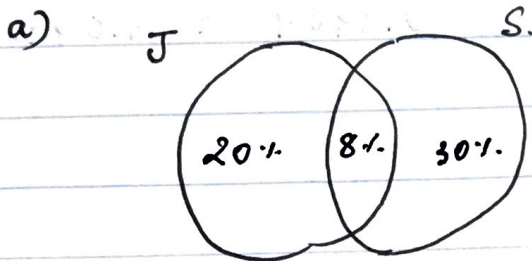


1.



	Susan at Bank	Susan not at Bank	
Terry at Bank	8%	12%	20%
Terry not at Bank	22%	58%	80%
	30%	70%	

a)  $p(J/S) = \frac{p(J \cap S)}{p(S)}$

$$= \frac{8}{30} = 0.266 = 26.67\%$$

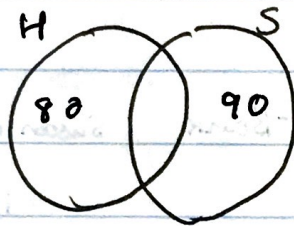
b)  $p(\text{Terry at Bank} / \text{Susan not there})$

$$p(J/S') = \frac{12}{70} = 0.1714 = 17.14\%$$

$$c) p(J \cap S) / p(J \cup S)$$

$$= \frac{8}{20+30-8} = 0.1904 = 19.04\%$$

2.



$$p(H) = 80\%$$

$$p(H \cup S) = 91$$

$$p(S) = 90\%$$

$$p(H \cup S) = p(H) + p(S) - p(H \cap S)$$

$$p(H \cap S) = p(H) + p(S) - p(H \cup S)$$

$$= 80 + 90 - 91$$

$$p(H \cap S) = 79$$

$$a) p(\text{only } H) = p(H) - p(H \cap S)$$

$$= 80 - 79$$

$$= 1\%$$

$$b) p(\text{only } S) = p(S) - p(H \cap S)$$

$$= 90 - 79$$

$$= 11\%$$

c) Probability that both won't get B

$$p(\overline{CH \cup B}) = 1 - p(CH \cup B)$$

$$= 1 - \frac{91}{100} = 0.09 = \boxed{9\%}$$

3. For two events to be independent

$$~~p(A \cap B) = p(A) \cdot p(B)~~ \quad p(C_j | S) = p(C_j)$$

$$p(C_j | S) = \frac{p(C_j \cap S)}{p(S)}$$

$$= \frac{8/100}{30/100} = \frac{8}{30} = \boxed{26.67\%}$$

Thus,  $p(C_j | S) \neq p(C_j)$

So, events are not independent

4.

$$a) p(\text{sum} = 6) = 5/36$$

$$p(\text{second die show } 5) = 6/36$$

$$= 1/6$$



$$P(\text{sum} = 6 \cap \text{second die show } 5) = \frac{1}{36}$$

For event to be independent

$$P(A \cap B) = P(A) P(B)$$

$$P(\text{sum} = 6) * P(\text{second die show } 5)$$

$$= \frac{5}{36} * \frac{1}{6}$$

$$= \frac{5}{216}$$

$$P(\text{sum} = 6 \cap \text{second die show } 5) \neq P(\text{sum} = 6) * P(\text{second die show } 5)$$

Thus, both events are not independent.

b)

$$P(\text{sum} = 7) = \frac{6}{36} = \frac{1}{6}$$

$$P(\text{first die show } 5) = \frac{6}{36} = \frac{1}{6}$$

$$p(\text{sum} = 7 \cap \text{first die show } 5) = \frac{1}{36}$$

&

$$\begin{aligned} & p(\text{sum} = 7) * p(\text{first die } 5) \\ &= \frac{1}{6} * \frac{1}{6} \\ &= \frac{1}{36} \end{aligned}$$

Thus, both events are independent.

5. chances of choosing

$$TX = 60\%$$

$$NJ = 10\%$$

$$AK = 100 - (60 + 10) = 30\%$$

Chances of finding oil

$$TX = \frac{60 \times 30}{100} = 18\% \quad AK = \frac{30 \times 20}{100} = 6\%$$

$$NJ = \frac{10 \times 10}{100} = 1\%$$

	Tx	AK	NJ	
Finding oil	18%	6%	1%	25%
Oil not found	<u>42%</u>	<u>24%</u>	<u>9%</u>	<u>75%</u>
	60%	30%	10%	100%

$$a) p(\text{Finding oil}) = 18\% + 6\% + 1\% \\ = \boxed{25\%}$$

$$b) p(\text{Drilled in Tx \& oil found})$$

$$= \frac{18\%}{25\%} = \boxed{72\%}$$

~~$$c) p(\text{Not survived}) = 1490$$~~

~~Passengers Not survived = 1490~~

~~Total Passengers = 2201~~

~~$$a) p(\text{Not survived}) = \frac{1490}{2201} = 0.6769 \\ = 67.69\%$$~~



6.

a) Passenger not survived

$$p(\text{Not survived}) = \frac{1490 - 673}{2201 - 885}$$

$$= \frac{817}{1316}$$

$$= 62.08\%$$

$$= 62.08\%$$

b) Passenger staying in first class.

$$p(\text{First class}) = \frac{325}{1316} = 24.69\%$$

$$= 24.69\%$$

c) Passenger survived & First class

$$p(S \cap F) = \frac{203}{499} = 40.68\%$$

$$= 40.68\%$$

d) For 2 event to be independent

$$p(A \cap B) = p(A) p(B)$$

$$p(S) = 100 - p(NS)$$

$$= 100 - 62.08$$

$$= 37.92\%$$

$$p(F) = 24.69\%$$

$$\begin{aligned}
 & p(CS) * p(F) \\
 &= 24.69 * 37.92 \\
 &= 9.36\%
 \end{aligned}$$

~~p(CS)~~

$$p(CS \cap F) = 40.68\%$$

$$p(CS \cap F) \neq p(CS) p(F)$$

So, the events are not independent.

e) Passenger survived, first class & child

$$p(C \text{ survived, first class \& child})$$

$$= \frac{6}{499}$$

$$= 1.2\%$$

f) Passenger survived & Adult

$$p(C \text{ survived \& adult}) = \frac{442}{499} = \underline{\underline{88.57\%}}$$



g) Passenger survived, age & staying in first class independent

$$\begin{aligned} p(\text{age passenger survived}) &= p(A/S) + p(C/S) \\ &= \frac{442}{499} + \frac{57}{499} \\ &= 1 \end{aligned}$$

$$p(\text{survived \& first class}) = 40.68\%$$

Thus,  $p(\text{age \& first class}) = 40.68\%$ .

So, events are independent.