Fundamentals of AI & ML

Monsoon Semester V 2021-22

Lab - 8

Date: 11 November 2021

Topic: Backpropagation Algorithm

AIM

Build an Artificial Neural Network by implementing the Backpropagation algorithm and test the same using appropriate data sets.

THEORY

BACKPROPAGATION Algorithm

BACKPROPAGATION (*training_example, η, n_{in}, n_{out}, n_{hidden}*)

Each training example is a pair of the form $(\vec{x}\ t)$, where (x) is the vector of network input values, (t) and is the vector of target network output values.

η is the learning rate (e.g., .0.5). n_i, is the number of network inputs, n_{hidden} the number of units in the hidden layer, and n_{out} the number of output units.

The input from unit i into unit j is denoted x_{ji}, and the weight from unit i to unit j is denoted w_{ji}

- Create a feed-forward network with n_i inputs, n_{hidden} hidden units, and n_{out} output units.
- Initialize all network weights to small random numbers
- Until the termination condition is met, Do
    - For each $(\vec{x}\ t)$, in training examples, Do

      Propagate the input forward through the network:

      1. Input the instance $\vec{x}$, to the network and compute the output o_u of every unit u in the network.

Propagate the errors backward through the network:

2. For each network output unit k, calculate its error term δ_k

$$\delta_k \leftarrow o_k(1 - o_k)(t_k - o_k)$$

3. For each hidden unit *h*, calculate its error term δ_h

$$\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in outputs} w_{h,k}\delta_k$$

4. Update each network weight w_{ji}

$$w_{ji} \leftarrow w_{ji} + \Delta w_{ji}$$

Where

$$\Delta w_{ji} = \eta \delta_j x_{i,j}$$

Training Examples:

Example	Sleep	Study	Expected % in Exams
1	2	9	92
2	1	5	86
3	3	6	89

Normalize the input

Example	Sleep	Study	Expected % in Exams
1	2/3 = 0.66666667	9/9 = 1	0.92
2	1/3 = 0.33333333	5/9 = 0.55555556	0.86
3	3/3 = 1	6/9 = 0.66666667	0.89

PROGRAM CODE

```
import numpy as np

X = np.array(([2, 9], [1, 5], [3, 6]), dtype=float)  # two inputs
[sleep,study]
y = np.array(([92], [86], [89]), dtype=float)  # one output [Expected % in
Exams]
X = X / np.amax(X, axis=0)  # maximum of X array longitudinally
y = y / 100


# Sigmoid Function
def sigmoid(x):
    return 1 / (1 + np.exp(-x))


# Derivative of Sigmoid Function
def derivatives_sigmoid(x):
    return x * (1 - x)


# Variable initialization
epoch = 5000  # Setting training iterations
lr = 0.1  # Setting learning rate
inputlayer_neurons = 2  # number of features in data set
hiddenlayer_neurons = 3  # number of hidden layers neurons
output_neurons = 1  # number of neurons at output layer


# weight and bias initialization
wh = np.random.uniform(size=(inputlayer_neurons, hiddenlayer_neurons))
# weight of the link from input node to hidden node
bh = np.random.uniform(size=(1, hiddenlayer_neurons))
# bias of the link from input node to hidden node
wout = np.random.uniform(size=(hiddenlayer_neurons, output_neurons))
# weight of the link from hidden node to output node
bout = np.random.uniform(size=(1, output_neurons))
# bias of the link from hidden node to output node


# draws a random range of numbers uniformly of dim x*y
for i in range(epoch):
    # Forward Propogation
    hinp1 = np.dot(X, wh)
    hinp = hinp1 + bh
    hlayer_act = sigmoid(hinp)
    outinp1 = np.dot(hlayer_act, wout)
    outinp = outinp1 + bout
    output = sigmoid(outinp)


    # Backpropagation
    EO = y - output
    outgrad = derivatives_sigmoid(output)
```

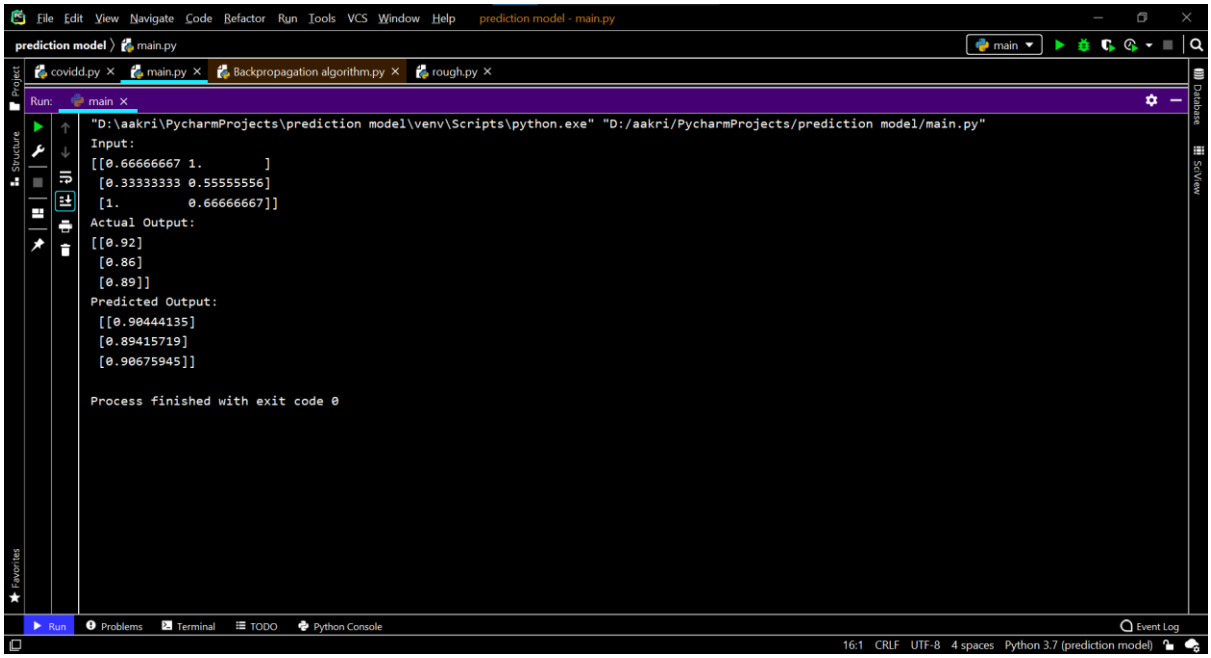
```
    d_output = EO * outgrad
    EH = d_output.dot(wout.T)


    # how much hidden layer weights contributed to error
    hiddengrad = derivatives_sigmoid(hlayer_act)
    d_hiddenlayer = EH * hiddengrad


# dotproduct of nextlayererror and currentlayerop
wout += hlayer_act.T.dot(d_output) * lr
wh += X.T.dot(d_hiddenlayer) * lr

print("Input: \n" + str(X))
print("Actual Output: \n" + str(y))
print("Predicted Output: \n", output)
```

OUTPUT



CONCLUSION

Hence, The BackPropagation Algorithm was implemented successfully.