FIITJEE Solutions to JEE(Main)-2020

Test Date: 7th January 2020 (First Shift)

PHYSICS, CHEMISTRY & MATHEMATICS

Paper - 1

Time Allotted: 3 Hours Maximum Marks: 300

Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

Important Instructions:

- 1. The test is of 3 hours duration.
- 2. This **Test Paper** consists of **75** questions. The maximum marks are **300**.
- 3. There are *three* parts in the question paper A, B, C consisting of *Physics*, *Chemistry* and *Mathematics* having 25 questions in each part of equal weightage out of which 20 questions are MCQs and 5 questions are numerical value based. Each question is allotted **4 (four)** marks for correct response.
- 4. **(Q. No. 01 20, 26 45, 51 70)** contains 60 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- 5. **(Q. No. 21 25, 46 50, 71 75)** contains 15 Numerical based questions with answer as numerical value. Each question carries **+4 marks** for correct answer. There is no negative marking.
- 6. Candidates will be awarded marks as stated above in **instruction No.3** for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer box.
- 7. There is only one correct response for each question. Marked up more than one response in any question will be treated as wrong response and marked up for wrong response will be deducted accordingly as per instruction 6 above.

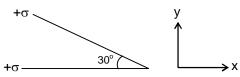
PART - A (PHYSICS)

- 1. A polarizer-analyser set is adjusted such that the intensity of light coming out of the analyser is just 10% of the original intensity. Assuming that the polarizer-analyser set does not absorb any light, the angle by which the analyser need to be rotated further to reduce the output intensity to be zero is
 - (A) 18.4°

(B) 45°

(C) 71.6°

- (D) 90°
- 2. Two infinite planes each with uniform surface charge density $+\sigma$ are kept in such a way that the angle between them is 30°. The electric field in the region shown between them is given by:



(A) $\frac{\sigma}{2\epsilon_0} \left[\left(1 - \frac{\sqrt{3}}{2} \right) \hat{y} - \frac{\hat{x}}{2} \right]$

 $(B) \ \frac{\sigma}{2\epsilon_0} \Bigg[\bigg(1 + \sqrt{3} \, \bigg) \hat{y} - \frac{\hat{x}}{2} \Bigg]$

(C) $\frac{\sigma}{2\epsilon_0} \left[\left(1 + \sqrt{3} \right) \hat{y} + \frac{\hat{x}}{2} \right]$

- $\text{(D) } \frac{\sigma}{\epsilon_0} \Bigg[\Bigg(1 + \frac{\sqrt{3}}{2} \Bigg) \hat{y} + \frac{\hat{x}}{2} \Bigg]$
- 3. A long solenoid of radius R carries a time (t) dependent current I (t) = I_0t (1 t). A ring of radius 2R is placed cordially near its middle. During the time internal $0 \le t \le 1$, the induced current (I_R) and the induced EMF (V_R) in the ring changes as:
 - (A) At t = 0.25 direction of I_R reverses and V_R is maximum.
 - (B) Direction of I_R remains unchanged and V_R is zero at t=0.25
 - (C) Direction of I_R remains unchanged and V_R is maximum at t=0.5
 - (D) At t = 0.5 direction of I_R reverses and V_R is zero.
- 4. Visible light of wavelength 6000×10^{-8} cm falls normally on a single slit and produces a diffraction pattern. It is found that the second diffraction minimum is at 60° from the central maximum. If the first minimum is produced at θ_1 then θ_1 is close to:
 - (A) 20°

(B) 30°

(C) 25°

- (D) 45°
- 5. A parallel plate capacitor has plates of area A separated by distance 'd' between them. It is filled with a dielectric which has a dielectric constant that varies as $k(n) = k(1 + \alpha n)$ where 'x' is he distance measured from one of the plates.



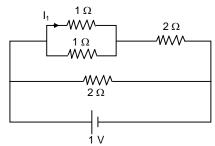
- If $(\alpha d) \ll 1$, the total capacitance of the system is best given by the expression:
- (A) $\frac{AK\epsilon_0}{d} \left(1 + \frac{\alpha d}{2}\right)$

(B) $\frac{A\epsilon_0 K}{d} \left(1 + \frac{\alpha^2 d^2}{2} \right)$

(C) $\frac{AK\epsilon_0}{d}$ (1+ αd)

(D) $\frac{A\epsilon_0 K}{d} \left[1 + \left(\frac{\alpha d}{2} \right)^2 \right]$

- 6. The current I_1 (in A) flowing through 1 Ω resistor in the following circuit is
 - (A) 0.25
 - (B) 0.4
 - (C) 0.2
 - (D) 0.5



- 7. The radius of gyration of a uniform rod of length ℓ , about an axis passing through a point
 - $\frac{\ell}{4}$ away from the centre of the rod, an perpendicular to it is:
 - (A) $\frac{1}{8}\ell$

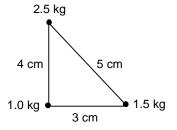
(B) $\sqrt{\frac{7}{48}} \ell$

(C) $\frac{1}{4}\ell$

- (D) $\sqrt{\frac{3}{9}} \ell$
- 8. Three point particles of masses 10 kg, 1.5 kg and 2.5 kg are placed at there corners of a right angle triangle of sides 4.0 cm, 3.0 ;cm and 5.0 cm as shown in the figure. The centre of mass of the system is at a point:



- (A) 0.6 cm right and 2.0 cm above 1 kg mass.
- (B) 2.0 cm right and 0.9 cm above 1 kg mass.
- (C) 1.5 cm right and 1.2 cm above 1 kg mass.
- (D) 0.9 cm right and 2.0 cm above 1 kg mass.



- 9. Consider a circular coil of wire carrying constant current I, forming a magnetic dipole. The magnetic flux through an infinite plane that contains the circular coil and excluding the circular coil area is given by ϕ . The magnetic flux through the area is given by ϕ_0 . Which of the following is correct?
 - (A) $\phi_i = -\phi_0$

(B) $\phi_i > \phi_0$

(C) $\phi_i = \phi_0$

- (D) $\phi_i < \phi_0$
- 10. As shown in the figure, a bob of mass m is tied by a massless string whose other end portion is wound on a fly wheel (disc) of radius r and mass m. When released from rest the bob starts falling vertically. When it has covered a distance of h, the angular speed of the wheel will be



(A) $r\sqrt{\frac{3}{4gh}}$

(B) $\frac{1}{r} \sqrt{\frac{2gh}{3}}$

- (D) $\frac{1}{r}\sqrt{\frac{4gh}{3}}$
- If we need a magnification of 375 from a compound microscope of tube length 150 mm 11. and an objective of focal length 5 mm, the focal length of the eye piece should be close
 - (A) 22 mm

(B) 33 m

(C) 12 m

(D) 2 mm

12.	Two moles of an ideal of	gas with $\frac{C_P}{C_V}$ =	$\frac{5}{3}$ are mixed	with 3 moles of	another ideal	gas with
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$$\frac{C_P}{C_V} = \frac{4}{3}$$
. The value of $\frac{C_P}{C_V}$ for the mixture is:

(A) 1.42

(B) 1.47

(C) 1.45

(D) 1.50

13. Speed of a transverse wave on a straight wire (mass 6.0 g, length 60 cm and area of cross- section 1.0 mm²) is 90 ms⁻¹. If the young's modulus of wire is 16×10^{11} Nm⁻², the extension of wire over its natural length is:

(A) 0.03 mm

(B) 0.01 mm

(C) 0.02 mm

(D) 0.04 mm

14. A litre of dry air at STP expands adiabatically to a volume of 3 litres. If $\gamma = 1.40$, the work done by air is: (3^{1.4} = 4.6555) [Take air to be an ideal gas]

(A) 48 J

(B) 90.5 J

(C) 100.8 J

(D) 60.7 J

15. A satellite of mass m is launched vertically upwards with an initial speed u from the surface of the earth. After it reaches height R (R = radius of the earth), it ejects a rocket of mass $\frac{m}{10}$ so that subsequently the satellite moves in a circular orbit. The kinetic energy of the rocket is (G is the gravitational constant; M is the mass of the earth)

(A) $\frac{m}{20} \left(u - \sqrt{\frac{2GM}{3R}} \right)^2$

(B) $\frac{3 \text{ m}}{8} \left(u + \sqrt{\frac{5GM}{6R}} \right)^2$

(C) $\frac{m}{20} \left(u^2 - \frac{113}{200} \frac{GM}{R} \right)$

(D) $5 \text{ m} \left(u^2 - \frac{119}{200} \frac{GM}{R} \right)$

16. The time period of revolution of electron in its ground state orbit in a hydrogen atom is 1.6×10^{-16} s. The frequency of revolution of the electron is its first excited state (in s⁻¹) is

(A) 7.8×10^{14}

(B) 1.6×10^{14}

(C) 6.2×10^{15}

(D) 5.6×10^{12}

17. A LCR circuit behaves like a damped harmonic oscillator. Comparing it with a physical spring-mass damped oscillator having damping constant 'b', the connect equivalence would be:

(A) $L \leftrightarrow \frac{1}{b}, C \leftrightarrow \frac{1}{m}, R \leftrightarrow \frac{1}{k}$

(B) $L \leftrightarrow k$, $C \leftrightarrow b$, $R \leftrightarrow m$

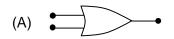
 $(C) \; L \leftrightarrow m, \; C \leftrightarrow \frac{1}{k}, \; R \leftrightarrow b$

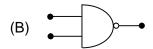
(D) L \leftrightarrow m, C \leftrightarrow k, R \leftrightarrow b

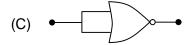
18. If the magnetic field in a plane electromagnetic wav is given by $\vec{B} = 3 \times 10^{-8} \sin(1.6 \times 10^3 \, \text{x} + 48 \times 10^{10} \, \text{t})$ j T, then what will be expression for electric field?

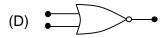
- (A) $\vec{E} = (60 \sin (1.6 \times 10^3 x + 48 \times 10^{10} t) \hat{k} V / m)$
- (B) $\vec{E} = (3 \times 10^{-8} \sin (1.6 \times 10^{3} x + 48 \times 10^{10} t) \hat{i} \text{ V / m})$
- (C) $\vec{E} = (9 \sin (1.6 \times 10^3 x + 48 \times 10^{10} t) \hat{k} \text{ V / m})$
- (D) $\vec{E} = (3 \times 10^{-8} \sin (1.6 \times 10^{3} x + 48 \times 10^{10} t) \hat{j} \text{ V / m})$

19. Which of the following given a reversible operation?







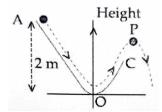


- 20. A 60 HP electric motor lifts an elevator having a maximum total load capacity of 2000 kg. If the frictional force on the elevator is 4000 N, the speed of the elevator at full load is close to: $(1 \text{ HP} = 746 \text{ W}, \text{ g} = 10 \text{ ms}^{-2})$
 - (A) 1.5 ms^{-1}

(B) 2.0 ms⁻¹

(C) 1.7 m/s⁻¹

- (D) 1.9 m/s⁻¹
- 21. A Carnot engine operates between two reservoirs of temperatures 900 K and 300 K. The engine performs 1200 J of work per cycle. The heat energy (in J) delivered by the engine to the low temperature reservoir, in a cycle is ______.
- 22. A loop ABCDEFA of straight edges has six corner points A (0, 0, 0), B (5, 0, 0), C(5, 5, 0), D(0, 5, 0), E(0, 5, 5) and F(0, 0, 5). The magnetic field in this region in $\vec{B} = (3\hat{i} + 4\hat{k})T$. The quantity of flux through the loop ABCDEFA (in Wb) is ______.
- 23. A non-isotropic solid metal cube has coefficients of linear expansion as: 5×10^{-5} / °C along the x = axis and 5×10^{-6} /°C along the y and the z-axis. If coefficient of volume expansion of the solid C × 10^{-6} /°C then the value of C is _____.
- 24. A particle (m = 1 kg) slides down a frictionless track (AOC) starting from rest of a point A (height 2 m). After reaching C, the particle continues to move freely in air as a projectile. When it leading its highest point P(height 1 m) the kinetic energy of the particle (in J) is: (Figure drawn is schematic and not to scale (take g = 10 ms⁻²)



25. A beam of electromagnetic radiation of intensity 6.4×10^{-5} W/cm² is comprised of wavelength, $\lambda = 310$ nm. It falls normally on a metal (work function $\varphi = 2$ eV) of surface area 1 cm². If one in 10^3 photons ejects an electron, total number of electrons ejected in is 10^x . (h_c = 1240 eVnm 1 eV = 1.6×10^{-19} J), then x is ______.

PART -B (CHEMISTRY)

26.	The relative	strenath	of interior	nic/interm	olecular :	forces in	decreasin	a order	ic
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- (A) ion-dipole > dipole-dipole > ion-ion
- (B) dipole-dipole > ion-dipole > ion- ion
- (C) ion-ion > ion-dipole > dipole-dipole
- (D) ion-dipole > ion-ion > dipole-dipole

27. Oxidation number of potassium in K₂O, K₂O₂ and KO₂ respectively is

(A) +1, +2 and +4

(B) +2, +1 and $+\frac{1}{2}$

(C) +1, +1 and +1

(D) +1, +4 and +2

28. At 35°C, the vapour pressure of CS₂ is 512 mm of Hg and that of acetone is 344 mm of Hg. A solution of CS₂ in acetone has a total vapour pressure of 600 mm of Hg. The false statement among the following is

- (A) CS₂ and acetone are less attracted to each other than to themselves
- (B) Heat must be absorbed in order to produce the solution at 35°C
- (C) Raoult's law is not obeyed by this system
- (D) a mixture of 100 mL CS₂ and 100 mL acetone has a volume of < 200 mL
- 29. The atomic radius of Ag is closest to
 - (A) Ni

(B) Cu

(C) Au

(D) Ha

(A) $CHCI_3 < CH_4 = CCI_4$

(B) $CCI_4 < CH_4 < CHCI_3$

(C) $CH_4 = CCI_4 < CHCI_3$

(D) $CH_4 < CCI_4 < CHCI_3$

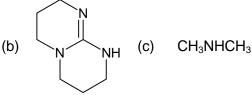
- (A) less efficient as it exchanges only anions
- (B) more efficient as it can exchange only cations
- (C) less efficient as the resin cannot be regenerated
- (D) more efficient as it can exchange both cation as well as anions

32. Amongst the following statements, that which was not proposed by Dalton was

- (A) matter consists of invisible atoms
- (B) when gases combine or reproduced in a chemical reaction they do so in a simple ratio by volume provided all gases are at the same temperature & pressure
- (C) chemical reactions involve reorganisation of atoms. These are neither created nor destroyed in a chemical reaction
- (D) All the atoms of a given element have identical properties including identical mass. Atoms of different elements differ in mass

33. The increasing order of pK_b for the following compounds will be

(a) $NH_2 - CH = NH_2$



(A) b < c < a

(B) c < a < b

(C) b < a < c

(D) a < b < c

34. What is the product of following reaction?

Hex
$$-3$$
 - ynal $\xrightarrow{\text{(ii) NaBH}_4}$ $\xrightarrow{\text{(iii) PBr}_3}$ $\xrightarrow{\text{(iii) Mg/ether}}$ $\xrightarrow{\text{(iv) CO}_2/\text{H}_3\text{O}^+}$

