#### W4995 Applied Machine Learning

# Imputation and Feature Selection

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# Dealing with missing values

- Missing values can be encoded in many ways
- Numpy has no standard format for it (often np.NaN)
- Sometimes: 999, ???, ?, np.inf, "N/A", "Unknown" ...
- Not discussing "missing output" that's semi-supervised learning.
- Add feature that encodes that data was missing!
- Often missingness is informative!

# Imputation methods

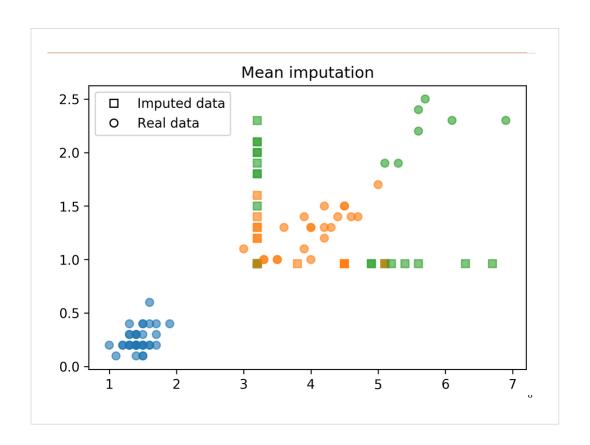
- Mean / median
- KNN
- Model-driven
- Iterative

from sklearn.linear\_model import LogisticRegressionCV
from sklearn.model\_selection import train\_test\_split, cross\_val\_score
X\_train, X\_test, y\_train, y\_test = train\_test\_split(X\_, y, stratify=y, random\_state=0)

nan\_columns = np.any(np.isnan(X\_train), axis=0)
X\_drop\_columns = X\_train[:, -nan\_columns]
scores = cross\_val\_score(LogisticRegressionCV(cv=5), X\_drop\_columns, y\_train, cv=10)
np.mean(scores)

0.77166666666666672

## Mean and Median



```
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler

nan_columns = np.any(np.isnan(X_train), axis=0)
X_drop_columns = X_train[:, ~nan_columns]
logreg = make_pipeline(StandardScaler(), LogisticRegression())
scores = cross_val_score(logreg, X_drop_columns, y_train, cv=10)
np.mean(scores)
```

#### 0.79388888888888887

```
mean_pipe = make_pipeline(Imputer(), StandardScaler(), LogisticRegression())
scores = cross_val_score(mean_pipe, X_train, y_train, cv=10)
np.mean(scores)
```

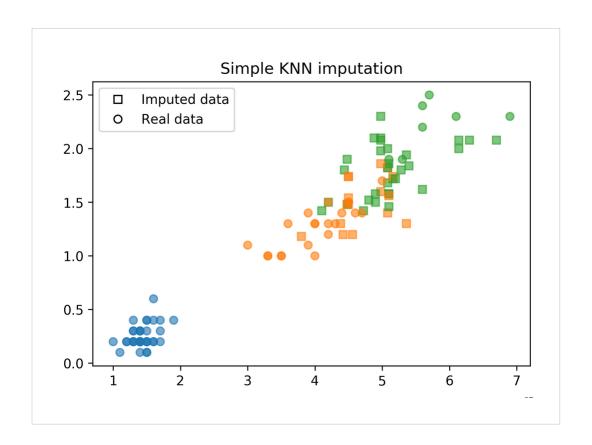
#### 0.7288888888888892

## KNN imputation

- Find k nearest neighbors that have non-missing values.
- Fill in all missing values using the average of the neighbors.
- Different strategies possible for finding neighbors that have missing values.
- Tricky if there is no feature that is always non-missing.
- PR in scikit-learn: https://github.com/scikit-learn/scikit-learn/pull/4844

## KNN imputation

```
\textbf{from} \  \, \textbf{sklearn.neighbors} \  \, \textbf{\underline{import}} \  \, \textbf{KNeighborsRegressor}
# imput feature 2 with KNN
feature2_missing = np.isnan(X_train[:, 2])
knn_feature2 = KNeighborsRegressor().fit(X_train[~feature2_missing, :2],
                                                   X_train[~feature2_missing, 2])
X train knn2 = X train.copy()
X train knn2[feature2 missing, 2] = knn feature2.predict(X train[feature2 missing, :2])
# impute feature 3 with KNN
feature3 missing = np.isnan(X_train[:, 3])
knn_feature3 = KNeighborsRegressor().fit(X_train[~feature3_missing, :2],
                                                    X train[~feature3 missing, 3])
X_train_knn3 = X_train_knn2.copy()
X_train_knn3[feature3_missing, 3] = knn_feature3.predict(X_train[feature3_missing, :2])
An efficient implementation would find nearest neighbors only once!
This approach is quite naive as is requires the first two features to always be present!
# this is cheating because I'm not using a pipeline
# we would need to write a transformer that does the imputation
scores = cross_val_score(logreg, X_train_knn3, y_train, cv=10)
np.mean(scores)
                                                                                                            11
0.855000000000000000
```



# Model-Driven Imputation

- Train regression model for missing values
- Possibly iterate: retrain after filling in
- Very flexible!

