

# FIITJEE

## Solutions to JEE(Main)-2020

Test Date: 9<sup>th</sup> January 2020 (First Shift)

### PHYSICS, CHEMISTRY & MATHEMATICS

Paper - 1

Time Allotted: 3 Hours

Maximum Marks: 300

- Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

#### **Important Instructions:**

1. The test is of **3 hours** duration.
2. This **Test Paper** consists of **75** questions. The maximum marks are **300**.
3. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry** and **Mathematics** having 25 questions in each part of equal weightage out of which 20 questions are MCQs and 5 questions are numerical value based. Each question is allotted **4 (four)** marks for correct response.
4. **(Q. No. 01 – 20, 26 – 45, 51 – 70)** contains 60 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
5. **(Q. No. 21 – 25, 46 – 50, 71 – 75)** contains 15 Numerical based questions with answer as numerical value. Each question carries **+4 marks** for correct answer. There is no negative marking.
6. Candidates will be awarded marks as stated above in **instruction No.3** for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer box.
7. There is only one correct response for each question. Marked up more than one response in any question will be treated as wrong response and marked up for wrong response will be deducted accordingly as per **instruction 6** above.

## PART – A (PHYSICS)

- Two particles of equal mass 'm' have respective initial velocities  $u\hat{i}$  and  $u\left(\frac{\hat{i}+\hat{j}}{2}\right)$ . They collide completely inelastically. The energy lost in the process is:
 

(A)  $\frac{1}{3}mu^2$  (B)  $\frac{1}{8}mu^2$   
 (C)  $\sqrt{\frac{2}{3}}mu^2$  (D)  $\frac{3}{4}mu^2$
- Radiation, with wavelength 6561 Å falls on a metal surface to produce photoelectrons. The electrons are made to enter a uniform magnetic field of  $3 \times 10^{-4}$  T. If the radius of the largest circular path followed by the electrons is 10 mm, the work function of the metal is close to:
 

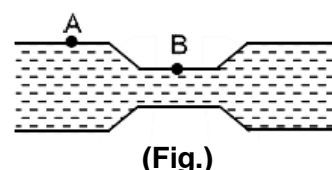
(A) 0.8 eV (B) 1.6 eV  
 (C) 1.8 eV (D) 1.1 eV
- Water flows in a horizontal tube (see figure). The pressure of water changes by  $700 \text{ Nm}^{-2}$  between A and B where the area of cross section are  $40 \text{ cm}^2$  and  $20 \text{ cm}^2$ , respectively. Find the rate of flow of water through the tube. (density of water =  $1000 \text{ kg m}^{-3}$ )
 

(A)  $1810 \text{ cm}^3/\text{s}$  (B)  $2420 \text{ cm}^3/\text{s}$   
 (C)  $2720 \text{ cm}^3/\text{s}$  (D)  $3020 \text{ cm}^3/\text{s}$
- The aperture diameter of a telescope is 5m. The separation between the moon and the earth is  $4 \times 10^5 \text{ km}$ . With light of wavelength of 5500 Å, the minimum separation between objects on the surface of moon, so that they are just resolved, is close to:
 

(A) 200 m (B) 600 m  
 (C) 60 m (D) 20 m
- A body A of mass m is moving in a circular orbit of radius R about a planet. Another body B of mass  $\frac{m}{2}$  collides with A with a velocity which is half  $\left(\frac{\vec{v}}{2}\right)$  the instantaneous velocity  $\vec{v}$  of A. The collision is completely inelastic. Then, the combined body:
 

(A) starts moving in an elliptical orbit around the planet.  
 (B) continues to move in a circular orbit.  
 (C) Escapes from the Planet's Gravitational field.  
 (D) Falls vertically downwards towards the planet.
- Consider two ideal diatomic gases A and B at some temperature T. Molecules of the gas A are rigid, and have a mass m. Molecules of the gas B have an additional vibrational mode and have mass  $\frac{m}{4}$ . The ratio of the specific heats ( $C_V^A$  and  $C_V^B$ ) of gas A and B, respectively is
 

(A) 3 : 5 (B) 5 : 7  
 (C) 7 : 9 (D) 5 : 9



7. Three harmonic waves having equal frequency  $\nu$  and same intensity  $I_0$ , have phase angles  $0, \frac{\pi}{4}$  and  $-\frac{\pi}{4}$  respectively. When they are superimposed the intensity of the resultant wave is close to:

(A)  $3I_0$  (B)  $I_0$   
(C)  $0.2I_0$  (D)  $5.8I_0$

8. A quantity  $f$  is given by  $f = \sqrt{\frac{hc^5}{G}}$  where  $c$  is speed of light,  $G$  universal gravitational constant and  $h$  is the Planck's constant. Dimension of  $f$  is that of:

(A) energy (B) momentum  
(C) area (D) volume

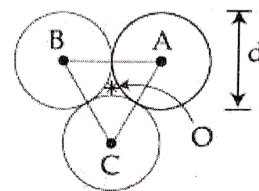
9. If the screw on a screw-gauge is given six rotations, it moves by 3 mm on the main scale.

If there are 50 divisions on the circular scale the least count of the screw gauge is

(A) 0.001 cm (B) 0.001 mm  
(C) 0.01 cm (D) 0.02 mm

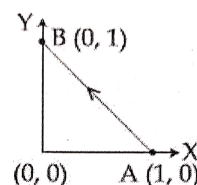
10. Three solid spheres each of mass  $m$  and diameter  $d$  are stuck together such that the lines connecting the centres form an equilateral triangle of side of length  $d$ . The ratio  $I_O/I_A$  of moment of inertia  $I_O$  of the system about an axis passing the centroid and about center of any of the spheres  $I_A$  and perpendicular to the plane of the triangle is

(A)  $\frac{15}{13}$  (B)  $\frac{13}{15}$   
(C)  $\frac{23}{13}$  (D)  $\frac{13}{23}$



11. Consider a force  $\vec{F} = -x\hat{i} + y\hat{j}$ . The work done by this force in moving a particle from point A(1, 0) to B(0, 1) along the line segment is: (all quantities are in SI units)

(A) 2 (B)  $\frac{1}{2}$   
(C) 1 (D)  $\frac{3}{2}$

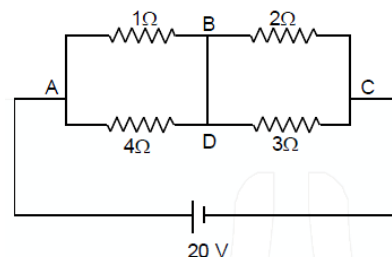


12. A vessel of depth  $2h$  is half filled with a liquid of refractive index  $2\sqrt{2}$  and the upper half with another liquid of refractive index  $\sqrt{2}$ . The liquids are immiscible. The apparent depth of the inner surface of the bottom of vessel will be

(A)  $\frac{h}{\sqrt{2}}$  (B)  $\frac{h}{2(\sqrt{2}+1)}$  (C)  $\frac{3}{4}h\sqrt{2}$  (D)  $\frac{h}{3\sqrt{2}}$

13. A particle moving with kinetic energy  $E$  has de Broglie wavelength  $\lambda$ . If energy  $\Delta E$  is added to its energy, the wavelength become  $\lambda/2$ . Value of  $\Delta E$ , is:  
 (A)  $E$  (B)  $3E$  (C)  $2E$  (D)  $4E$

14. In the given circuit diagram, a wire is joining points B and D. The current in this wire is:  
 (A) zero  
 (B)  $2A$   
 (C)  $0.4 A$   
 (D)  $4A$



15. A long, straight wire of radius  $a$  carries a current distributed uniformly over its cross-section. The ratio of the magnetic fields due to the wire at distance  $\frac{a}{3}$  and  $2a$ , respectively from the axis of the wire is:

- (A)  $\frac{2}{3}$  (B)  $\frac{1}{2}$  (C)  $2$  (D)  $\frac{3}{2}$

16. The electric fields of two plane electromagnetic plane waves in vacuum are given by  
 $\vec{E}_1 = E_0 \hat{j} \cos(\omega t - kx)$  and  
 $\vec{E}_2 = E_0 \hat{k} \cos(\omega t - ky)$

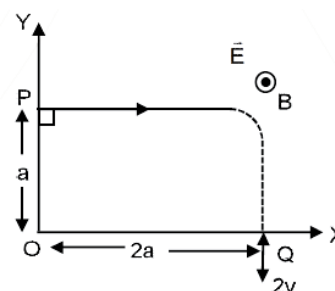
At  $t = 0$ , a particle of charge  $q$  is at origin with velocity  $\vec{v} = 0.8 c \hat{j}$  ( $c$  is the speed of light in vacuum). The instantaneous force experienced by the particle is:

- (A)  $E_0 q (0.8 \hat{i} - \hat{j} + 0.4 \hat{k})$  (B)  $E_0 q (0.4 \hat{i} - 3 \hat{j} + 0.8 \hat{k})$   
 (C)  $E_0 q (0.8 \hat{i} + \hat{j} + 0.2 \hat{k})$  (D)  $E_0 q (-0.8 \hat{i} + \hat{j} + \hat{k})$

17. An electric dipole of moment  $\vec{p} = (-\hat{i} - 3\hat{j} + 2\hat{k}) \times 10^{-29} \text{ cm}$  is at the origin  $(0, 0, 0)$ . The electric field due to this dipole at  $\vec{r} = +\hat{i} + 3\hat{j} + 5\hat{k}$  (note that  $\vec{r} \cdot \vec{p} = 0$ ) is parallel to:

- (A)  $(-\hat{i} - 3\hat{j} + 2\hat{k})$  (B)  $(+\hat{i} - 3\hat{j} - 2\hat{k})$   
 (C)  $(-\hat{i} + 3\hat{j} - 2\hat{k})$  (D)  $(+\hat{i} + 3\hat{j} - 2\hat{k})$

18. A charged particle of mass ' $m$ ' and charge ' $q$ ' moving under the influence of uniform electric field  $E \hat{i}$  and a uniform magnetic field  $B \hat{k}$  follows a trajectory from point P to Q as shown in figure. The velocities at P and Q are respectively,  $v \hat{i}$  and  $-2v \hat{j}$ . Then which of the following statements (A, B, C, D) are the correct? (Trajectory shown is schematic and not to scale)



(a)  $E = \frac{3}{4} \left( \frac{mv^2}{qa} \right)$

(b) Rate of work done by the electric field at P is  $\frac{3}{4} \left( \frac{mv^3}{a} \right)$

(c) Rate of work done by both the fields at Q is zero.

(d) The difference between the magnitude of angular momentum of the particle at P and Q is  $2 m a v$ .

