

Competitive Coding

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(4)

Experiments

We define $f(x, y)$ as number of different corresponding bits in the binary representation of x and y . For eg $\rightarrow f(2, 7) = 2$, since the binary representation of 2 and 7 are 010 and 111, respectively. The first and the third bit differs, so $f(2, 7) = 2$.

Test cases: ① Input $A = [1, 3, 5]$ Output $A = 8$ ② Input $A = [2, 3]$ Output $A = 2$

You are given an array of N positive integers $A_1, A_2, A_3, \dots, A_N$. Find sum of $f(A_i, A_j)$ for all pairs (i, j) such that $1 \leq i, j \leq N$. Return the ans modulo $10^9 + 7$.

Solution → Given

$f(x, y) = \text{no. of different bits in binary of } x \text{ and } y$

[Checking every pair of bits $\rightarrow TC = (n^2) \rightarrow TLE$]

To solve this, we can use the concept of bit manipulation by checking the bits of x and y .

Let's look at a particular k^{th} bit

If k^{th} bit of x is 1 and k^{th} bit of y is 0.
Or vice versa

So ans = 2 for pair (x, y) and (y, x)

\rightarrow Let cnt1 = nos having bit $k=1$

cnt0 = nos having bit $k=0$

Contribution = ② \times (cnt1 \times cnt0)

(for (x, y) and (y, x))

→ Steps to solve

for every bit ($0 \rightarrow 31$)

1) Count numbers having that bit set.

2) Compute pairs

3) Add to answer

Code :

```
#include <bits/stdc++.h>
using namespace std;

const long long MOD = 1e9 + 7;
long long totalpairs(vector<int> &A) {
    long long n = A.size();
    long long ans = 0;
    for (int bit = 0; bit < 32; bit++) {
        long long cnt1 = 0;
        for (int i = 0; i < n; i++) {
            if (A[i] & (1 << bit)) {
                cnt1++;
            }
        }
        long long cnt0 = n - cnt1;
        long long contribution = (cnt1 * cnt0) % MOD;
        contribution = (2 * contribution) % MOD;
        ans = (ans + contribution) % MOD;
    }
    return ans;
}
```

Dry Run

Input = {1, 3, 5}

1 → 001

3 → 011

5 → 101

for Bit → 1(1), 3(1), 5(1)

$$\Rightarrow \text{Cnt} + 1 = 0$$

$$\text{Cnt} + 0 = 0$$

$$\text{Contribution} = 2 \times 3 \times 0 = 0$$

for Bit 1 \rightarrow 1(0), 3(1), 5(0)

$$\Rightarrow \text{Cnt} + 1 = 1$$

$$\text{Cnt} + 0 = 2$$

$$\text{Contribution} = 2 \times 1 \times 2 = 4$$

for Bit 2 \rightarrow 1(0), 3(0), 5(1)

$$\Rightarrow \text{Cnt} + 1 = 1$$

$$\text{Cnt} + 0 = 2$$

$$\text{Contribution} = 2 \times 1 \times 2 = 4$$

$$\text{Total answer} = 0 + 4 + 4 = 8$$

pair	$f(n, y)$
(1, 1)	0
(1, 3)	1
(1, 5)	1
(3, 1)	1
(3, 3)	0
(3, 5)	2
(5, 1)	1
(5, 3)	2
(5, 5)	0