

NOTE: Answer ALL Questions.

① (a) Define "Mach cone" and explain its significance in Compressible Fluid Flows. (4)

(b). A Converging Nozzle of throat area is supplied from a reservoir containing compressed air. The conditions in the reservoir are P_0, S_0, T_0, C_0, S_0 etc. Assuming the flow to be steady, one dimensional, isentropic, inviscid and air to be a perfect gas ($\gamma=1$) derive the expression for the exit pressure P^* at which choking takes place. Calculate the expression for the mass flow through the nozzle at this condition. (6).

② The Velocity profile and skin friction coefficient in the turbulent B.L. over a flat plate is given by,

$$u/u_\infty = (\frac{y}{\delta})^{1/7} \quad 0 \leq \frac{y}{\delta} \leq 1, \quad u/u_\infty = 1 \text{ for } y \geq \delta, \quad C_f = \frac{\tau_w}{\frac{1}{2} \rho u_\infty^2} = \frac{0.045}{(u_\infty \delta / \nu)^{1/4}}$$

Starting from Momentum Integral Equation, derive the expression for $\delta(x)$ and C_D . Assume that B.L. is turbulent from the leading edge only. Using this result, calculate the expressions for skin friction drag on a ship 100m long, having a wetted area of $400m^2$ moving through water [$\rho_{\text{water}} = 10^3 \text{ Kg/m}^3$ and ($\mu_{\text{water}} = 1 \text{ CP}$)] at a Velocity of 5 m/s. Estimate the power required to overcome this drag. What is the value of B.L. displacement thickness at the trailing edge of the ship? (10).

③ Consider the flow of water ($\rho = 10^3 \text{ Kg/m}^3, \mu = 1 \text{ CP}$) through a circular pipe of 100mm diameter having an average roughness height of $k_s = 0.05 \text{ mm}$. Calculate the maximum value of average velocity (U_{av} in m/s) so that pipe can be considered as hydraulically smooth. (Assume $f = 0.32 / Re^{1/4}$). (9).

④ (a) Explain the Variation of C_D for a flow over a sphere as Reynolds Re is varied. Identify the various flow regimes.

(b). Briefly describe any three methods by which separation can be delayed on a body. (5+5).

⑤ Define Prandtl's mixing length and explain its physical significance. Describe the Variation of mixing length in

(a) Wall turbulent flows

(b) Free Turbulent flows.

(8) ..

⑥ What is Orr-Sommerfeld Equation and explain how it can be used for predicting transition in a boundary layer. Explain the factors that affect the shape of the Neutral Stability curve. (8).

⑦ Briefly Explain the following .

(a) Reynolds Analogy for heat transfer in B.L flow over a flat plate .

(b) . Stokes stream function for axisymmetric, inviscid, incompressible, irrotational flows.

(c). Reynolds Stress Tensor and the concept of eddy viscosity. (15).

⑧ The propeller of an airplane having a diameter of 2m is moving through still air at a velocity of 100 m/s. The theoretical efficiency of the propeller is 60%. Use integral flow analysis to derive expression for thrust developed by the propeller and calculate its value. Assume air is incompressible and its density is 1.1 kg/m^3 . What is the power required to drive the propeller in kW ? (10).