## Model-driven Imputation w RF

```
fr = RandomForestRegressor(n_estimators=100)
for i in range(10):
    last = X_imputed.copy()
    # imput feature 2 with rf

    rf.fit(X_imputed[~feature2_missing][:, inds_not_2], X_train[~feature2_missing, 2])

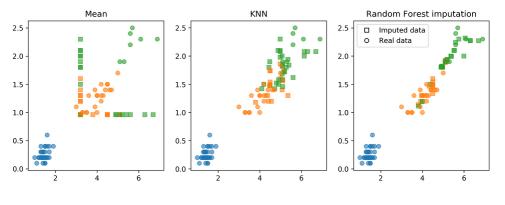
    X_imputed[feature2_missing, 2] = rf.predict(X_imputed[feature2_missing][:, inds_not_2])
# impute feature 3 with rf

    rf.fit(X_imputed[~feature3_missing][:, inds_not_3], X_train[~feature3_missing, 3])
    X_imputed[feature3_missing, 3] = rf.predict(X_imputed[feature3_missing][:, inds_not_3])
# this would make more sense if we scaled the data beforehand
if (np.linalg.norm(last - X_imputed)) < .5:
        break</pre>
```

```
scores = cross_val_score(logreg, X_imputed, y_train, cv=10)
np.mean(scores)
```

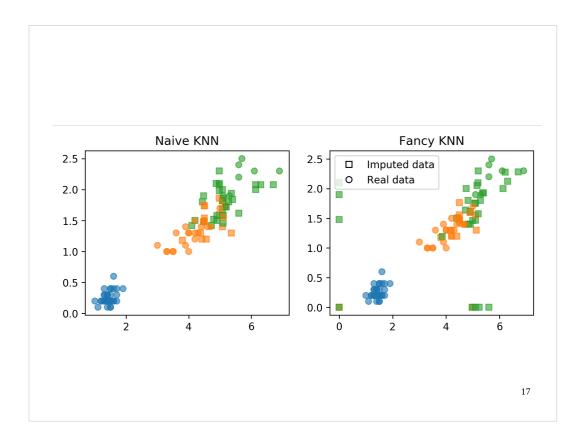
0.8533333333333333

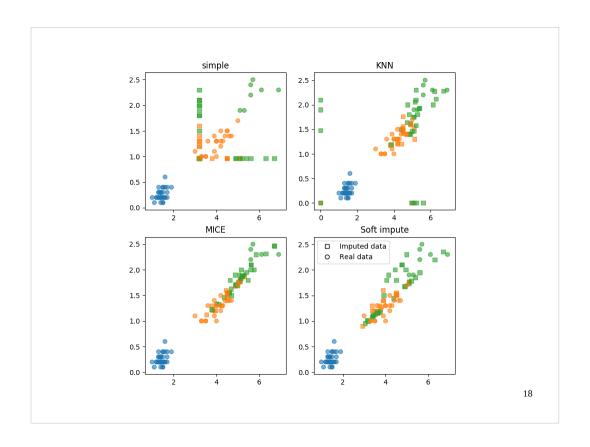




## Fanyimpute

- pip install fancyimpute
- Has many methods but no fit-transform paradigm
- MICE is iterative and works well often
- Try different things in practice, MICE might be best



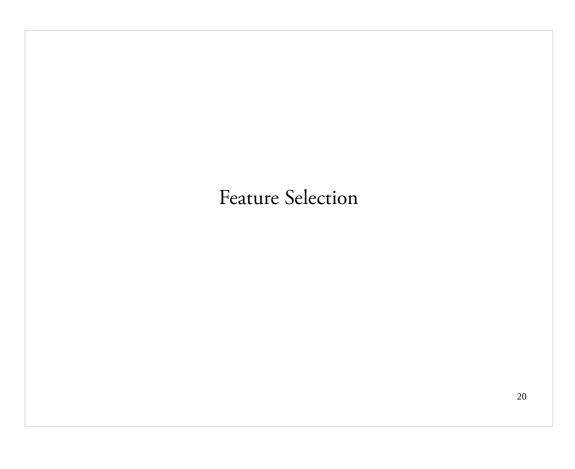


# Applying fancyimpute

X\_train\_fancy\_mice = fancyimpute.MICE(verbose=0).complete(X\_train)
scores = cross\_val\_score(logreg, X\_imputed, y\_train, cv=10)
scores.mean()

0.84833333333333327

Again, cheating with the imputation :(
This is allowed for the homework because the current tools make it hard to do the right thing.



