

2. From re\_der I get -2.4783497330, which agrees with manually calculated derivative for all but last shown decimal. Relative errors of derivatives with various n are shown below. They differ somewhat from re\_der and WolframAlpha.

n	central diff	re_der
4	-4.5247938828e-09	4.1015831904e-11
6	-6.3249950314e-11	-5.2888637544e-09
8	-3.0310423649e-09	1.3720468244e-07
10	-2.1805600221e-07	2.9124720360e-05
12	6.7649196950e-05	2.5709034249e-03
14	-3.2697173674e-03	2.8927047776e-02

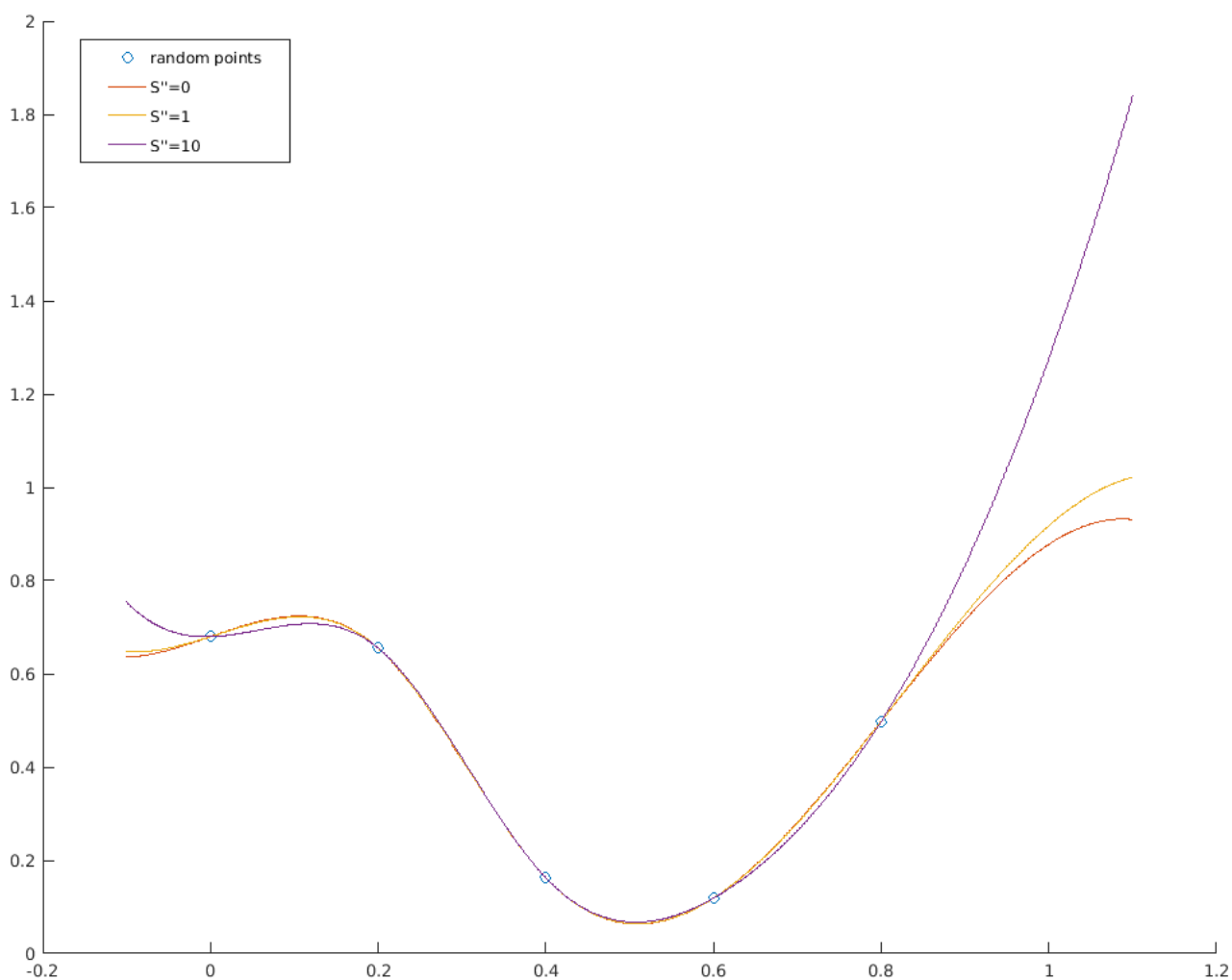
Error of re\_der seems to grow when h gets smaller from  $10^{-4}$  whereas central difference method gives best results with  $h=10^{-6}$ .

3. I generated 5 or 20 random y-values in range  $[0,1]$  with equally many evenly spaced values in range  $[0, 1[$  (spacing with which range  $[0,1]$  would have contained 11 points ie. 0.2 or 0.05). For getting the spline I used matlab function `csape` giving 'second' and wanted second derivatives like for  $S''=0$

```
p1 = csape(x, y, 'second', [0, 0])
```

`Csape` returns a polynomial, values of which I evaluated and then plotted together with the original points.

Plot with 5 points:



plot with 20 points:

