Round: Practice Team

**Problem 1.** Determine the value of  $(3^{3^2} - 3^{2^3} + 3^{2^2} - 2^{3^3})(3 + 3 - 3 + 2)^3(3^2 - 2^3 - 1)(3^3 + 2^2 + 1^1)$ .

**Problem 2.** Michael has a playlist with 6 songs in it, but 1 of the songs is a repeat of another. If he presses shuffle, how many possible orders are there for his playlist?

**Problem 3.** Edwin is swimming in a circular lake. He swims at  $2\pi$  meters per minute. If it takes him 2400 seconds to swim around the edge of the lake, what is the radius of the lake?

**Problem 4.** If  $x + \frac{1}{x} = 4$ , what is  $x^2 + \frac{1}{x^2}$ ?

**Problem 5.** What is the area of a square with all four of its vertices on a circle of radius 10?

**Problem 6.** Timmy rolls 4 standard, fair, six-sided die. What is the probability that at least one of the number he rolls is prime?

**Problem 7.** Let a, b, and c be real numbers such that a + b + 2c = 2015, a + 2b + c = 2016, and 2a + b + c = 2017. What is the value of a + b + c?

**Problem 8.** Additya is downloading an Android app. Every second, his phone has an equal chance to either download 20% of the app or do nothing. What is the probability that after 8 seconds, the app will have finished downloading?

**Problem 9.** A triangle with integer side lengths has a perimeter of 5. What is its area?

**Problem 10.** What is the largest prime factor of  $17^3 + 1$ ?