

KIET Group of Institutions

(Roll Number: _____)

(Department of Applied Science)
B.Tech, IV Semester
CT-2 Examination, (2019-20)Even Semester
(Mathematics-IV) (KAS-402)

Duration: 2hrs

Max. Marks: 60

Section-A

Attempt all the questions of this section

(2X10=20)

| Q. No. | Question | Marks | CO | BL |
|--------|---|-------|----|----|
| 1. | a Define radio equation. | 2 | 2 | 1 |
| | b Explain the moments about mean. | 2 | 3 | 2 |
| | c Define the lines of regression. | 2 | 3 | 1 |
| | d Describe the relation between the second moment about origin and second moment about mean. | 2 | 3 | 2 |
| | e Discuss the types of Kurtosis. | 2 | 3. | 2 |
| | f Show that if one of the regression coefficients is greater than unity then other will be less than unity. | 2 | 3 | 3 |
| | g Describe addition law of probability. | 2 | 4 | 2 |
| | h Describe the two dimensional wave equation. | 2 | 2 | 2 |
| | i Determine the normal equations of the curve $y = \frac{a}{x} + b\sqrt{x}$. | 2 | 3 | 3 |
| | j Define moment generating function of a distribution. | 2 | 3 | 1 |

Section-B

Attempt all the questions of this Section

(5X4=20)

| Q. No. | Question | Marks | CO | BL | | | | | | | | | | | | | | | | | | | | |
|--|--|--------|--------|--------|--------|----|-----|-------|--------|--------|--------|--------|---|---|----|----|----|----|----|---|---|---|---|---|
| 2 | Calculate the variance and third central moment from following data <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td></tr><tr><td>f</td><td>1</td><td>9</td><td>26</td><td>59</td><td>72</td><td>52</td><td>29</td><td>7</td><td>1</td></tr></table> Also calculate the value of β_1 . | x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | f | 1 | 9 | 26 | 59 | 72 | 52 | 29 | 7 | 1 | 5 | 3 | 3 |
| | x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | | | | | | | | | | | | | |
| | f | 1 | 9 | 26 | 59 | 72 | 52 | 29 | 7 | 1 | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | |
| Calculate the values a and b so that the curve $y = ae^{bx}$ fits the data given in the table. <table><tr><td>x</td><td>2</td><td>4</td><td>6</td><td>8</td><td>10</td></tr><tr><td>y</td><td>4.077</td><td>11.084</td><td>30.128</td><td>81.897</td><td>222.62</td></tr></table> | x | 2 | 4 | 6 | 8 | 10 | y | 4.077 | 11.084 | 30.128 | 81.897 | 222.62 | | | | | | | | | | | | |
| x | 2 | 4 | 6 | 8 | 10 | | | | | | | | | | | | | | | | | | | |
| y | 4.077 | 11.084 | 30.128 | 81.897 | 222.62 | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | If $2x + 3y = 7$ and $5x + 4y = 9$ are two lines of regression, then describe the following: (i) mean values of x and y , (ii) the regression coefficients, (iii) the correlation coefficient between x and y . | 5 | 3 | 2 | | | | | | | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | |

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| | | | | |
|---|--|---|---|---|
| | Describe coefficient of correlation. If θ is the acute angle between the two lines of regression then prove that $\tan \theta = \frac{1-r^2}{r} \frac{\sigma_x \sigma_y}{\sigma_x^2 + \sigma_y^2}$ where r , σ_x , σ_y have their usual meaning. Also give the significance of the formula when $r = 0, \pm 1$. | | | |
| 4 | <p>A student takes his examination in four subjects a, b, c, d. He estimates his chances of passing in a as $\frac{4}{5}$, in b as $\frac{3}{4}$, in c as $\frac{5}{6}$ in d as $\frac{2}{3}$. To qualify, he must pass in a, and at least two other subjects. Calculate the probability that he qualifies.</p> <p>OR</p> <p>A husband and wife appear in an interview for two vacancies in the same post. The probability of husband's selection is $\frac{1}{7}$ and that of wife's selection is $\frac{1}{5}$. Calculate the probability that (i) both of them will be selected (ii) only one of them will be selected and (iii) none of them will be selected.</p> | 5 | 4 | 3 |
| 5 | <p>Determine the moment generating function of the exponential distribution $f(x) = \frac{1}{c} e^{-x/c}$, $0 \leq x \leq \infty$, $c > 0$. Also find mean and standard deviation.</p> <p>OR</p> <p>First four moments of a distribution about 2 are 1, 2.5, 5.5 and 16. Determine the first four moments about the mean and origin.</p> | 5 | 3 | 3 |

| | Section-C | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--|---|----|-----------|----|----|-----|----|-----|----|-----|-----|----|----|----|----|----|----|-----|----|-----|----|-----|-----|----|----|----|---|
| Attempt all the questions of this Section | | | (10X2=20) | | | | | | | | | | | | | | | | | | | | | | | | |
| Q. No. | Question | | Marks | CO | BL | | | | | | | | | | | | | | | | | | | | | | |
| 6 | A square plate is bounded by lines $x = 0, y = 0, x = 20, y = 20$. It's faces are insulated. The temperature along the upper horizontal edge is given by $u(x, 20) = x(20 - x)$ and other three edges are kept at zero temperature. Evaluate the steady state temperature in the plate | | 10 | 2 | 5 | | | | | | | | | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Evaluate the voltage v in a transmission line of length $5m$ if t seconds after its ends are suddenly grounded; given that R and G are negligible and $i(x, 0) = i_o, v(x, 0) = v_0 \sin \frac{3\pi x}{5}$. | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7 | Calculate the correlation coefficient for the following data: <table border="1"><tr><td>x</td><td>21</td><td>23</td><td>30</td><td>54</td><td>57</td><td>58</td><td>72</td><td>78</td><td>87</td><td>90</td></tr><tr><td>y</td><td>60</td><td>71</td><td>72</td><td>83</td><td>110</td><td>84</td><td>100</td><td>92</td><td>113</td><td>135</td></tr></table> | x | 21 | 23 | 30 | 54 | 57 | 58 | 72 | 78 | 87 | 90 | y | 60 | 71 | 72 | 83 | 110 | 84 | 100 | 92 | 113 | 135 | | 10 | 3 | 3 |
| | x | 21 | 23 | 30 | 54 | 57 | 58 | 72 | 78 | 87 | 90 | | | | | | | | | | | | | | | | |
| | y | 60 | 71 | 72 | 83 | 110 | 84 | 100 | 92 | 113 | 135 | | | | | | | | | | | | | | | | |
| OR | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Calculate the rank correlation coefficient for the following data: <table border="1"><tr><td>x</td><td>74</td><td>75</td><td>78</td><td>72</td><td>78</td><td>77</td><td>79</td><td>81</td><td>79</td><td>76</td><td>72</td><td>71</td></tr><tr><td>y</td><td>47</td><td>44</td><td>40</td><td>48</td><td>49</td><td>45</td><td>46</td><td>42</td><td>42</td><td>39</td><td>46</td><td>40</td></tr></table> | x | 74 | 75 | 78 | 72 | 78 | 77 | 79 | 81 | 79 | 76 | 72 | 71 | y | 47 | 44 | 40 | 48 | 49 | 45 | 46 | 42 | 42 | 39 | 46 | 40 | |
| x | 74 | 75 | 78 | 72 | 78 | 77 | 79 | 81 | 79 | 76 | 72 | 71 | | | | | | | | | | | | | | | |
| y | 47 | 44 | 40 | 48 | 49 | 45 | 46 | 42 | 42 | 39 | 46 | 40 | | | | | | | | | | | | | | | |

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