# FIITJEE Solutions to JEE(Main)-2020

Test Date: 9th January 2020 (Second Shift)

## PHYSICS, CHEMISTRY & MATHEMATICS

Paper - 1

Time Allotted: 3 Hours Maximum Marks: 300

Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

#### Important Instructions:

- 1. The test is of 3 hours duration.
- 2. This **Test Paper** consists of **75** questions. The maximum marks are **300**.
- 3. There are *three* parts in the question paper A, B, C consisting of *Physics*, *Chemistry* and *Mathematics* having 25 questions in each part of equal weightage out of which 20 questions are MCQs and 5 questions are numerical value based. Each question is allotted **4 (four)** marks for correct response.
- 4. **(Q. No. 01 20, 26 45, 51 70)** contains 60 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- 5. **(Q. No. 21 25, 46 50, 71 75)** contains 15 Numerical based questions with answer as numerical value. Each question carries **+4 marks** for correct answer. There is no negative marking.
- 6. Candidates will be awarded marks as stated above in **instruction No.3** for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer box.
- 7. There is only one correct response for each question. Marked up more than one response in any question will be treated as wrong response and marked up for wrong response will be deducted accordingly as per instruction 6 above.

# PART - A (PHYSICS)

1. A small spherical droplet of density d is floating exactly half immersed in a liquid of density p and surface tension T. The radius of the droplet is (take note that the surface tension applies an upward force on the droplet):

(A) 
$$r = \sqrt{\frac{3T}{(2d-\rho)g}}$$

(B) 
$$r = \sqrt{\frac{T}{(d-\rho)g}}$$

(C) 
$$r = \sqrt{\frac{2T}{3(d+\rho)g}}$$

(D) 
$$r = \sqrt{\frac{T}{(d+\rho)g}}$$

2. There is a small source of light at some depth below the surface of water (refractive index =  $\frac{4}{3}$ ) in a tank of large cross sectional surface area. Neglecting any reflection from the bottom and absorption by water, percentage of light that emerges out of surface is (nearly):

[Use the fact that surface area of spherical cap of height h and radius of curvature r is  $2\pi rh1$ 

(A) 21%

(C) 50%

- (B) 17% (D) 34%
- For the four sets of three measured physical quantifies as given below. Which of the 3. following options is correct?
  - (i)  $A_1 = 24.36$ ,  $B_1 = 0.0724$ ,  $C_1 = 256.2$
  - (ii)  $A_2 = 24.44$ ,  $B_2 = 16.082$ ,  $C_2 = 240.2$
  - (iii)  $A_3 = 25.2$ ,  $B_3 = 19.2812$ ,  $C_3 = 236.183$
  - (iv)  $A_4 = 25$ ,  $B_4 = 236.191$ ,  $C_4 = 19.5$
  - (A)  $A_4 + B_4 + C_4 < A_1 + B_1 + C_1 = A_2 + B_2 + C_2 = A_3 + B_3 + C_3$
  - (B)  $A_1 + B_1 + C_1 < A_3 + B_3 + C_3 < A_2 + B_2 + C_2 < A_4 + B_4 + C_4$
  - (C)  $A_1 + B_1 + C_1 = A_2 + B_2 + C_2 = A_3 + B_3 + C_3 = A_4 + B_4 + C_4$
  - (D)  $A_4 + B_4 + C_4 < A_1 + B_1 + C_1 < A_3 + B_3 + C_3 < A_2 + B_2 + C_2$
- A plane electromagnetic wave is propagating along the direction  $\frac{i+j}{\sqrt{2}}$ , with its 4.

polarization along the direction k. The correct form of the magnetic field of the wave would be (here B<sub>0</sub> is an appropriate constant)

(A) 
$$B_0 \frac{\hat{j} - \hat{i}}{\sqrt{2}} \cos \left(\omega t + k \frac{\hat{i} + \hat{j}}{\sqrt{2}}\right)$$

(B) 
$$B_0 \hat{k} \cos \left(\omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}}\right)$$

(C) 
$$B_0 \frac{\hat{i} - \hat{j}}{\sqrt{2}} cos \left( \omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$$

(D) 
$$B_0 \frac{\hat{i} + \hat{j}}{\sqrt{2}} \cos \left( \omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$$

- A wire of length L and mass per unit length  $6.0 \times 10^{-3}$  kg m<sup>-1</sup> is put under tension of 540 5. N. Two consecutive frequencies that it resonates at are: 420 Hz and 490 Hz. Then L in meters is
  - (A) 1.1 m

(B) 5.1 m

(C) 2.1 m

(D) 8.1 m

- A particle of mass m is projected with a speed u form the ground at an angle  $\theta = \frac{\pi}{3}$  w.r.t. 6. horizontal (x-axis). When it has reached its maximum height, it collides completely inelastically with another particle of the same mass and velocity ui. The horizontal distance covered by the combined mass before reaching the ground is:
  - (A)  $\frac{5}{8} \frac{u^2}{a}$
- (B)  $\frac{3\sqrt{2}}{4} \frac{u^2}{a}$  (C)  $\frac{3\sqrt{3}}{8} \frac{u^2}{a}$
- (D)  $2\sqrt{2}\frac{u^2}{a}$
- 7. In LC circuit the inductance L = 40 mH and capacitance C = 100  $\mu$ F. If a voltage V(t) = 10 sin (314 t) is applied to the circuit, the current in the circuit is given as
  - (A) 5.2 cos 314 t

(B) 0.52 sin 314 t

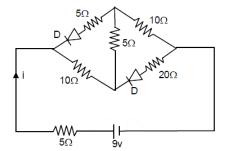
(C) 0.52 cos 314 t

- (D) 10 cos 314 t
- 8. Two gases argon (atomic radius 0.07 nm, atomic weight 40) and xenon (atomic radius 0.1 nm, atomic weight 140) have the same number density and are at the same temperature. The ratio of their respective mean free times is closest to:
  - (A) 1.83

(B) 2.3

(C) 3.67

- (D) 4.67
- 9. The current i in the network is:
  - (A) 0.6 A
  - (B) 0 A
  - (C) 0.2 A
  - (D) 0.3 A



- A rod of length L has non-uniform linear mass density given by  $\rho(x) = a + b \left(\frac{x}{L}\right)^2$ , where 10. a and b are constants and  $0 \le x \le L$ . The value of x for the centre of mass of the rod is
  - (A)  $\frac{3}{2} \left( \frac{a+b}{2a+b} \right) L$

(B)  $\frac{4}{3}\left(\frac{a+b}{2a+3b}\right)L$ 

(C)  $\frac{3}{4} \left( \frac{2a+b}{3a+b} \right) L$ 

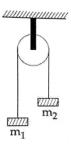
- (D)  $\frac{3}{2}\left(\frac{2a+b}{3a+b}\right)L$
- Two steel wires having same length are suspended from a ceiling under the same load. 11. If the ratio of their energy stored per unit volume is 1:4, the ratio of their diameters is
  - (A) 1:  $\sqrt{2}$
- (B) 2:1
- (C)  $\sqrt{2}:1$
- (D) 1:2
- Planet A has mass M and radius R. Plant B has half the mass and half the radius of 12. Planet A. If the escape velocities from the planets A and B are v<sub>A</sub> and v<sub>B</sub>, respectively,
  - then  $\frac{v_A}{v_B} = \frac{n}{4}$ . The value of 'n' is:
  - (A) 2

(B) 1

(C) 4

(D) 3

13. A uniformly thick wheel with moment of inertia I and radius R is free to rotate about its centre of mass (see fig). A massless string is wrapped over its rim and two blocks of masses  $m_1$  and  $m_2$  ( $m_1 > m_2$ ) are attached to the ends of the string. The system is released for rest. The angular speed of the wheel when  $m_1$  descents by a distance h is:



$$\text{(A)} \left[ \frac{2(m_1 + m_2)gh}{(m_1 + m_2)\,R^2 + 1} \right]^{\!\frac{1}{2}}$$

(B) 
$$\left[\frac{2(m_1 - m_2)gh}{(m_1 + m_2)R^2 + 1}\right]^{\frac{1}{2}}$$

(C) 
$$\left[\frac{(m_1 - m_2)}{(m_1 + m_2) R^2 + 1}\right]^{\frac{1}{2}} gh$$

(D) 
$$\left[\frac{(m_1 + m_2)}{(m_1 + m_2) R^2 + 1}\right]^{\frac{1}{2}} gh$$

- 14. The energy required to ionize a hydrogen like ion in its ground state is 9 Rydbergs. What is the wavelength of the radiation emitted when the electron in this ion jumps from the second excited state to the ground state?
  - (A) 11.4 nm

(B) 35.8 nm

(C) 24.2 nm

- (D) 8.6 nm
- 15. An electron of mass m and magnitude of charge  $|\mathbf{e}|$  initially at rest gets accelerated by a constant electric field E. The rate of change of de-Broglie wavelength of this electron at time t ignoring relativistic effects is
  - (A)  $\frac{|e|Et}{h}$

(B)  $-\frac{h}{|e|Et}$ 

(C)  $-\frac{h}{|e|E\sqrt{t}}$ 

- (D)  $-\frac{h}{|e|Et^2}$
- 16. A particle starts from the origin at t = 0 with an initial velocity of 3.0  $\hat{i}$  m/s and moves in the x-y plane with a constant acceleration  $(6.0 \ \hat{i} + 4.0 \ \hat{j})$  m/s<sup>2</sup>. The x-coordinate of the particle at the instant when its y-coordinate is 32 m is D meters. The value of D is
  - (A) 40

(B) 60

(C) 32

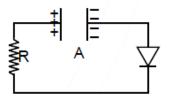
- (D) 50
- 17. A small circular loop of conducting wire has radius a and carries current I. It is placed in a uniform magnetic field B perpendicular to its plane such that when rotated slightly about its diameter and released, it starts performing simple harmonic motion of time period T. If the mass of the loop is m then:
  - (A)  $T = \sqrt{\frac{\pi m}{IB}}$

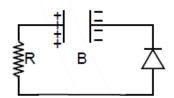
(B)  $T = \sqrt{\frac{\pi m}{2IB}}$ 

(C)  $T = \sqrt{\frac{2\pi m}{IB}}$ 

(D)  $T = \sqrt{\frac{2m}{IB}}$ 

18. Two identical capacitors A and B, charged to the same potential 5V are connected in two different circuits as shown below at time t = 0. If the charge on capacitors A and B at time t = CR is  $Q_A$  and  $Q_B$  respectively, then (Here e is the base of natural logarithm)





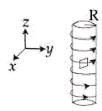
(A) 
$$Q_A = VC, Q_B = CV$$

$$(B) \ Q_{A} = \frac{VC}{e}, Q_{B} = \frac{CV}{2}$$

(C) 
$$Q_A = VC, Q_B = \frac{VC}{P}$$

(D) 
$$Q_A = \frac{VC}{2}, Q_B = \frac{VC}{e}$$

19. An electron gun is placed inside a long solenoid of radius R on its axis. The solenoid has n turns/length and carries a current I. The electron gun shoots an electron along the radius of the solenoid with speed v. If the electron does not hit the surface of the solenoid, maximum possible value of v is (all symbols have their standard meaning):



(A) 
$$\frac{2e\mu_0 nIR}{m}$$

(B) 
$$\frac{e\mu_0 nIR}{m}$$
 (C)  $\frac{e\mu_0 nIR}{4m}$ 

(C) 
$$\frac{e\mu_0 nIR}{4m}$$

(D) 
$$\frac{e\mu_0 nIR}{2m}$$

20. A spring mass system (mass m, spring constant k and natural length  $\ell$ ) rests in equilibrium on a horizontal disc. The free end of the spring is fixed at the centre of the disc. If the disc together with spring mass system, rotates about it's axis with an angular velocity  $\omega$ , (k>>m $\omega^2$ ) the relative change in the length of the spring is best given by the option:

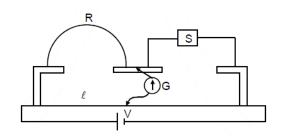
(A) 
$$\frac{m\omega^2}{3k}$$

(B) 
$$\frac{m\omega^2}{k}$$

(C) 
$$\frac{2m\omega^2}{3k}$$

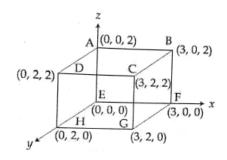
(D) 
$$\sqrt{\frac{2}{3}} \left( \frac{m\omega^2}{k} \right)$$

21. In a meter bridge experiment S is a standard resistance. R is a resistance wire. It is found that balancing length is  $\ell = 25$ cm. If R is replaced by a wire of half length and half diameter that of R of same material, then the balancing distance  $\ell'$  (in cm) will now be \_\_\_\_\_

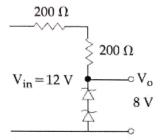


22. Starting at temperature 300 K, one mole of an ideal diatomic gas ( $\gamma$  = 1.4) is first compressed adiabatically form volume  $V_1$  to  $V_2 = \frac{V_1}{16}$ . It is then allowed to expand isobarically to volume 2V2. If all the processes are the quasi-static then the final temperature of the gas (in °K) is (to the nearest integer)

23. An electric field  $\vec{E} = 4x\hat{i} - (y^2 + 1)\hat{j}\,N/C$  passes through the box shown in figure. The flux of the electric field through surfaces ABCD and BCGF are marked as  $\phi_I$  and  $\phi_{II}$  respectively. The difference between  $(\phi_I - \phi_{II})$  is (in Nm²/C) \_\_\_\_\_.



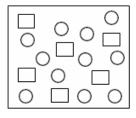
- 24. In a Young's double's slit experiment 15 fringes are observed on a small portion of the screen when light of wavelength 500 nm is used. Ten fringes are observed on the same section of the screen when another light source of wavelength  $\lambda$  is used. Then the value of  $\lambda$  is (in nm) \_\_\_\_\_\_.
- 25. The circuit as shown in figure is working as a 8 V dc regulated voltage source. When 12 V is used as input, the power dissipated (in mW) in each diode is (considering both zener diodes are identical)



# PART -B (CHEMISTRY)

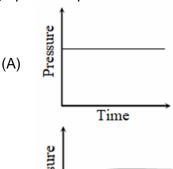
26.	Amongst the following, the form of water wit (A) sea water (B) distilled water (C) saline water used for intravenous injection (D) water from a well	
27.	The correct order of the spin-only magnetic (I) $[Cr(H_2O)_6]Br_2$ (III) $Na_3[Fe(C_2O_4)_3](D0 > P)$ (A) (I) > (IV) > (III) > (II) (C) (III) > (I) > (IV) > (II)	moments of the following complexes is: (II) $Na_4[Fe(CN)_6]$ (IV) $(Et_4N)_2[CoCl_4]$ (B) (II) » (I) > (IV) > (III) (D) (III) > (I) > (IV)
28.	Which polymer has 'chiral' monomer(s)? (A) Nylon 6, 6 (C) PHBV	(B) Neoprene (D) Buna-N
29.		es of a metal are 496 and 4560 kJ mol <sup>-1</sup> , $H_2SO_4$ , respectively, will be needed to reacted?  (B) 1 and 2  (D) 1 and 0.5
30.	Among the statements (a) – (d), the correct (a)Lithium has the highest hydration enthals (b) Lithium chloride is insoluble in pyridine. (c) Lithium cannot form ethynide upon its re (d) Both lithium and magnesium react slowly (A) (a), (b) and (d) only (C) (b) and (c) only	by among the alkali metals.  action with ethyne
31.	The solubility product of $Cr(OH)_3$ at 298 K ions in a saturated solution of $Cr(OH)_3$ will be (A) $(18 \times 10^{-31})^{1/4}$ (C) $(18 \times 10^{-31})^{1/2}$	is $6.0 \times 10^{-31}$ . The concentration of hydroxide to e:  (B) $(4.86 \times 10^{-29})^{1/4}$ (D) $(2.22 \times 10^{-31})^{1/4}$
32.	5 g of zinc is treated separately with an exce (a) dilute hydrochloric acid and The ratio of the volumes of H <sub>2</sub> evolved in the (A) 1:4 (C) 1:2	(b) aqueous sodium hydroxide.

