using IntelliJ, you need to edit the configuration with input file before running program.

Below is screenshot for my configuration:



Problem 4: Compare the performance of the codes from Problem 3 for each input size. Give your analysis. [which one is faster and what is the reason for faster performance.]

Problem 5. (*Josephus.java*) In the Josephus problem from antiquity, N people are in dire straits and agree to the following strategy to reduce the population. They arrange themselves in a circle (at positions numbered from 0 to $N - 1$) and proceed around the circle, eliminating every M th person until only one person is left. Legend has it that Josephus figured out where to sit to avoid being eliminated. Write a Queue client *Josephus.java* that takes N and M from the command line and prints out the order in which people are eliminated (and thus would show Josephus where to sit in the circle).

```
$ java Josephus 7 2
1 3 5 0 4 2 6
$ java Josephus 20 3
2 5 8 11 14 17 0 4 9 13 18 3 10 16 6 15 7 1 12 19
```

Problem 6. (*KthString.java*) Write a Queue client *KthString.java* that takes a command-line argument k and prints the k th string from the end found on standard input, assuming that standard input has k or more strings

```
$ java KthString 9
it was the best of times it was the worst of times best
<ctr-d>
best
```

Problem 7. (*Parantheses.java*) Implement the static method `match()` in `Parantheses.java` that takes a string `s` as argument and uses a stack to determine whether its parentheses are properly balanced, and returns `true` if they are and `false` otherwise. You may assume that `s` only consists of parentheses (curly, square, and round).

```
$ java Parantheses
[()]{ }{ [ ( ) ] ( ) }
true
$ java Parantheses
[ ( ] )
<ctr-d>
false
```