

Supervised machine learning for text classification

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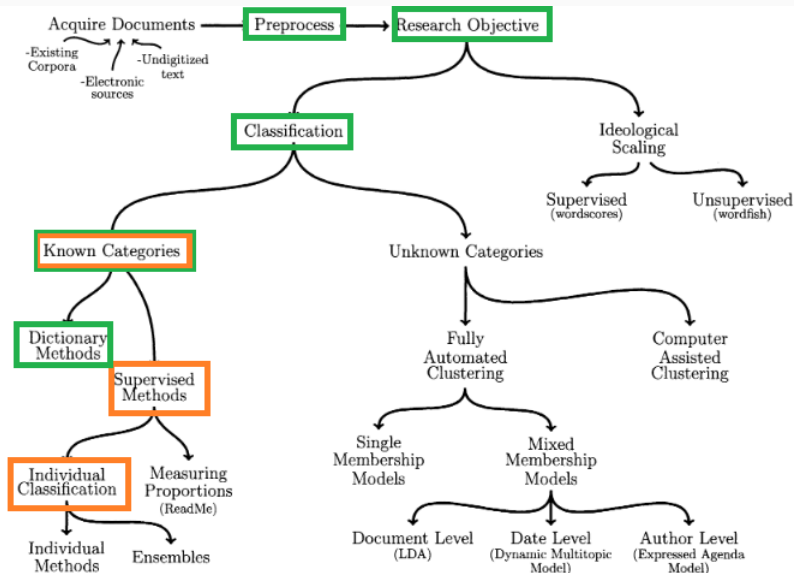
2019 October

TK PTI

For today

1. Supervised vs. unsupervised methods
2. Key concepts
3. Naive Bayes
4. SVM

Where we are



Classification

- **Objective:** classify our data into n categories.
- Our **response variable** is categorical/qualitative (eg.: gender, pass/fail, etc.)

Key general terms in the statistical learning domain

- X_n : input variables, also called: predictors, independent variables, features
- Y : output variable, also called: response, target or dependent variable

A classification problem

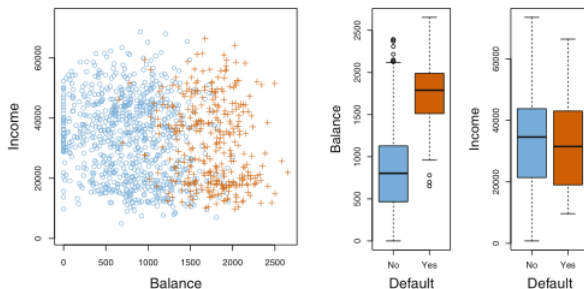


FIGURE 4.1. The **Default** data set. Left: The annual incomes and monthly credit card balances of a number of individuals. The individuals who defaulted on their credit card payments are shown in orange, and those who did not are shown in blue. Center: Boxplots of **balance** as a function of **default** status. Right: Boxplots of **income** as a function of **default** status.

James, Witten, Hastie and Tibshirani (2017), p.129

Supervised vs. unsupervised learning

Supervised learning:

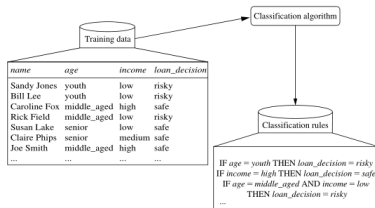
- **Classification problems** where we know the exact categories of our response variable
- We have labelled data, which "supervises" the training of the classifier
- **Having labelled data is a must!**
- Key terms:
 - **learning algorithm/classifier:** maps documents to classes (in case of text)
 - **training set:** a subset of our labelled data, which is used to train the classifier
 - **test set:** a smaller subset of our data to see how our classifier performs on 'unseen' data

Supervised vs. unsupervised learning

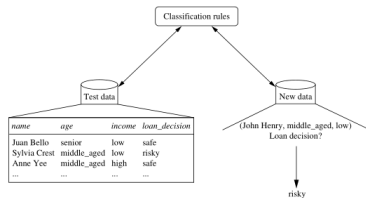
Unsupervised learning:

- **Clustering problems**, we don't know the number of categories of our response variable
- The clustering algorithm finds clusters in the data without any "supervision"
- We don't have any labelled data
- Useful in exploratory analysis or discovering clusters in our data

A classification problem



(a)



(b)

- 8.1** The data classification process: (a) *Learning*: Training data are analyzed by a classification algorithm. Here, the class label attribute is *loan_decision*, and the learned model or classifier is represented in the form of classification rules. (b) *Classification*: Test data are used to estimate the accuracy of the classification rules. If the accuracy is considered acceptable, the rules can be applied to the classification of new data tuples.

A classification problem

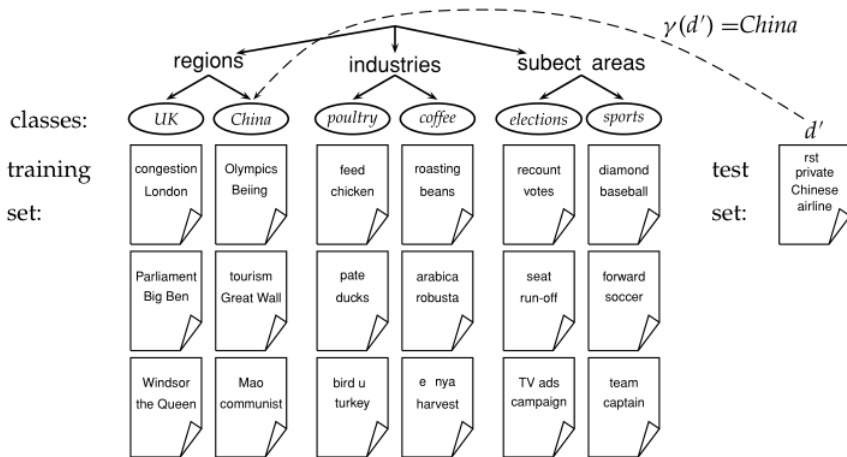


Figure 13.1 Classes, training set, and test set in text classification.

Manning, Raghavan and Schütze (2008), p.238

Assessing classifier performance: confusion matrix

		Predicted	
		cat1	cat0
Actual	cat1	TP	FN
	cat0	FP	TN

- TP for words that are class 1 and predicted in class 1
- FN for words that are class 1 and predicted in class 0
- FP for words that are class 0 and predicted in class 1
- TN for words that are class 0 and predicted in class 0

Metrics from the confusion matrix

- Accuracy = $\frac{TP+TN}{TP+TN+FP+FN}$
- Precision: $(p) = \frac{TP}{TP+FP}$
- Recall: $(r) = \frac{TP}{TP+FN}$
- Error rate: $ER = \frac{FN+FP}{TP+TN+FP+FN}$
- Specificity = $\frac{TN}{TN+FP}$

Be mindful of the trade-offs. If we want to increase recall by increasing the TP, this will likely also increase our FP, thus lowering specificity.

Also known as:

Name	Definition	Synonyms
False Pos. rate	FP/N	Type I error, $1 - \text{Specificity}$
True Pos. rate	TP/P	$1 - \text{Type II error}$, power, sensitivity, recall
Pos. Pred. value	TP/P^*	Precision, $1 - \text{false discovery proportion}$
Neg. Pred. value	TN/N^*	

James, Witten, Hastie and Tibshirani (2017), p.149

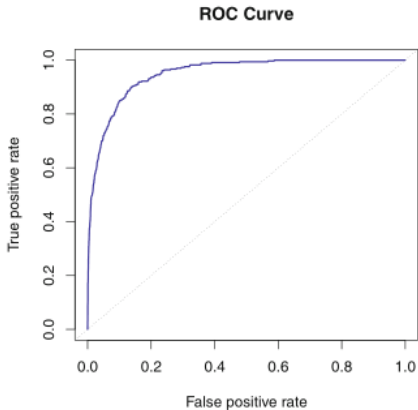
		Predicted	
		cat1	cat0
Actual	cat1	150	40
	cat0	60	250