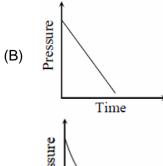
33. If the figure shown below reactant A (represented by square) is in equilibrium with product B (represented by circle). The equilibrium constant is:

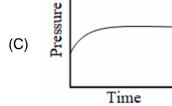


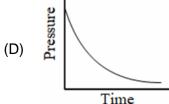
(A) 8 (C) 4

- (B) 2 (D) 1
- 34. A mixture of gases O<sub>2</sub>, H<sub>2</sub> and CO are taken in a closed vessel containing charcoal. The graph that represents the correct behaviour of pressure with time is:









- 35. The number of sp<sup>2</sup> hybrid orbitals in a molecule of benzene is
  - (A) 18

(B) 6

(C) 12

- (D) 24
- 36. Biochemical Oxygen Demand (BOD) is the amount of oxygen required (in ppm):
  - (A) for the photochemical breakdown of waste present in 1 m³ volume of a water body.
  - (B) for sustaining life in a water body.
  - (C) by bacteria to break-down organic waste in a certain volume of a water sample.
  - (D) by anaerobic bacteria to breakdown inorganic waste present in a water body.
- 37. The true statement amongst the following is:
  - (A) S is a function of temperature but DS is not a function of temperature.
  - (B) Both DS and S are functions of temperature.
  - (C) S is not a function of temperature but DS is a function of temperature.
  - (D) Both S and DS are not functions of temperature

38. A, B and C are three biomolecules. The results of the tests performed on them are given below:

	Molisch's Test	Barfoed Test	Biuret Test
(A)	Positive	Negative	Negative
(B)	Positive	Positive	Negative
(C)	Negative	Negative	Positive

A, B and C are respectively:

- (A) A = Lactose, B = Glucose, C = Alanine (B) A = Lactose, B = Glucose, C = Albumin
- (C) A = Glucose, B = Fructose, C = Albumin (D) A = Lactose, B = Fructose, C = Alanine
- 39. Consider the following reactions:

(i) NaNO<sub>2</sub>/HCl, 0-5°C  
(ii) 
$$\beta$$
-naphthol/NaOH  
Colored Solid

[P]
$$Br_2/H_2O \longrightarrow C_7H_6NBr_3$$

The compound[P] is

$$(A) \qquad \begin{array}{c} NH_2 \\ CH_3 \\ NH_2 \\ (C) \\ \end{array} \qquad (B) \qquad \begin{array}{c} NH_2 \\ NHCH_3 \\ \end{array}$$

40. Which of the following reactions will not produce a racemic product?

(A) 
$$H_3C$$
 $HC1$ 
 $CH_3$ 
(B)  $CH_3CH_2CH=CH_2$ 
 $HBr$ 
 $CH_3$ 

(C) 
$$\begin{array}{c} O \\ HCH_3-CCH_2CH_3 \end{array} \xrightarrow{HCN}$$
 (D)  $\begin{array}{c} CH_3 \\ CH_3-C-CH=CH_2 \end{array} \xrightarrow{HCl}$ 

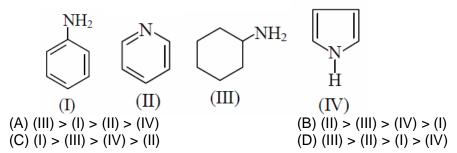
- 41. Which of the following has the shortest C–Cl bond?
  - (A)  $CI CH = CH NO_2$

(B) 
$$CI - CH = CH - OCH_3$$

(C)  $CI - CH = CH - CH_3$ 

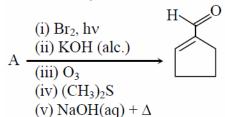
(D) 
$$CI - CH = CH_2$$

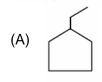
42. The decreasing order of basicity of the following amines is



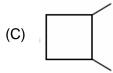
- 43. The reaction of  $H_3N_3B_3Cl_3(A)$  with LiBH<sub>4</sub> in tetrahydrofuran gives inorganic benzene (B). Further, the reaction of (A) with (C) leads to  $H_3N_3B_3(Me)_3$ . Compounds (B) and (C) respectively, are:
  - (A) Borazine and MeBr
  - (C) Diborane and MeMgBr

- (B) Boron nitride and MeBr
- (D) Borazine and MeMgBr
- 44. In the following reaction A is:









- (D)
- 45. The isomer (s) of  $[Co(NH_3)_4CI_2]$  that has/have a CI-Co-CI angle of 90°, is/are:
  - (A) meridional and trans

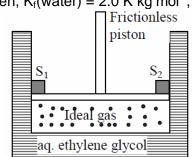
(B) cis only

(C) trans only

- (D) cis and trans
- 46. The sum of the total number of bonds between chromium and oxygen atoms in chromate and dichromate ions is \_\_\_\_\_\_
- 47. A sample of milk splits after 60 min. at 300 K and after 40 min. at 400 K when the population of *lactobacillus acidophilus* in it doubles. The activation energy (in kJ/mol) for this process is closest to \_\_\_\_\_

(Given, R = 8.3 J mol<sup>-1</sup>K<sup>-1</sup>, 
$$\ell n \left(\frac{2}{3}\right) = 0.4$$
,  $e^{-3} = 4.0$ )

48. A Cylinder containing an ideal gas (0.1 mol of 1.0 dm<sup>3</sup>) is in thermal equilibrium with a large volume of 0.5 molal aqueous solution of ethylene glycol at its freezing point. If the stoppers  $S_1$  and  $S_2$  (as shown in the figure) are suddenly withdrawn, the volume of the gas in litres after equilibrium is achieved will be\_. (Given,  $K_f(water) = 2.0 \text{ K kg mol}^1$ ,  $R = 0.08 \text{ dm}^3$  atm  $K^{-1}$  mo<sup>-1</sup>)



49. Consider the following reactions

$$A \xrightarrow{\quad (i) \ CH_3MgBr \quad} B \xrightarrow{\quad Cu \quad} \text{2-methyl-2-butene}$$

The mass percentage of carbon in A is\_\_\_\_.

50. 10.30 mg of  $O_2$  is dissolved into a liter of sea water of density 1.03 g/mL. The concentration of  $O_2$  in ppm is\_\_\_\_\_\_.

# PART-C (MATHEMATICS)

51.	If $x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$ and $y =$	$=\sum_{n=0}^{\infty}\cos^{2n}\theta,$	for $0 < \theta <$	$\frac{\pi}{4}$ , then:		
	(A) $y(1-x)=1$	-	(B) $y(1+x)$			
	(C) $x(1+y)=1$		(D) $x(1-y)$	v) = 1		
52.	If $p \rightarrow (p \land \sim q)$ is false, then the	ne truth value	s of p and o	are respecti	vely:	
	(A) F, T (C) T, T		(B) F, F (D) T, F			
53.	Let $a,b \in R, a \neq 0$ be such that	t the equatio	n ax² – 2b	x+5=0 has	s a repeated	d root $lpha$ ,
	which is also a root of the equation, then $\alpha^2 + \beta^2$ is equa		2bx – 10 =	0. If β is the	he other ro	ot of this
	(A) 28 (C) 26		(B) 24 (D) 25			
54.	Let [t] denote the greatest	: integer ≤1	t and lim	$\int_{X} \left[ \frac{4}{X} \right] = A$ .	Then the	function,
	$f(x) = \left[x^2\right] \sin(\pi x) \text{ is discontinuous, when x is equal to:}$					
	(A) $\sqrt{A + 21}$		(B) $\sqrt{A + }$			
	(C) √A		(D) $\sqrt{A+1}$	•		
55.	Let a function $f:[0,5] \rightarrow R$ be	continuous,	f(1) = 3 an	d F be define	ed as:	
	$F(x) = \int_{1}^{x} t^2 g(t) dt$ , where $g(t)$	$=\int_{1}^{t}f(u)du.$	Then for the	e function F,	the point x	= 1 is:
	(A) a point of local minima (C) not a critical point	1	(B) a poin	t of inflection. of local maxi		
56.	A random variable X has the fo	ollowing proba	ability distrik 2	oution: 3	4	5
	P(X) :	$K^2$	2K	K	2K	5K <sup>2</sup>
	Then $P(X > 2)$ is equal to:	•				
	(A) $\frac{1}{36}$		(B) $\frac{7}{12}$			
	(C) $\frac{23}{36}$		(D) $\frac{1}{6}$			
	36		6			