# Why Select Features?

- Avoid overfitting
- Faster prediction and training
- Less storage for model and dataset

# Types of Feature Selection

- Unsupervised vs Supervised
- Univariate vs Multivariate
- Model-based or not

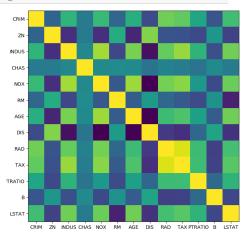
# Unsupervised feature selection

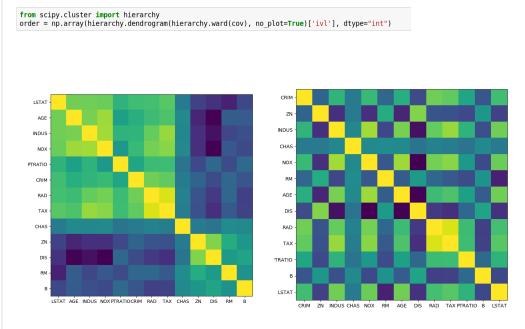
- May discard important information
- Variance-based: 0 variance or few unique values
- Covariance-based: remove correlated features
- PCA: remove linear subspaces

## Covariance

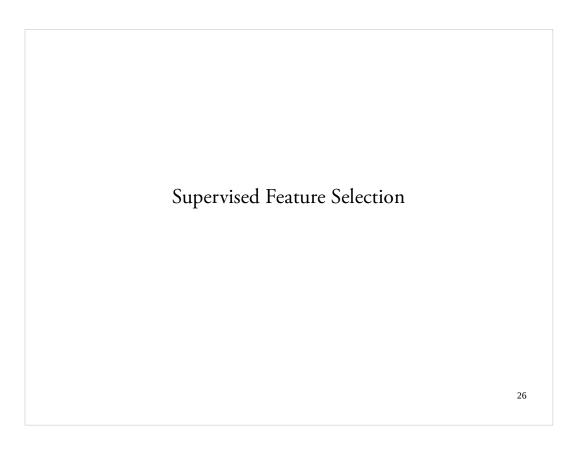
boston = load\_boston()
X, y = boston.data, boston.target
X\_train, X\_test, y\_train, y\_test = train\_test\_split(X, y, random\_state=0)

from sklearn.preprocessing import scale
X\_train\_scaled = scale(X\_train)
cov = np.cov(X\_train\_scaled, rowvar=False)





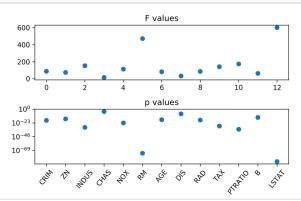
Can use this to iteratively remove most correlated pairs. Beware: might discard important information!



## Simple univariate selection

- Pick statistic, check p-values!
- f\_regression, f\_classif, chi2 in scikit-learn

from sklearn.feature\_selection import f\_regression
f\_values, p\_values = f\_regression(X, y)



```
from sklearn.feature_selection import SelectKBest, SelectPercentile, SelectFpr
from sklearn.linear_model import RidgeCV

select = SelectKBest(k=2, score_func=f_regression)
select.fit(X_train, y_train)
print(X_train.shape)
print(select.transform(X_train).shape)

(379, 13)
(379, 2)

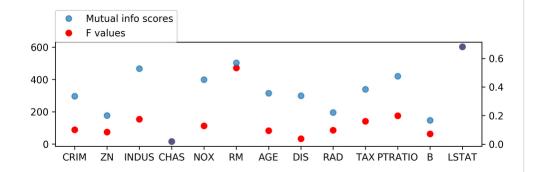
all_features = make_pipeline(StandardScaler(), RidgeCV())
select_2 = make_pipeline(StandardScaler(), SelectKBest(k=2, score_func=f_regression), RidgeCV())

np.mean(cross_val_score(all_features, X_train, y_train))
0.70430367076024736

np.mean(cross_val_score(select_2, X_train, y_train))
0.63293351088220251
```

## Mutual Information

from sklearn.feature\_selection import mutual\_info\_regression
scores = mutual\_info\_regression(X\_train, y\_train, discrete\_features=[3])



Mutual information (as implemented here) is also univariate, but doesn't assume a linear model (like the F statistics do) Can be used with SelectKBest etc

## Model-Based Feature selection

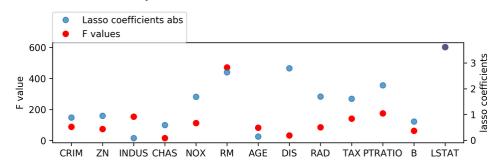
- Get best fit for a particular model
- Ideally: exhaustive search over all possible combinations
- Exhaustive is infeasible (and has multiple testing issues)
- Use heuristics in practice.