(A) COOH

- (B) COOH
- (C) COOH
- (D) COOH

35. The number of orbitals associated with quantum number n = 5, $m_s = +\frac{1}{2}$ is

(A) 15

(B) 11

(C) 50

(D) 25

(A) scrap iron and pig iron

(B) wrought iron

(C) cast iron

(D) pig iron

37. The theory that can completely/properly explain the nature of bonding in [Ni(CO)₄] is

(A) Werner's theory

- (B) Crystal field theory
- (C) Molecular orbital theory
- (D) Valence bond theory

38. The IUPAC name of the complex is [Pt(NH₃)₂Cl(NH₂CH₃)]Cl is

- (A) Diamminechlorido(aminomethane)platinum(II)chloride
- (B) Diamminechlorido(methanamine)platinum(II)chloride
- (C) Diammine(methanamine)chlorido platinum(II)chloride
- (D) Bisammine (methanamine) chloride platinum (II) chloride

39. 1-methyl ethylene oxide when treated with an excess of HBr, produces

(A)
$$\longrightarrow$$
 $\stackrel{Br}{\underset{Br}{}}$

40. Consider the following reaction:

The product 'X' is used

- (A) in protein estimation as an alternative to ninhydrin
- (B) as food grade colourant
- (C) in laboratory test for phenols
- (D) in acid-base titration as an indicator

41. Match the following

Column – I	Column – II			
(i) Riboflamin	(a) Beriberi			
(ii) Thiamine	(b) Scurvy			
(iii) Pyridoxine	(c) Cheilosis			
(iv) Ascorbic acid	(d) Convulsions			
(A) $i \rightarrow c$, $ii \rightarrow a$, $iii \rightarrow d$, $iv \rightarrow b$	(B) $i \rightarrow c$, $ii \rightarrow d$, $iii \rightarrow a$, $iv \rightarrow b$			
(C) $i \rightarrow a$, $ii \rightarrow d$, $iii \rightarrow c$, $iv \rightarrow b$	(D) $i \rightarrow d$, $ii \rightarrow b$, $iii \rightarrow a$, $iv \rightarrow c$			

42. Given that the standard potential (E°) of Cu²+/Cu and Cu+/Cu are 0.34 V and 0.522 V respectively, the E° of Cu²+/Cu+ is

(A) -0.158 V

(B) 0.182 V

(C) +0.158 V

(D) -0.182 V

- 43. A solution of m-chloroaniline, m-chlorophenol and m-chlorobenzoic acid in ethyl acetate was extracted initially with a saturated solution of NaHCO₃ to give fraction A. The left over organic phase was extracted with dilute NaOH solution to give fraction B. The final organic layer was labelled as fraction C. Fraction A, B and C contain respectively
 - (A) m-chlorobenzoic acid, m-chlorophenol and m-chloroaniline
 - (B) m-chlorophenol, m-chlorobenzoic acid and m-chloroaniline
 - (C) m-chlorobenzoic acid, m-chloroaniline and m-chlorophenol
 - (D) m-chloroaniline, m-chlorobenzoic acid and m-chlorophenol
- 44. The order of electron gain enthalpy in kJ/mol of fluorine, chlorine, bromine and iodine, respectively are

(A) -333, -325, -349 and -296

(B) -333, -349, -325 and -296

(C) -349, -333, -325 and -296

(D) -296, -325, -333 and -349

45. Consider the following reactions, which of these reaction(s) will not produce Saytzeff product?

(a) (CH₃)₃CCH(OH)CH₃
$$\xrightarrow{cons.H_2SO_4}$$
 \rightarrow

(c) $(CH_3)_2CHCH(Br)CH_3 \xrightarrow{(CH_3)_3O^{\Theta}K^{\Theta}}$

(b) $(CH_3)_2CHCH$ (Br) $CH_3 \xrightarrow{cons.KOH}$

(d) $(CH_3)_2$ C- CH_2 - $CHO \xrightarrow{\Delta}$ OH

Which of these reaction(s) will not produce Saytzeff product?

(A) (b) and (d)

(B) (c) only

(C) (a), (c) and (d)

(D) (d) only

- 46. Two solutions A and B, each of 100 L was made by dissolution of 4g of NaOH and 9.8 g of H₂SO₄ in water, respectively. The pH of the resultant solution obtained from mixing 40 L of solution A and 10 L of solution B is
- 47. During the nuclear explosion, one of the product of 90 Sr with half life of 6.93 years. If 1 μg of 90 Sr absorbed in the bones of newly born baby in place of Ca, how much time, in years is required to reduce it by 90% if it is not lost metabolically
- 48. Chlorine reacts with hot and concentrated NaOH and produces compound(X) and (Y). Compound(X) gives white precipitate with silver nitrate solution. The average bond order between Cl and O atoms in (Y) is

- 49. The number of chiral carbons in chloramphenicol is
- 50. For the reaction $A(I) \longrightarrow 2B(g)$ $\Delta U = 2.1 \text{ Kcal}, \Delta S = 20 \text{ cal K}^{-1} \text{ at } 300 \text{ K}$ Hence ΔG in Kcal is

PART-C (MATHEMATICS)

51. If f(a+b+1-x) = f(x), for all x, where a and b are fixed positive real numbers, then

$$\frac{1}{a+b}\int_{a}^{b}x(f(x)+f(x+1))dx$$
 is

(A)
$$\int_{a+1}^{b+1} f(x) dx$$

(B)
$$\int_{a-1}^{b-1} f(x) dx$$

(C)
$$\int_{a-1}^{b-1} f(x+1) dx$$

(D)
$$\int_{a+1}^{b+1} f(x+1) dx$$

52. Let the function, $f:[-7,0] \to R$ be continuous on [-7,0] and differentiable on (-7,0). If f(-7)=-3 and $f'(x) \le 2$, for all $x \in (-7,0)$, then for all such functions f, f(-1)+f(0) lies in the interval:

(A)
$$[-3, 11]$$

(B)
$$\left(-\infty, 20\right]$$

(C)
$$[-6, 20]$$

(D)
$$\left(-\infty,11\right]$$

53. If the distance between the foci of an ellipse is 6 and the distance between its directrices is 12, then the length of its latus rectum is:

(A)
$$\sqrt{3}$$

(B)
$$3\sqrt{2}$$

(C)
$$\frac{3}{\sqrt{2}}$$

(D)
$$2\sqrt{3}$$

54. An unbiased coin is tossed 5 time. Suppose that a variable X is assigned the value k when k consecutive heads are obtained for k = 3, 4, 5, otherwise X takes the value -1. Then the expected value of X, is

(A)
$$-\frac{3}{16}$$

(B)
$$-\frac{1}{8}$$

(C)
$$\frac{1}{8}$$

(D)
$$\frac{3}{16}$$

- 55. Five numbers are in A.P., whose sum is 25 and product is 2520. If one of these five numbers is $-\frac{1}{2}$, then the greatest number amongst them is:
 - (A) 7

(B)
$$\frac{21}{2}$$

(C) 16

- (D) 27
- 56. If the system of linear equations 2x + 2ay + az = 0, 2x + 3by + bz = 0, 2x + 4cy + cz = 0 where $a,b,c \in R$ are non zero and distinct; has a non zero solution, then:

(A)
$$a+b+c=0$$

(C)
$$\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$$
 are in A.P.

- Let P be a plane passing through the points (2, 1, 0), (4, 1, 1) and (5, 0, 1) and R be any 57. point (2, 1, 6). Then the image of R in the plane P is:
 - (A) (6, 5, 2)

(C) (6, 5, -2)

- (D)(3.4.-2)
- If $Re\left(\frac{z-1}{2z+i}\right) = 1$, where z = x + iy, then the point (x, y) lies on a: 58.