57. If  $\int \frac{d\theta}{\cos^2\theta \left(\tan 2\theta + \sec 2\theta\right)} = \lambda \tan\theta + 2\log_e \left|f\left(\theta\right)\right| + C$  where C is a constant of

integration, then the ordered pair  $\left(\lambda,\,f\left(\theta\right)\right)$  is equal to:

(A)  $\left(-1,1+\tan\theta\right)$ 

(B)  $(1,1-\tan\theta)$ 

(C)  $(1,1+\tan\theta)$ 

- (D)  $(-1,1-\tan\theta)$
- 58. If  $\frac{dy}{dx} = \frac{xy}{x^2 + y^2}$ ; y(1) = 1; then a value of x satisfying y(x) = e is:
  - (A)  $\sqrt{2}e$

(B)  $\frac{1}{2}\sqrt{3}e$ 

(C) √3e

- (D)  $\frac{e}{\sqrt{2}}$
- 59. Let  $a_n$  be the n<sup>th</sup> term of a G.P. of positive terms. If  $\sum_{n=1}^{100} a_{2n+1} = 200$  and  $\sum_{n=1}^{100} a_{2n} = 100$ , then  $\sum_{n=1}^{200} a_n$  is equal to:
  - (A) 225

(B) 300

(C) 150

- (D) 175
- 60. If z be a complex number satisfying |Re(z)| + |Im(z)| = 4, then |z| cannot be:
  - (A)  $\sqrt{\frac{17}{2}}$

(B)  $\sqrt{10}$ 

(C) √8

- (D)  $\sqrt{7}$
- 61. Given :  $f(x) = \begin{cases} x, & 0 \le x < \frac{1}{2} \\ \frac{1}{2}, & x = \frac{1}{2} \\ 1 x, & \frac{1}{2} < x \le 1 \end{cases}$  and  $g(x) = \left(x \frac{1}{2}\right)^2, x \in \mathbb{R}$ . Then the area (in sq.

units) of the region bounded by the curves, y = f(x) and y = g(x) between the lines 2x = 1 and  $2x = \sqrt{3}$ , is:

(A)  $\frac{1}{3} + \frac{\sqrt{3}}{4}$ 

(B)  $\frac{1}{2} + \frac{\sqrt{3}}{4}$ 

(C)  $\frac{\sqrt{3}}{4} - \frac{1}{3}$ 

(D)  $\frac{1}{2} - \frac{\sqrt{3}}{4}$ 

62.	In the expansion of $\left(\frac{x}{\cos \theta}\right)$	$\left(\frac{1}{x\sin\theta}\right)^{16}$ , if $I_1$ is the least value of the term independent
		n the ratio $I_2:I_1$ is equal to:
	(A) 1:16	(B) 1:8
	(C) 8:1	(D) 16 : 1

63. If 10 different balls are to be placed in 4 distinct boxes at random, then the probability that two of these boxes contain exactly 2 and 3 balls is:

(A) 
$$\frac{945}{2^{11}}$$
 (B)  $\frac{945}{2^{10}}$  (C)  $\frac{965}{2^{11}}$  (D)  $\frac{965}{2^{10}}$ 

64. If  $A = \{x \in R : |x| < 2\}$  and  $B = \{x \in R : |x - 2| \ge 3\}$ ; then:

(A) 
$$B - A = R - (-2, 5)$$
 (B)  $A \cap B = (-2, -1)$ 

(C) 
$$A - B = [-1, 2]$$
 (D)  $A \cup B = R - (2, 5)$ 

65. Let 
$$a-2b+c=1$$
. If  $f(x) = \begin{vmatrix} x+a & x+2 & x+1 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$ , then:

(A) 
$$f(-50) = 501$$
 (B)  $f(50) = 1$ 

(C) 
$$f(50) = -501$$
 (D)  $f(-50) = -1$ 

66. Let f and g be differentiable functions on R such that fog is the identity function. If for some  $a,b \in R,g'(a) = 5$  and g(a) = b, then f'(b) is equal to:

(A) 1 (B) 5 (C) 
$$\frac{1}{5}$$
 (D)  $\frac{2}{5}$ 

67. If one end of a focal chord AB of the parabola  $y^2 = 8x$  is at  $A\left(\frac{1}{2}, -2\right)$ , then the equation of the tangent to it at B is:

(A) 
$$2x - y - 24 = 0$$
  
(B)  $x - 2y + 8 = 0$   
(C)  $2x + y - 24 = 0$   
(D)  $x + 2y + 8 = 0$ 

68. If  $x = 2\sin\theta - \sin2\theta$  and  $y = 2\cos\theta - \cos2\theta$ ,  $\theta \in \left[0, 2\pi\right]$ , then  $\frac{d^2y}{dx^2}$  at  $\theta = \pi$  is:

(A) 
$$-\frac{3}{8}$$
 (B)  $\frac{3}{2}$ 

(C) 
$$\frac{3}{4}$$
 (D)  $-\frac{3}{4}$ 

69. The length of the minor axis (along y – axis) of an ellipse in the standard form is  $\frac{4}{\sqrt{3}}$ . If this ellipse touches the line, x + 6y = 8; then its eccentricity is:

(A) 
$$\frac{1}{3}\sqrt{\frac{11}{3}}$$

(B) 
$$\frac{1}{2}\sqrt{\frac{5}{3}}$$

(C) 
$$\frac{1}{2}\sqrt{\frac{11}{3}}$$

(D) 
$$\sqrt{\frac{5}{6}}$$

70. The following system of linear equation

$$7x + 6y - 2z = 0$$

$$3x + 4y + 2z = 0$$
 has

$$x-2y-6z=0,$$

- (A) infinitely many solutions, (x, y, z) satisfying x = 2z.
- (B) no solution
- (C) only the trivial solution.
- (D) infinitely many solutions, (x, y, z) satisfying y = 2z.
- 71. If the curves,  $x^2 6x + y^2 + 8 = 0$  and  $x^2 8y + y^2 + 16 k = 0$ , (k > 0) touch each other at a point, then the largest value of k is \_\_\_\_\_.
- 72. If  $C_r = {}^{25}C_r$  and  $C_0 + 5.C_1 + 9.C_2 + \dots + (101).C_{25} = 2^{25}.k$ , then k is equal to
- 73. Let  $\vec{a}, \vec{b}$  and  $\vec{c}$  be three vectors such that  $\left| \vec{a} \right| = \sqrt{3}, \left| \vec{b} \right| = 5, \ \vec{b}.\vec{c} = 10$  and the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$ . If  $\vec{a}$  is perpendicular to the vector  $\vec{b} \times \vec{c}$ , then  $\left| \vec{a} \times \left( \vec{b} \times \vec{c} \right) \right|$  is equal to\_\_\_\_.
- 74. If the distance between the plane, 23x-10y-2z+48=0 and the plane  $\frac{x+1}{2}=\frac{y-3}{4}=\frac{z+1}{3} \text{ and } \frac{x+3}{2}=\frac{y+2}{6}=\frac{z-1}{\lambda}\big(\lambda\in R\big) \text{ is equal to } \frac{k}{\sqrt{633}}, \text{ then k is equal to } \underline{\hspace{1cm}}$
- 75. The number of terms common to the two A.P.'s 3, 7, 11,..........407 and 2, 9, 16, .....709 is \_\_\_\_\_\_