(A) (b), (c), (d)

(B) (a), (b), (c)

(C) (a), (c), (d)

(D) (a), (b), (c), (d)

19. Consider a sphere of radius  $R$  which carries a uniform charge density  $\rho$ . If a sphere of radius  $\frac{R}{2}$  is carved out of it,

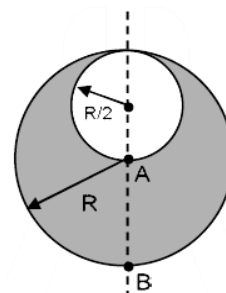
as shown the ratio  $\frac{|\vec{E}_A|}{|\vec{E}_B|}$  of magnitude of electric field  $\vec{E}_A$  and  $\vec{E}_B$ , respectively, at point A and B due to the remaining portion is:

(A)  $\frac{18}{34}$

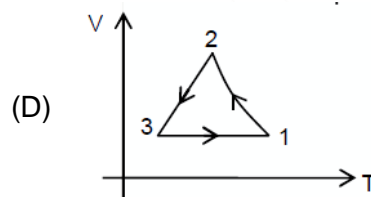
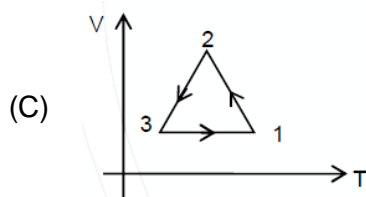
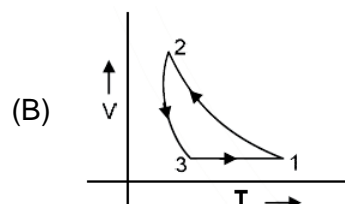
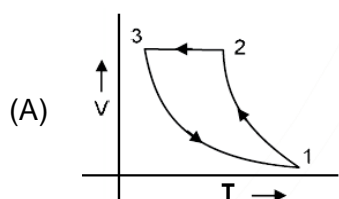
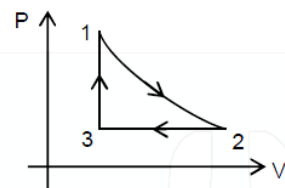
(B)  $\frac{17}{54}$

(C)  $\frac{18}{54}$

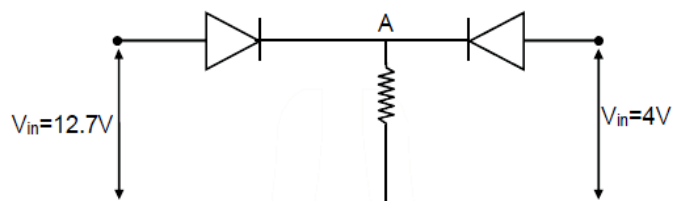
(D)  $\frac{21}{34}$



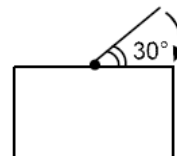
20. Which of the following is an equivalent cyclic process corresponding to the thermodynamic cyclic given in the figure? Where,  $1 \rightarrow 2$  is adiabatic. (Graphs are schematic and are not to scale)



21. Both the diodes used in the circuit shown are assumed to be ideal and have negligible resistance when these are forward biased. Built in potential in each diode is  $0.7 \text{ V}$ . For the input voltages shown in the figure, the voltage (in Volts) at point A is \_\_\_\_\_.



22. One end of a straight uniform 1 m long bar is pivoted on horizontal table. It is released from rest when it makes an angle  $30^\circ$  from the horizontal (see figure). Its angular speed when it hits the table is given as  $\sqrt{n} \text{ s}^{-1}$ , where  $n$  is an integer. The value of  $n$  is \_\_\_\_\_.



23. In a fluorescent lamp choke (a small transformer) 100 V of reverse voltage is produced when the choke current changes uniformly from 0.25 A to 0 in a duration of 0.025 ms. The self-inductance of the choke (in mH) is estimated to be \_\_\_\_\_.
24. A body of mass  $m = 10 \text{ kg}$  is attached to one end of a wire of length 0.3 m. The maximum angular speed (in  $\text{rad s}^{-1}$ ) with which it can be rotated about its other end in space station is (Breaking stress of wire =  $4.8 \times 10^7 \text{ Nm}^{-2}$  and area of cross-section of the wire =  $10^{-2} \text{ cm}^2$ ) is \_\_\_\_\_.
25. The distance  $x$  covered by a particle in one dimensional motion varies with time  $t$  as  $x^2 = at^2 + bt + c$ . If the acceleration of the particle depends on  $x$  as  $x^{-n}$ , where  $n$  is an integer, the value of  $n$  is \_\_\_\_\_.

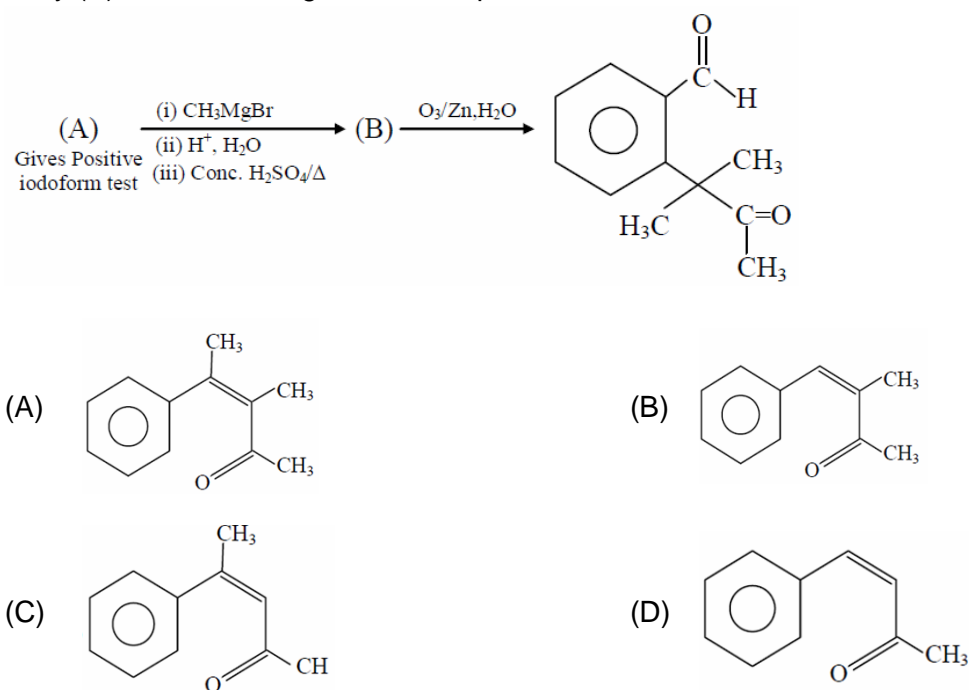
## PART -B (CHEMISTRY)

26. If the magnetic moment of a dioxygen species is 1.73 B.M, it may be:  
 (A)  $O_2, O_2^-$  or  $O_2^+$  (B)  $O_2$  or  $O_2^-$   
 (C)  $O_2 + O_2^+$  (D)  $O_2^-$  or  $O_2^+$
27. The compound that cannot act both as oxidising and reducing agent is:  
 (A)  $H_2O_2$  (B)  $H_2SO_3$   
 (C)  $HNO_2$  (D)  $H_3PO_4$
28.  $[Pd(F)(Cl)(Br)(I)]^{2-}$  has n number of geometrical isomers. Then, the spin-only magnetic moment and crystal field stabilisation energy [CFSE] of  $[Fe(CN)_6]^{n-6}$ , respectively, are:  
 [Note: Ignore the pairing energy]  
 (A) 2.84 BM and  $-1.6 \Delta_0$  (B) 1.73 BM and  $-2.0 \Delta_0$   
 (C) 5.92 BM and 0 (D) 0 BM and  $-2.4 \Delta_0$
29. The electronic configurations of bivalent europium and trivalent cerium are: (atomic number: Xe = 54, Ce = 58, Eu = 63)  
 (A)  $[Xe] 4f^7 6s^2$  and  $[Xe] 4f^2 6s^2$  (B)  $[Xe] 4f^7$  and  $[Xe] 4f^1$   
 (C)  $[Xe] 4f^2$  and  $[Xe] 4f^7$  (D)  $[Xe] 4f^4$  and  $[Xe] 4f^9$
30. For following reactions  

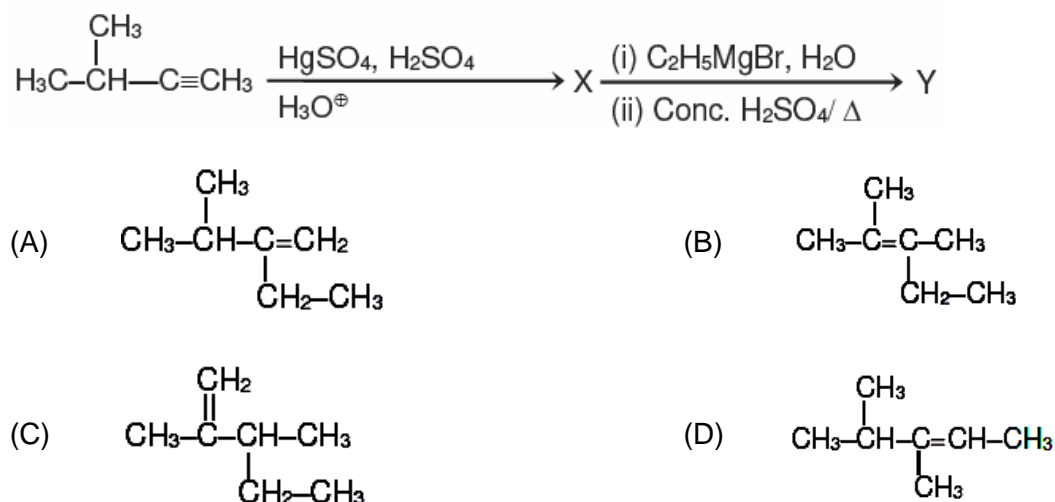
$$A \xrightarrow{700\text{ K}} \text{Product}$$

$$A \xrightarrow[\text{catalyst}]{500\text{ K}} \text{Product}$$
 it was found that the  $E_a$  is decreased by 30 kJ/mol in the presence of catalyst. If the rate remains unchanged, the activation energy for catalysed reaction is (Assume pre exponential factor is same):  
 (A) 135 kJ/mol (B) 105 kJ/mol  
 (C) 75 kJ/mol (D) 198 kJ/mol
31. The increasing order of basicity for the following intermediates is (from weak to strong)
- |  |  |                                   |                       |                     |
|--|--|-----------------------------------|-----------------------|---------------------|
| $\begin{array}{c} \text{CH}_3 \\   \\ \text{H}_3\text{C}-\text{C}^\ominus \\   \\ \text{CH}_3 \end{array}$ | $\text{H}_2\text{C}=\text{CH}-\text{CH}_2^\ominus$ | $\text{HC}\equiv\text{C}^\ominus$ | $\text{CH}_3^\ominus$ | $\text{CN}^\ominus$ |
| (i)  | (ii)   | (iii)                             | (iv)                  | (iv)                |
- (A) (v) < (iii) < (ii) < (iv) < (i) (B) (iii) < (i) < (ii) < (iv) < (v)  
 (C) (v) < (i) < (iv) < (ii) < (iii) (D) (iii) < (iv) < (ii) < (i) < (v)

