

Diary of a software engineer using categories

Angeline Aguinaldo

July 6, 2021

Berkeley Seminar, Topos Institute

Contents

- Background
- Reflections on CT
- Related to engineering
- Applications!
- ACT outreach for engineers
- Acknowledgements

About Me



**B.S. Biomedical Engineering
M.S. Electrical Engineering
Drexel University, 2017**

LEVER: stem cell segmentation, tracking, and lineage. Bioimage Lab. Drexel University.





FEMA

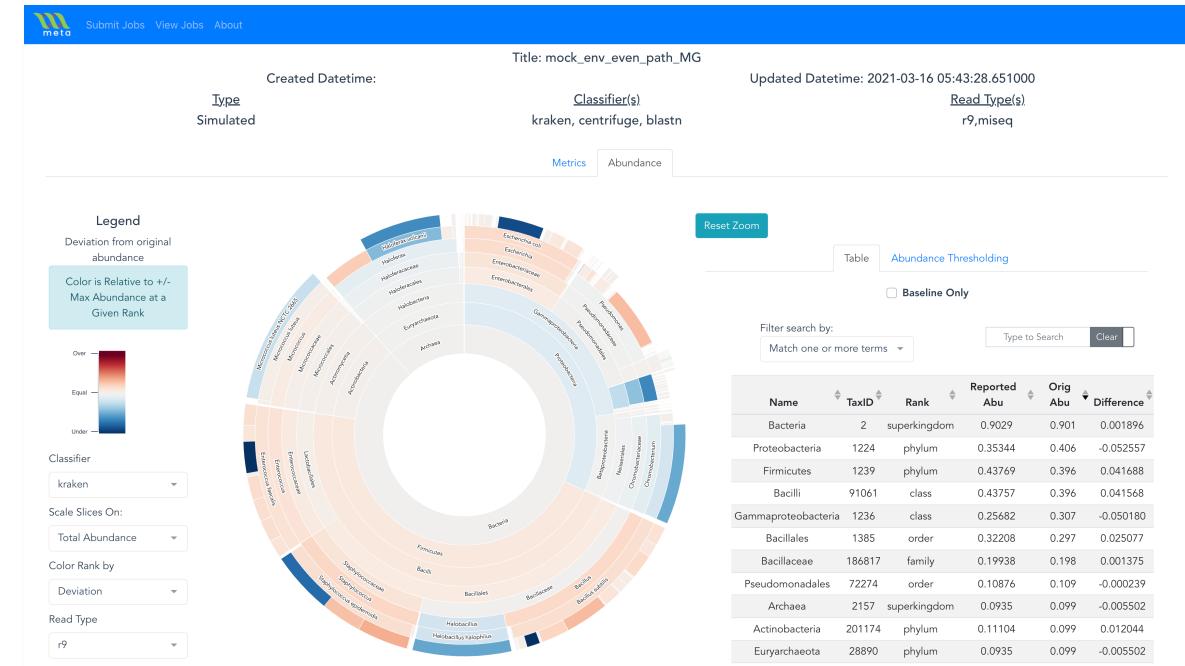


Humanitarian Assistance and Disaster Relief (HADR) Data Products for Hurricane Dorian 2019 Response



JOHNS HOPKINS
APPLIED PHYSICS LABORATORY

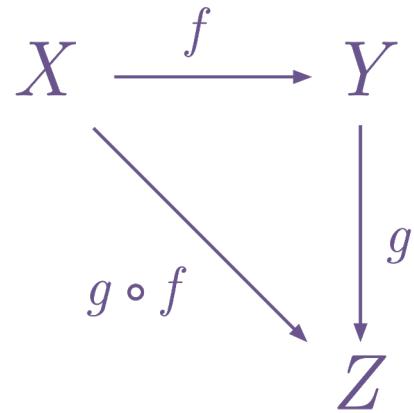
Software Engineer Project Lead



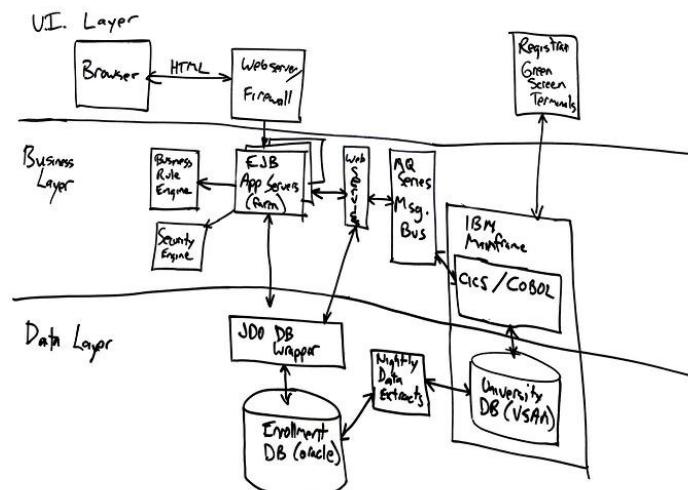
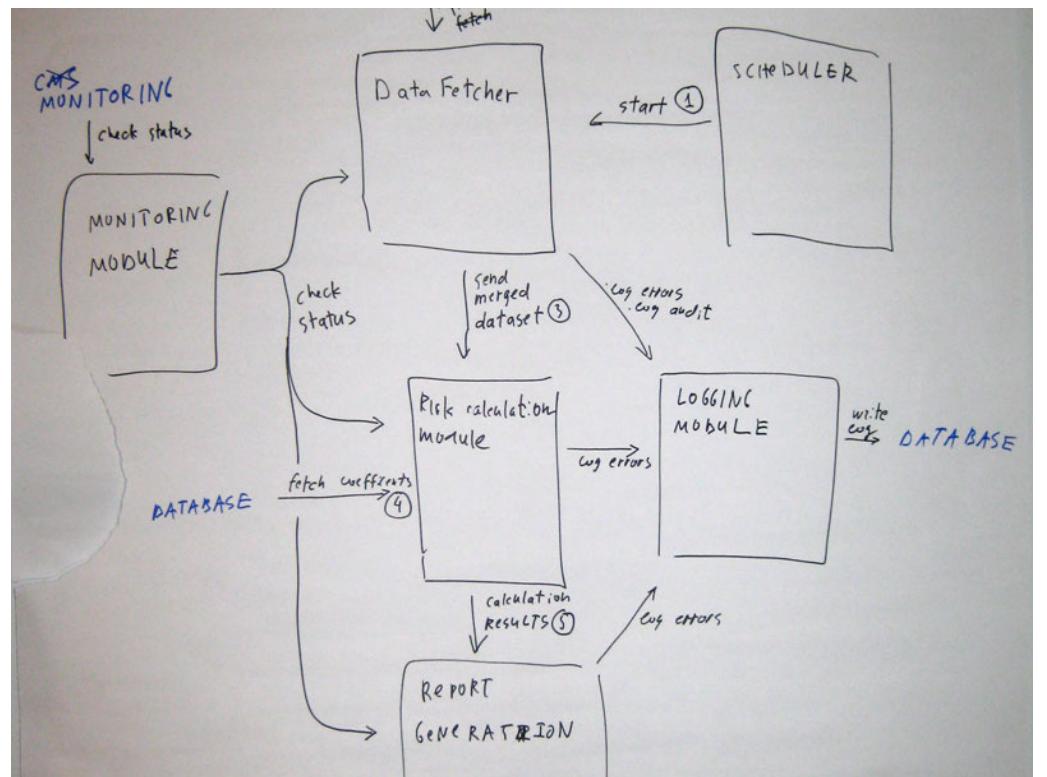
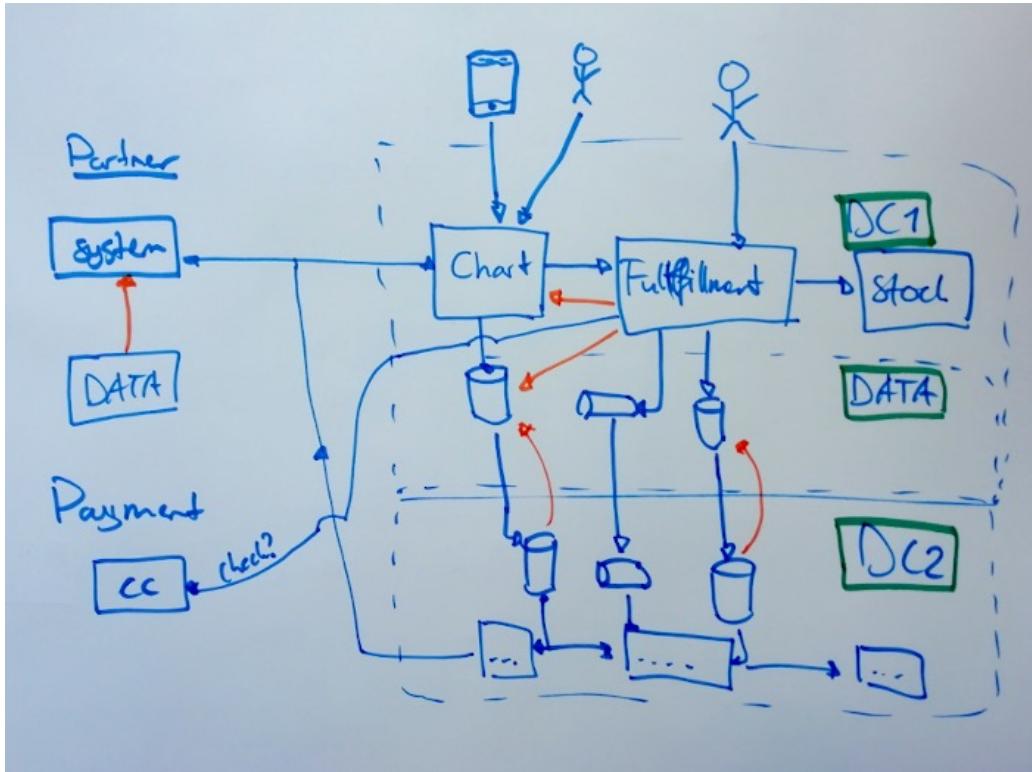
Metagenomic Evaluation, Testing, and Evaluation (META) Tool. Sunburst visualization.