Accuracy = 0.8

		Predicted	
		cat1	cat0
Actual	cat1	250	45
	cat0	5	200

Accuracy = 0.9

The Receiver Operating Characteristic (ROC) curve



James, Witten, Hastie and Tibshirani (2017), p.148

The Receiver Operating Characteristic (ROC) curve

- **True positive rate** = Recall (or Sensitivity)
- **False positive rate** = 1-Specificity
- Diagonal: random guess
- **(TP, FP):**
 - (0,0): everything is negative
 - (1,1): everything is positive
 - (1,0): ideal, what we want
- Area under the curve (AOC): ideal: 1, random guess: 0.5

Naive Bayes (NB)

- Classifies documents into categories based on posterior probability
- The posterior is established via the Bayes theorem
- Widely used classifier for texts
- "naive" because it assumes:
 - conditional independence between words
 - positional independence of words (due to bag-of-words approach)

Naive Bayes

The Bayes theorem:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

Where:

- $P(A|B)$ posterior probability (conditional probability of A, given that B occurred)
- $P(A)$ prior probability (how likely is event A, without any additional information)
- $P(B|A)$ likelihood of B, given A

At the term levels, with N documents and K classes:

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j)}$$

At the document level

The document level class:

$$P(c|d) = P(c) \prod_j \frac{P(w_j|c)}{P(w_j)}$$

Naive Bayes example

	#	features	is WtP?
training set	1	Forest, Tiger, Forest	yes
	2	Forest, Honey, Forest	yes
	3	Mad, Hatter, Forest	no
	4	Forest, Piglet	yes
test set	5	Forest, Forest, Forest, Mad, Hatter	?

Adapted from Manning, Raghavan and Schütze, Introduction to Information Retrieval (Table 13.1)

NB exercise

- Prior Winnie the Pooh: $P(c) = 3/4$ (for not Winnie: $1/4$)
- conditional probability for each term:
 $P(\text{Forest}|c) = (5 + 1)/(8 + 6) = 3/7$
- $P(\text{Mad}|c) = P(\text{Hatter}|c) = (0 + 1)/(8 + 6) = 1/14$
- $P(\text{Forest}|c_{\neg}) = (1 + 1)/(3 + 6) = 2/9$
- $P(\text{Mad}|c_{\neg}) = P(\text{Hatter}|c_{\neg}) = (1 + 1)/(3 + 6) = 2/9$

Our test document then:

- $P(c|d_5) = 3/4 * (3/7)^3 * (1/14)^2 = 0.0003$
- $P(c_{\neg}|d_5) = 1/4 * (2/9)^3 * (2/9)^2 = 0.0001$
- **the test document belongs to Winnie the Pooh**

Some details:

- The +1 in the nominator is called *Laplace smoothing* and it helps avoid 0 probability (see second row above)
- 8 and 3 are the length of the respective texts in each category, and 6 is the unique word count constant.

Support Vector Machine

- Developed in 1990s
- The SVM is the generalization of the maximal margin classifier
- Very flexible, flavour of the decade
- Performs well, *"considered one of the best "out of the box" classifiers"* (ISL, p.337)
- The SVM's goal is to locate the hyperplane with the largest margin (maximum marginal hyperplane)

Goal of SVM

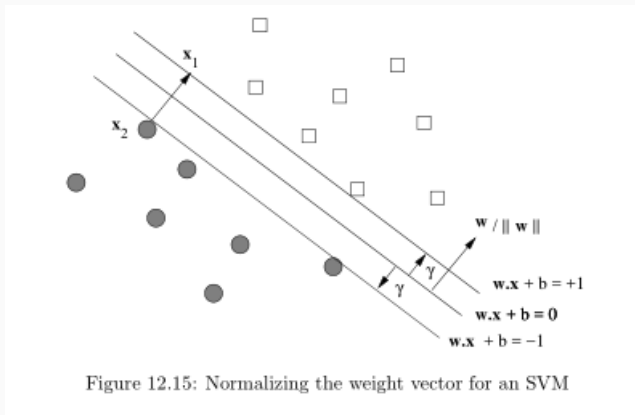
Equation for a separating hyperplane: $W * X + b$ where \mathbf{W} is a weight vector $W = \{w_1, w_2, \dots, w_n\}$ for n attributes and b is a scalar, called bias.