32. 'X' melts at low temperature and is a bad conductor of electricity in both liquid and solid state. X is:  
 (A) Silicon carbide (B) Mercury  
 (C) Zinc sulphide (D) Carbon tetrachloride
33. The de Broglie wavelength of an electron in the 4<sup>th</sup> Bohr orbit is:  
 (A)  $6\pi a_0$  (B)  $4\pi a_0$   
 (C)  $2\pi a_0$  (D)  $8\pi a_0$
34. Identify (A) in the following reaction sequence:

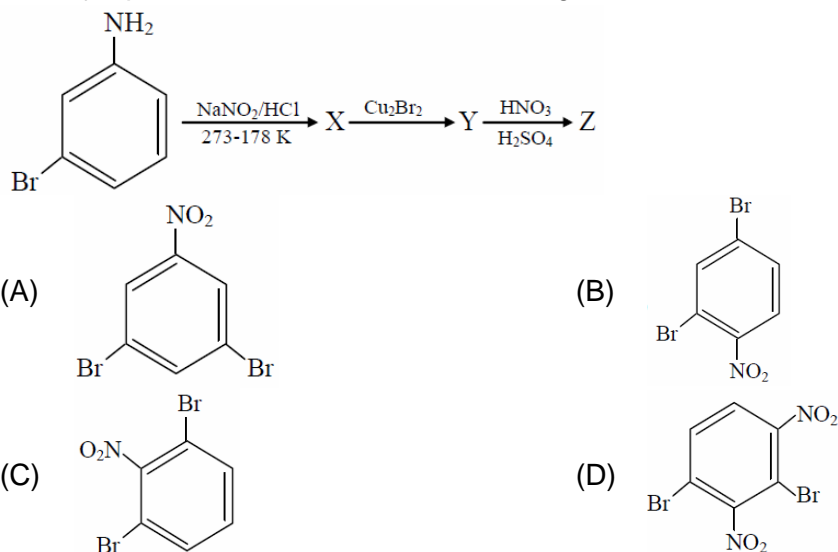


35. The major product (Y) in the following reactions is:

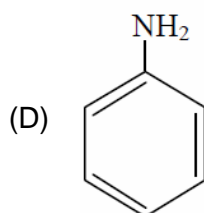
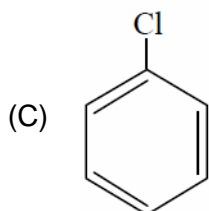
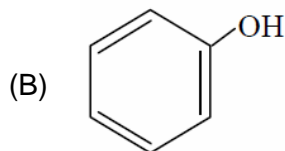
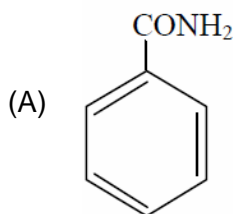




36. Complex X of composition  $\text{Cr}(\text{H}_2\text{O})_6\text{Cl}_n$  has a spin only magnetic moment of 3.83 BM. It reacts with  $\text{AgNO}_3$  and shows geometrical isomerism. The IUPAC nomenclature of X is:  
 (A) Dichloridotetraqua chromium (IV) chloride dihydrate  
 (B) Tetraaquadichlorido chromium (III) chloride dihydrate  
 (C) Tetraaquadichlorido chromium (IV) chloride dihydrate  
 (D) Hexaaqua chromium (III) chloride  
 IUPAC name = Tetraaquadichlorido chromium (III) chloride dihydrate
37. The acidic, basic and amphoteric oxides, respectively, are:  
 (A)  $\text{Cl}_2\text{O}$ ,  $\text{CaO}$ ,  $\text{P}_4\text{O}_{10}$  (B)  $\text{MgO}$ ,  $\text{Cl}_2\text{O}$ ,  $\text{Al}_2\text{O}_3$   
 (C)  $\text{Na}_2\text{O}$ ,  $\text{SO}_3$ ,  $\text{Al}_2\text{O}_3$  (D)  $\text{N}_2\text{O}_3$ ,  $\text{Li}_2\text{O}$ ,  $\text{Al}_2\text{O}_3$
38. The  $K_{\text{sp}}$  for the following dissociation is  $1.6 \times 10^{-5}$   
 $\text{PbCl}_2(\text{s}) \rightleftharpoons \text{Pb}^{2+}(\text{aq}) + 2\text{Cl}^{-}(\text{aq})$   
 Which of the following choices is correct for a mixture of 300 mL 0.134 M  $\text{Pb}(\text{NO}_3)_2$  and 100 mL 0.4 M  $\text{NaCl}$ ?  
 (A) Not enough data provided (B)  $Q > K_{\text{sp}}$   
 (C)  $Q < K_{\text{sp}}$  (D)  $Q = K_{\text{sp}}$
39. A chemist has 4 samples of artificial sweetener A, B, C and D. To identify these samples, he performed certain experiments and noted the following observations:  
 (i) A and D both form blue-violet colour with ninhydrin.  
 (ii) Lassaigne extract of C gives positive  $\text{AgNO}_3$  test and negative  $\text{Fe}_4[\text{Fe}(\text{CN})_6]_3$  test.  
 (iii) Lassaigne extract of B and D gives positive sodium nitroprusside test.  
 Based on these observations which option is correct?  
 (A) A : Aspartame; B : Alitame; C : Saccharin; D : Sucralose  
 (B) A : Aspartame; B : Saccharin; C : Sucralose; D : Alitame  
 (C) A : Alitame; B : Saccharin; C : Aspartame; D : Sucralose  
 (D) A : Saccharin; B : Alitame; C : Sucralose; D : Aspartame
40. The major product Z obtained in the following reaction scheme is:



41. Which of these will produce the highest yield in Friedel Crafts reaction?



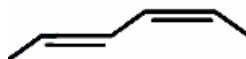
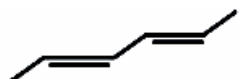
42. B has a smaller first ionization enthalpy than Be. Consider the following statements:

- (i) it is easier to remove 2p electron than 2s electron.
- (ii) 2p electron of B is more shielded from the nucleus by the inner core of electrons than the 2s electrons of Be.
- (iii) 2s electron has more penetration power than 2p electron
- (iv) atomic radius of B is more than Be (atomic number B = 5, Be = 4)

The correct statements are:

- (A) (i), (iii) and (iv)
- (B) (i), (ii) and (iii)
- (C) (i), (ii) and (iv)
- (D) (ii), (iii) and (iv)

43. The correct order of heat of combustion for following alkadienes is:



- (a)

- (b)

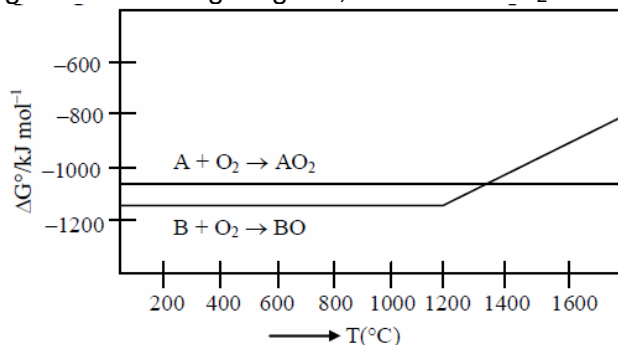
- (c)

- (A)  $(a) < (b) < (c)$                       (B)  $(a) < (c) < (b)$   
(C)  $(c) < (b) < (a)$                       (D)  $(b) < (c) < (a)$

44. If enthalpy of atomisation for  $\text{Br}_2(\text{A})$  is  $x$  kJ/mol and bond enthalpy for  $\text{Br}_2$  is  $y$  kJ/mol, the relation between them:

- (A) is  $x = y$  (B) is  $x > y$   
(C) does not exist (D) is  $x < y$

45. According to the following diagram, A reduces  $\text{BO}_2$  when the temperature is:



- (A)  $> 1400\text{ }^{\circ}\text{C}$  (B)  $< 1400\text{ }^{\circ}\text{C}$   
 (C)  $< 1200\text{ }^{\circ}\text{C}$  (D)  $> 1200\text{ }^{\circ}\text{C}$  but  $< 1400\text{ }^{\circ}\text{C}$
46. The molarity of  $\text{HNO}_3$  in a sample which has density  $1.4\text{ g/mL}$  and mass percentage of 63% is (Molecular Weight of  $\text{HNO}_3 = 63$ )
47. The mass percentage of nitrogen in histamine is\_\_\_\_\_.
48. How much amount of  $\text{NaCl}$  should be added to  $600\text{ g}$  of water ( $\rho = 1.00\text{ g/mL}$ ) to decrease the freezing point of water to  $-0.2^{\circ}\text{C}$  ?\_\_\_\_\_.  
 (The freezing point depression constant for water =  $2\text{ K kg mol}^{-1}$ )
49.  $108\text{ g}$  of silver (molar mass  $108\text{ g mol}^{-1}$ ) is deposited at cathode from  $\text{AgNO}_3$  (aq) solution by a certain quantity of electricity. The volume (in L) of oxygen gas produced at  $273\text{ K}$  and  $1\text{ bar}$  pressure from water by the same quantity of electricity is\_\_\_\_\_.
50. The hardness of a water sample containing  $10^{-3}\text{ M}$   $\text{MgSO}_4$  expressed as  $\text{CaCO}_3$  equivalents (in ppm) is\_\_\_\_\_.  
 (molar mass of  $\text{MgSO}_4$  is  $120.38\text{ g/mol}$ )

PART-C (MATHEMATICS)