# JEE (Main) – 2020 ANSWERS

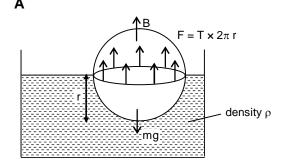
#### PART -A (PHYSICS)

1.	Α	2.	В	3.	Bonus	4.	С
5.	С	6.	С	7.	С	8.	Α
9.	D	10.	С	11.	С	12.	С
13.	В	14.	Α	15.	D	16.	В
17.	С	18.	С	19.	D	20.	В
21.	40	22.	1819	23.	48	24.	750
25.	40						
		PAF	RT -B (CH	EMIS	TRY)		
26.	В	27.	Α	28.	С	29.	D
30.	D	31.	Α	32.	В	33.	В
34.	D	35.	Α	36.	С	37.	В
38.	В	39.	В	40.	D	41.	Α
42.	D	43.	D	44.	В	45.	В
46.	12	47.	3.98	48.	2.18	49.	66.67
50.	10						
PART-C (MATHEMATICS)							
51.	Α	52.	С	53.	D	54.	D
55.	Α	56.	С	57.	Α	58.	С
59.	С	60.	D	61.	С	62.	D
63.	Bonus	64.	Α	65.	В	66.	С
67.	В	68.	Bonus mark	69.	С	70.	Α
71.	36	72.	51	73.	30	74.	3
75.	14						

### HINTS AND SOLUTIONS

#### PART -A (PHYSICS)

1. Sol.



$$dVg = \rho \left(\frac{V}{2}\right)g + T(2\pi r)$$

$$mq = B + F$$

$$mg = B + F$$

$$\Rightarrow d\frac{4}{3}\pi r^{3}g = \rho \cdot \frac{2}{3}\pi r^{2}g + 2\pi T$$

$$\Rightarrow \frac{2}{3}r^2g(2d-\rho) = 2T$$

$$\Rightarrow \quad r = \sqrt{\frac{3T}{(2d - \rho)g}}$$

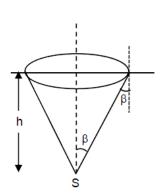
2.

Sol. 
$$\sin \beta = \frac{3}{4}, \cos \beta = \frac{\sqrt{7}}{4}$$

Solid angle  $d\Omega = 2\pi R^2 (1 - \cos \beta)$ 

Percentage of light = 
$$\frac{2\pi R^2 (1 - \cos \beta)}{4\pi R^2} \times 100$$

$$=\frac{1-\cos\beta}{2}\times100=\left(\frac{4-\sqrt{7}}{8}\right)\times100\approx17\%$$



3. **Bonus** 

Sol. 
$$A_1 + B_1 + C_1 = 24.36 + 0.0724 + 256.2 = 280.6324 = 280.6$$
  
 $A_2 + B_2 + C_2 = 24.44 + 16.082 + 240.2 = 280.722 = 280.7$   
 $A_3 + B_3 + C_3 = 25.2 + 19.2812 + 236.183 = 280.6642 = 280.7$   
 $A_4 + B_4 + C_4 = 25 + 236.191 + 19.5 = 280.691 = 281$ 

Answer should be 
$$A_4 + B_4 + C_4 > A_3 + B_3 + C_3 = A_2 + B_2 + C_2 > A_1 + B_1 + C_1$$

4.

Sol. EM wave is in direction 
$$\rightarrow \frac{\hat{i} + \hat{j}}{\sqrt{2}}$$

Electric field is in direction  $\rightarrow k$ 

 $\vec{E} \times \vec{B} \rightarrow$  direction of propagation of EM wave.

5.

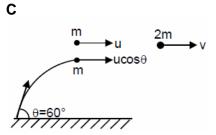
Sol. Fundamental frequency = 
$$490 - 420 = 70$$
 Hz. 
$$70 = \frac{1}{2\ell} \sqrt{\frac{T}{U}}$$

$$\Rightarrow 70 = \frac{1}{2\ell} \sqrt{\frac{540}{6 \times 10^{-3}}}$$

$$\Rightarrow \ell = \frac{1}{2 \times 70} \sqrt{90 \times 10^{3}} = \frac{300}{140}$$

$$\Rightarrow \ell \approx 2.14 \text{ m}$$

6. Sol.



 $p_i = p_f$   $mu + mu \cos 60 = 2mv$   $v = \frac{3u}{4}$ 

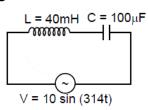
so horizontal range after collision

$$= v \sqrt{\frac{2H_{max}}{g}}$$

$$= \frac{3}{4} u \sqrt{\frac{2u^2 \sin^2(60^\circ)}{2g^2}}$$

$$= \frac{3}{4} u^2 \frac{\sqrt{\frac{3}{4}}}{a} = \frac{3\sqrt{3}u^2}{8a}$$

7. Sol.



$$V = 10 \sin (312)$$

$$V_{L}$$

$$V_{C}$$

$$V_{C}$$

$$V_{C}$$

$$z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$R = 0$$

$$Z = X_{L} - X_{C}$$

$$= \left| \omega L - \frac{1}{\omega C} \right|$$

$$= 31.84 - 12.56$$

$$\begin{array}{l} X_L = X_C \\ V_L = V_C \end{array}$$

$$i = \frac{V_0}{z} \sin \left( 314t + \frac{\pi}{2} \right)$$

$$\therefore i = \frac{V_0}{7} \cos(314t)$$

$$\Rightarrow i = \frac{10}{19.28} \cos(314t)$$

$$\Rightarrow$$
 i = 0.52 cos (314t)

8. **A** 

Sol. Mean free time = 
$$\frac{1}{\sqrt{2}n\pi d^2} V_{rms}$$

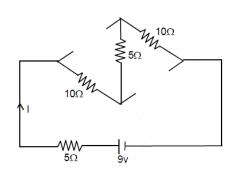
$$\begin{split} &\frac{t_{Ar}}{t_{Xe}} = \frac{d_{xe}^2}{d_{Ar}^2} \times \sqrt{\frac{m_1}{m_2}} \\ &= \left(\frac{0.1}{0.07}\right)^2 \times \sqrt{\frac{40}{140}} = 1.07 \end{split}$$

Hence, the nearest answer is 1.

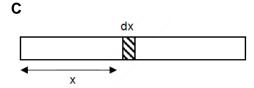
9.

Sol. Both diodes are in reverse biased.

$$I = \frac{9}{30} = \frac{3}{10} A = 0.3 A$$



10. Sol.



$$X_{cm} = \frac{1}{M} \int_{0}^{\ell} X.dM$$

$$dM = \rho.dx = \left(a + b\left(\frac{x}{L}\right)^{2}\right) \cdot dx$$

$$x_{cm} = \frac{\int x dM}{\int dM} = \frac{\int x \rho dx}{\int \rho dx} = \frac{\int\limits_{0}^{L} x \left(a + \frac{bx^2}{L^2}\right) dx}{\int\limits_{0}^{L} \left(a + \frac{bx^2}{L^2}\right) dx}$$

$$=\frac{a\left(\frac{x^{2}}{2}\right)_{0}^{L}+\frac{b}{L^{2}}\left(\frac{x^{4}}{4}\right)_{0}^{L}}{a(x)_{0}^{L}+\frac{b}{L^{2}}\left(\frac{x^{3}}{3}\right)_{0}^{L}}=\frac{(2a+b)L}{(3a+b)4}\times3$$

$$=\frac{3\ell}{4}\bigg(\frac{2a+b}{3a+b}\bigg)$$

Sol. 
$$\frac{du}{dv} = \frac{1}{2} stress \times \frac{stress}{y}$$
$$= \frac{1}{2} \frac{F^2}{A^2 y}$$

$$\frac{du}{dv} \propto \frac{1}{d^4} \quad ; \quad \frac{\left(\frac{du}{dv}\right)_1}{\left(\frac{du}{dv}\right)_2} = \frac{d_2^4}{d_1^4} = \frac{1}{4}$$

$$\frac{d_1}{d_2} = (4)^{1/4} \quad ; \quad \frac{d_1}{d_2} = \sqrt{2} : 1$$

12. **C**
Sol. 
$$v_e = \sqrt{\frac{2GM}{R}}$$

$$\therefore \frac{v_1}{v_2} = \frac{\sqrt{\frac{2GM}{R}}}{\sqrt{\frac{2GM/2}{R/2}}} = 1 = \frac{n}{4}$$

$$\Rightarrow n = 4.$$

Sol. 
$$k_{i} + U_{i} = k_{1} + k_{2} + u_{1} + u_{2}$$

$$0 + 0 = \frac{1}{2}m_{2}v^{2} + \frac{1}{2}m_{1}v^{2} + \frac{1}{2}I\omega^{2} - m_{1}gh + m_{2}gh$$

$$(m_{1} - m_{2})gh = \frac{1}{2}m_{2}(\omega R)^{2} + \frac{1}{2}m_{1}(\omega R^{2}) + \frac{1}{2}I\omega^{2}$$

$$\frac{2(m_{1} - m_{2})gh}{\sqrt{(m_{1} + m_{2} + \frac{1}{R^{2}})R^{2}}} = \omega$$

$$\omega = \sqrt{\frac{2(m_{1} - m_{2})gh}{(m_{1} + m_{2})R^{2} + I}}$$

Sol. 
$$\frac{hc}{\lambda} = (13.6 \text{ eV})z^{2} \left[ \frac{1}{n_{1}^{2}} - \frac{1}{n_{2}^{2}} \right]$$

$$n_{1} = 1 \quad ; \quad n_{2} = 3$$

$$\frac{hc}{\lambda} = (13.6 \text{ eV}) (3^{2}) \left[ \frac{1}{1^{2}} - \frac{1}{3^{3}} \right]$$

$$\Rightarrow \frac{hc}{\lambda} = (13.6 \text{ eV}) (9) \left( \frac{8}{9} \right)$$
Wavelength =  $\frac{1240}{8 \times 13.6}$  nm
$$\lambda = 11.39 \text{ nm}$$

Sol. 
$$\lambda_D = \frac{h}{mv}$$

$$\therefore v = at$$

$$v = \frac{eE}{m}t$$

$$\lambda_D = \frac{h}{m\left(\frac{eE}{m}\right)t}$$

$$\lambda_0 = \frac{h}{eEt}$$

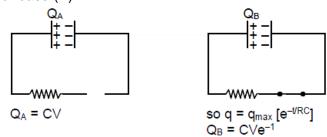
$$\frac{d\lambda_d}{dt} = -\frac{h}{|e|Et^2}$$

Sol. 
$$s_y = u_y t + \frac{1}{2} a_y t^2$$
  
 $32 = 0 + \frac{1}{2} \times 4 t^2 \implies t = 4 \text{ sec}$   
 $S_x = u_x t + \frac{1}{2} a_x t^2$   
 $= 3 \times 4 + \frac{1}{2} \times 6 \times 16 = 60 \text{ m.}$ 

Sol. 
$$\tau = MB \sin \theta = I\alpha$$
 
$$\pi R^2 I B\theta = \frac{mR^2}{2} \alpha$$
 
$$\omega = \sqrt{\frac{2\pi IB}{m}} = \frac{2\pi}{T} \quad ; \quad T = \sqrt{\frac{2\pi m}{IB}}$$

#### 18. **C**

Sol. Maximum charge on capacitor = 5CV
(A) is reverse biased and (B) is forward biased for case (A).



$$\begin{split} \text{Sol.} \qquad R_{\text{max}} = & \frac{R}{2} = \frac{m v_{\text{max}}}{q B} = \frac{m v_{\text{max}}}{e \mu_0 l n} \\ V_{\text{max}} = & \frac{Re \, \mu_0 l n}{2m} \end{split}$$

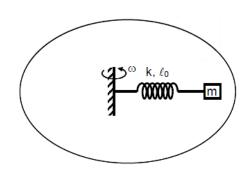
Sol. 
$$m\omega^2 (\ell_0 + x) = kx$$

$$\left(\frac{\ell_0}{x} + 1\right) = \frac{k}{m\omega^2}$$

$$x = \frac{\ell_0 m\omega^2}{k - m\omega^2}$$
$$k >> m\omega^2$$

$$k \gg m\omega^2$$

So, 
$$\frac{x}{\ell_0}$$
 is equal to  $\frac{m\omega^2}{k}$ 



#### 21.

Sol. 
$$\frac{x}{R} = \frac{75}{25} = 3$$

$$R = \frac{\rho \ell}{A} = \frac{4\rho \ell}{\pi d^2}$$

$$R' = \frac{4\rho\left(\frac{\ell}{2}\right)}{\pi\left(\frac{d}{2}\right)^2} = 2R \quad ; \quad \text{then } \frac{X}{R'} = \left(\frac{100 - \ell}{\ell}\right)$$

$$\frac{100-\ell}{\ell} = \frac{X}{2R} = \frac{3}{2}$$

$$\ell$$
 = 40.00 cm

Sol. 
$$PV^{\gamma} = constant$$

$$TV^{\gamma-1} = constant$$

$$300 (V_1)^{14-1} = T_B \left(\frac{V_1}{16}\right)^{2/5}$$

$$T_B = 300 \times 2^{8/5}$$

$$T_{B} = 300 \times 2^{8/5}$$
Now for BC process
$$\frac{V_{B}}{T_{B}} = \frac{V_{C}}{T_{C}}$$

$$\frac{\mathbf{v}_{\mathsf{B}}}{\mathsf{T}_{\mathsf{B}}} = \frac{\mathsf{v}_{\mathsf{C}}}{\mathsf{T}_{\mathsf{C}}}$$

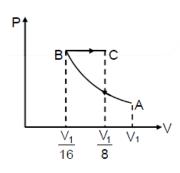
$$T_{\rm C} = \frac{V_{\rm C}T_{\rm B}}{V_{\rm B}} = 2 \times 300 \times 2^{8/5}$$

$$T_C = 1818.859$$
  
 $T_C = 1819$  K

$$T_{\rm C} = 1819 \text{ K}$$

$$\varphi_1 = \int \vec{E} d\vec{A} = 0$$

$$\varphi_2 = \int \vec{E} d\vec{A}$$



$$\begin{split} & \varphi_2 = \int \vec{E} \vec{A} = \left[ 4x \hat{i} - (y^2 + 1) \hat{j} \right] \cdot 4 \hat{i} \\ & = 16x, \ x = 3 \\ & \varphi_2 = 48 \frac{N - m^2}{C} \ ; \ \varphi_1 - \varphi_2 = -48 \frac{N - m^2}{C} \end{split}$$

Sol. 
$$15 \times 500 \times \frac{D}{d} = 10 \times \lambda_2 \times \frac{D}{d}$$
  
 $\lambda_2 = 15 \times 50 \text{ nm}$   
 $\lambda_2 = 750 \text{ nm}$ 

Sol. 
$$i = \frac{(12-8)}{(200+200)} A = \frac{4}{400} = 10^{-2} A$$
  
 $\therefore P = v \times i$ 

Power loss in each diode =  $(4) (10^{-2}) W = 40 \text{ mW}$ .

#### PART -B (CHEMISTRY)

- 26.
- Sol. The form of H<sub>2</sub>O with the lowest ionic conductance at 298 K is distilled water.
- 27. Α

Sol. 
$$[Cr(H_2O)_6]Br_2 : Cr^{2+} = [Ar] 4s^0 3d^4$$

$$n = 4$$
,  $\mu = \sqrt{n(n+2)} = \sqrt{24} \text{ BM}$ 

$$Na_4[Fe(CN)_6]: Fe^{2+} = [Ar] 4s^0 3d^6$$

$$n = 0, \mu = 0$$

$$Na_3[Fe(C_2O_4)_3]: Fe^{3+} = [Ar] 3d^5$$

$$t_{2g}^5 eg^0$$

$$n = 1, \mu = \sqrt{3} BM$$

$$(Et_4N)_2 [CoCl_4] : Co^{2+} = [Ar] 3d^7$$

$$e_g^4 t_{2g}^3$$

$$n=3,~\mu=\sqrt{15}~BM$$

- 28. C
- Sol.

- 3-Hydroxybutanoic acid
- 3-Hydroxypentanoic acid

- 29. D
- Metal: First ionization enthalpies = 496 kJ/mole Sol.

Second ionization enthalpies = 4560 kJ/mol

According to the given information, ionization enthalpies Metal belong to 1st group i.e. Monovalent cation.

$$\underset{1 \text{ mole}}{\mathsf{MOH}} + \underset{1 \text{ mole}}{\mathsf{HCI}} \longrightarrow \mathsf{MCI} + \underset{2}{\mathsf{H}_2}\mathsf{O}$$

$$2 \underset{\text{1mole}}{\mathsf{MOH}} + \underset{\text{1/2 mole}}{\mathsf{H}_2} \underset{\text{SO}_4}{\longrightarrow} M_2 \underset{\text{SO}_4}{\mathsf{SO}_4} + \underset{\text{P}_2}{\mathsf{O}}$$

30. E

Sol. Lithium has the highest hydration enthalpy among the alkali metals due to small size. Lithium chloride is covalent in nature so it's soluble in non-polar solvent. Lithium and Magnesium react slowly with H<sub>2</sub>O

31. A

Sol. 
$$Cr(OH)_3 \rightleftharpoons Cr^{3+} + 3OH^-$$
  
 $K_{sp} = [Cr^{3+}][OH^-]^3$   
 $6 \times 10^{-31} = S \times (3S)^3$   
 $6 \times 10^{-31} = 27 S^4$   
 $S = \left(\frac{6}{27} \times 10^{-31}\right)^{1/4}$   
 $[OH^-] = 3S$   
 $= 3\left(\frac{6}{27} \times 10^{-31}\right)^{1/4} = (18 \times 10^{-31})^{1/4} M$ 

32. B

Sol. 
$$Zn + 2 dil.HCl \longrightarrow ZnCl_2 + H_2$$

$$Zn + 2NaOH \longrightarrow Na_2ZnO_2 + H_2$$

Mole of Zn = 
$$\frac{\frac{\text{Mole of dil. HCl}}{2} = \frac{\text{Mole of NaOH}}{2}}{\frac{\text{volume of HCl}}{\text{volume of NaOH}}} = \frac{1}{1}$$

**33**. B

Sol. 
$$A \rightarrow B$$

$$K_{eq} = \frac{\begin{bmatrix} B \end{bmatrix}}{\begin{bmatrix} A \end{bmatrix}} = \frac{11}{6}$$

34. D Sol.

On increasing time, pressure will be decreases.

35. A

Sol.

Benzene : 
$$C_6H_6$$
  $sp^2$   $sp^2$   $sp^2$   $sp^2$ 

In benzene, each carbon is sp<sup>2</sup> Hybridize Total number of carbon = 6(sp<sup>2</sup> Hybri)

 $\therefore$  Total hybrid orbital =  $6 \times 3 = 18$ 

**36**. C

Sol. Biochemical oxygen demand(BOD)

The amount of oxygen required by bacteria to break down the organic matter present in a certain volume of a sample of water.

37. E

Sol. 
$$S = \int \frac{dq}{T}$$

$$\Delta S = nC \int_{T_4}^{T_2} dT$$

Both  $\Delta S$  and S are function of temperature.

38. B

Sol. Lactose: Molisch's test

Glucose: Molisch's test and Barfoed test

Alumin: Biuret test

39. B

Sol.

$$\begin{array}{c} NaNO_2/HCl \\ O-5^{\circ}C \\ \hline \\ CH_3 \\ \hline \\ Br_2/H_2O \\ \hline \\ Br \\ \hline \\ CH_3 \\ \hline \\ Br \\ \hline \\ CH_3 \\ \hline \\ Br \\ \hline \\ CH_3 \\ CH_3 \\ \hline \\ CH_3 \\ \hline \\ CH_3 \\ CH_3 \\ \hline \\ CH_3 \\ CH_3 \\ CH_3 \\ CH_3 \\ CH_3 \\ CH_4 \\ CH_5 \\$$

40. D

Sol. 
$$CH_3$$
  $CH_3$   $CH$ 

41. A

42. D

Sol  $NH_2$ : Nitrogen  $\ell.p.$  not participate in resonance.  $NH_2$ 

: Nitrogen \( \ell \).p. participate in resonance.

: Nitrogen  $\ell$ .p. participate in resonance and increase the stability of the compound due to aromicit H

: Nitrogen  $\ell$ .p. not participate in resonance due to increase the stability of the compound.

43. D

 $\begin{array}{ccc} \text{Sol.} & B_3N_3H_3Cl_3 + \text{LiBH}_4 & \longrightarrow & B_3N_3H_6 \\ & & & & \text{(B)} \\ & & & & \text{Inorganic} \\ & & & \text{Benzene} \\ & & & \text{or} \\ & & & \text{Borazine} \\ \\ & & & & \\ & & & \\ & & & & \\$ 

44. B

45. B
Sol. [Co(NH<sub>3</sub>)<sub>4</sub>Cl<sub>2</sub>]  $\begin{array}{c}
H_3N & \downarrow \\
H_3N & \downarrow \\
\end{array}$ NH<sub>3</sub>

46. 12 Sol. Chromate = 
$$\operatorname{CrO}_4^{2-}$$
  $\operatorname{Cr}_{O}$   $\operatorname$ 

Total number of Cr-O bond = 12

$$\begin{array}{ll} \text{47.} & \text{3.98} \\ \text{Sol.} & \ell n \frac{K_2}{K_1} = \frac{Ea}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right] \\ & \ell n \frac{60}{40} = \frac{Ea}{8.3} \left[ \frac{1}{300} - \frac{1}{400} \right] \\ & \text{Ea} = 3.98 \text{ kJ/mole.} \end{array}$$

$$\begin{array}{ll} 48. & 2.18 \\ \text{Sol.} & \Delta T_f = K_f \times i \times m \\ & \Delta T_f = 2.0 \times 1 \times 0.5 \\ & \Delta T_f = 1 \\ & 273 - T_1 = 1 \\ & T_1 = 272 \text{ K} \\ & P = \frac{nRT}{V} \\ & P = \frac{0.1 \times 0.08 \times 272}{1} \\ & P = 2.176 \text{ atm} \\ & \text{Apply Boyle's law} \\ & P_1 V_1 = P_2 V_2 \\ & 2.176 \times 1 = 1 \times V_2 \\ & V_2 = 2.17 \\ \end{array}$$

50.

