

Competitive Coding  
Name- Aaditya Anand  
UID-23BCS10446  
Section- KRC-3A

4

### experiments

we define  $f(x, y)$  as number of different corresponding bits in the binary representation of  $x$  and  $y$ . for eg  $\rightarrow f(2, 7) = 2$ , since the binary representation of 2 and 7 are 010 and 111, respectively. the first and the third bit differs, so  $f(2, 7) = 2$

Test Cases: ① Input  $A = [1, 3, 5]$   
Output  $A = 8$

② Input  $A = [2, 3]$   
Output  $A = 2$

you are given an array of  $n$  positive integers  $A_1, A_2, A_3 \dots A_n$ . find sum of  $f(A_i, A_j)$  for all pairs  $(i, j)$  such that  $1 \leq i, j \leq n$ .

Return the ans modulo  $10^9 + 7$ .

Solution  $\rightarrow$  Given

$f(x, y)$  = no. of different bits in binary of  $x$  and  $y$   
[checking every pair of bits  $\rightarrow TC = (n^2) \rightarrow TLE$ ]

To solve this, we can use the concept of bit manipulation by checking the bits of  $x$  and  $y$ .

Let's look at a particular  $k^{th}$  bit

if  $k^{th}$  bit of  $x$  is 1 and  $k^{th}$  bit of  $y$  is 0.  
or vice versa

so ans = 2 for pair  $(m, y)$  and  $(y, n)$

$\rightarrow$  let  $cnt1$  = nos having bit  $k=1$

$cnt0$  = nos having bit  $k=0$

contribution =  $(2) \times cnt1 \times cnt0$

(for  $(m, y)$  and  $(y, n)$ )

→ Steps to solve

for every bit (0 → 31)

1) Count numbers having that bit set.

2) Compute pairs

3) Add to answer

Code : #include <bits/stdc++.h>  
using namespace std;

const long long MOD = 1e9 + 7;

long long totalpairs(vector<int> &A) {

long long n = A.size();

long long ans = 0;

for (int bit = 0; bit < 32; bit++) {  
long long cnt1 = 0;

for (int i = 0; i < n; i++) {  
if (A[i] & (1 << bit)) {  
cnt1++; } }

long long cnt0 = n - cnt1;

long long Contribution = (cnt1 \* cnt0) % MOD;

Contribution = (2 \* Contribution) % MOD;

ans = (ans + Contribution) % MOD; }

return ans; }

DRY Run

Input = {1, 3, 5}

1 → 001

3 → 011

5 → 101

for Bits → 1(1), 3(1), 5(1)



$$\Rightarrow \text{Cnt } 1 = 0$$

$$\text{Cnt } 0 = 0$$

$$\text{Contribution} = 2 \times 3 \times 0 = 0$$

$$\text{for Bit } 1 \rightarrow 1(0), 3(1), 5(0)$$

$$\Rightarrow \text{Cnt } 1 = 1$$

$$\text{Cnt } 0 = 2$$

$$\text{Contribution} = 2 \times 1 \times 2 = 4$$

$$\text{for Bit } 2 \rightarrow 1(0), 3(0), 5(1)$$

$$\Rightarrow \text{Cnt } 1 = 1$$

$$\text{Cnt } 0 = 2$$

$$\text{Contribution} = 2 \times 1 \times 2 = 4$$

$$\text{Total answer} = 0 + 4 + 4 = 8$$

pair	$f(m, y)$
(1, 1)	0
(1, 3)	1
(1, 5)	1
(3, 1)	1
(3, 3)	0
(3, 5)	2
(5, 1)	1
(5, 3)	2
(5, 5)	0