Basic Differentiation Formulas

http://www.math.wustl.edu/~freiwald/Math131/derivativetable.pdf

In the table below, u = f(x) and v = g(x) represent differentiable functions of x

Derivative of a constant Derivative of constant

multiple

Derivative of sum or difference

 $\frac{dc}{dx} = 0$ $\frac{d}{dx}(cu) = c \frac{du}{dx}$

(We could also write (cf)' = cf', and could use the "prime notion" in the other formulas as well)

$$\frac{d}{dx}(uv) = u\frac{dv}{dx} + v\frac{du}{dx}$$

 $\frac{d}{dx}(u \pm v) = \frac{du}{dx} \pm \frac{dv}{dx}$

Quotient Rule

Product Rule

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v\frac{du}{dx} - u\frac{dv}{dx}}{v^2}$$

Chain Rule

$$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$$

$$\frac{d}{dx}x^n = nx^{n-1}$$

$$\frac{d}{dx}u^n = nu^{n-1}\frac{du}{dx}$$

$$\frac{d}{dx} a^x = (\ln a) a^x$$

$$\frac{d}{dx} a^u = (\ln a) a^u \frac{du}{dx}$$

$$(\text{If } a = e)$$

$$\frac{d}{dx}e^x = e^x$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx}\log_a x = \frac{1}{(\ln a)x}$$

$$\frac{d}{dx} \log_a u = \frac{1}{(\ln a)u} \frac{du}{dx}$$

(If
$$a = e$$
)
$$\frac{d}{dx} \ln x = \frac{1}{x}$$

$$\frac{d}{dx} \ln u = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \sin u = \cos u \, \frac{du}{dx}$$

$$\frac{d}{dx}\cos x = -\sin x$$

$$\frac{d}{dx}\cos u = -\sin u \, \frac{du}{dx}$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\frac{d}{dx} \tan u = \sec^2 u \, \frac{du}{dx}$$

$$\frac{d}{dx} \cot x = -\csc^2 x$$

$$\frac{d}{dx} \cot u = -\csc^2 u \, \frac{du}{dx}$$

$$\frac{d}{dx} \sec x = \sec x \tan x$$

$$\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}$$

$$\frac{d}{dx} \csc x = -\csc x \cot x$$

$$\frac{d}{dx} \csc u = -\csc u \cot u \frac{du}{dx}$$

$$\frac{d}{dx} \sin^{-1} x =$$

$$\frac{d}{dx} \sin^{-1} u =$$

$$\frac{d}{dx} \arcsin x = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \arcsin u = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$\frac{d}{dx} \tan^{-1} x =$$

$$\frac{d}{dx} \tan^{-1} u =$$

$$\frac{d}{dx}$$
 arctan $x = \frac{1}{1+x^2}$

$$\frac{d}{dx} \arctan u = \frac{1}{1+u^2} \frac{du}{dx}$$