

**MEL 221 MAJOR TEST NOV 2008**  
**OR PART (must be answered in a separate booklet)**  
**The method used is very important**

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Q1. Find the mean & variance of

- a) The Binomial distribution
  - b) The Exponential distribution
- by first principles.

If  $X$  is exponentially distributed with parameter ' $\mu$ ' what is the expected value & variance of  $X$  plus  $2a$  where  $a$  is a constant. What is the variance of  $2aX$ ? (6)

Q2. 
$$\begin{aligned} \max \quad & 3x + 2y \\ \text{s.t.} \quad & 2x + y \leq 100 \\ & x + y \leq 80 \\ & x \leq 40 \\ & x, y \geq 0 \end{aligned}$$

- a) Solve the above problem by the simplex & the revised simplex methods.  
The following parts must be solved using the result obtained in part (a)
- b) The profit on  $y$  drops from 2 to 1. What is the new solution?
- c) One additional constraint is added  $y \leq 40$ . What is the new solution?
- d) The constraint added is  $y \geq 40$  instead of  $\leq$ . What is the new solution?
- e) If the right hand side changes from 80 to 90 what would the new solution be. (14)

Q.3 Solve the following transportation Problem:

Shipping Costs, Supply, and Demand for Powerco

From	TO				Supply (million kwh)
	City1	City2	City3	City4	
Plant 1	Rs.08	Rs.06	Rs.10	Rs.09	35
Plant 2	Rs.09	Rs.12	Rs.13	Rs.07	50
Plant 3	Rs.14	Rs.09	Rs.16	Rs.05	40
Demand (million kwh)	45	20	30	30	

(The following part must be solved using the optimal solution already obtained)  
If the per unit cost of supplying electricity from a) plant 1 to city 1 decreases from Rs. 8 to Rs. 2 what is the new optimal solution? b) Instead, plant 1 to city 2 increases from Rs. 6 to Rs. 7 what is the new optimal solution? C) If in the original problem the supply from plant 1 & the demand to city 2 were both increased by 2 what would the new solution be? (10)