51. The product  $2^{\frac{1}{4}} \cdot 4^{\frac{1}{16}} \cdot 8^{\frac{1}{48}} \cdot 16^{\frac{1}{128}} \dots$  to  $\infty$  is equal to  
 (A)  $2^{\frac{1}{2}}$  (B) 2  
 (C) 1 (D)  $2^{\frac{1}{4}}$
52. Let the observations  $x_i (1 \leq i \leq 10)$  satisfy the equation  $\sum_{i=1}^{10} (x_i - 5) = 10$  and  $\sum_{i=1}^{10} (x_i - 5)^2 = 40$ . If  $\mu$  and  $\lambda$  are the mean and the variance of the observations,  $x_1 - 3, x_2 - 3, \dots, x_{10} - 3$ , then the ordered pair  $(\mu, \lambda)$  is equal to:  
 (A) (6, 6) (B) (3, 3)  
 (C) (3, 6) (D) (6, 3)
53. If  $e_1$  and  $e_2$  are the eccentricities of the ellipse,  $\frac{x^2}{18} + \frac{y^2}{4} = 1$  and the hyperbola,  $\frac{x^2}{9} - \frac{y^2}{4} = 1$  respectively and  $(e_1, e_2)$  is a point on the ellipse,  $15x^2 + 3y^2 = k$ , then  $k$  is equal to:  
 (A) 16 (B) 14  
 (C) 17 (D) 15
54. If the matrices  $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{bmatrix}$ ,  $B = \text{adj} A$  and  $C = 3A$ , then  $\frac{|\text{adj} B|}{|C|}$  is equal to:  
 (A) 72 (B) 8  
 (C) 16 (D) 2
55. If  $f(x) = \begin{cases} \frac{\sin(a+2)x + \sin x}{x}; & x < 0 \\ b; & x = 0 \\ \frac{(x+3x^2)^{1/3}}{x^{4/3}}; & x > 0 \end{cases}$   
 (A) -2 (B) -1  
 (C) 0 (D) 1

56. If the number of five digit numbers with distinct digits and 2 at the 10<sup>th</sup> place is 336 k, then k is equal to:  
 (A) 6 (B) 7  
 (C) 4 (D) 8
57. In a box, there are 20 cards, out of which 10 are labeled as A and the remaining 10 are labelled as B. Cards are drawn at random, one after the other and with replacement, till a second A – card is obtained. The probability that the second A – card appears before the third B – card is:  
 (A)  $\frac{9}{16}$  (B)  $\frac{15}{16}$   
 (C)  $\frac{13}{16}$  (D)  $\frac{11}{16}$
58. The number of real roots of the equation,  $e^{4x} + e^{3x} - 4e^{2x} + e^x + 1 = 0$  is:  
 (A) 2 (B) 4  
 (C) 3 (D) 1
59. A spherical iron ball of 10 cm radius is coated with a layer of ice of uniform thickness that melts at a rate of 50 cm<sup>3</sup>/ min. When the thickness of ice is 5 cm, then the rate (in cm/min) at which of the thickness of ice decreases, is:  
 (A)  $\frac{5}{6\pi}$  (B)  $\frac{1}{36\pi}$   
 (C)  $\frac{1}{18\pi}$  (D)  $\frac{1}{54\pi}$
60. The value of  $\int_0^{2\pi} \frac{x \sin^8 x}{\sin^8 x + \cos^8 x} dx$  is equal to:  
 (A)  $2\pi$  (B)  $4\pi$   
 (C)  $\pi^2$  (D)  $2\pi^2$
61. Let z be a complex number such that  $\left| \frac{z-i}{z+2i} \right| = 1$  and  $|z| = \frac{5}{2}$ . Then the value of  $|z+3i|$  is:  
 (A)  $\frac{15}{4}$  (B)  $2\sqrt{3}$   
 (C)  $\sqrt{10}$  (D)  $\frac{7}{2}$
62. Negation of the statement:  
 ' $\sqrt{5}$  is an integer or 5 is irrational' is:  
 (A)  $\sqrt{5}$  is an integer and 5 is irrational  
 (B)  $\sqrt{5}$  is not an integer or 5 is not irrational  
 (C)  $\sqrt{5}$  is not an integer and 5 is not irrational  
 (D)  $\sqrt{5}$  is irrational or 5 is an integer

63. Let C be the centroid of the triangle with vertices (3, -1), (1, 3) AND (2, 4). Let P be the point of intersection of the lines  $x + 3y - 1 = 0$  and  $3x - y + 1 = 0$ . Then the line passing through the points C and P also passes through the point:  
 (A) (-9, -7) (B) (-9, -6)  
 (C) (7, 6) (D) (9, 7)
64. If for some  $\alpha$  and  $\beta$  in  $\mathbb{R}$ , the intersection of the following three planes  
 $x + 4y - 2z = 1$   
 $x + 7y - 5z = \beta$   
 $x + 5y + \alpha z = 5$   
 is a line in  $\mathbb{R}^3$ , then  $\alpha + \beta$  is equal to:  
 (A) 0 (B) 2  
 (C) 10 (D) -10
65. Let  $f$  be any function continuous on  $[a, b]$  and twice differentiable on  $(a, b)$ . If for all  $x \in (a, b)$ ,  $f'(x) > 0$  and  $f''(x) < 0$ , then for any  $c \in (a, b)$   $\frac{f(c) - f(a)}{f(b) - f(c)}$  is greater than:  
 (A)  $\frac{c - a}{b - c}$  (B)  $\frac{b + a}{b - a}$   
 (C)  $\frac{b - c}{c - a}$  (D) 1
66. The value of  $\cos^3\left(\frac{\pi}{8}\right) \cdot \cos\left(\frac{3\pi}{8}\right) + \sin^3\left(\frac{\pi}{8}\right) \cdot \sin\left(\frac{3\pi}{8}\right)$  is:  
 (A)  $\frac{1}{\sqrt{2}}$  (B)  $\frac{1}{4}$   
 (C)  $\frac{1}{2}$  (D)  $\frac{1}{2\sqrt{2}}$
67. A circle touches the  $y$  - axis at the point (0, 4) and passes through the point (2, 0). Which of the following lines is not a tangent to this circle?  
 (A)  $3x - 4y - 24 = 0$  (B)  $3x + 4y - 6 = 0$   
 (C)  $4x - 3y + 17 = 0$  (D)  $4x + 3y - 8 = 0$
68. If for all real triplets (a, b, c),  $f(x) = a + bx + cx^2$ ; then  $\int_0^1 f(x) dx$  is equal to:  
 (A)  $\frac{1}{2} \left\{ f(1) + 3f\left(\frac{1}{2}\right) \right\}$  (B)  $\frac{1}{6} \left\{ f(0) + f(1) + 4f\left(\frac{1}{2}\right) \right\}$   
 (C)  $\frac{1}{3} \left\{ f(0) + f\left(\frac{1}{2}\right) \right\}$  (D)  $2 \left\{ 3f(1) + 2f\left(\frac{1}{2}\right) \right\}$

69. If  $f'(x) = \tan^{-1}(\sec x + \tan x)$ ,  $-\frac{\pi}{2} < x < \frac{\pi}{2}$ , and  $f(0) = 0$ , then  $f(1)$  is equal to:
- (A)  $\frac{\pi-1}{4}$  (B)  $\frac{\pi+1}{4}$   
 (C)  $\frac{\pi+2}{4}$  (D)  $\frac{1}{4}$
70. The integral  $\int \frac{dx}{(x+4)^{8/7}(x-3)^{6/7}}$  is equal to:  
 (where C is a constant of integration)
- (A)  $-\frac{1}{13} \left( \frac{x-3}{x+4} \right)^{-13/7} + C$  (B)  $-\left( \frac{x-3}{x+4} \right)^{-1/7} + C$   
 (C)  $\left( \frac{x-3}{x+4} \right)^{1/7} + C$  (D)  $\frac{1}{2} \left( \frac{x-3}{x+4} \right)^{3/7} + C$
71. The projection of the line segment joining the points (1, -1, 3) and (2, -4, 11) on the line joining the points (-1, 2, 3) and (3, -2, 10) is \_\_\_\_\_
72. If the vectors,  $\vec{p} = (a+1)\hat{i} + a\hat{j} + a\hat{k}$ ,  $\vec{q} = a\hat{i} + (a+1)\hat{j} + a\hat{k}$  and  $\vec{r} = a\hat{i} + a\hat{j} + (a+1)\hat{k}$  ( $a \in \mathbb{R}$ ) are coplanar and  $3(\vec{p} \cdot \vec{q})^2 - \lambda |\vec{r} \times \vec{q}|^2 = 0$ , then the value of  $\lambda$  is \_\_\_\_\_.
73. If for  $x \geq 0$ ,  $y = y(x)$  is the solution of the differential equation,  $(x+1)dy = ((x+1)^2 + y - 3)dx$ ,  $y(2) = 0$ , then  $y(3)$  is equal to \_\_\_\_\_
74. The coefficient of  $x^4$  in the expansion of  $(1+x+x^2)^{10}$  is \_\_\_\_\_.
75. The number of distinct solutions of the equation,  $\log_{\frac{1}{2}} |\sin x| = 2 - \log_{\frac{1}{2}} |\cos x|$  in the interval  $[0, 2\pi]$ , is \_\_\_\_\_.

# JEE (Main) – 2020

## ANSWERS

### PART –A (PHYSICS)

1. <b>B</b>	2. <b>A</b>	3. <b>C</b>	4. <b>C</b>
5. <b>A</b>	6. <b>B</b>	7. <b>D</b>	8. <b>A</b>
9. <b>A</b>	10. <b>D</b>	11. <b>C</b>	12. <b>C</b>
13. <b>B</b>	14. <b>B</b>	15. <b>A</b>	16. <b>C</b>
17. <b>D</b>	18. <b>B</b>	19. <b>A</b>	20. <b>D</b>
21. <b>12</b>	22. <b>15</b>	23. <b>10</b>	24. <b>4</b>
25. <b>3</b>			

### PART –B (CHEMISTRY)

26. <b>D</b>	27. <b>D</b>	28. <b>B</b>	29. <b>B</b>
30. <b>B</b>	31. <b>A</b>	32. <b>D</b>	33. <b>D</b>
34. <b>B</b>	35. <b>B</b>	36. <b>B</b>	37. <b>D</b>
38. <b>B</b>	39. <b>B</b>	40. <b>B</b>	41. <b>B</b>
42. <b>D</b>	43. <b>A</b>	44. <b>B</b>	45. <b>A</b>
46. <b>14</b>	47. <b>37.84</b>	48. <b>0.176</b>	49. <b>0.568</b>
50. <b>100</b>			

### PART-C (MATHEMATICS)

51. <b>B</b>	52. <b>B</b>	53. <b>C</b>	54. <b>B</b>
55. <b>C</b>	56. <b>D</b>	57. <b>D</b>	58. <b>D</b>
59. <b>C</b>	60. <b>C</b>	61. <b>D</b>	62. <b>C</b>
63. <b>B</b>	64. <b>C</b>	65. <b>A</b>	66. <b>D</b>
67. <b>D</b>	68. <b>B</b>	69. <b>B</b>	70. <b>C</b>
71. <b>8</b>	72. <b>1</b>	73. <b>3</b>	74. <b>615</b>
75. <b>8</b>			



# HINTS AND SOLUTIONS

## PART -A (PHYSICS)

1. **B**

Sol. Conserving momentum

$$mv \hat{i} + m \left( \frac{v}{2} \hat{i} + \frac{v}{2} \hat{j} \right) = 2m (v_1 \hat{i} + v_2 \hat{j})$$

On solving

$$v_1 = \frac{3v}{4} \text{ and } v_2 = \frac{v}{4}$$

Change in K.E.

$$\left[ \frac{1}{2}mv^2 + \frac{1}{2}m \left( \frac{v}{2} \sqrt{2} \right)^2 \right] - \left[ \frac{1}{2}(2M) \left( \frac{9v^2}{16} + \frac{v^2}{16} \right) \right]$$

$$= \frac{3mv^2}{4} - \frac{5mv^2}{8} = \frac{mv^2}{8}$$

2. **A**

Sol.  $KE_{\max} = E - \phi$

$$= \frac{12400}{\lambda(\text{in } \text{\AA})} - \phi \quad (\text{in eV})$$

$$\therefore r = \frac{\sqrt{2mKE}}{eB}$$

$$KE_{\max} = \frac{r^2 e^2 B^2}{2m} \quad (\text{in J})$$

$$= \frac{r^2 e B^2}{2m} \quad (\text{in eV})$$

$$\therefore \phi = \frac{12400}{6561} - \frac{r^2 e B^2}{2m} = 1.1 \text{ eV}$$

3. **C**

Sol. Using equation of continuity

$$40 V_A = 20 V_B$$

$$\Rightarrow 2V_A = V_B$$

Using Bernoullies equation

$$P_A + \frac{1}{2} \rho V_A^2 = P_B + \frac{1}{2} \rho V_B^2$$

$$\Rightarrow P_A - P_B = \frac{1}{2} \rho (V_B^2 - V_A^2)$$

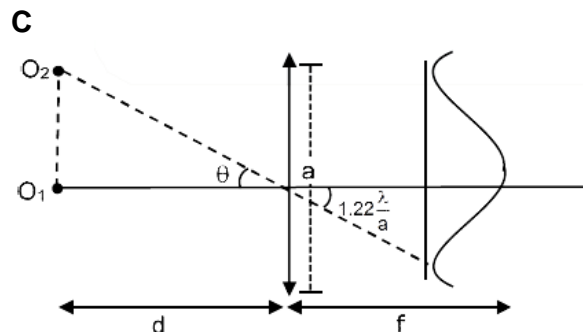
$$\Rightarrow \Delta P = \frac{1}{2} 1000 \left( V_B^2 - \frac{V_B^2}{4} \right)$$

$$\Rightarrow \Delta P = 500 \times \frac{3V_B^2}{4}$$

$$\Rightarrow V_B = \sqrt{\frac{(\Delta P) \times 4}{1500}} = \sqrt{\frac{(700) \times 4}{1500}} \text{ m/s}$$

$$\text{Volume flow rate} = 20 \times 100 \times V_B = 2732 \text{ cm}^3/\text{s}$$

4.  
Sol.



$$\theta = 1.22 \frac{\lambda}{a}$$

$$\text{Distance} = O_1O_2 = d\theta = 1.22 \frac{\lambda}{a} d$$

$$\text{Distance} = O_1O_2 = \frac{1.22 \times 5893 \times 10^{-10} \times 4 \times 10^8}{5} \approx 57.5 \text{ m}$$

$\therefore$  answer from options = 60 m (minimum distance)

5.  
Sol.

**A**  
Conserving momentum

$$\frac{m}{2} \frac{v}{2} + mv = \left(m + \frac{m}{2}\right) V_f$$

$$V_f = \frac{5mV}{4 \times \frac{3m}{2}} = \frac{5V}{6}$$

$V_f < v_{\text{orb}} (= v)$  thus the combined mass will go on to an elliptical path

$V_f < v_{\text{orb}} (= v)$

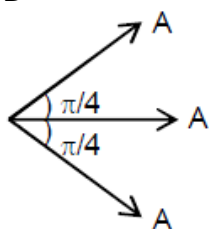
6. **B**

Sol. Molar heat capacity of A at constant volume =  $\frac{5R}{2}$

Molar heat capacity of B at constant volume =  $\frac{7R}{2}$

$$\text{Dividing both, } \frac{(C_v)_A}{(C_v)_B} = \frac{5}{7}$$

7. **D**  
Sol.



$$A_{\text{res}} = (\sqrt{2} + 1) A$$

$$I_{\text{res}} = (\sqrt{2} + 1)^2 I_0$$

$$= (3 + 2\sqrt{2}) I_0 = 5.8 I_{0s}$$

8. **A**  
Sol.

$$[ML^2T^{-2}]$$

$$[hc] = [ML^3T^{-2}]$$

$$[c] = [LT^{-1}]$$

$$[G] = [M^{-1}L^3T^{-2}]$$

9. **A**

Sol. Pitch =  $\frac{3}{6} = 0.5 \text{ mm}$

$$\text{L.C.} = \frac{0.5 \text{ mm}}{50} = \frac{1}{100} \text{ mm} = 0.01 \text{ mm}$$

$$= 0.001 \text{ cm}$$

10. **D**

Sol. M. I. about P =  $3 \left[ \frac{2}{5} M \left( \frac{d}{2} \right)^2 + M \left( \frac{d}{\sqrt{3}} \right)^2 \right] = \frac{13}{10} Md^2$

M. I. about B =  $2 \left[ \frac{2}{5} M \left( \frac{d}{2} \right)^2 + M(d^2) \right] + \frac{2}{5} M \left( \frac{d}{2} \right)^2 = \frac{23}{10} Md^2$

Now ratio =  $\frac{13}{23}$

11. **C**

Sol.  $W = \int \vec{F} \cdot d\vec{s}$

$$= (-x\hat{i} + y\hat{j}) \cdot (dx\hat{i} + dy\hat{j})$$

$$= \int_1^0 -x dx + \int_0^1 y dy$$

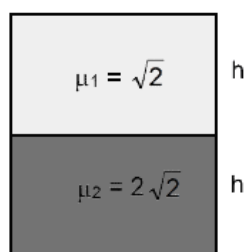
$$= -\frac{x^2}{2} \Big|_1^0 + \frac{y^2}{2} \Big|_0^1 = \left( 0 + \frac{1}{2} \right) + \left( \frac{1}{2} \right) = 1 \text{ J}$$

12. **C**

Sol.

$$d = \frac{h}{\sqrt{2}} + \frac{h}{2\sqrt{2}}$$

$$\Rightarrow d = \frac{h}{\sqrt{2}} \times \frac{3}{2} = \frac{3\sqrt{2}h}{4}$$



13. **B**

Sol.

$$\lambda = \frac{h}{\sqrt{2(KE)m}} \Rightarrow \lambda \propto \frac{1}{\sqrt{KE}}$$

$$\frac{\lambda}{\lambda/2} = \frac{\sqrt{KE_f}}{\sqrt{KE_i}}$$

$$4KE_i = KE_f$$

$$\Rightarrow \Delta E = 4KE_i - KE_i = 3KE = 3E$$

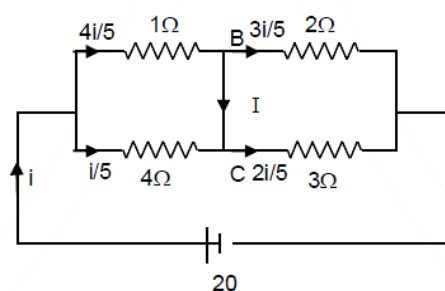
14. **B**

Sol.

$$R_{\text{eff}} = \frac{4}{5} + \frac{6}{5} = 2\Omega$$

$$i = \frac{20}{2} = 10A$$

$$I = \frac{4i}{5} - \frac{3i}{5} = +\frac{i}{5} = 2A$$



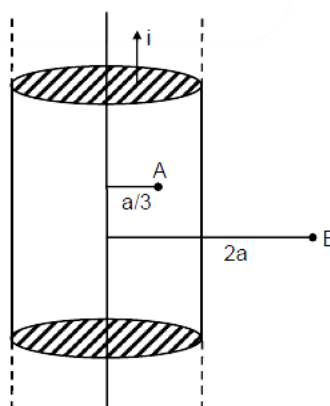
15. **A**

Sol.

$$B_A = \frac{\mu_0 i r}{2\pi a^2} = \frac{\mu_0 i \frac{a}{3}}{2\pi a^2} = \frac{\mu_0 i}{\pi a^2} \frac{a}{6} = \frac{\mu_0 i}{6\pi a}$$

$$B_B = \frac{\mu_0 i}{2\pi(2a)}$$

$$\frac{B_A}{B_B} = \frac{4}{6} = \frac{2}{3}$$



16. **C**

Sol. Magnetic field vectors associated with this electromagnetic wave are given by

$$\vec{B}_1 = \frac{E_0}{c} \hat{k} \cos(kx - \omega t) \text{ \& } \vec{B}_2 = \frac{E_0}{c} \hat{i} \cos(ky - \omega t)$$

$$\vec{F} = q\vec{E} + q(\vec{V} \times \vec{B})$$

$$= q(\vec{E}_1 + \vec{E}_2) + q(\vec{V} \times (\vec{B}_1 + \vec{B}_2))$$

By putting the value of  $\vec{E}_1, \vec{E}_2, \vec{B}_1$  &  $\vec{B}_2$

The net Lorentz force on the charged particle is

$$\vec{F} = qE_0 [0.8 \cos(kx - \omega t) \hat{i} + \cos(kx - \omega t) \hat{j} + 0.2 \cos(ky - \omega t) \hat{k}]$$

At  $t = 0$  and at  $x = y = 0$

$$\vec{F} = qE_0 [0.8 \hat{i} + \hat{j} + 0.2 \hat{k}]$$

17. **D**

Sol. Since  $\vec{p} \cdot \vec{r} = 0$

$\vec{E}$  must be antiparallel to  $\vec{p}$

$$\text{So, } \vec{E} = -\lambda(\vec{p})$$

Where  $\lambda$  is a arbitrary positive constant

$$\text{Now } \vec{A} = a\hat{i} + b\hat{j} + c\hat{k}$$

$$\vec{A} \parallel \vec{E}$$

$$\frac{a}{\lambda} = \frac{b}{3\lambda} = \frac{c}{-2\lambda} = k$$

$$\text{So, } \vec{A} = \lambda k(\hat{i} + 3\hat{j} - 2\hat{k})$$

18. **B**

Sol. (a) By work energy theorem

$$W_{\text{mag}} + W_{\text{ele}} = \frac{1}{2}m(2v)^2 - \frac{1}{2}m(v)^2$$

$$0 + qE_0 2a = \frac{3}{2}mv^2$$

$$E_0 = \frac{3}{4} \frac{mv^2}{qa}$$

$$\begin{aligned} \text{(b) Rate of work done at A} &= \text{power of electric force } A = qE_0 V \\ &= \frac{3}{4} \frac{mv^3}{a} \end{aligned}$$

$$\text{(c) at Q, } \frac{dw}{dt} = 0 \text{ for both forces}$$

$$\begin{aligned} \text{(d) } \Delta \vec{L} &= (-m2v2a\hat{k}) - (-ma\hat{k}) \\ |\Delta \vec{L}| &= 3mva \end{aligned}$$

19. **A**

Sol. For a solid sphere

$$E = \frac{\rho r}{3\epsilon_0} \quad ; \quad E_A = \frac{-\rho R}{2(3\epsilon_0)} \quad ; \quad |E_A| = \frac{-\rho R}{6\epsilon_0}$$

Electric field at point B =  $E_B = E_{1A} + E_{2A}$

$$E_{1A} = \text{Electric field due to solid sphere of radius } R \text{ at point B} = \frac{\rho R}{3\epsilon_0}$$

$E_{2A}$  = Electric field due to solid sphere of radius  $R/2$  (which having charge density  $-\rho$ )

$$E_{2A} = R/2 = -\frac{KQ' \times 4}{9R^2} = -\frac{\rho R}{54\epsilon_0}$$

$$E_B = E_{1A} + E_{2A} = \frac{\rho R}{3\epsilon_0} - \frac{\rho R}{54\epsilon_0} = \frac{17\rho R}{54\epsilon_0}$$

$$\left| \frac{E_A}{E_B} \right| = \frac{9}{17}$$

20. **D**

Sol. For process A – B

$$PV = nRT \quad ; \quad \text{as } P \text{ increases}$$

For process B – C

$$PV^\gamma = \text{Constant}$$

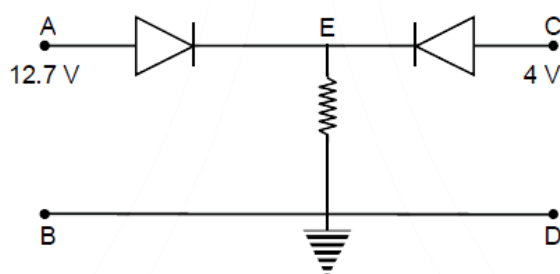
$$\Rightarrow TV^{\gamma-1} = \text{Constant}$$

For process C – A ; pressure is constant

$$V = kT$$

21. **12**

Sol.



$$\text{Let } V_B = 0$$

Right diode is reversed biased and left diode is forward biased

$$\therefore V_E = 12.7 - 0.7 = 12 \text{ Volt}$$

22. **15**

$$\text{Sol. } mg \frac{\ell}{2} \sin 30^\circ = \frac{1}{2} \frac{m\ell^2}{3} \omega^2$$

Solving,

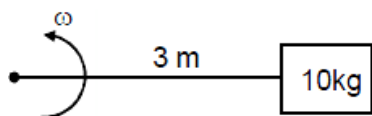
$$\omega^2 = 15 \quad ; \quad \omega = \sqrt{15}$$

23. **10**

Sol.  $100 = \frac{L(0.25)}{0.025} \times 10^3$   
 $\therefore L = 100 \times 10^{-4} \text{ H}$   
 $= 10 \text{ mH}$

24. **4**

Sol.



$$\frac{T}{A} = \sigma \quad \dots(1)$$

$$T = m\omega^2 \ell \quad \dots(2)$$

Solving,  
 $\omega = 4 \text{ rad/s}$

25. **3**

Sol.

$$x^2 = at^2 + 2bt + c$$

$$2xv = 2at + 2b$$

$$xv = at + b$$

$$v^2 + ax = a$$

$$ax = a - \left( \frac{at + b}{x} \right)^2$$

$$a = \frac{a(at^2 + 2bt + c) - (at + b)^2}{x^3}$$

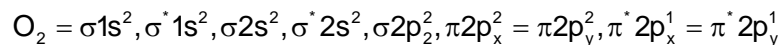
$$a = \frac{ac - b^2}{x^3} \quad ; \quad a \propto x^{-3}$$

PART -B (CHEMISTRY)

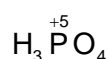
26. D

Sol. Magnetic moment = 1.73 BM

Unpaired electron = 1

Hence  $O_2^-, O_2^+$  have one unpaired electron.

27. D

Sol.  $H_2O_2^{-1}$        $H_2SO_3^{+4}$ In  $H_3PO_4$  phosphorus is in maximum oxidation state so cannot increase its oxidation number.

28. B

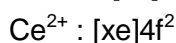
Sol. Number of geometrical isomers in square planar  $[PdFCIBr]^{2-}$  are 3Hence,  $n = 3$  $Fe^{3+} = 3d^5$ , according to CFT configuration planar is  $t_{2g}^{221}e_g^{00}$ 

$$\mu = \sqrt{n(n+2)} = 1.73 \text{ B.M}$$

$$CFSE = -0.4\Delta_0 \times n_{t_{2g}} + 0.6\Delta_0 \times n_{e_g}$$

$$= -0.4\Delta_0 \times 5 = -2.0\Delta_0$$

29. B

Sol.  $Eu^{2+} \rightarrow [xe]4f^2$ 

30. B

Sol.  $K_{\text{catalyst}} = K$ 

$$Ae^{-\frac{Ea_1}{RT_1}} = Ae^{-\frac{Ea_2}{RT_2}}$$

 $Ea_1$  = energy of activation in presence of catalyst

$$T_1 = 500 \text{ K}$$

$$T_2 = 700 \text{ K}$$

$$\frac{Ea_1}{T_1} = \frac{Ea_2}{T_2}$$

But  $Ea_1 = Ea_2 - 30$ 

$$\frac{Ea_2 - 30}{500} = \frac{Ea_2}{700}$$

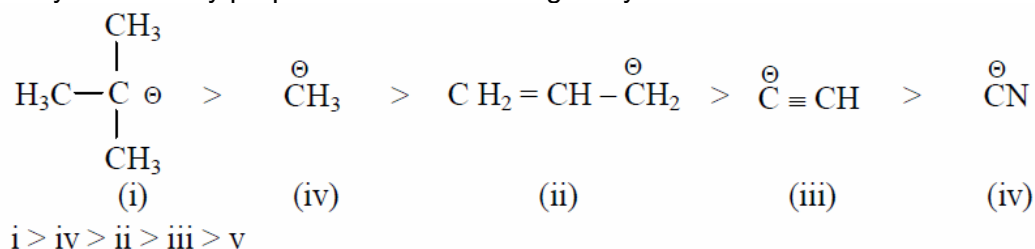


$$5E_{a2} = 7E_{a2} - 210$$

$$E_{a2} = \frac{210}{2} = 105 \text{ kJ/mole}$$

31. A

Sol. Basicity is inversely proportional to electronegativity.



32. D

Sol.  $\text{CCl}_4$  is a non conductor in solid and liquid phase.

33. D

Sol.  $2\pi r = n\lambda$ 

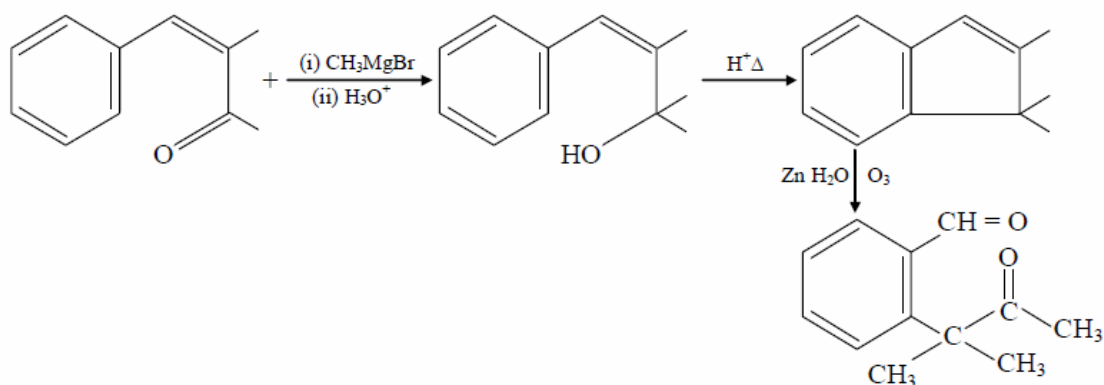
$$n = 4 \text{ \& } r = a_0 \frac{n^2}{Z} \Rightarrow 2\pi a_0 \frac{n^2}{Z} = n\lambda$$

$$2\pi \frac{4^2 a_0}{1} = 4\lambda$$

$$\lambda = 8\pi a_0$$

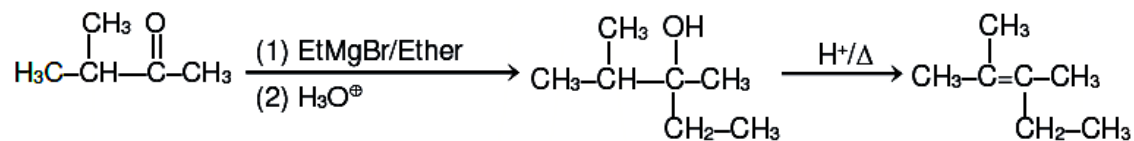
34. B

Sol.



35. B

Sol.

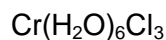


36. B

Sol.  $\text{Cr}(\text{H}_2\text{O})_6\text{Cl}_n$

$$(\mu_{\text{complex}})_{\text{spin}} = 3.8 \text{ B.M}$$

$$n = 3$$



Oxidation number of Cr should be +3

Compound so G.I so it will be  $[\text{Cr}(\text{H}_2\text{O})_4\text{Cl}_2]\text{Cl} \cdot 2\text{H}_2\text{O}$

IUPAC name = Tetraaquadichlorido chromium (III) chloride dihydrate

37. D

Sol. Non-metal oxides are acidic in nature

Alkali metal oxides are basic in nature

$\text{Al}_2\text{O}_3$  is amphoteric.

