

Please note: Answer all parts of a question at the same place. Scattered parts will not be graded. Write all assumptions and show intermediate steps.

1. M-ary Signaling [12]

Consider the 16 point M-ary signaling system defined below:

$$s(t) = \sqrt{\frac{2E}{T}} a_i \sin(2\pi f_c t) + \sqrt{\frac{2E}{T}} b_i \cos(2\pi f_c t) \quad (1)$$

where a_i can take the values $\{-3, -1, 1, 3\}$ and b_i can take the values $\{-3, -1, 1, 3\}$.

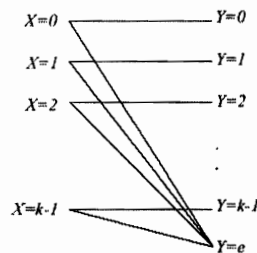
- Draw** the signal-space diagram and clearly label the axes. [2]
- Find** the average energy per symbol, E_{av} [3]
- For the above-mentioned **expression** for the average probability of **symbol error**, P_s , in the presence of AWGN with zero mean and power spectral density $N_0/2$ is given by [7]

$$P_e \approx \frac{3}{2} \operatorname{erfc} \left(\sqrt{\frac{E_{av}}{10N_0}} \right) \quad (2)$$

Is the above statement mentioned in (c) **True or False** ? **Justify** mathematically [5]

2. Mutual Information [5 + 5]

- Determine** the mutual information, $I(X;Y)$ for the channel shown below. Give your answer in terms of $H(X)$.



- Define the random variable E as follows:

$$E = 1 \text{ if } Y = e \\ = 0 \text{ otherwise}$$

Find $H(Y, E)$.

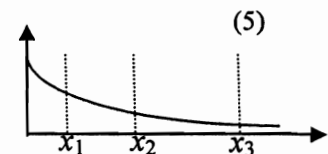
(4)

3. Entropy [8]

The input to a quantizer is a random signal having an amplitude probability density function:

$$f_X(x) = \begin{cases} ae^{-ax} & , x \geq 0 \\ 0 & , x < 0 \end{cases}$$

The signal is to be quantized to four quantizing levels as shown (yes four!).
Determine x_i , $i = 1, 2, 3$ so that the entropy at the quantizer output is maximized.



(5)



-RB