- (A) straight line whose slope is $\frac{3}{2}$ (B) circle whose diameter is $\frac{\sqrt{5}}{2}$ (C) straight line whose slope is $-\frac{2}{3}$ (D) circle whose centre is at $\left(-\frac{1}{2}, -\frac{3}{2}\right)$
- If $y(\alpha) = \sqrt{2\left(\frac{\tan\alpha + \cot\alpha}{1 + \tan^2\alpha}\right) + \frac{1}{\sin^2\alpha}}, \alpha \in \left(\frac{3\pi}{4}, \pi\right)$ then $\frac{dy}{d\alpha}$ at $\alpha = \frac{5\pi}{6}$ is: 59.
 - (A) 4

(B) $-\frac{1}{4}$

(C) -4

- (D) $\frac{4}{3}$
- Let α be a root of the equation $x^2 + x + 1 = 0$ and the matrix $A = \frac{1}{\sqrt{3}} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \alpha & \alpha^2 \\ 1 & 2 & 4 \end{bmatrix}$, 60.

then the matrix A³¹ is equal to:

(A) A^3

(B) A

 $(C) I_3$

- (D) A^2
- If $g(x) = x^2 + x 1$ and $(gof)(x) = 4x^2 10x + 5$, then $f(\frac{5}{4})$ is equal to
 - (A) $\frac{3}{2}$

(B) $\frac{1}{2}$

(C) $-\frac{3}{2}$

- (D) $-\frac{1}{2}$
- If y = mx + 4 is a tangent to both the parabolas, $y^2 = 4x$ and $x^2 = 2by$, then b is equal 62. to:
 - (A) -32

(B) -128

(C) -64

- (D) 128
- The logical statement $(p \Rightarrow q) \land (q \Rightarrow \sim p)$ is equivalent to: 63.
 - $(A) \sim q$

(B) p

(C) q

 $(D) \sim p$

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64.	Let $x^k + y^k = a^k$, $(a, k > 0)$ and $\frac{dy}{dx} + (\frac{y}{x})^{\frac{1}{3}}$	= 0, then k is:
	(A) $\frac{3}{2}$	(B) $\frac{4}{3}$
	(A) $\frac{3}{2}$ (C) $\frac{1}{3}$	(B) $\frac{4}{3}$ (D) $\frac{2}{3}$
	3	3
65.	Let α and β be two real roots of the where $k\left(\neq -1\right)$ and λ are real numbers. If (A) 10 (C) $5\sqrt{2}$	equation $(k+1)\tan^2 x - \sqrt{2} \cdot \lambda \tan x = (1-k)$ $\tan^2 (\alpha + \beta) = 50$, then a value of λ is: (B) 5 (D) $10\sqrt{2}$
66.	If $y = y(x)$ is the solution of the differ	ential equation, $e^y \left(\frac{dy}{dx} - 1 \right) = e^x$ such that
	y(0) = 0, then $y(1)$ is equal to: (A) $1 + \log_e 2$ (C) $\log_e 2$	(B) 2e (D) 2 + log _e 2
67.	The area of the region, enclosed by the circumstance region bounded by the parabola $y^2 = x$ and (A) $\frac{1}{3}(12\pi - 1)$ (C) $\frac{1}{6}(12\pi - 1)$	rcle $x^2 + y^2 = 2$, which is not common to the od the straight line $y = x$, is: (B) $\frac{1}{3}(6\pi - 1)$ (D) $\frac{1}{6}(24\pi - 1)$
68.	A vector $\vec{a} = \alpha \hat{i} + 2\hat{j} + \beta \hat{k} (\alpha, \beta \in R)$ lies $\vec{c} = \hat{i} - \hat{j} + 4\hat{k}$. If \vec{a} bisects the angle between (A) $\vec{a} \cdot \hat{k} + 4 = 0$ (C) $\vec{a} \cdot \hat{i} + 3 = 0$	in the plane of the vectors, $\vec{b} = \hat{i} + \hat{j}$ and \vec{c} , then: (B) $\vec{a} \cdot \hat{k} + 2 = 0$ (D) $\vec{a} \cdot \hat{i} + 1 = 0$
69.	The greatest positive integer k, for $49^{125} + 49^{124} + \dots + 49^2 + 49 + 1$, is: (A) 65 (C) 32	which $49^k + 1$ is a factor of the sum (B) 63 (D) 60
70.	appear, is (A) 5^6	ch only and all the five digits 1, 3, 5, 7 and 9 (B) 6!
	(C) $\frac{5}{2}(6!)$	(D) $\frac{1}{2}$ (6!)

- 71. Let S be the set of points where the function, $f(x) = |2 |x 3|, x \in \mathbb{R}$, is not differentiable. Then $\sum_{x \in S} f(f(x))$ is equal to _____
- 72. If the sum of the coefficients of all even powers of x in the product $(1+x+x^2+.....+x^{2n})(1-x+x^2-x^3+.....+x^{2n})$ is 61, then n is equal to
- 73. If the variance of the first n natural numbers is 10 and the variance of the first m even natural numbers is 16, then m + n is equal to _______
- 74. $\lim_{x \to 2} \frac{3^x + 3^{3-x} 12}{3^{-x/2} 3^{1-x}}$ is equal to ______
- 75. Let A(1,0),B(6,2) and $C(\frac{3}{2},6)$ be the vertices of a triangle ABC. If P is a point inside the triangle ABC such that the triangles APC, APB and BPC have equal areas, then the length of the line segment PQ, where Q is the point $\left(-\frac{7}{6},-\frac{1}{3}\right)$ is ______

JEE (Main) – 2020 ANSWERS

PART A - PHYSICS

1.	Α	2.	Α	3.	D	4.	С	
5.	Α	6.	С	7.	В	8.	D	
9.	Α	10.	D	11.	Α	12.	Α	
13.	Α	14.	В	15.	D	16.	Α	
17.	С	18.	С	19.	С	20.	D	
21.	600	22.	175	23.	60	24.	10	
25.	11							
PART B - CHEMISTRY								
26.	С	27.	С	28.	D	29.	С	
30.	С	31.	В	32.	В	33.	В	
34.	С	35.	D	36.	В	37.	D	
38.	В	39.	D	40.	D	41.	Α	
42.	С	43.	Α	44.	В	45.	В	
46.	10.60	47.	23.03	48.	1.67	49.	2	
50.	-2.70							
PART C - MATHEMATICS								
51.	С	52.	В	53.	В	54.	D	
55.	С	56.	С	57.	С	58.	В	
59.	Α	60.	Α	61.	D	62.	В	
63.	D	64.	D	65.	Α	66.	Α	
67.	С	68.	В	69.	В	70.	С	
71.	3	72.	30	73.	18	74.	36	
75.	5							

HINTS AND SOLUTIONS

PART A - PHYSICS

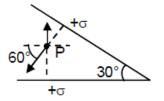
Sol.
$$I = I_0 \cos^2 \theta$$
$$\frac{I_0}{10} = I_0 \cos^2 \theta$$

$$\cos \theta = \frac{1}{\sqrt{10}} = 0.31 < \frac{1}{\sqrt{2}}$$
 which is 0.707

So, $\theta > 45^\circ$ and $90 - \theta < 45^\circ$ so only one option is correct i.e. 18.4° Angle rotated should be = $90^\circ - 71.6^\circ = 18.4^\circ$.

2. **A**

$$\begin{split} \text{Sol.} \qquad \vec{E} &= \frac{\sigma}{2\epsilon_0} \cos 60^\circ (-\hat{x}) + \left[\frac{\sigma}{2\epsilon_0} - \frac{\sigma}{2\epsilon_0} \sin 60^\circ \right] (\hat{y}) \\ \vec{E} &= \frac{\sigma}{2\epsilon_0} \left[\left(1 - \frac{\sqrt{3}}{2} \right) \hat{y} - \frac{1}{2} \hat{x} \right] \end{split}$$



3

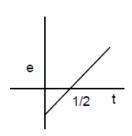
Sol.
$$I = I_0 t - I_0 t^2$$

$$\phi = BA$$

$$\phi = \mu_0 n IA$$

$$V_{R} = \frac{d\phi}{dt} = -\mu_0 nAI_0 (1-2t)$$

$$V_R = 0$$
 at $t = \frac{1}{2}$ and $I_R = \frac{V_R}{\text{Resistance of loop}}$



4.

$$d \sin\theta = 2\lambda$$

$$\sin \theta = \frac{\sqrt{3}}{2} \text{ (given)}$$

$$\Rightarrow \frac{\lambda}{d} = \frac{\sqrt{3}}{4}$$
 ...(i)

So for 1st minima is

$$d \sin\theta = \lambda$$

$$\sin \theta = \frac{\lambda}{d} = \frac{\sqrt{3}}{4}$$
 (from equation (i))

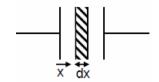
$$\theta$$
 = 25.65° (from sin table)

$$\theta \approx 25^{\circ}$$
.

5.

Sol. Capacitance of element

Capacitance of element,
$$C' = \frac{K(1 + \alpha x)\epsilon_0 A}{dx}$$



$$\sum \frac{1}{C'} = \int_{0}^{d} \frac{dx}{K \epsilon_{0} A (1 + \alpha x)}$$

$$\frac{1}{C} = \frac{1}{K\epsilon_0 A\alpha} \ell n (1 + \alpha d)$$

Given:
$$\alpha d \ll 1$$

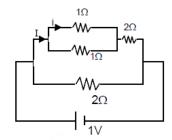
$$\frac{1}{C} = \frac{1}{K\epsilon_0 A\alpha} \left(\alpha d - \frac{\alpha^2 d^2}{2} \right) \quad ; \quad \frac{1}{C} = \frac{d}{K\epsilon_0 A} \left(1 - \frac{\alpha d}{2} \right)$$

$$C = \frac{K\varepsilon_0 A}{d} \left(1 + \frac{\alpha d}{2} \right)$$



Sol.
$$I = \frac{1}{2.5} = 0.4 \text{ A}$$

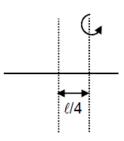
$$I = \frac{I}{2} = 0.2 \text{ A}$$



Sol.
$$\frac{M\ell^2}{12} + M\left(\frac{\ell}{4}\right) = MK^2$$

$$\frac{\ell^2}{12} + \frac{\ell^2}{16} = K^2$$

$$K = \sqrt{\frac{7}{48}} \; \ell$$

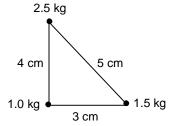


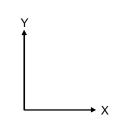
8.

Sol.

Take 1 kg mass at origin
$$X_{cm} = \frac{1 \times 0 + 1.5 \times 3 + 2.5 \times 0}{5} = 0.9 \text{ cm}$$

$$Y_{cm} = \frac{1 \times 0 + 1.5 \times 0 + 2.5 \times 4}{5} = 2 \text{ cm}$$





9.

Sol. As magnetic field lines always form a closed loop, hence every magnetic field line creating magnetic flux in the inner region must be passing through the outer region. Since flux in two regions are in opposite direction,

$$\therefore$$
 $\phi_i = -\phi_0$

Sol.
$$mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

$$v = \omega R \text{ (no slipping)}$$

$$mgh = \frac{1}{2}m\omega^2 R^2 + \frac{1}{2}\frac{mR^2}{2}\omega^2$$

$$mgh = \frac{3}{4}m\omega^2 R^2$$

$$\omega = \sqrt{\frac{4gh}{3R^2}} = \frac{1}{R}\sqrt{\frac{4gh}{3}}$$

11. Α

Sol. Case-I:

If final image is at least distance of clear vision

$$\begin{split} \text{M.P.} &= \frac{L}{f_o} \Biggl(1 + \frac{D}{f_e} \Biggr) \; ; \; 375 = \frac{150}{5} \Biggl[1 + \frac{25}{f_e} \Biggr] \\ &\frac{375}{30} = 1 + \frac{25}{f_e} \quad ; \; \frac{345}{30} = \frac{25}{f_e} \\ &f_e = \frac{750}{345} = 2.17 \, \text{cm} \; ; \; f_e \approx 22 \, \text{mm} \end{split}$$

Case-II:

In final image is at infinity

$$M.P. = \frac{L}{f_0} \left(\frac{D}{f_e} \right) = 375$$

$$f_e = 22 \text{ mm}$$

12.

$$\text{Sol.} \qquad \gamma_{\text{mixture}} = \frac{n_1 C_{P_1} + n_2 C_{P_2}}{n_1 C_{V_1} + n_2 C_{V_2}} = \frac{n_1 \frac{\gamma_1 R}{\gamma_1 - 1} + n_2 \frac{\gamma_2 R}{\gamma_2 - 1}}{\frac{n_1 R}{\gamma_1 - 1} + \frac{n_2 R}{\gamma_2 - 1}}$$

on rearranging we get

$$\begin{split} &\frac{n_1 + n_2}{\gamma_{\text{mix}} - 1} = \frac{n_1}{\gamma_1 - 1} + \frac{n_2}{\gamma_2 - 1} \; ; \quad \frac{5}{\gamma_{\text{mix}} - 1} = \frac{3}{1/3} + \frac{2}{2/3} \\ &\frac{5}{\gamma_{\text{mix}} - 1} = 9 + 3 = 12 \qquad \qquad \Rightarrow \quad \gamma_{\text{mixture}} = \frac{17}{12} + 1 + \frac{5}{12} \quad ; \quad \gamma_{\text{mix}} = 1.42 \end{split}$$

Sol.
$$v = \sqrt{\frac{T}{\mu}}$$

$$T = \mu v^2 \quad ; \quad \frac{\mu v^2}{\Delta} = Y \frac{\Delta \ell}{\ell}$$

$$\Delta \ell = \frac{\mu v^2 \ell}{\Delta V}$$

after substituting value of μ , ν , ℓ , A and Y we get

$$\Delta \ell$$
 = 0.03 mm

Sol.
$$P_1 = 1$$
 atm, $T_1 = 273$ K

$$P_1V_1^{\gamma}=P_2V_2^{\gamma}$$

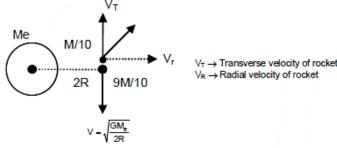
$$P_2 = P_1 \left[\frac{V_1}{V_2} \right]^{\gamma}$$
$$= 1 \operatorname{atm} \left(\frac{1}{3} \right)^{1.4}$$

Now work done =
$$\frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$$
 = 88.7 J

Closes answer is 90.5 J.

$$Sol. \qquad \frac{-GM_{\rm e}M}{R} + \frac{1}{2}Mu^2 = \frac{-GM_{\rm e}M}{2R} + \frac{1}{2}Mv^2$$

$$v = \sqrt{u^2 - \frac{GM_e}{R}}$$



$$\frac{M}{10} \, V_T = \frac{9M}{10} \, \sqrt{\frac{GM_e}{2R}} \quad \; ; \quad \frac{M}{10} \, V_r = M \, \sqrt{u^2 - \frac{GM_e}{R}} \label{eq:VT}$$

Kinetic energy =
$$\frac{1}{2} \frac{M}{10} (V_T^2 + V_r^2) = \frac{M}{20} \left(81 \frac{GM_e}{2R} + 100 u^2 - 100 \frac{GM_e}{R} \right)$$

$$= \frac{M}{20} \left(100 \, u^2 - \frac{119 GM_e}{2R} \right)$$

$$= 5M \left(u^2 - \frac{119GM_e}{200R} \right)$$

$$Sol. \qquad T = \frac{2\pi}{\omega} = 2\pi \frac{r}{v} \propto \frac{n^2}{\frac{1}{n}} \propto n^3$$

$$\therefore \quad \nu = \frac{1}{T} \propto \frac{1}{n^3}$$

$$\frac{v_2}{v_1} = \frac{1^3}{2^3} = \frac{1}{8}$$

$$\therefore \quad v_2 = \frac{1}{8} \times \frac{1}{T} = \frac{1}{8} \times \frac{10^{16}}{1.6} = 7.8 \times 10^{14}$$