38. B

Sol.  $Q = [\text{Pb}^{2+}][\text{Cl}^-]^2$

$$= \left( \frac{300 \times 0.134}{400} \right) \left( \frac{100 \times 0.4}{400} \right)^2 = \frac{3 \times 0.134}{4} (0.1)^2$$

$$Q = 1.005 \times 10^{-3}$$

$$Q > K_{\text{sp}}$$

39. B

Sol. A – Aspartame

B – Saccharin

C – Sucralose

D – Alitame

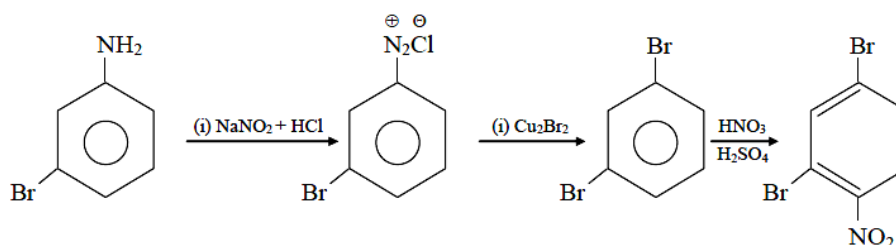
(i) A & D give positive test with ninhydrin because both have free carboxylic and amine group.

(ii) C form precipitate with  $\text{AgNO}_3$  because it has chlorine atoms.

(iii) B & D give positive test because both have S-atom.

40. B

Sol.



41. B

Sol. Aniline react lewis acid form anilinium complex. So phenol is most reactive among for nucleophilic substitution reaction.

42. D

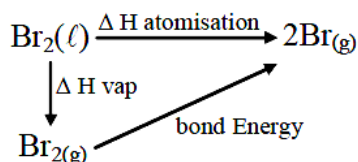
Sol. Radius of Boron is less than Radius of Be Hence IV statement is false. Rest are True.  
Statement

43. A

Sol. In isomers of Hydrocarbon heat of combustion depend upon their stability. Stability increase heat of combustion decrease.  
Stability  $a > b > c$   
Heat of combustion  $c > b > a$

44. B

Sol.

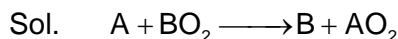


$$\Delta H_{\text{atomisation}} = \Delta H_{\text{Vap}} + \text{Bond Energy}$$

Hence.

$$x > y$$

45. A



$$\Delta G = -ve$$

Only above  $1400^\circ\text{C}$ 

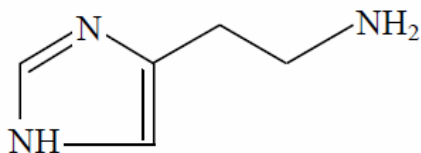
46. 14

Sol.  $d = 1.4 \text{ g/mL}$  $63\text{w/w}$ 

$$\text{Molarity} = \frac{63 \times 1.4}{63 \times 100} \times 1000 \text{ mole / litre} = 14 \text{ mole / L}$$

47. 37.84

Sol. Structure of Histamine is



$$\text{Molecular formula} = \text{C}_5\text{H}_9\text{N}_3$$

$$\text{Molecular mass} = 111$$

$$\% \text{ of N} = \frac{42}{111} \times 100 = 37.84\%$$

48. 0.176

Sol.  $\Delta T_f = 0.2$ 

$$\Delta T_f = i K_f m$$

$$i = 2 \text{ for NaCl}$$

$$0.2 = 2 \times 2 \times m$$

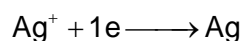
$$m = \frac{w}{58.5} \times \frac{1000}{600}$$

$$0.2 = 2 \times 2 \times \frac{w}{58.5} \times \frac{1000}{600}$$

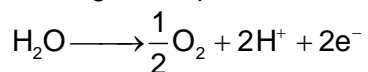
$$w = \frac{0.2 \times 58.5 \times 600}{4 \times 1000} = \frac{1.2 \times 58.5}{40} = 0.176$$

49. 0.568

Sol.  $[n_{\text{Ag}}]_{\text{deposit}} = \frac{108}{108} = 1 \text{ mole}$



If charge is required for 1 mole of Ag



2F charge deposit =  $\frac{1}{2}$  mole

1 F charge deposit =  $\frac{1}{4}$  mole

$$PV = nRT$$

$$V = \frac{1}{4} \times \frac{0.83 \times 273}{1} = 5.675 \text{ L}$$

50. 100

Sol. Given:  $10^{-3} \text{ M MgSO}_4$

i.e.  $10^{-3}$  mole  $\text{MgSO}_4$  present in 1 litre solution

$$n_{\text{MgSO}_4} = n_{\text{CaCO}_3}$$

$$\text{Mass of CaCO}_3 = 10^{-3} \times 100$$

$$\text{ppm (in terms of CaCO}_3) = \frac{10^{-3} \times 100}{1000} \times 10^6 = 100$$

PART-C (MATHEMATICS)

51. B

Sol. 
$$\frac{1}{2^4} + \frac{2}{16} + \frac{3}{48} + \dots \infty$$

$$= 2^{\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots \infty} = \sqrt{2}$$

52. B

Sol. Mean  $(x_i - 5) = \frac{\sum (x_i - 5)}{10} = 1$   
 $\therefore \lambda = \{\text{Mean}(x_i - 5)\} + 2 = 3$   
 $\mu = \text{var}(x_i - 5) = \frac{\sum (x_i - 5)^2}{10} - \frac{\sum (x_i - 5)^2}{10} = 3$

53. C

Sol. 
$$e_1 = \sqrt{1 - \frac{4}{18}} = \sqrt{\frac{7}{9}} = \frac{\sqrt{7}}{3}$$

$$e_2 = \sqrt{1 + \frac{4}{9}} = \sqrt{\frac{13}{9}} = \frac{\sqrt{13}}{3}$$

$$15e_1^2 + 3e_2^2 = k \Rightarrow k = 15\left(\frac{7}{9}\right) + 3\left(\frac{13}{9}\right)$$

$$\therefore k = 16$$

54. B

Sol. 
$$|A| = \begin{vmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{vmatrix} = ((9+4) - 1(3-4) + 2(-1-3)) = 13+1-8 = 6$$

$$|\text{adj}B| = |\text{adjadj}A| = |A|^{(n-1)^2} = |A|^4 = (36)^2$$

$$|C| = |BA| = 3^3 \times 6$$

$$\frac{|\text{adj}B|}{|C|} = \frac{36 \times 36}{3^3 \times 6} = 8$$

55. C

Sol. LHL =  $a + 3$

$f(0) = b$

$$\text{RHL} = \lim_{h \rightarrow 0} \left( \frac{(1+3h)^{\frac{1}{3}} - 1}{h} \right) = 1$$

$$\begin{aligned}\therefore a &= -2 \\ b &= 1 \\ \therefore a + 2b &= 0\end{aligned}$$

56. D

Sol. Number of numbers

$$= 8 \times 8 \times 7 \times 6 = 2688 = 336k \Rightarrow k = 8$$

			2	
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57. D

Sol. AA + ABA + BAA + ABBA + BBAA + BABA

$$= \frac{1}{4} + \frac{1}{8} + \frac{1}{8} + \frac{1}{16} + \frac{1}{16} + \frac{1}{16} = \frac{11}{16}$$

58. D

Sol. Let  $e^x = t \in (0, \infty)$

$$\text{Given equation } t^4 + t^3 - 4t^2 + t + 1 = 0$$

$$t^2 + t - 4 + \frac{1}{t} + \frac{1}{t^2} = 0$$

$$\left(t^2 + \frac{1}{t^2}\right) + \left(t + \frac{1}{t}\right) - 4 = 0$$

$$\text{Let } t + \frac{1}{t} = \alpha$$

$$(\alpha^2 - 2) + \alpha - 4 = 0$$

$$\alpha^2 + \alpha - 6 = 0$$

$$\alpha = -3, 2$$

$$\Rightarrow \alpha = 2$$

$$\Rightarrow e^x + e^{-x} = 2$$

$$x = 0 \text{ only solution}$$

59. C

Sol. Let thickness = x cm

$$\text{Total volume } v = \frac{4}{3}\pi(10+x)^3$$

$$\frac{dv}{dt} = 4\pi(10+x)^2 \frac{dx}{dt} \quad \dots\dots\dots(i)$$

$$\text{Given } \frac{dv}{dt} = 50 \text{ cm}^3 / \text{min}$$

$$\text{At } x = 5 \text{ cm}$$

$$50 = 4\pi(10+5)^2 \frac{dx}{dt}$$

$$\frac{dx}{dt} = \frac{1}{18\pi} \text{ cm / min}$$

60. C

Sol. 
$$\int_0^{\pi} \frac{x \sin^8 x}{\sin^8 x + \cos^8 x} + \frac{(2\pi - x) \sin^8 x}{\sin^8 x + \cos^8 x} dx = \int_0^{\pi} \frac{2\pi \sin^8 x}{\sin^8 x + \cos^8 x} dx$$

$$= 2\pi \int_0^{\pi/2} \frac{\sin^8 x}{\sin^8 x + \cos^8 x} + \frac{\cos^8 x}{\sin^8 x + \cos^8 x} dx$$

$$= 2\pi \int_0^{\pi/2} 1 dx = 2\pi \times \frac{\pi}{2} = \pi^2$$

61. D

Sol.  $x^2 + (y-1)^2 = x^2 + (y+2)^2$

$$-2y + 1 = 4y + 4$$

$$6y = -3 \Rightarrow y = -\frac{1}{2}$$

$$x^2 + y^2 = \frac{25}{4} \Rightarrow x^2 = \frac{24}{4} = 6$$

$$\Rightarrow z = \pm\sqrt{6} - \frac{i}{2}$$

$$|z + 3i| = \sqrt{6 + \frac{25}{4}} = \sqrt{\frac{49}{4}}$$

$$|z + 3i| = \frac{7}{2}$$

62. C

Sol.  $\sqrt{5}$  is not an integer and 5 is not an irrational number  $\sim (p \vee q) = \sim p \wedge \sim q$

63. B

Sol. D (2, 2)

Point of intersection  $P\left(-\frac{1}{5}, \frac{2}{5}\right)$  equation of line DP  $8x - 11y + 6 = 0$