3rd Year Ph.D. Student
Computer Science

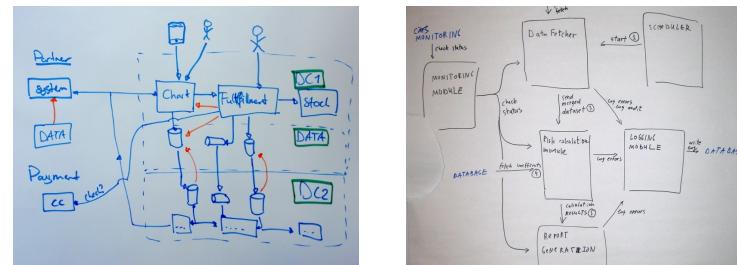


How did I get here?



Generalization

Mathematics



Engineering

Implementation

So, how has it been?

Proposition 2.3. (Yoneda lemma)

Let \mathcal{C} be a locally small category, with category of presheaves denoted $[\mathcal{C}^{\text{op}}, \text{Set}]$, according to Def. 2.1.

For $X \in [\mathcal{C}^{\text{op}}, \text{Set}]$ any presheaf, there is a canonical isomorphism

$$\text{Hom}_{[\mathcal{C}^{\text{op}}, \text{Set}]}(y(c), X) \simeq X(c)$$

between the hom-set of presheaf homomorphisms from the representable presheaf $y(c)$ to X , and the value of X at c .

This is the standard notation used mostly in pure category theory and enriched category theory. In other parts of the literature it is customary to denote the presheaf represented by c as h_c . In that case the above is often written

$$\text{Hom}(h_c, X) \simeq X(c)$$

or

$$\text{Nat}(h_c, X) \simeq X(c)$$

to emphasize that the morphisms of presheaves are natural transformations of the corresponding functors.

Proof. The proof is by chasing the element $\text{Id}_c \in C(c, c)$ around both legs of a naturality square for a natural transformation $\eta: C(-, c) \rightarrow X$ (hence a homomorphism of presheaves):

$$\begin{array}{ccc}
 C(c, c) & \xrightarrow{\eta_c} & X(c) \\
 C(f, c) \downarrow & & \downarrow_{X(f)} \\
 C(b, c) & \xrightarrow[\eta_b]{} & X(b)
 \end{array}
 \quad
 \begin{array}{ccc}
 \text{Id}_c & \mapsto & \eta_c(\text{Id}_c) \stackrel{\text{def}}{=} \xi \\
 \downarrow & & \downarrow_{X(f)} \\
 f & \mapsto & \eta_b(f)
 \end{array}$$

μ :: $a \times a \rightarrow a$
 e

η :: $() \rightarrow a$

$\mu(\mu(x,y),z) = \mu(x, \mu(y,z))$

$\mu(\eta(),x) = x$

$\mu(x, \eta()) = x$

$(a \times a) \times a$

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Category Theory 10.2: Monoid in the category of endofunctors

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Archives

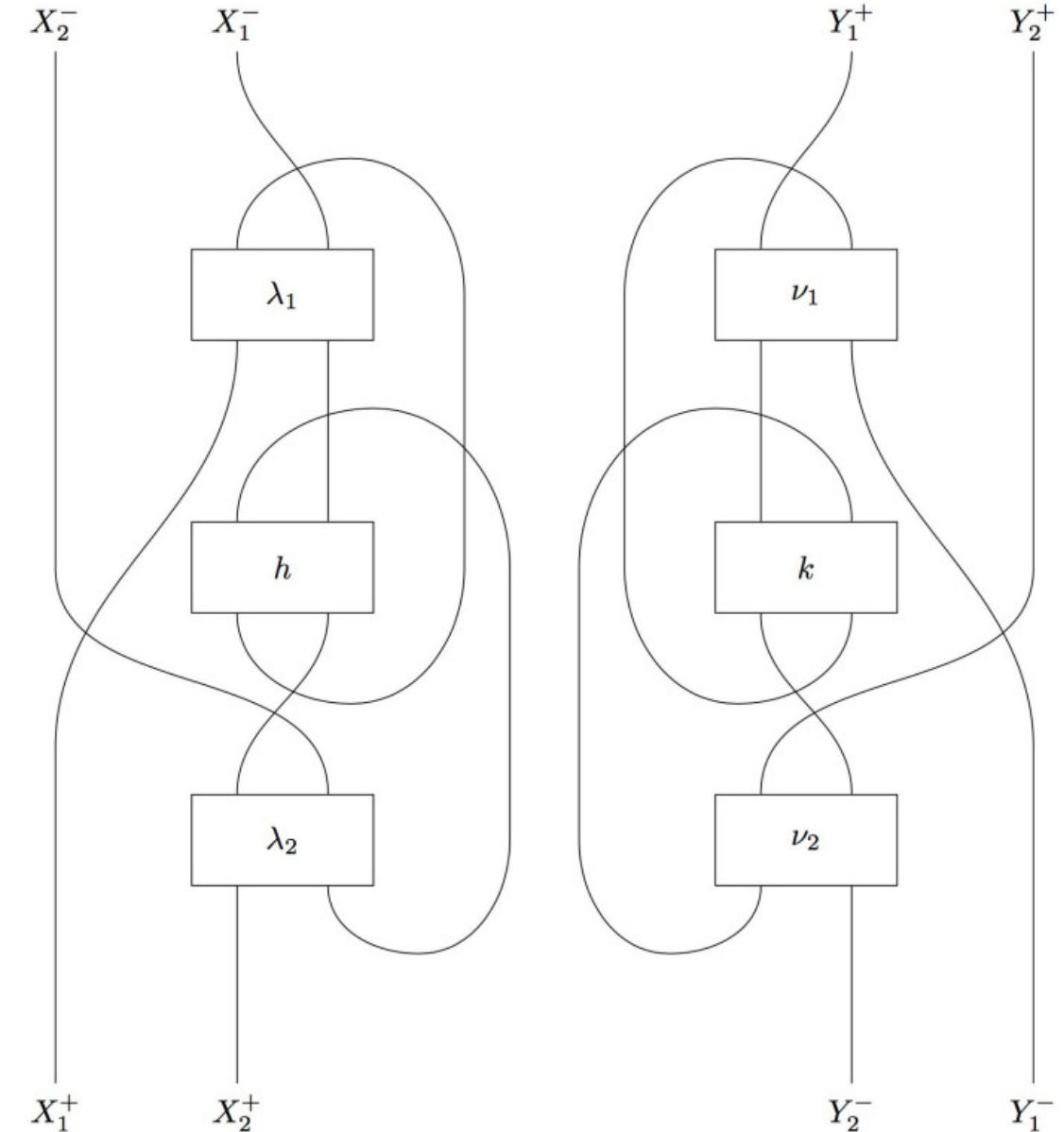
What is Category Theory Anyway?

January 17, 2017 • Category Theory

A quick browse through my [Twitter](#) or [Instagram](#) accounts, and you might guess that I've had category theory on my mind. You'd be right, too! So I have a few category-theory themed posts lined up for this semester, and to start off, I'd like to (attempt to) answer the question, *What is category theory, anyway?* for anyone who may not be familiar with the subject.

Now rather than give you a list of definitions--which are [easy enough to find](#) and may feel a bit unmotivated at first--I thought it would be nice to tell you what category theory is *in the grand scheme of (mathematical) things*. You see, it's very different than other branches of math. Rather than being another sibling lined up in the family photograph, it's more like a common gene that unites them in the first place.

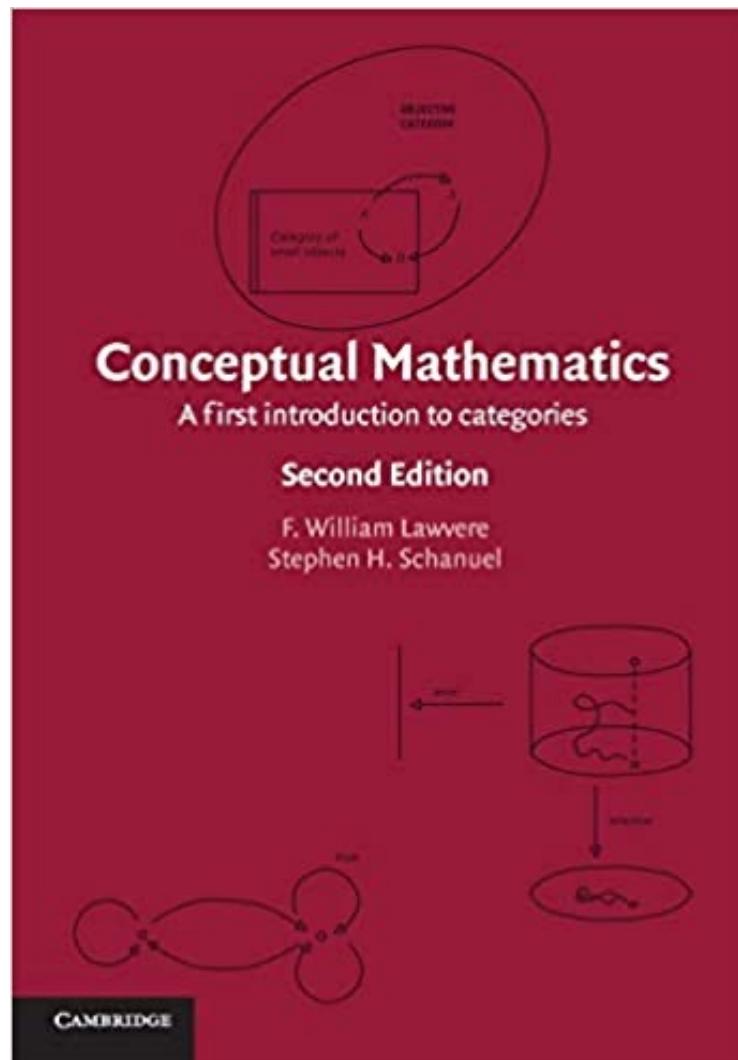
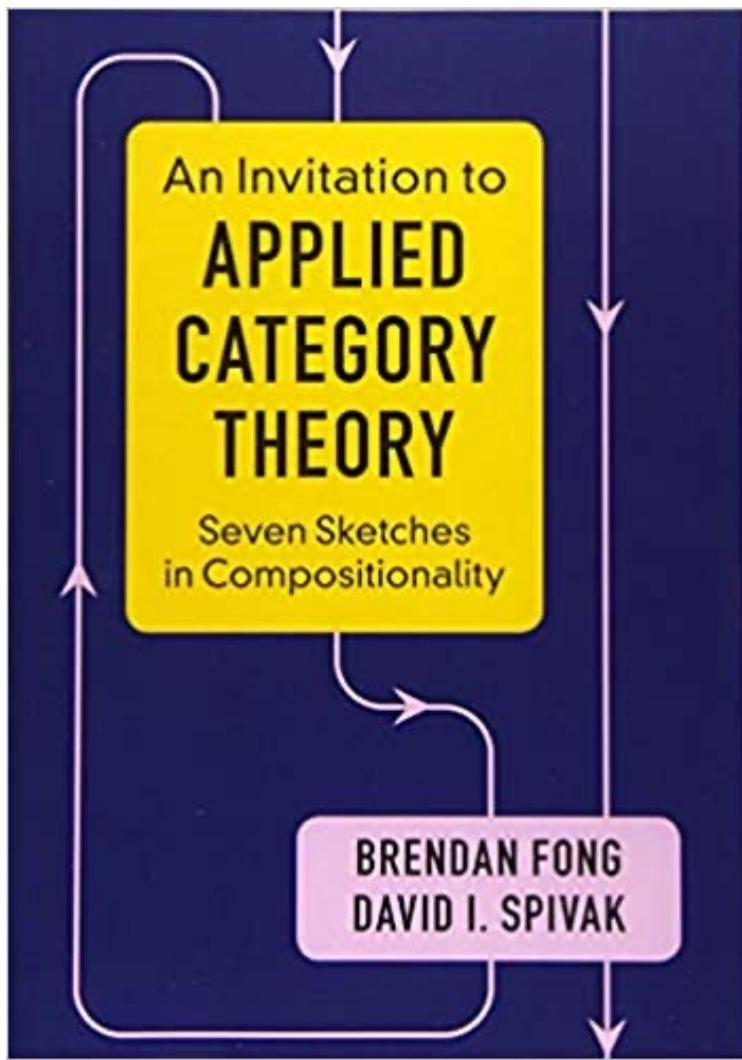
Let me explain.



Graphical Linear Algebra

17. Maths with Diagrams

The discussion over the last few episodes has now led us to the point where we have two different languages to talk about the same thing. The two languages, however, are rather different. One consists of diagrams, the other of matrices populated with natural numbers. If you already knew about matrix algebra, maybe you're asking yourself the question "What's the point of all these diagrams then? They don't tell me anything that I didn't know before. Is this guy claiming that this diagrammatic language is *better* in some way?"



Dragon: Schema Integration at Uber Scale

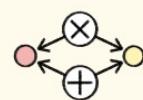
This presentation was delivered by Uber Data Platform's Joshua Shinavier for the US Semantic Technologies Symposium on March 11, 2020. An [abstract](#) is available on the conference website. Watch for an upcoming article with the same title on [Uber Engineering Blog](#).

Algebraic Property Graphs

- Uber's schema languages are overwhelmingly **algebraic**
 - ...and not only Uber's
- What the model needs
 - Primitive types, product and sum types, and also labels as aliases for other types
 - Graph features
 - Element identity
 - Taxonomy of graph elements (vertices, edges, properties, and generalized elements)
- Formalization is straightforward using **Category Theory**
 - CT is also strong on compositionality and structure-preserving mappings
- Note: **RDF Schema** was seriously considered as an alternative
 - An early version¹ of the language supported subclass property inheritance
 - "schema.org for Uber" turned out not to be a good fit

[1] <https://www.slideshare.net/joshsh/evolution-of-the-graph-schema>

Shinavier, J., & Wisnesky, R. (2019). *Algebraic property graphs*. arXiv (Vol. 1). Association for Computing Machinery.



$$\text{---} \circ \mapsto \{ ((\tau), \tau + v) \mid \tau, v \in k^{\mathbb{Z}} \} : 2 \rightarrow 1$$

$$\circ \text{---} \mapsto \{ (\text{---}, 0) \} \subseteq k^{\mathbb{Z}} : 0 \rightarrow 1$$

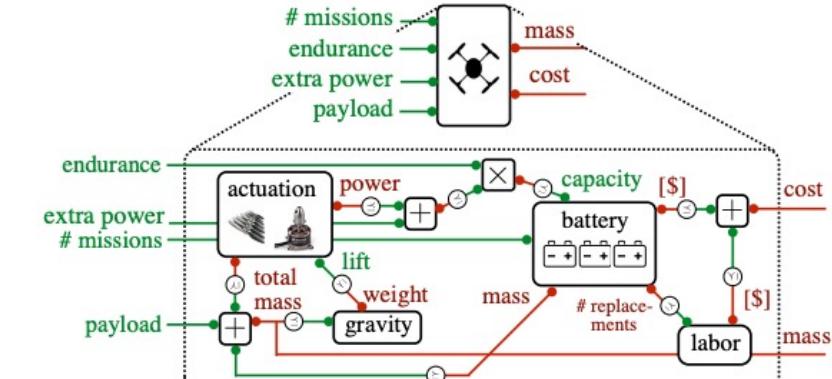
$$\text{---} \bullet \text{---} \mapsto \{ (\tau, (\tau)) \mid \tau \in k^{\mathbb{Z}} \} : 1 \rightarrow 2$$

$$\text{---} \bullet \text{---} \mapsto \{ (\tau, (\text{---})) \mid \tau \in k^{\mathbb{Z}} \} : 1 \rightarrow 0$$

$$\text{---} a \text{---} \mapsto \{ (\tau, a \cdot \tau) \mid \tau \in k^{\mathbb{Z}} \} : 1 \rightarrow 1 \quad (a \in k)$$

$$\text{---} s \text{---} \mapsto \{ (\tau, s \cdot \tau) \mid \tau \in k^{\mathbb{Z}} \} : 1 \rightarrow 1$$

Fong, B., Sobociński, P., & Rapisarda, P. (2016). A categorical approach to open and interconnected dynamical systems. *Proceedings - Symposium on Logic in Computer Science, 05-08-July(1)*



(a) Co-design diagram corresponding to (34)–(35).

```

1 mcdp {
2   provides endurance [s]
3   provides extra_payload [kg]
4   provides extra_power [W]
5   provides num_missions [R]
6   provides velocity [m/s]
7
8   requires total_cost [$]
9   requires total_mass [g]
10
11   battery = instance `Batteries
12   actuation = instance `Actuation
13
14   total_power = extra_power +
15     power required by actuation
16
17   missions_provided_by battery >= num_missions
18
19   energy = provided endurance * total_power
20   capacity_provided_by battery >= energy
21
22   total_mass = (
23     mass required by battery +
24     actuator_mass required by actuation +
25     extra_payload)
26
27   required total_mass >= total_mass
28
29   gravity = 9.81 m/s^2
30   weight = total_mass * gravity
31
32   lift_provided_by actuation >= weight
33   velocity_provided_by actuation >= velocity
34
35   replacements = maintenance required by battery
36   cost_per_replacement = 10 $
37   labor_cost = cost_per_replacement * replacements
38
39   required total_cost >= (
40     cost required by actuation +
41     cost required by battery +
42     labor_cost)
43 }
```

(b) MCDPL code for (34)–(35). The “instance” statements refer to previously defined models for batteries (Fig. 45b) and actuation (not shown).

Andrea Censi. A mathematical theory of co-design. Technical Report, Laboratory for Information and Decision Systems, MIT, September 2016. Submitted and conditionally accepted to IEEE Transactions on Robotics.

What do I like about it?

Benefits

- Organization
- Graphical syntax
- Parallel universes

Challenges

- Hard to intuit
- Hard to communicate without special terminology
- Hard to get it right

What have I learned?

Examples

Category Theory Results

Operad

Define new composition operator

Natural
Isomorphism

Show this thing is equal to this
other thing

Decorated
Cospan

Show the categorical
representation of an existing
algorithm has benefits

String Diagram

Define new graphical syntax

Natural
Transformation
/Functors

Show this thing is analogous to
this other thing

*How does it relate to
engineering?*

Engineering Problems

Security and Safety (Verification)
"Did I build the product right?"

Effectiveness (Validation)
"Did I build the right product?"

Efficiency
"Can I make this run faster or with fewer computations?"

Comprehensibility
"Can I understand what this product is doing?"

Innovation
"How can I push the boundaries of this tools in this space?"

Examples

Category Theory Results

Engineering Problems

Operad

Define new composition operator

Security and Safety (Verification)

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Natural Isomorphism

Show this thing is equal to this other thing

Effectiveness (Validation)
"Did I build the right product?"

Decorated Cospan

Show the categorical representation of an existing algorithm has benefits

Efficiency
"Can I make this run faster or with fewer computations?"

String Diagram

Define new graphical syntax

Comprehensibility
"Can I understand what this product is doing?"

Natural Transformation /Functors

Show this thing is analogous to this other thing

Innovation
"How can I push the boundaries of this tools in this space?"