17. **C**

Sol. In damped oscillation

$$ma + bv + kx = 0$$

$$m\frac{d^2x}{dt^2}+b\frac{dx}{dt}+kx=0 \hspace{1cm} ... \hbox{(i)}$$

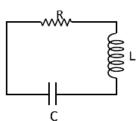
In the circuit

$$-iR - L\frac{di}{dt} - \frac{q}{c} = 0$$

$$L\frac{d^2q}{dt^2} + R\frac{dq}{dt} + \frac{1}{c}q = 0 \qquad ...(ii)$$

Comparing equation (i) and (ii)

$$m = L, b = R, k = \frac{1}{c}$$



Sol.
$$\frac{E_0}{B_0} = C$$
 (speed of light in vacuum)
 $E_0 = B_0 C = 3 \times 10^{-8} \times 3 \times 10^8 = 9 \text{ N/C}$
So, $\vec{E} = \left(9 \sin{(1.6 \times 10^3 \text{ x} + 48 \times 10^{10} \text{ t})} \hat{k} \text{ V/m}\right)$

Sol. A logic gate is reversible if we can recover input data fro the output eg. NOT gate.

Sol.
$$4000 \times V + mg \times V = P$$

 $\frac{60 \times 746}{2000 \times 4000} = V$

$$V = 1.86 \text{ m/s} \approx 1.9 \text{ m/s}.$$

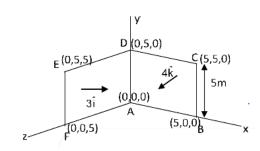
Sol.
$$n = \frac{W}{Q_h} = 1 - \frac{300}{900} = \frac{2}{3}$$

$$Q_h = \frac{3}{2}W = 1800 J$$

$$Q_L = O_h - W = 600 J$$

Sol.
$$\phi = \vec{B} \cdot \vec{A} = (3\hat{i} + 4\hat{k}) \cdot (25\hat{i} + 25\hat{k})$$

$$\phi = (3 \times 25) + (4 \times 25) = 175$$
 weber



Sol.
$$V = 2\alpha_2 + \alpha_1$$

= 10 × 10⁻⁶ + 5 × 10⁻⁵
= 60 × 10⁻⁶ / °C

Sol.
$$KE = PE_1 - PE_2 = mgh_1 - mgh_2$$

Sol. Energy of photon,
$$E = \frac{1240}{310} = 4eV > 2eV$$
 (so photoelectric effect will take place)

$$= 4 \times 1.6 \times 10^{-19} = 6.4 \times 10^{-19}$$
 Joule

Number of photons falling per second

$$=\frac{6.4\times10^{-5}\times1}{6.4\times10^{-19}}=10^{14}$$

Number of photoelectron emitted per second

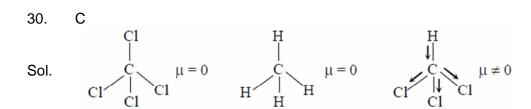
$$=\frac{10^{14}}{10^3}=10^{11}$$

PART B - CHEMISTRY

Sol.
$$K_2O \longrightarrow X=+1$$

$$K_2O_2 \longrightarrow x=+1$$

$$KO_2 \longrightarrow x=+1$$



- 31.
- Sol. Theory based.
- 32.
- Theory based. Sol.
- 33.

Sol.
$$pK_b \propto \frac{1}{K_b} \propto \frac{1}{Basic\ strength}$$

34. С

Sol.
$$CH_{3}-CH_{2}-C\equiv C-CH_{2}-C-H \xrightarrow{NaBH_{4}} CH_{3}-CH_{2}-C\equiv C-CH_{2}$$

$$CH_{3}-CH_{2}-C\equiv C-CH_{2} \xrightarrow{CH_{2}-OH} CH_{2}-OH$$

$$CH_{3}-CH_{2}-C\equiv C-CH_{2} \xrightarrow{CH_{2}-C} CH_{2}-CH_$$

35. D Sol. $\begin{array}{l} m \to -\ell \text{ to} \\ \to 0 \to 0 \\ \to 1 \to -1, 0, 1 \\ \to 2 \to -2, -1, 0, 1, 2 \\ \to 3 \to -3, -2, -1, 0, 1, 2, 3 \\ \to 4 \to -4, -3, -2, -1, 0, 1, 2, 3, 4 \end{array}$ n=5

Total 25 orbitals are possible

- 36.
- Theory based. Sol.
- 37.
- [Ni(CO)₄] bonding diagram and energy can be explained by MOT clearly. Sol.

Sol.
$$[Pt(NH_3)_2CI(NH_2CH_3)CI$$

 $x + 0 - 1 + 0 = +1$
 $x = +2 \rightarrow Pt^{2+}$

Diamminechlorido(methanamine)platinum(II)chloride

Sol.
$$CH_3$$
— CH_2 — CH_2 — $Excess$ CH_3 — CH_3 — CH_4 — CH_2 — CH_4 —

$$\begin{array}{c} \text{Me} \\ \text{N} \\ \text{Me} \\ \text{N} \\ \text{N} \\ \text{Me} \\ \text{N} \\ \text{N} \\ \text{Methyl orange} \\ \text{Methyl orange} \\ \text{N} \\ \text{Methyl orange is used as an indicator)} \\ \\ \text{N} \\$$

Theory based Sol.

42.

$$e^{-} + Cu^{+2} \xrightarrow{E_1^0} Cu^{\oplus} \xrightarrow{0.522V} Cu$$

$$0.34$$

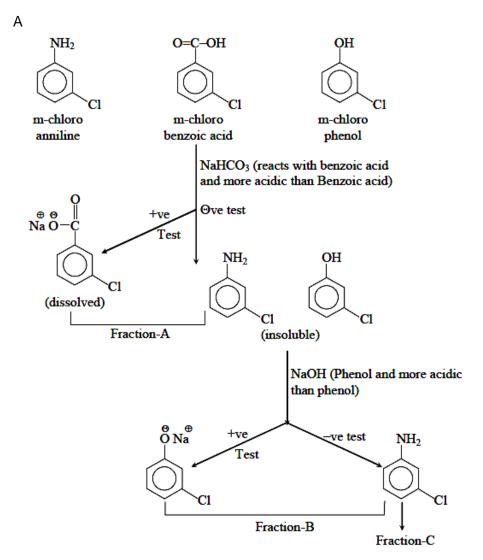
$$2 \times 0.34 = E_1^0 + 1 \times 0.522$$

$$2 \times 0.34 = E_1^0 + 1 \times 0.522$$

$$E_1^0 = 0.68 - 0.522$$

$$E_1^0 = 0.158$$





- 44. E
- Sol. Electron gain enthalpy increases with electro negativity chlorine has higher electron gain enthalpy than fluorine (exception)
- 45. E
- Sol. Bulky base always prefer Hoffmann product
- 46. 10.60

Sol.
$$M_{(H_2SO_4)} = \frac{9.8}{98 \times 100} = 10^{-3} \text{m}$$

 $M_{NaOH} = \frac{4}{40 \times 100} = 10^{-3} \text{m}$

Equivalents of resulting solution[OH⁻] =
$$\frac{40 \times 10^{-3} - 10 \times 10^{-3} \times 2}{50} = \frac{2}{5} \times 10^{-3}$$

pOH = 3.39 | pH = 10.6

47. 23.03 Sol.
$$\frac{t_{90\%}}{t_{50\%}} = \frac{\ell n \frac{100}{10}}{\ell n 2}$$

$$t_{90\%} = \frac{\ell n_{10}}{\ell n_2} \times t_{50\%} = \frac{6.93 \times \ell n_{10}}{0.693} = 23.03 \text{ years}$$

Sol.
$$3 \text{Cl}_2 + 6 \text{NaOH} \longrightarrow 5 \text{NaCl} + \text{NaClO}_3 + 3 \text{H}_2 \text{O}$$

$$\text{NaCl} + \text{AgNO}_3 \longrightarrow \underset{(\text{White})}{\text{AgCl}} + \text{NaNO}_3$$

Y is NaClO₃
$$\rightarrow$$
 ClO₃

Bond order =
$$\frac{5}{3}$$
 = 1.67

Sol.

