

**CHL202: PROCESS SYSTEMS ANALYSIS & CONTROL**  
**MAJOR – Thursday 6 May 2010 from 8:00 – 10:00 AM in Room WS 209**

1. A process is described by the following transfer function

$$G_P(s) = \frac{4 - 16s}{(10s + 1)(3s + 1)}$$

- a) What type of process is depicted by this kind of transfer function? Make a rough sketch of the response of the system to a unit step change.  
 b) When this system is placed in a closed loop with a proportional controller, and it is known that

$$G_V(s) = \frac{2}{s + 1}, \quad G_M = 1, \text{ determine the stability limits of } K_C.$$

**(2+3+5 marks)**

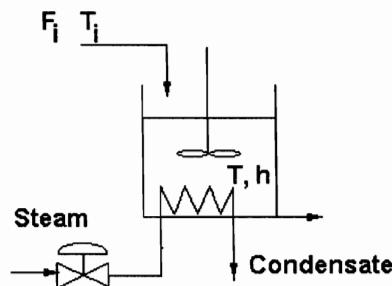
2. a) Substrate concentration is being controlled in a fed-batch bioreactor using a PI controller. The process transfer function is  $G_p = \frac{0.5}{2s + 1}$ , substrate measurement transfer function  $G_m = \frac{3}{0.2s + 1}$  and

the PI controller transfer function is  $G_C = 25 \left( 1 + \frac{1}{20s} \right)$ . Assume that the other components do not influence the closed-loop dynamics. Prepare a Table of the frequencies ranges and transfer functions, and draw the Bode Diagram.

- b) With the help of a simple sketch, describe (i) Gain Margin (ii) Phase Margin

**(6+2+2 marks)**

3. Derive the dynamic mass and energy balance of a stirred tank heater (No Reaction) shown below. Next assume that  $F_i$  does not change and that the inlet temperature  $T_i$  is the disturbance. The amount of heat  $Q$  supplied by steam is the manipulated variable. The control objective is to keep the liquid temperature,  $T$ , at the desired set point value,  $T_{SP}$ . Develop the *static* and *dynamic* feed forward control laws for temperature for this process and *compare* the results.



**(2+3+3+2 marks)**

4. a) Derive the elements of the Relative Gain Array (RGA) for a general 2X2 system.  
 b) A distillation process is described by the following transfer function

$$x_D = \frac{0.6e^{-1.1s}}{(5s + 1)(2s + 1)} R(s) - \frac{0.5e^{-1.0s}}{(6s + 1)(3s + 1)} V(s)$$

$$x_B = \frac{0.3e^{-1.3s}}{(5s + 1)(s + 1)} R(s) - \frac{0.5e^{-1.0s}}{(5s + 1)(s + 1)} V(s)$$

Where compositions of the distillate  $x_D$  and bottoms  $x_B$  product are regulated by the reflux flow  $R$  and the vapour flow  $V$ .

Determine the elements of the RGA and recommend the pairing for the control loops.

**(5+5 marks)**