# Model based (single fit)

- Build a model, select features most important to model.
- Lasso, other linear models, tree-based models
- Multivariate linear models assume linear relation

```
from sklearn.linear_model import LassoCV
X_train_scaled = scale(X_train)
lasso = LassoCV().fit(X_train_scaled, y_train)
print(lasso.coef_)
```

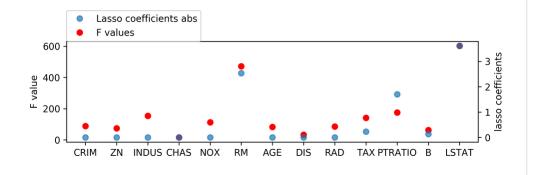
[-0.881 0.951 -0.082 0.59 -1.69 2.639 -0.146 -2.796 1.695 -1.614 -2.133 0.729 -3.615]





```
from sklearn.linear_model import Lasso
X_train_scaled = scale(X_train)
lasso = Lasso().fit(X_train_scaled, y_train)
print(lasso.coef_)
```

[-0. 0. -0. 0. -0. 2.529 -0. -0. -0. -0.228 -1.701 0.132 -3.606]



#### SelectFromModel

```
from sklearn.feature_selection import SelectFromModel
select_lassocv = SelectFromModel(LassoCV(), threshold="median")
select_lassocv.fit(X_train, y_train)
print(select_lassocv.transform(X_train).shape)
```

(379, 7)

pipe\_lassocv = make\_pipeline(StandardScaler(), select\_lassocv, RidgeCV())
np.mean(cross\_val\_score(pipe\_lassocv, X\_train, y\_train))

0.69547599764583534

np.mean(cross\_val\_score(all\_features, X\_train, y\_train))

0.70430367076024736

# could grid-search alpha in lasso
select\_lasso = SelectFromModel(Lasso())
pipe\_lasso = make\_pipeline(StandardScaler(), select\_lasso, RidgeCV())
np.mean(cross\_val\_score(pipe\_lasso, X\_train, y\_train))

0.66651484975652764

## Iterative Model-Based Selection

- Fit model, find least important feature, remove, iterate.
- Or: Start with single feature, find most important feature, add, iterate.

## Recursive Feature Elimination

- Uses feature importances / coefficients, similar to "SelectFromModel"
- Iteratively removes features (one by one or in groups)
- Runtime:

```
(n_features - n_feature_to_keep) / stepsize
```

```
from sklearn.linear_model import LinearRegression
from sklearn.feature_selection import RFE

# create ranking among all features by selecting only one
rfe = RFE(LinearRegression(), n_features_to_select=1)
rfe.fit(X train_scaled, y_train)
rfe.ranking_
array([ 9, 8, 13, 11, 5, 2, 12, 4, 7, 6, 3, 10, 1])

RFE ranking
LR coefficients

Output

O
```

## **RFECV**

• Efficient CV for n\_features\_to\_keep

```
from sklearn.linear_model import LinearRegression
from sklearn.feature_selection import RFECV

rfe = RFECV(RidgeCV())
rfe.fit(X train_scaled, y_train)
print(rfe.support_)
print(boston.feature_names[rfe.support_])

[False False False False True True False True False True]
['NOX' 'RM' 'DIS' 'PTRATIO' 'LSTAT']

pipe_rfe_ridgecv = make_pipeline(StandardScaler(), RFECV(RidgeCV()))
np.mean(cross_val_score(pipe_rfe_ridgecv, X_train, y_train, cv=10))
0.70961371790492289
```

If we want to predict with the same model as used for selection, RFECV can be used as the prediction step. Could also use RFECV as transformer and use any other model!

```
from sklearn.preprocessing import PolynomialFeatures
pipe_rfe_ridgecv = make pipeline(StandardScaler(), PolynomialFeatures(), RFECV(LinearRegression(), cv=10), RidgeCV())
np.mean(cross_val_score(pipe_rfe_ridgecv, X_train, y_train, cv=10))
```

: 0.82031507795394398

# Wrapper Methods

- Can be applied for ANY model!
- Shrink / grow feature set by greedy search
- Called Forward or Backward selection
- Complexity: n\_features \* (n\_features + 1) / 2
- Implemented in mlxtend

# SequentialFeatureSelector