64. C

Sol.  $\Delta = 0 \Rightarrow \begin{vmatrix} 1 & 4 & -2 \\ 1 & 7 & -5 \\ 1 & 5 & \alpha \end{vmatrix} = 0$

$$(7\alpha + 25) - (4\alpha + 10) + (-20 + 14) = 0$$

$$3\alpha + 9 = 0 \Rightarrow \alpha = -3$$

Also  $D_z = 0 \Rightarrow \begin{vmatrix} 1 & 4 & 1 \\ 1 & 7 & \beta \\ 1 & 5 & 5 \end{vmatrix} = 0$

$$1(35 - 5\beta) - (15) + 1(4\beta - 7) = 0$$

$$\beta = 13$$

65. A

Sol. Let use LMVT for  $x \in [a, c]$

$$\frac{f(c) - f(a)}{c - a} = f'(\alpha), \alpha \in (a, c)$$

also use LMVT for  $x \in [c, b]$

$$\frac{f(b) - f(c)}{b - c} = f'(\beta), \beta \in (c, b)$$

$\therefore f''(x) < 0 \Rightarrow f'(x)$  is decreasing

$$f'(\alpha) > f'(\beta)$$

$$\frac{f(c) - f(a)}{c - a} > \frac{f(b) - f(c)}{b - c}$$

$$\frac{f(c) - f(a)}{f(b) - f(c)} > \frac{c - a}{b - c} \quad (\because f(x) \text{ is increasing})$$

66. D

$$\begin{aligned} \text{Sol. } & \cos^3 \frac{\pi}{8} \left[ 4 \cos^3 \frac{\pi}{8} - 3 \cos \frac{\pi}{8} \right] + \sin^3 \frac{\pi}{8} \left[ 3 \sin \frac{\pi}{8} - 4 \sin^3 \frac{\pi}{8} \right] \\ &= 4 \cos^6 \frac{\pi}{8} - 4 \sin^6 \frac{\pi}{8} - 3 \cos^4 \frac{\pi}{8} + 3 \sin^4 \frac{\pi}{8} \\ &= 4 \left[ \left( \cos^2 \frac{\pi}{8} - \sin^2 \frac{\pi}{8} \right) \right] \left[ \left( \sin^4 \frac{\pi}{8} + \cos^4 \frac{\pi}{8} + \sin^2 \frac{\pi}{8} \cos^2 \frac{\pi}{8} \right) \right] - 3 \left[ \left( \cos^2 \frac{\pi}{8} - \sin^2 \frac{\pi}{8} \right) \right] \\ &= \cos \frac{\pi}{4} \left[ 4 \left( 1 - \sin^2 \frac{\pi}{8} \cos^2 \frac{\pi}{8} \right) - 3 \right] = \frac{1}{\sqrt{2}} \left[ 1 - \frac{1}{2} \right] = \frac{1}{2\sqrt{2}} \end{aligned}$$

67. D

Sol. Equation of family of circle

$$(x - 0)^2 + (y - 4)^2 + \lambda x = 0$$

$\Rightarrow$  passes  $(2, 0)$

$$4 + 16 + 2\lambda = 0 \Rightarrow \lambda = -10$$

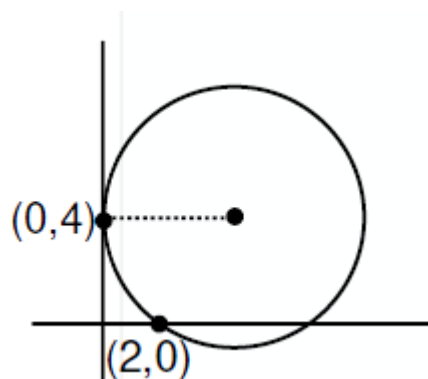
$$x^2 + y^2 - 10x - 8y + 16 = 0$$

centre  $(5, 4)$ .  $R = \sqrt{25 + 16 - 16} = 5$

Check the options.

Option (4)

$$\left| \frac{4 \times 5 + 3 \times 4 - 8}{5} \right| = \frac{24}{5} \neq 5$$



68. B



Sol.  $\int_0^1 (a + bx + cx^2) dx = ax + \frac{bx^2}{2} + \frac{cx^3}{3} \Big|_0^1 = a + \frac{b}{2} + \frac{c}{3}$

$$f(1) = a + b + c$$

$$f(0) = a$$

$$f\left(\frac{1}{2}\right) = a + \frac{b}{2} + \frac{c}{4}$$

$$\begin{aligned} \text{Now } \frac{1}{6} \left( f(1) + f(0) + 4f\left(\frac{1}{2}\right) \right) &= \frac{1}{6} \left( a + b + c + a + 4 \left( a + \frac{b}{2} + \frac{c}{4} \right) \right) \\ &= \frac{1}{6} (6a + 3b + 2c) = a + \frac{b}{2} + \frac{c}{3} \end{aligned}$$

69. B

Sol.  $f'(x) = \tan^{-1}(\sec x + \tan x) = \tan^{-1}\left(\frac{1 + \sin x}{\cos x}\right)$

$$= \tan^{-1} \left( \frac{1 - \cos\left(\frac{\pi}{2} + x\right)}{\sin\left(\frac{\pi}{2} + x\right)} \right) = \tan^{-1} \left( \frac{2 \sin^2\left(\frac{\pi}{4} + \frac{x}{2}\right)}{2 \sin\left(\frac{\pi}{4} + \frac{x}{2}\right) \cos\left(\frac{\pi}{4} + \frac{x}{2}\right)} \right)$$

$$= \tan^{-1} \left( \tan\left(\frac{\pi}{4} + \frac{x}{2}\right) \right) = \frac{\pi}{4} + \frac{x}{2}$$

$$(f'(x)) dx = \frac{\pi}{4} + \frac{x}{2} dx$$

$$f(x) = \frac{\pi}{4}x + \frac{x^2}{4} + c$$

$$f(0) = c = 0 \Rightarrow f(x) = \frac{\pi}{4}x + \frac{x^2}{4}$$

$$\text{So } f(1) = \frac{\pi + 1}{4}$$

70. C

Sol.  $\int \left( \frac{x-3}{x+4} \right)^{\frac{-6}{7}} \frac{1}{(x+4)^2} dx$

$$\text{Let } \frac{x-3}{x+4} = t^7,$$

$$\frac{7}{(x+4)^2} dx = 7t^6 dt$$

$$\int t^{-6} t^6 dt = t + c$$

71. 8

Sol. Let  $A(1, -1, 3), B(2, -4, 11)$

$$\overrightarrow{AB} = \hat{i} - 3\hat{j} + 8\hat{k}$$

$C(-1, 2, 3), D(3, -2, 10)$

$$\overrightarrow{CD} = 4\hat{i} - 4\hat{j} + 7\hat{k}$$

$$\text{projection of } \overrightarrow{AB} \text{ on } \overrightarrow{CD} = \frac{\overrightarrow{AB} \cdot \overrightarrow{CD}}{|\overrightarrow{CD}|}$$

$$= \left( \frac{4 + 12 + 56}{\sqrt{16 + 16 + 49}} \right) = \frac{72}{9} = 8$$

72. 1

$$\text{Sol. } \begin{vmatrix} a+1 & a & a \\ a & a+1 & a \\ a & a & a+1 \end{vmatrix} = 0 \Rightarrow a+1+a+a=0$$

$$\Rightarrow a = -\frac{1}{3}$$

$$\vec{P} = \frac{2}{3}\hat{i} - \frac{1}{3}\hat{j} - \frac{1}{3}\hat{k}$$

$$\vec{Q} = \frac{1}{3}(-\hat{i} + 2\hat{j} - \hat{k})$$

$$\vec{R} = \frac{1}{3}(-\hat{i} - \hat{j} + 2\hat{k})$$

$$\vec{P} \cdot \vec{Q} = \frac{1}{9} \begin{vmatrix} i & j & k \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{vmatrix} = \frac{1}{9}(i(4-1) - j(-2-1) + k(1+2))$$

$$= \frac{1}{9}(3i + 3j + 3k) = \frac{i+j+k}{3}$$

$$|\vec{R} \times \vec{Q}| = \frac{1}{3}\sqrt{3} \Rightarrow |\vec{R} \times \vec{Q}|^2 = \frac{1}{3}$$

$$3(\vec{P} \times \vec{Q})^2 - \lambda |\vec{R} \times \vec{Q}|^2 = 0$$

$$3 \cdot \frac{1}{9} - \lambda \cdot \frac{1}{3} = 0 \Rightarrow \lambda = 1$$

73. 3

$$\text{Sol. } \frac{dy}{dx} = (1+x) + \left( \frac{y-3}{1+x} \right)$$

$$\frac{dy}{dx} - \frac{1}{(1+x)}y = (1+x) - \frac{3}{(1+x)}$$

$$\text{I.F.} = e^{-\int \frac{1}{(1+x)} dx} = \frac{1}{(1+x)}$$

$$\therefore \frac{d}{dx} \left( \frac{y}{1+x} \right) = 1 - \frac{3}{(1+x)^2}$$

$$\frac{y}{1+x} = x + 3(1+x)^{-1} + c$$

$$y = (1+x) \left[ x + \frac{3}{(1+x)} + c \right]$$

$$\therefore \text{ at } x=2, y=0 \therefore 0 = 3(2+1+c) \Rightarrow c = -3$$

$$\therefore \text{ at } x=3, y=3$$

74. 615

Sol. General term  $\frac{10!}{\alpha! \beta! \gamma!} x^{\beta+2\gamma}$

for coefficient of  $x^4 \Rightarrow \beta + 2\gamma = 4$

$$\gamma = 0, \beta = 4, \alpha = 6 \quad \Rightarrow \quad \frac{10!}{6!4!0!} = 210$$

$$\gamma = 1, \beta = 2, \alpha = 7 \quad \Rightarrow \quad \frac{10!}{7!2!1!} = 360$$

$$\gamma = 2, \beta = 0, \alpha = 8 \quad \Rightarrow \quad \frac{10!}{8!0!2!} = 45$$

Total = 615

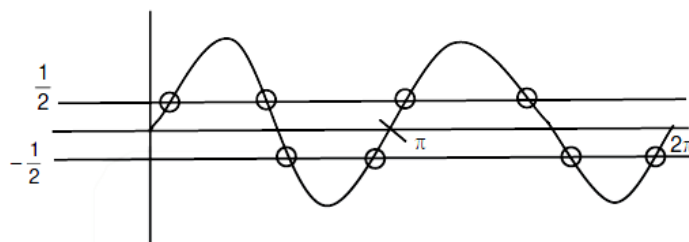
75. 8

Sol.  $\log_{1/2} |\sin x| = 2 - \log_{1/2} |\cos x|$

$$\log_{1/2} |\sin x \cos x| = 2$$

$$|\sin x \cos x| = \frac{1}{4}$$

$$\sin 2x = \pm \frac{1}{2}$$



Number of solution = 8.