

EEL713 (Microwave Theory and circuits) Major

Nov 30, 2006

Marks : 2 + 5 + 5 + 5 + 5 + 5 + 5 + 8. Time 2 hrs.

$[\epsilon_0 = 8.8 \times 10^{-12}$, $\mu_0 = 4\pi \times 10^{-7}$ in S.I. units]

1. Under what circumstances will a lossy transmission line be non-dispersive (i.e. propagation constant is directly proportional to frequency) ?
2. Prove that if the real part of input impedance > 0 for a one-port , then $|S_{11}| < 1$ for that one-port, for any real reference impedance level.
3. A plane wave (10 GHz) traveling in air along +z, is normally incident on a dielectric ($\epsilon_r = 4$) which occupies the region $0 < z < 3.75$ mm (rest of space is air). What is the reflection coefficient (magnitude and phase) if $z=0$ is taken as the reference plane ?
4. For TE_{10} mode , in a waveguide with 'a' = 20mm, at what frequency will group velocity be half of phase velocity ? ($1/v_g = d\beta/d\omega$)
5. Sketch the E and H fields for the dominant TM mode in a dielectric slab guide with one side metal coated. Show cross-sectional as well as longitudinal planes, or use a 3-D sketch.
6. Match the impedance $Z = 20 - j 20$ ohms, to 50 ohms , using double short-circuited stub matching with the central line length being $\lambda / 6$. Give the electrical lengths of the two stubs in degrees as your answer. Smith Chart may be helpful.
7. Explain how a balanced mixer gets rid of LO AM noise.
8. Show (comparing S or ABCD matrices is the easiest way) that a series capacitor, cascaded with small equal lengths of transmission lines (choose Z_0 of these lines as the reference for all S-matrices) on either side, is equivalent to a J-inverter with small J. If the line lengths are negative, how can we interpret this ?