

Obtain the disjunctive normal form using truth table:

$$(p \wedge q) \vee (\sim p \wedge r) \vee (q \wedge r)$$

p	q	r	$\sim p$	$p \wedge q$	$\sim p \wedge r$	$(p \wedge q) \vee (\sim p \wedge r)$	$q \wedge r$	A
T	T	T	F	T	F	T	T	T ✓
T	T	F	F	T	F	T	F	T ✓
T	F	T	F	F	F	F	F	F
T	F	F	F	F	F	F	F	F
F	T	T	T	F	T	T	T	T ✓
F	T	F	T	F	F	F	F	F
F	F	T	T	F	T	T	F	T ✓
F	F	F	T	F	F	F	F	F

\therefore dnf is,

$$(p \wedge q \wedge r) \vee (p \wedge q \wedge \sim r) \vee (\sim p \wedge q \wedge r) \vee (\sim p \wedge \sim q \wedge r)$$

Obtain the conjunctive normal form using truth table: $(\sim p \rightarrow r) \wedge (q \leftrightarrow p)$

p	q	r	$\sim p$	$\sim p \rightarrow r$	$q \leftrightarrow p$	A
T	T	T	F	T	T	T
T	T	F	F	T	T	T
T	F	T	F	T	F	F ✓
T	F	F	F	T	F	F ✓
F	T	T	T	T	F	F ✓
F	T	F	T	F	F	F ✓
F	F	T	T	T	T	T
F	F	F	T	F	T	F ✓

Here truth value is F.

$$(p \wedge \sim q \wedge r) \vee (p \wedge \sim q \wedge \sim r) \vee (\sim p \wedge q \wedge r) \vee (\sim p \wedge q \wedge \sim r) \vee (\sim p \wedge \sim q \wedge \sim r)$$

Hence cnf is,

$$(\sim p \vee q \vee r) \wedge (\sim p \vee q \vee \sim r) \wedge (p \vee \sim q \vee r) \wedge (p \vee \sim q \vee \sim r) \wedge (p \vee q \vee r)$$

