

## Major Exam

### Advanced Hydraulics

Max<sup>m</sup> Marks: 55

Q(1) The deposition and dredging requirements of a navigational channel in a wide river are to be studied using a movable bed model. The bed material in river is sand (Sp. Gr. of 2.65) with median size 0.4 mm. The model bed has specific gravity of 1.25.

- Determine the median diameter for model bed and the required length scale. Assume  $R_r = Y_r$
- Assuming that the dimensionless sediment transport  $q_s / U_* d_s$  is a function of  $\Psi$  from Shield's diagram, where  $q_s$  is the volumetric sediment discharge per unit width and  $U_*$  is the shear velocity, determine the sediment transport ratio  $q_{sr}$  and from the result.
- Determine also the time ratio  $t_r$  for sediment modeling.
- Determine the sediment transport ratio based on weight  $g_{sr}$
- If the model study indicates that dredging of the model channel is required every 100 hours. calculate the frequency with which the prototype channel will require dredging.

$$R_r Y_r / \sigma_r d_r X_r = 1, \quad R_r Y_r d_r^2 / X_r = 1, \quad d_r^{1/6} = R_r^{2/3} / X_r^{1/2}$$

(10 marks)

Q(2) The velocity distribution in a river is found to vary in accordance with the seventh power law  $(u/U_0) = (y/D)^{1/7}$ , where  $u$  is the velocity at height  $y$  and  $U_0$  is the velocity at the free surface.  $D$  is the flow depth. The river is 1.5 m deep and 100 m wide and the suspended sediment sample collected at 75 mm depth above the bed has a concentration of  $10 \text{ N/m}^3$ . If the surface velocity is 2 m/s, what is the sediment transport rate in N/s above the height of 75 mm.

$$c/C_a = ((D-y)/a) / (y(D-a))^{1/7}, \text{ take } Z^* = 1$$

(7 marks)

Q(3) Assuming Manning's  $n$  is the same in both a wide and a narrow reach of a river, and  $\tau_0 \gg \tau_c$ , which is probably true for moderate to high flows in such a river, at steady state, show that

$$(y_2 / y_1) = (B_1 / B_2)^a \text{ and } (S_1 / S_2) = (B_1 / B_2)^b, \text{ determine } a \text{ and } b.$$

Use Duboy's Eqn. for sediment transport  $g_b = C_s \tau_0 (\tau_0 - \tau_c)$ , where  $g_b$  is the weight discharge of sediment per unit width.

(8 marks)

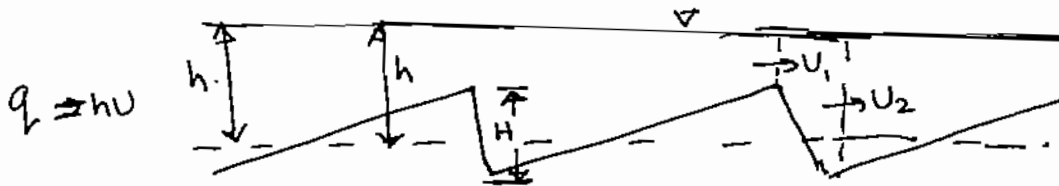
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Q(4) (a) Derive the differential equation that describes the most efficient shape of an ideal stable channel.

Why is such a channel better than a trapezoidal channel?

(b) Derive the Duboy's bed load formula  $q_b = C_s \tau_0 (\tau_0 - \tau_c)$ , and list all drawbacks of this analysis.

(c) Show that the head loss due to one bed form in Engelund's model of the divided slope approach is expressed as  $h_L = \alpha U^2 / 2g (H/h)^2$  when  $h \gg H$ , where  $h$  = mean depth of flow,  $\alpha$  = loss coefficient and  $H$  = average height of a bed form



(d) Einstein in 1950 presented the most extensive analysis on bed load transport based on fluid mechanics and probability theory. what were their important conclusions?

(12 marks)

Q(5) A 38 m high dam fails suddenly. The initial reservoir height was 35 m above the downstream channel invert and the downstream channel was filled with 0.5 m of water initially at rest.

(a) Estimate the free surface profile 7 mins after the failure.

(b) Calculate the time at which the wave will reach a point 10 km downstream of the dam and the surge front height.

Assume an infinitely long reservoir and a horizontal smooth channel.

$$(d_0/d_1)^{0.5} = (0.5U / (gd_1)^{0.5}) (1 - (1/X)) + (X)^{0.5} \text{ and } X = d_2/d_1 = 0.5((1 + (8U^2/gd_1))^{0.5} - 1)$$

$$x/t = 2((gd_0)^{0.5} - 3((gd)^{0.5})$$

(10 marks)

Q(6) Water flows in an irrigation canal at steady state,  $V = 0.9$  m/s and  $d = 1.65$  m. The canal is assumed smooth and horizontal with flow controlled by a downstream gate. At  $t=0$ , the gate is very slowly raised and the water depth upstream of the gate decreases at a rate of 5cm/min until the water depth becomes 0.85m.

Determine  $V$ ,  $c$ ,  $d$  at the gate at  $t=10$  mins.

What is the maximum extent of disturbance at 10 mins?

(8 marks)