Goal is to find a set of weights that specify two hyperplanes:

$$\vec{w} * \vec{x} + b \geq +1$$

$$\vec{w} * \vec{x} + b \leq -1$$

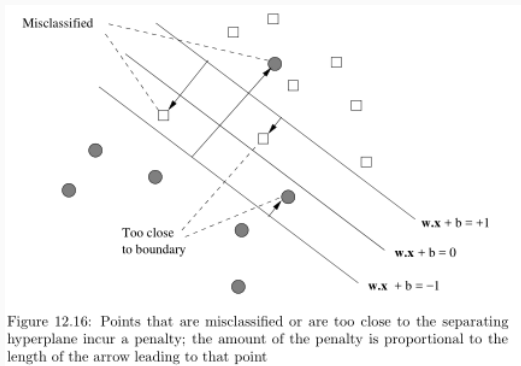
Maximizing the margin is minimizing $\|w\|$ or $\|w\|^2$ (Euclidean distance)



Leskovec, Rajaraman, Ullman (2014), p.463

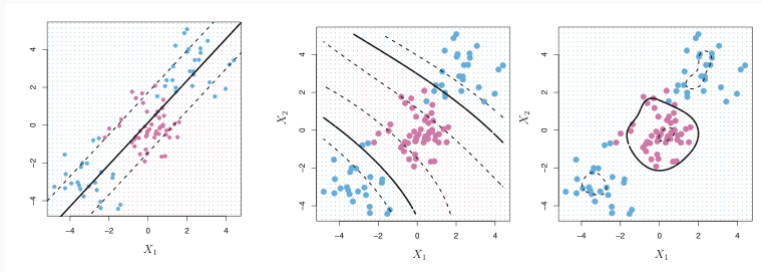
- loss function C , which regulates the tolerance to misclassification
- if data is not linearly separable: different kernels (radial, polynomial or sigmoid)

SVM illustrations



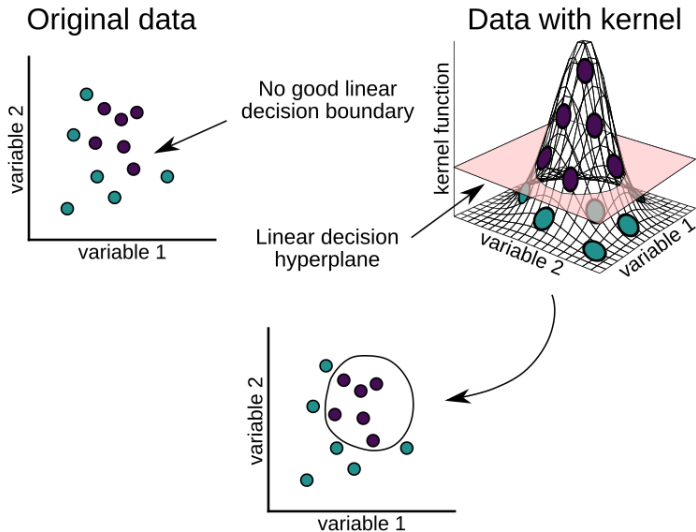
Leskovec, Rajaraman, Ullman (2014), p.465

SVM illustrations



James, Witten, Hastie and Tibshirani (2017), p.353

SVM illustrations



<https://machinelearningwithmlr.wordpress.com/2019/10/10/example-post/>

Additional materials in this session

Han, Kamber, Pei: Data Mining - Concepts and Techniques (Third edition), 2012 (Ch8)

Manning, Raghavan, Schütze: Introduction to Information Retrieval, 2008 (Ch 13)

James, Witten, Hastie, Tibshirani: An Introduction to Statistical Learning, 2017 (Ch2, Ch4)

Leskovec, Rajaraman, Ullman: Mining of Massive Datasets, 2014 (Ch12.3)