*How can I apply category
theory?*

Examples	Category Theory Results	Engineering Problems	Applications
Operad	Define new composition operator	Security and Safety (Verification) <i>"Did I build the product right?"</i>	Goal-Oriented Robot Programming
Functor	Show this thing is equal to this other thing	Effectiveness (Validation) <i>"Did I build the the right product?"</i>	Modeling P-Code for Reverse Engineering
Decorated Cospan	Show there exists another map between these things	Efficiency <i>"Can I make this run faster or with fewer computations?"</i>	Analyzing Zeek Connection Log for Network Security
String Diagram	Define new graphical syntax	Comprehensibility <i>"Can I understand what this product is doing?"</i>	Visualize Classical AI Planning Solutions
Natural Transformation	Show this thing is analogous to this other thing	Innovation <i>"How can I push the boundaries of this tools in this space?"</i>	Robot Programming vs. Assembly Compiler

Steps for Applying Category Theory

1. Decide the CT tools



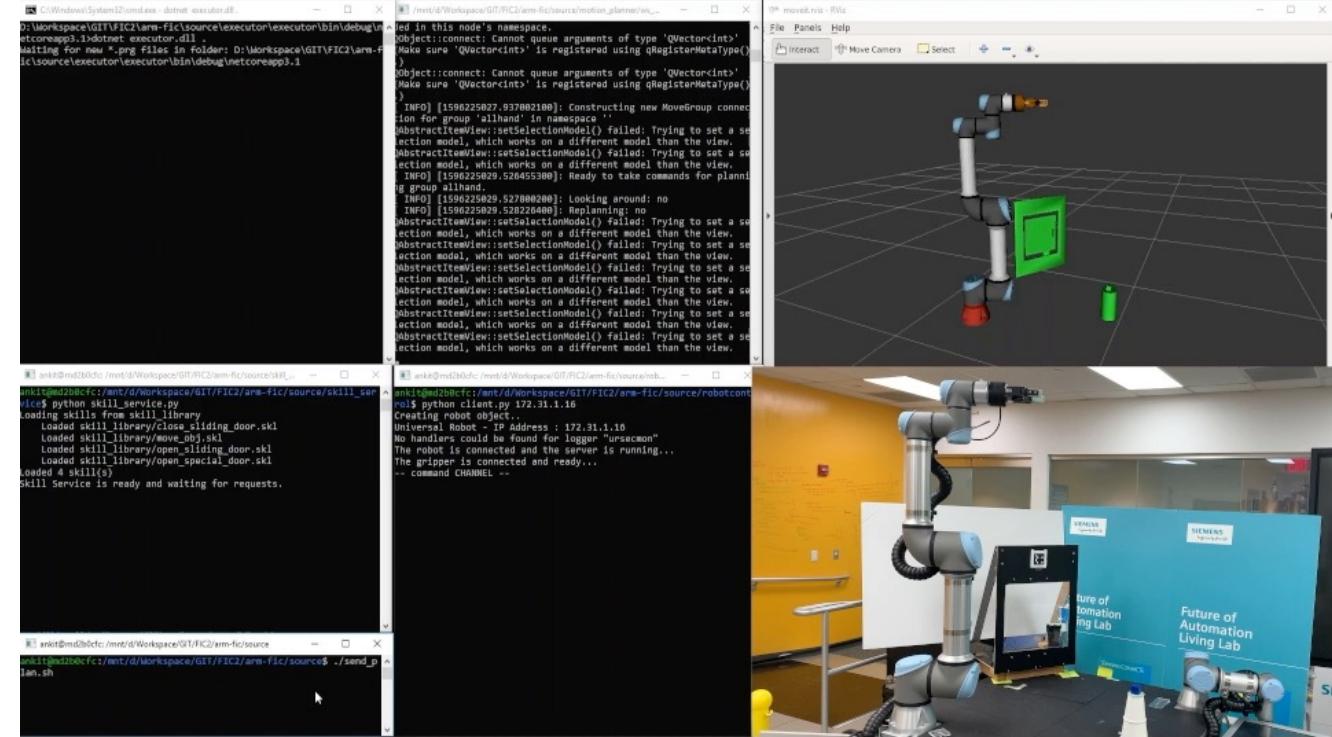
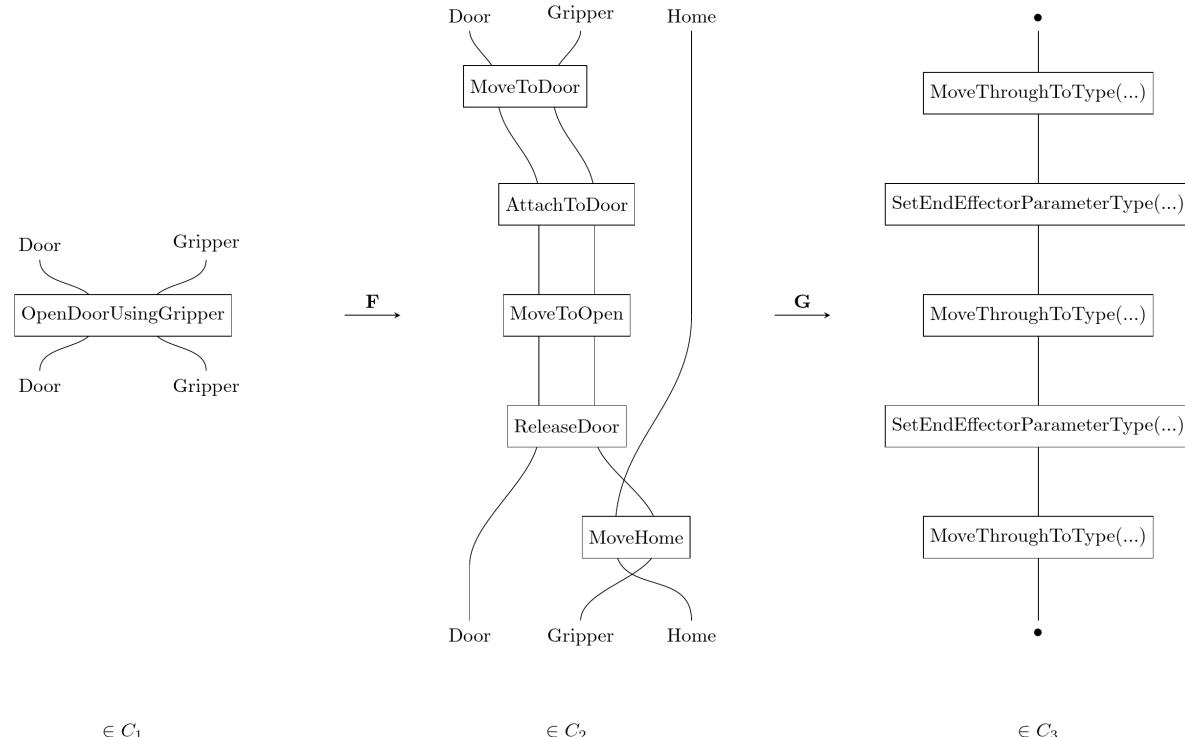
2. Align the application concepts



3. Encode the model

Goal-Oriented Robot Programming

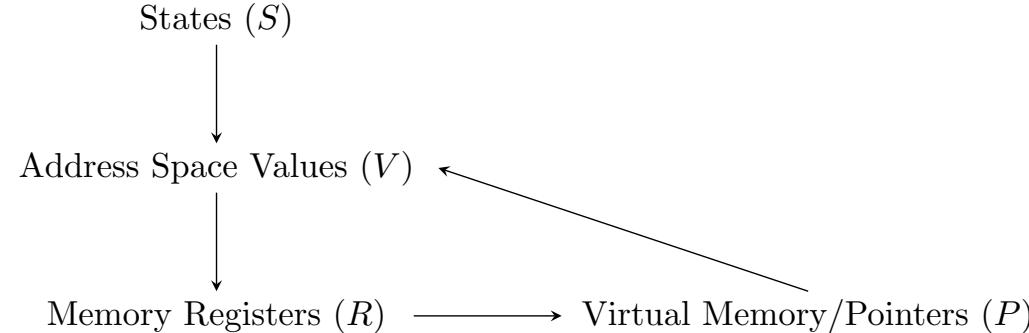
Tools: Symmetric Monoidal Categories, Monoids, Functor



A. Aguinaldo, J. Bunker, B. Pollard, A. Canedo, G. Quiros, W. Regli. *RoboCat: A category theoretic framework for robotic interoperability using goal-oriented programming*. IEEE Transactions for Automated Science and Engineering. 2021.