Sol.
$$\Delta H = \Delta U + \Delta ngRT$$

= 2.1 × 10³ + 2(B) (300) = 3300 calories
 $\Delta G = \Delta H - T\Delta S$
= 3300 - 300(20) = -2700 calories = -2.7 KCal

PART C - MATHEMATICS

$$I = \frac{1}{(a+b)} \int_{a}^{b} \times [f(x) + f(x+1)] dx \qquad \dots (1)$$

$$x \rightarrow a+b-x$$

$$I = \frac{1}{(a+b)} \int_{a}^{b} (a+b-x) \Big[f(a+b-x) + f(a+b+1-x) \Big] dx$$

$$I = \frac{1}{(a+b)} \int_{a}^{b} (a+b-x) [f(x+1)+f(x)] dx \dots (2)$$

[: put
$$x \rightarrow x+1$$
 in given equation]

$$(1) + (2)$$

$$2I = \int_{a}^{b} \left[f(x+1) + f(x) \right] dx$$

$$2I = \int_{a}^{b} f(x+1) dx + \int_{a}^{b} f(x) dx$$

$$\int_{a}^{b} f(a+b+1-x) dx + \int_{a}^{b} f(x) dx$$

$$2I = 2 \int_{a}^{b} f(x) dx$$

$$I = \int_{a}^{b} f(x) dx$$
Put $x = t+1 \Rightarrow I = \int_{a-1}^{b-1} f(t+1) dt$

Sol. Using LMVT
$$x \in [-7, -1]$$

$$\frac{f\left(-1\right)-f\left(-7\right)}{\left(-1+7\right)}\leq 2$$

$$\frac{f(-1)+3}{6} \le 2 \Rightarrow f(-1) \le 9$$

Using LMVT for $x \in [-7,0]$

$$\frac{f\left(0\right)-f\left(-7\right)}{\left(0+7\right)}\leq 2$$

$$\frac{f(0)+3}{7} \le 2 \Rightarrow f(0) \le 11$$

$$\therefore f(0) + f(-1) \le 20$$

Sol.
$$2ae = 6$$
 and $\frac{2a}{e} = 12$

$$\Rightarrow ae = 3 \text{ and } \frac{a}{e} = 6$$

$$\Rightarrow b^2 = a^2 - a^2e^2 = 18 - 9 = 9$$

$$\Rightarrow L.R. = \frac{2b^2}{a} = \frac{2 \times 9}{3\sqrt{2}} = 3\sqrt{2}$$

54. D Sol.

k = number of times head occur consecutively Now expectation

$$= \sum xP(k) = (-1) \times \frac{1}{32} + (-1) \times \frac{12}{32} + (-1) \times \frac{11}{32} + 3 \times \frac{5}{32} + 4 \times \frac{2}{32} + 5 \times \frac{1}{32} = \frac{1}{8}$$

Sol. Let terms be
$$a - 2d$$
, $a - d$, $a + d$, $a + 2d$

Sum
$$5a = 25 \Rightarrow a = 5$$

Product = 2520

$$(5-2d)(5-d)5(5+d)(5+2d) = 2520$$

$$\Rightarrow \left(25 - 4d^2\right)\left(25 - d^2\right) = 504$$

$$\Rightarrow$$
 625 - 100d² - 25d² + 4d⁴ = 504

$$\Rightarrow 4d^4 - 125d^2 + 625 - 504 = 0$$

$$\Rightarrow 4d^4 - 125d^2 + 121 = 0$$

$$\Rightarrow 4d^2 - 121d^2 - 4d^2 + 121 = 0$$

$$\Rightarrow \left(d^2 - 1\right)\left(4d^2 - 121\right) = 0$$

$$\Rightarrow$$
 d = ±1, d = ± $\frac{11}{2}$

$$d = \pm 1$$
, does not give $\frac{\{1\}2}{}$ as a term

$$d = \pm 1$$

$$\therefore d = \frac{11}{2}$$

$$\therefore \text{ Largest term } = 5 + 2d = 5 + 11 = 16$$

$$(3bc - 4bc) - (2ac - 4ac) + (2ab - 3ab) = 0$$

$$-bc + 2ac - ab = 0$$

$$ab + bc = 2ac$$

 $a, b, c \text{ in H.P.}$
 $\Rightarrow \frac{1}{a}, \frac{1}{b}, \frac{1}{c} \text{ in A.P.}$

Sol. Plane is
$$x + y - 2z = 3$$

$$\Rightarrow \frac{x - 2}{1} = \frac{y - 1}{1}$$

$$= \frac{z - 6}{-2} = \frac{-2(2 + 1 - 12 - 3)}{6}$$

$$\Rightarrow (x, y, z) = (6, 5, -2)$$

Sol.
$$\left(\frac{z-1}{2z+i}\right) = \frac{\left(x-1\right)+iy}{2\left(x+iy\right)+i} = \frac{\left(x-1\right)+iy}{2x+\left(2y+1\right)i} \times \frac{2x-\left(2y+1\right)i}{2x-\left(2y+1\right)i}$$

$$Re\left(\frac{z+1}{2z+i}\right) = \frac{2x\left(x-1\right)+y\left(2y+1\right)}{\left(2x\right)^2+\left(2y+1\right)^2} = 1$$

$$\Rightarrow 2x^2+2y^2-2x+y=4x^2+4y^2+4y+1$$

$$\Rightarrow 2x^2+2y^2+2x+3y+1=0$$

$$r = \sqrt{\frac{1}{4}+\frac{9}{16}-\frac{1}{2}} = \sqrt{\frac{4+9-8}{16}} = \frac{\sqrt{5}}{4}$$

Sol.
$$y = \sqrt{\frac{2\cos^2 \alpha}{\sin \alpha \cos \alpha} + \frac{1}{\sin^2 \alpha}}$$
$$= \sqrt{2\cot \alpha + \csc^2 \alpha} = |1 + \cot \alpha| = -1 - \cot \alpha$$
$$\frac{dy}{d\alpha} = \csc^2 \alpha$$
$$\Rightarrow \text{ at } \alpha = \frac{5\alpha}{6}, \frac{dy}{d\alpha} = 4$$

Sol.
$$A^{2} = \frac{1}{3} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \omega & \omega^{2} \\ 1 & \omega^{2} & \omega \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \omega & \omega^{2} \\ 1 & \omega^{2} & \omega \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$
$$\Rightarrow A^{4} = I$$
$$\Rightarrow A^{30} - A^{28} \times A^{3} - A^{3}$$

61. D
Sol.
$$g(f(x)) = f^{2}(x) + f(x) - 1$$

$$g(f(\frac{5}{4})) = f^{2}(\frac{5}{4}) + f(\frac{5}{4}) - 1$$

$$-\frac{5}{4} = f^{2}(\frac{5}{4}) + f(\frac{5}{4}) - 1$$

$$f^{2}(\frac{5}{4}) + f(\frac{5}{4}) + \frac{1}{4} = 0$$

$$(f(\frac{5}{4}) + \frac{1}{2})^{2} = 0$$

$$f(\frac{5}{4}) = -\frac{1}{2}$$

Sol.
$$y = mx + 4$$
(i)

