## Department of Chemical Engineering, Indian Institute of Technology Delhi CHL721: Advance Chemical Engineering Thermodynamics Semester II, 2009-2010

Closed Book & Closed Notes Date: 04/05/10

## Major Examination Time: 2 Hrs.

Marks: 35

Note:

- 1. Do not answer a question in more than one place. If the answer to a question is given at different places, only the first continuous attempt will be evaluated.
- 2. Show all the intermediate steps of the methods employed for the solution of the problems.
- 3. Supplementary answer-sheets will not be provided.
- 1. Derive the following

a. [7 Marks] Show that for grand canonical ensemble 
$$\sigma_N^2 = \left(\frac{\partial \langle N \rangle}{\partial \beta \mu}\right)_{\beta, N}$$

- b. [7 Marks] Show that for a system of uncorrelated particles  $\sigma_N^2 = \langle N \rangle$ .
- c. [4 Marks] Using the above two results derive ideal gas EOS.
- 2. [6 Marks] Derive the expression for partition function of a canonical ensemble (in terms of  $E_j$ , and  $\beta$ ) using method of maximum probable distribution and Lagrange multiplier.
- 3. [6 Marks] Derive the Gibbs entropy formula:  $dS = -k_B \sum_i P_i \ln P_i$
- 4. [5 Marks] The following isomerization reaction occurs in liquid phase:

$$A \rightarrow B$$

where A and B are miscible liquids for which:

$$\frac{G^{E}}{RT} = 0.1x_{A}x_{B}$$

if  $\Delta G_{298}^0 = -1000 J$ , what is the equilibrium composition of the mixture at 25 °C? How much error is introduced if one assumes that A and B form an ideal solution? [The reaction is at low enough pressure that painting factor correction can be ignored].