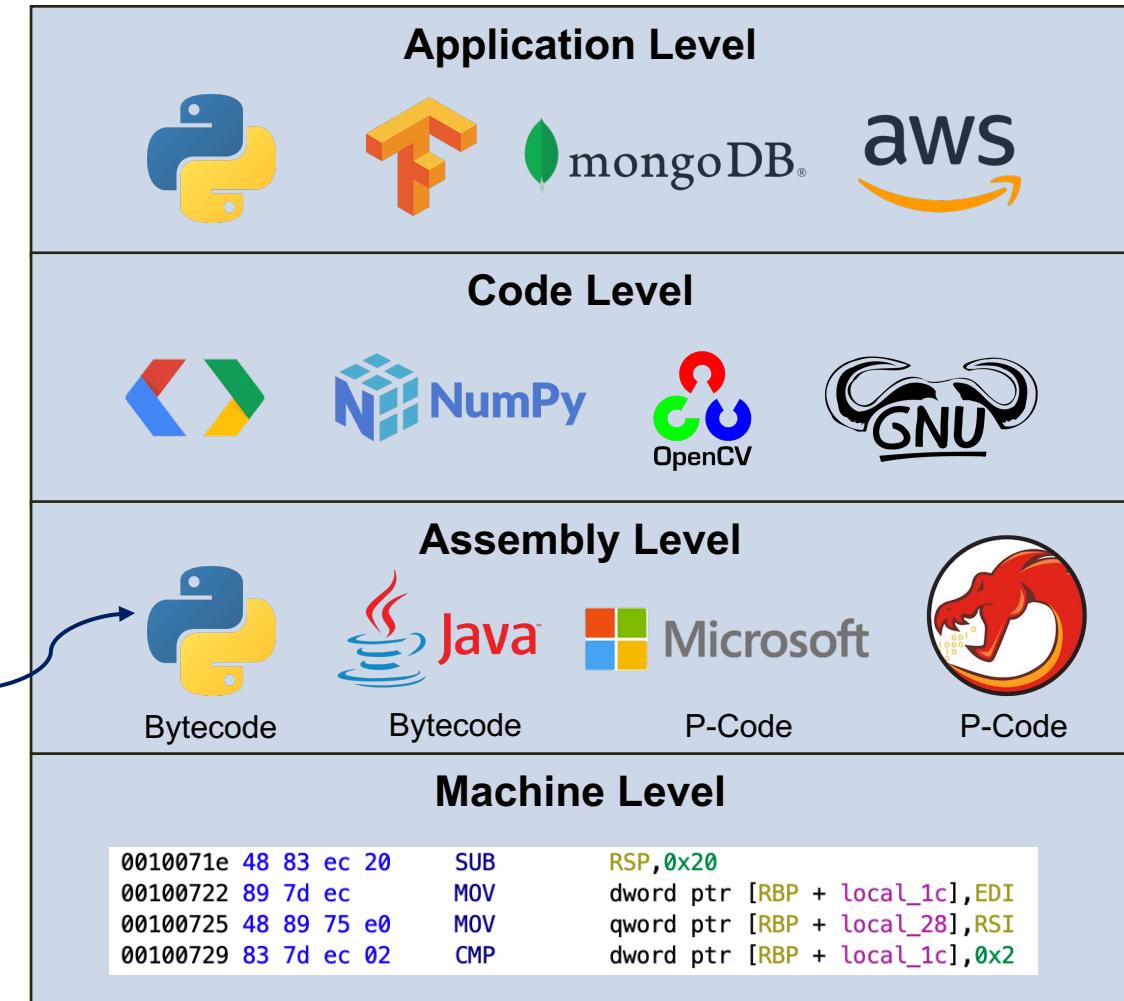
Modeling P-Code for Reverse Engineering

Tools: (In Progress)



```

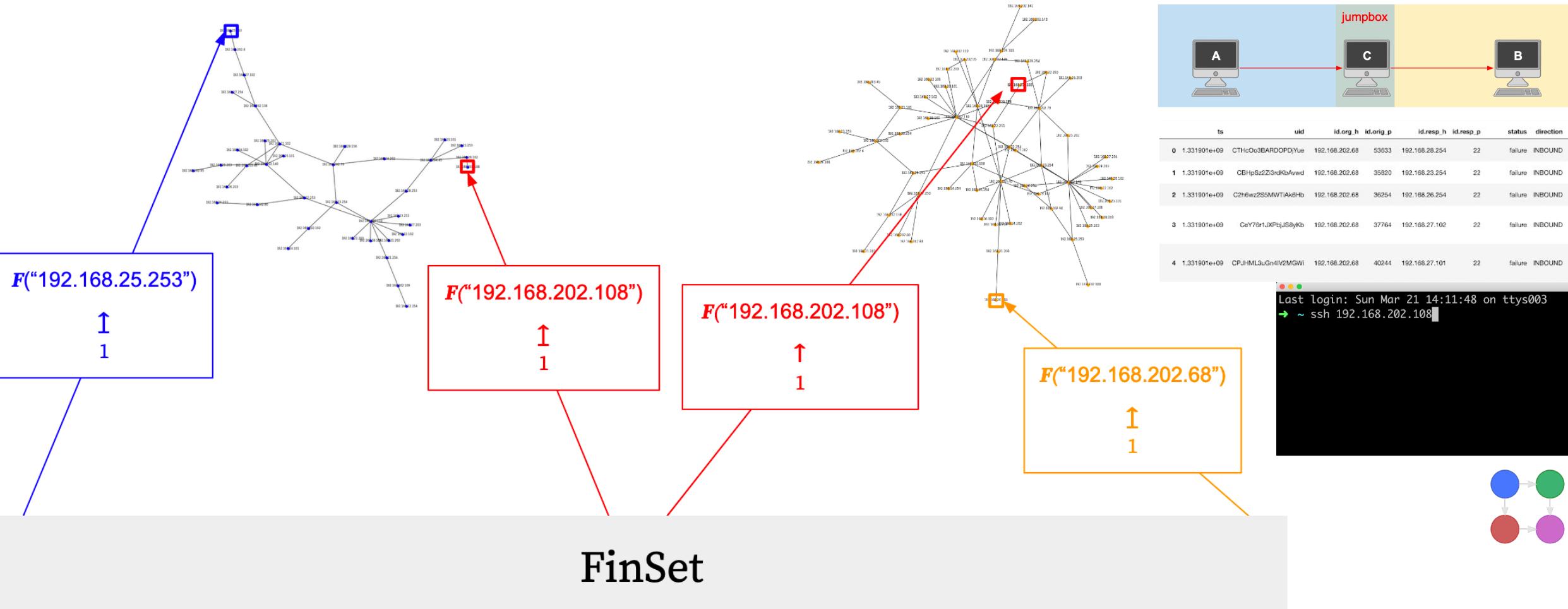
(unique, 0x10000110, 8) INT_ADD (register, 0x110, 8) , (const, 0x28, 8)
(unique, 0x1ff0, 8) LOAD (const, 0x1b1, 4) , (unique, 0x9e0, 8)
(unique, 0x9e0, 8) CAST (unique, 0x10000110, 8)
(unique, 0x2250, 1) INT_SLESS (register, 0x38, 4) , (const, 0x2, 4)
--- CBRANCH (ram, 0x100743, 1) , (unique, 0x2250, 1)
(unique, 0x1ff0, 8) LOAD (const, 0x1b1, 4) , (register, 0x30, 8)
--- CALL (ram, 0x1005d0, 8) , (unique, 0x10000a8, 8) , (unique, 0x1ff0, 8)
(register, 0x110, 8) INDIRECT (register, 0x110, 8) , (const, 0x32, 4)
(stack, 0xfffffffffffffc7, 4) INDIRECT (stack, 0xfffffffffffffc7, 4) , (const, 0x32, 4)
(stack, 0xfffffffffffffc9, 1) INDIRECT (stack, 0xfffffffffffffc9, 1) , (const, 0x32, 4)
(stack, 0xfffffffffffffc, 8) INDIRECT (stack, 0xfffffffffffffc, 8) , (const, 0x32, 4)
(stack, 0xfffffffffffffd4, 8) INDIRECT (stack, 0xfffffffffffffd4, 8) , (const, 0x32, 4)
(stack, 0xfffffffffffffdc, 8) INDIRECT (stack, 0xfffffffffffffdc, 8) , (const, 0x32, 4)
(stack, 0xfffffffffffffe4, 2) INDIRECT (stack, 0xfffffffffffffe4, 2) , (const, 0x32, 4)
(stack, 0xfffffffffffff0, 8) INDIRECT (unique, 0x1ff0, 8) , (const, 0x32, 4)
(unique, 0x10000a8, 8) COPY (const, 0x1008a4, 8)
--- BRANCH (ram, 0x1007ff, 1)
  
```



Collaboration with: G. Bakirtzis, S. Breiner, E. Subrahmanian

Analyzing Zeek Connection Log for Network Security

Tools: Decorated Cospans



Visualize Classical AI Planning Solutions

Tools: String diagrams

Domain file

```
(define (domain BLOCKS)
(:requirements :strips)
(:predicates (on ?x ?y)
(ontable ?x)
(clear ?x)
(handempty)
(holding ?x)
)

(:action pick-up
:parameters (?x)
:precondition (and (clear ?x)
(ontable ?x) (handempty))
:effect
(and (not (ontable ?x))
(not (clear ?x))
(not (handempty))
(holding ?x)))
...
)
```

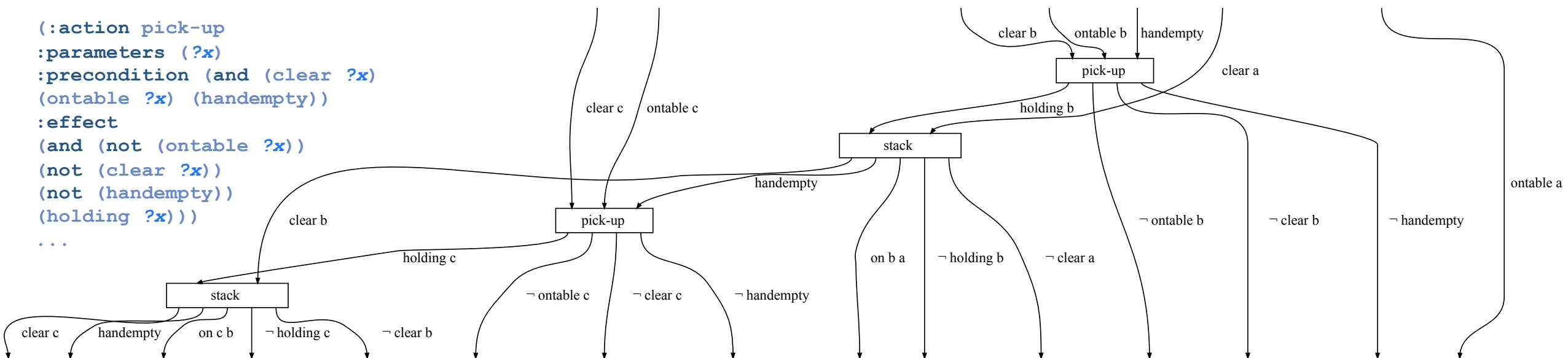
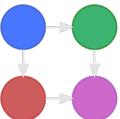
Problem file

```
(define (problem BLOCKS-3-0)
(:domain BLOCKS)
(:objects a b c)
(:init (clear c) (clear a) (clear b)
(ontable c) (ontable a) (ontable b)
(handempty))
(:goal (AND (on c b) (on b a))))
```

Solution

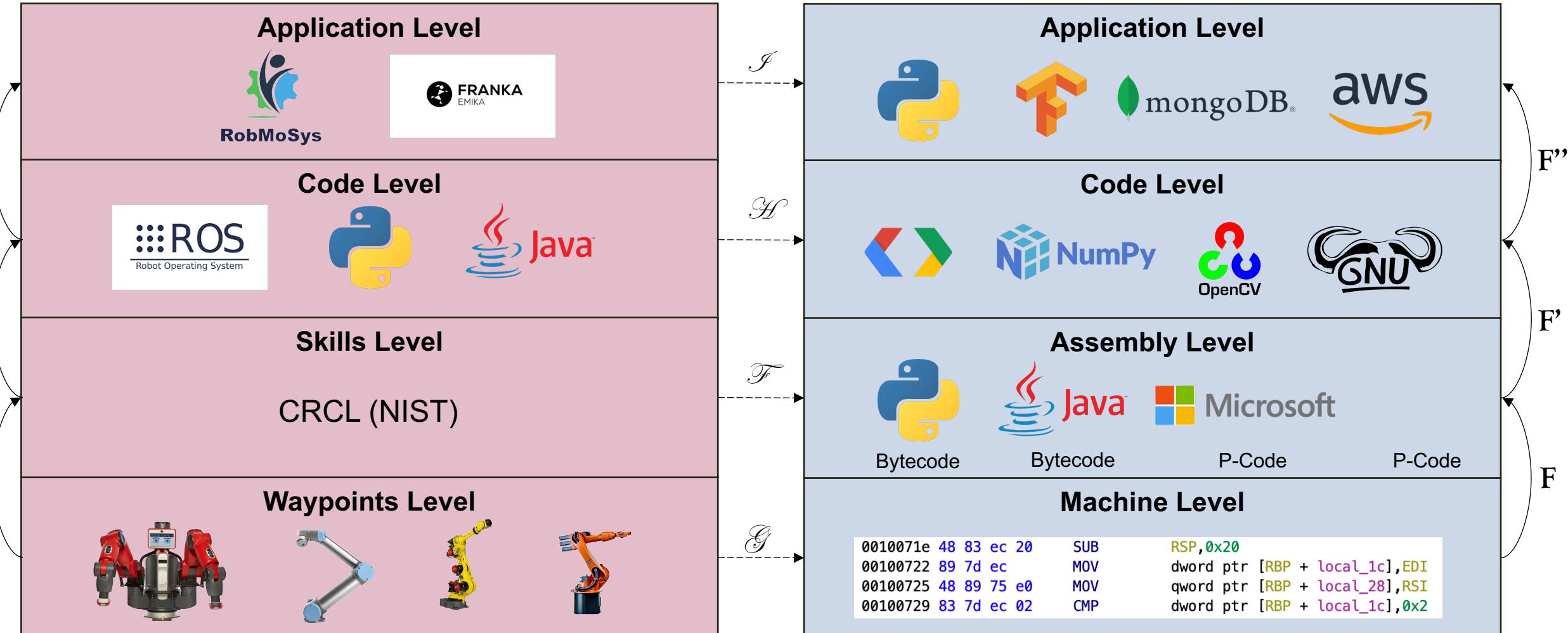
```
pick-up b
stack b a
pick-up c
stack c b
```

Angeline Aguinaldo and William Regli. *Encoding Compositionality in Classical Planning Solutions*. International Joint Conference for Artificial Intelligence (IJCAI) Generalization in Planning Workshop. 2021.