Tangent of $y^2 = 4x$

$$y = mx + \frac{a}{m} \Rightarrow y = mx + \frac{1}{m} \qquad(ii)$$

$$\therefore 4 = \frac{1}{m} \Rightarrow m = \frac{1}{4}$$

Line $y = \frac{1}{4}x + 4$ is also tangent to parabola $x^2 = 2by$,

$$\therefore x^2 = 2b \left(\frac{x+16}{4} \right)$$

$$\Rightarrow$$
 2x² -bx -16b = 0

$$\Rightarrow$$
 D = 0 \Rightarrow b² - 4 × 2 × (-16b) = 0

$$\Rightarrow$$
 $b^2 + 32 \times 4b = 0$

$$b=-128, b=0 \ \ (not\ possible)$$

Clearly
$$(p \rightarrow q) \land (q \rightarrow \sim p)$$
 is equivalent to $\sim p$

Sol.
$$k.x^{k-1} + k.y^{k-1} \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = -\left(\frac{x}{y}\right)^{k-1}$$

$$\frac{dy}{dx} + \left(\frac{x}{y}\right)^{k-1} = 0$$

$$k - 1 = -\frac{1}{3}$$

$$k = 1 - \frac{1}{3} = \frac{2}{3}$$

Sol.
$$(k+1)\tan^2 x - \sqrt{2}\lambda \tan x + (k-1) = 0$$

$$\tan\alpha + \tan\beta = \frac{\sqrt{2}\lambda}{k+1}$$

$$\tan\alpha\tan\beta = \frac{k-1}{k+1}$$

$$\tan(\alpha+\beta) = (k-1) = 0 \frac{\sqrt{2}\lambda}{k+1}$$

$$\tan\alpha\tan\beta = \frac{k-1}{k+1}$$

$$\tan(\alpha+\beta) = (k-1) = 0 \frac{\frac{\sqrt{2}\lambda}{k+1}}{1 - \frac{k-1}{k+1}} = \frac{\sqrt{2}\lambda}{2} = \frac{\lambda}{\sqrt{2}}$$

$$\tan^2\left(\alpha+\beta\right) = \frac{\lambda^2}{2} = 50$$

Sol.
$$e^y = t$$

$$e^y \frac{dy}{dx} = \frac{dt}{dx}$$

$$\frac{dt}{dx} - t = e^x$$

$$IF = e^{\int -1.dx} = e^{-x}$$

$$t(e^{-x}) = \int e^x \cdot e^{-x} dx$$

$$e^{y-x} = x + c$$

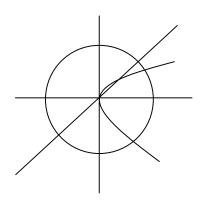
Putting
$$x = 0, y = 0, c = 1$$

$$e^{y-x} = x + 1$$

$$y = x + \log_e(x+1)$$

at
$$x = 1$$
, $y = 1 + \log_{e} 2$

Sol.
$$A = 2\pi - \int_{0}^{1} \sqrt{x} - x \, dx$$
$$2\pi - \left(\frac{2x^{3/2}}{3} - \frac{x^2}{2}\right)_{0}^{1}$$
$$2\pi = \left(\frac{2}{3} - \frac{1}{2}\right) \Rightarrow 2\pi - \left(\frac{1}{6}\right) \Rightarrow \frac{12\pi - 1}{6}$$



Sol. For angle bisector
$$\vec{a} = \lambda (\hat{b} + \hat{c})$$
 or $\vec{a} = \mu (\hat{b} - \hat{c})$

$$\vec{a} = \lambda \left(\frac{\hat{i} + \hat{j}}{\sqrt{2}} + \frac{\hat{i} + \hat{j} + 4\hat{k}}{3\sqrt{2}} \right)$$

$$= \frac{\lambda}{3\sqrt{2}} \left[3\hat{i} + 3\hat{j} + \hat{i} - \hat{j} + 4\hat{k} \right]$$

$$= \frac{\lambda}{3\sqrt{2}} \left[4\hat{i} + 2\hat{j} + 4\hat{k} \right]$$

but
$$\vec{a} = \alpha \hat{i} + 2\hat{j} + \beta \hat{k}$$

$$\frac{2\lambda}{3\sqrt{2}}=2 \Rightarrow \lambda=3\sqrt{2}$$

$$\vec{a} = 4\hat{i} + 2\hat{j} + 4\hat{k}$$

Now if
$$\vec{a} = \mu \left(\frac{\hat{i} + \hat{j}}{\sqrt{2}} - \frac{\hat{i} - \hat{j} + 4\hat{k}}{3\sqrt{2}} \right)$$

$$\vec{a} = \frac{\mu}{3\sqrt{2}} \Big(3\hat{i} + 3\hat{j} - \hat{i} + \hat{j} - 4\hat{k} \Big)$$

$$=\frac{\mu}{3\sqrt{2}}\Big(2\hat{i}+4\hat{j}-4\hat{k}\Big)$$

Comparing $\vec{a} = \alpha \hat{i} + 2\hat{j} + \beta \hat{k}$

$$\frac{4\mu}{3\sqrt{2}} = 2 \Longrightarrow \mu = \frac{3\sqrt{2}}{2}$$

$$\vec{a} = \hat{i} + 2\hat{j} - 2\hat{k}$$

$$\vec{a} \cdot \hat{k} + 2 = 0$$

$$-2 + 2 = 0$$

Sol.
$$\frac{\left(49\right)^{126} - 1}{48} = \frac{\left(\left(49\right)^{63} + 1\right)\left(49^{63} - 1\right)}{48}$$

For digit to repeat we have 5C_1 choice

And six digits can be arrange in $\frac{6!}{2!}$ ways.

Hence total such number = $\frac{5}{2}$ (6!)

Sol.
$$:: f(x)$$
 is non differentiable at $x = 1,3,5$

$$\sum_{x \in A} f(f(x)) = f(f(1)) + f(f(3)) + f(f(5))$$
= 1 + 1 + 1
= 3

Sol. Let
$$(1-x+x^2....)(1-x+x^2....)=a_0+a_1x+a_2x^2+....$$

Putting
$$x = 1$$

$$1(2n+1) = a_0 + a_1 + a_2 + \dots + a_{2n}$$
 (i

Putting
$$x = -1$$

$$(2n+1)\times 1 = a_0 - a_1 + a_2 + \dots a_{2n}$$
(ii)

$$(i) + (ii)$$

$$4n + 2 = 2(a_0 + a_2 +)$$

$$=2\times61$$

$$\Rightarrow$$
 2n + 1 = 61 \Rightarrow n = 30

Sol.
$$Var(1,2,...,n) = \frac{1^2 + 2^2 + ... + n^2}{n} - \left(\frac{1 + 2 + ... + n}{n}\right)^2 = 10$$

$$\Rightarrow \frac{(n+1)(2n+1)}{6} - \left(\frac{n+1}{2}\right)^2 = 10$$

$$\Rightarrow$$
 n² -1 = 120

$$\Rightarrow$$
 n = 11

$$Var(2,4,6,...,2m) = 16 \Rightarrow var(1,2,...,m) = 4$$

$$\Rightarrow$$
 m² -1 = 48 \Rightarrow m = 7 \Rightarrow m + n = 18

74. 36
Sol. Let
$$3^{x/2} = t$$

$$\lim_{t \to 3} \frac{t^2 + \frac{27}{t^2} - 12}{\frac{1}{t} - \frac{3}{t^2}} = \lim_{t \to 3} \frac{t^4 + 27 - 12t^2}{t - 3}$$

$$\lim_{t \to 3} \frac{\left(t^2 - 3\right)(t + 3)(t - 3)}{(t - 3)} = 6 \times 6 = 36$$

Sol. P will be centroid of $\triangle ABC$

$$P\left(\frac{17}{6}, \frac{8}{3}\right) \Rightarrow PQ = \sqrt{\left(\frac{24}{6}\right)^2 + \left(\frac{9}{3}\right)} = 5$$