Robot Programming vs. Assembly Compiler

Tools: (In Progress)



*How can we improve ACT
outreach?*

Describe what aspects of the problem helped you decide on the tools

Categorify existing engineering abstractions

Incorporate cognitive vs. categorical translation table

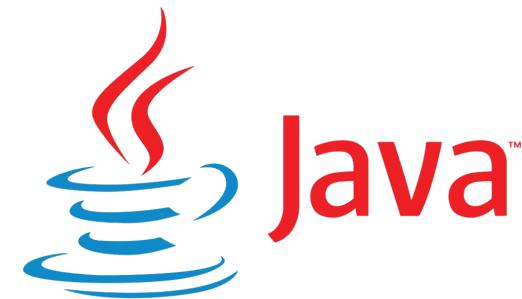
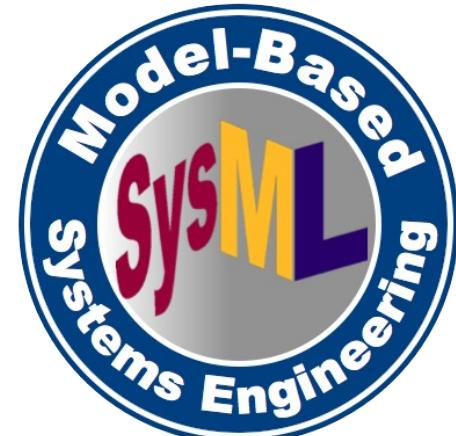
Visualize taxonomy of categories to show how they generalize or restrict

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Visualize taxonomy of categories to show how they generalize or restrict

Step	Cognitive	Categorical
1	Obtain two datasets representing SSH connections for two networks, i.e. Network 1 and Network 2	Pick two objects from the category of FinSet
2	Compute two graphs using the origin IP and response IP columns of each dataset	Define functor from \mathbf{F} : FinSet \rightarrow Graph
3	Pick jumpbox IP	Pick span that will be the common leg
4	Pick starting IP in Network 1 and target IP in Network 2	Pick input element in cospan 1 and output element in cospan 2
5	Combine rows of datasets, but add labels saying which dataset each row came from except for the jumpbox IP	Compute disjoint union of finite sets quotiented by identified element images in the apexes (i.e. pushout)
6	Compute graph of combined dataset	Compute graph for pushout using decoration functor coherence maps
7	Check if starting IP is connected to target IP in graph	Use coequalizer to compute connected components

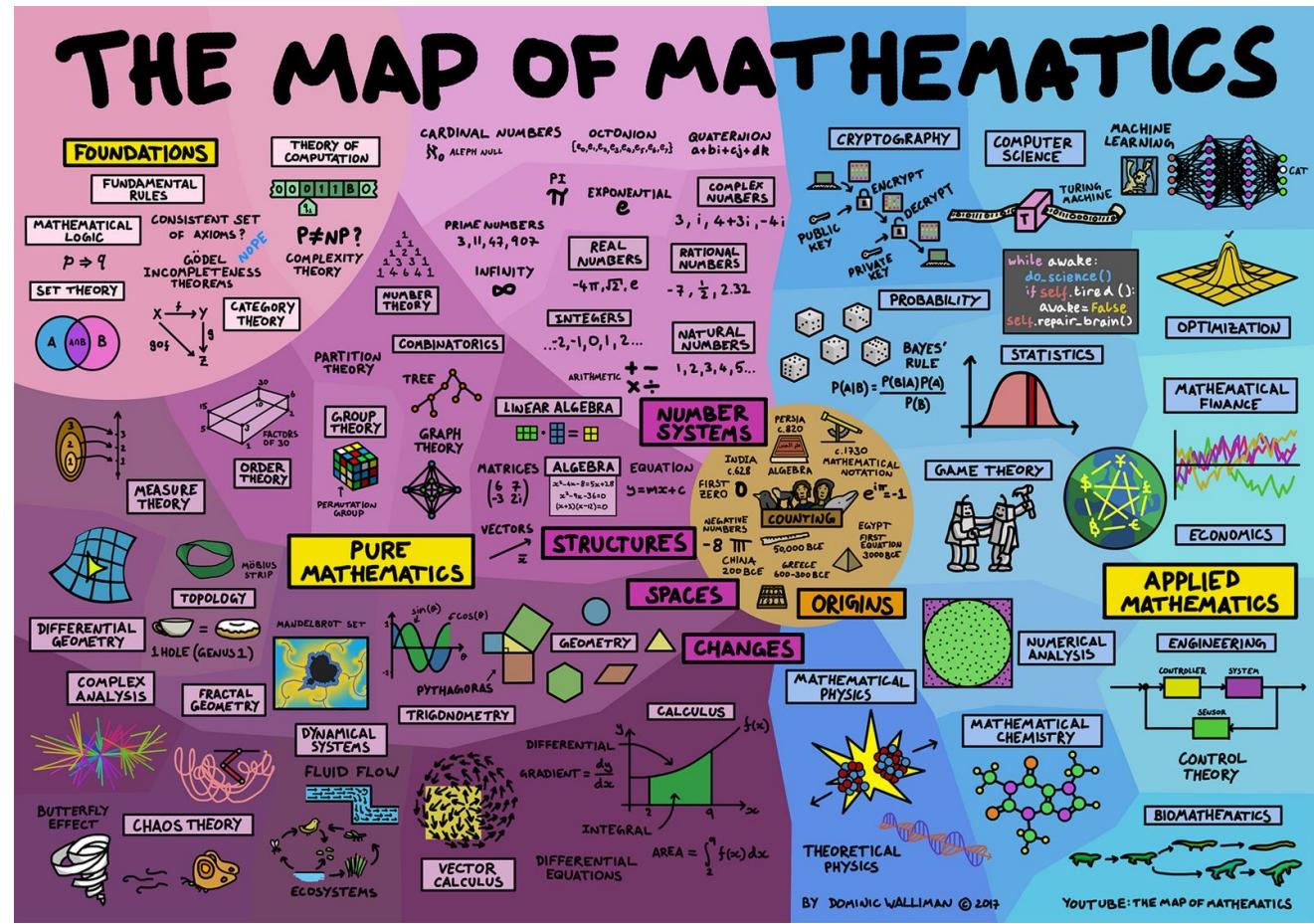
Decorated Cospans for Network Security

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Visualize taxonomy of categories to show how they generalize or restrict



Domain of Science (DoS), Youtube

Acknowledgements

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James Fairbanks

Owen Lynch

Christian Williams

David Spivak

Arquimedes Canedo

Jacob Bunker

Blake Pollard

Gustavo Quiros

William Regli

Thanks for listening!

Angeline Aguinaldo

aaguinal@umd.edu

angeline.aguinaldo@jhuapl.edu