49. 66.67 Sol. 
$$\begin{array}{c} \text{OH} \\ \text{CH}_3\text{--C-CH}_2\text{--CH}_3 & \xrightarrow{\text{CH}_3\text{MgBr}} \text{CH}_3\text{--C-CH}_2\text{--CH}_3 \\ \text{CH}_3 & \text{CH}_3\text{--C-CH-CH}_3 \\ \text{CH}_3 & \text{CH}_3\text{--C-CH-CH}_3 \\ \text{CH}_3 & \text{CH}_3\text{--C-CH-CH}_3 \\ \text{CH}_3 & \text{CH}_3 & \text{CH}_3\text{--C-CH-CH}_3 \\ \text{CH}_3 & \text{CH}_3 & \text{CH}_3\text{--C-CH-CH}_3 \\ \text{Molar mass} & \times \text{Atomicity} \\ \text{Molar mass} & \times 100 \\ \text{=} & \frac{12 \times 4}{72} \times 100 = 66.66\% \\ \end{array}$$

Sol. PPM = 
$$\frac{\text{Mass of O}_2}{\text{Mass of water}} \times 10^6 = \frac{10.30 \times 10^{-3}}{1030} \times 10^6 = 10$$

## PART-C (MATHEMATICS)

Sol. Use 
$$1+r+r^2+....\infty = \frac{1}{1-r}, |r| < 1$$

$$x = \frac{1}{1 + \tan^2 \theta} = \cos^2 \theta$$

$$y = \frac{1}{1 + \tan^2 \theta} = \cos^2 \theta$$

$$y = \frac{1}{1 - \cos^2 \theta} = \frac{1}{\sin^2 \theta}$$

$$x + \frac{1}{y} = 1$$

Sol.

Р	Q	~ Q	$P \land \sim Q$	$P \rightarrow (P \land \sim Q)$
Т	Т	F	F	F
Т	F	Т	Т	Т
F	Т	F	F	Т
F	F	Т	F	Т

Sol. 
$$2\alpha = \frac{2b}{a} \Rightarrow \alpha = \frac{b}{a} \text{ and } \alpha^2 = \frac{5}{a}$$

$$\Rightarrow \frac{b^2}{a^2} = \frac{5}{a}$$

$$\Rightarrow$$
 b<sup>2</sup> = 5a .....(i) (a  $\neq$  0)

$$\alpha + \beta = 2b$$
 .....(ii)

and 
$$\alpha\beta = -10$$
 .....(iii)

$$\alpha = \frac{b}{a}$$
 is also root of  $x^2 - 2bx - 10 = 0$ 

$$\Rightarrow b^2 - 2ab^2 - 10a^2 = 0$$

by (i) 
$$\Rightarrow 5a - 10a^2 - 10a^2 = 0$$

$$\Rightarrow$$
 20a<sup>2</sup> = 5a

$$\Rightarrow$$
 a =  $\frac{1}{4}$  and b<sup>2</sup> =  $\frac{5}{4}$ 

$$\alpha^2 = 20$$
 and  $\beta^2 = 5$ 

Now 
$$\alpha^2 + \beta^2$$
  
= 5 + 20 = 25

Sol. 
$$\lim_{x \to 0} \left( \frac{4}{x} - \left\{ \frac{4}{x} \right\} \right) = A \Rightarrow \lim_{x \to 0} 4 - x \left\{ \frac{4}{x} \right\} = A$$
$$\Rightarrow 4 - 0 = A$$

check when

(A) 
$$x = \sqrt{A + 21} \Rightarrow x = 5 \Rightarrow$$
 continuous

(B) 
$$x = \sqrt{A+5} \Rightarrow x = 3 \Rightarrow continuous$$

(C) 
$$x = \sqrt{A} \Rightarrow x = 2 \Rightarrow$$
 continuous

(D) 
$$x = \sqrt{A+1} \Rightarrow x = \sqrt{5} \Rightarrow$$
 discontinuous

Sol. 
$$F'(x) = x^2g(x)$$
  
 $\Rightarrow F'(1) = 1.g(1) = 0$  ......(1)  $(\because g(1) = 0)$   
Now  $F''(x) = 2xg(x) + x^2g'(x)$   
 $\Rightarrow F''(x) = 2xg(x) + x^2f(x)$   $(\because g'(x) = f(x))$   
 $\Rightarrow F''(1) = 0 + 1 \times 3$   
 $\Rightarrow F''(1) = 3$  .....(2)

From (1) and (2) F (x) has local minimum at x = 1

Sol. 
$$\sum p_i = 1 \Rightarrow 6k^2 + 5k = 1$$

$$6k^2 + 5k - 1 = 0$$

$$6k^2 + 6k - k - 1 = 0$$

$$(6k - 1)(k + 1) = 0 \Rightarrow k = -1 \text{ (rejected)}; \ k = \frac{1}{6}$$

$$P(x > 2) = k + 2k + 5k^2$$

$$= \frac{1}{6} + \frac{2}{6} + \frac{5}{36} = \frac{6 + 12 + 5}{36} = \frac{23}{36}$$

Sol. 
$$\int \frac{\sec^2 \theta}{\frac{1 + \tan^2 \theta}{1 - \tan^2 \theta}} + \frac{2 \tan \theta}{1 - \tan^2 \theta} d\theta$$
$$= \int \frac{\sec^2 \theta \left(1 + \tan^2 \theta\right)}{\left(1 + \tan \theta\right)^2} d\theta$$

$$= \int \frac{\sec^2 \theta \left(1 - \tan \theta\right)}{1 + \tan \theta} d\theta$$

$$\tan \theta = t \Rightarrow \sec^2 \theta d\theta = dt$$

$$= \int \left(\frac{1 - t}{1 + t}\right) dt = \int \left(-1 + \frac{2}{1 + t}\right) dt$$

$$= -t + 2\log(1 + t) + C$$

$$= -\tan \theta + 2\log(1 + \tan \theta) + C$$

$$\Rightarrow \lambda = -1 \text{ and } f(\theta) = 1 + \tan \theta$$

58. C  
Sol. Put 
$$y = vx$$
  

$$\Rightarrow V + x \frac{dy}{dx} = \frac{vx^2}{x^2 + v^2x^2}$$

$$\Rightarrow \left(\frac{1 + V^2}{V^3}\right) dv = -\frac{dx}{x}$$

$$\Rightarrow \frac{-1}{2V^2} + \ln V = -\ln x + c$$

$$\Rightarrow -\frac{x^2}{2y^2} + \ln y = c$$
When  $x = 1$ ,  $y = 1 \Rightarrow c = \frac{-1}{2}$ 
When  $y = e \Rightarrow \frac{-x^2}{2c^2} + 1 = \frac{-1}{2}$ 

$$\Rightarrow$$
  $x^2 = 3e^2$ 

Sol. 
$$a_3 + a_5 + a_7 + \dots + a_{204} = \frac{ar^2 \left(1 - r^{200}\right)}{1 - r^2} \rightarrow (1)$$

$$a_2 + a_4 + a_6 + \dots + a_{200} = \frac{ar \left(1 - r^{200}\right)}{1 - r^2} \rightarrow (2)$$

$$(1) + (2) \Rightarrow a_2 + a_3 + a_4 + \dots + a_{201} = 300$$

$$r \left(a_1 + a_2 + a_3 + \dots + a_{201}\right) = 300$$

$$\sum_{n=1}^{100} a_n = \frac{300}{r}$$
Also  $(1) \div (2) \Rightarrow r = 2$ 

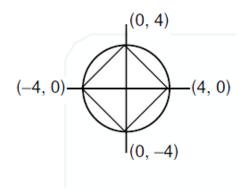
Sol. 
$$z = x + iy$$
  
 $|x| + |y| = 4$ 

Minimum value of  $|z| = 2\sqrt{2}$ 

Maximum value of |z| = 4

$$|z| \in [\sqrt{8}, \sqrt{16}]$$

So |z| can't be  $\sqrt{7}$ 



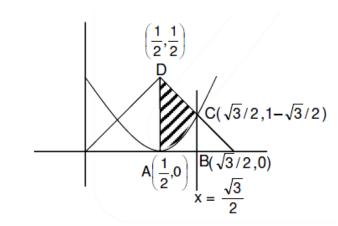
#### 61. C

Sol. Required area

= Area of trapezium ABCD 
$$-\int_{1/2}^{\sqrt{3}/2} \left(x - \frac{1}{2}\right)^2 dx$$

$$= \frac{1}{2} \left( \frac{\sqrt{3} - 1}{2} \right) \left( \frac{1}{2} + 1 - \frac{\sqrt{3}}{2} \right) - \frac{1}{3} \left( \left( x - \frac{1}{2} \right)^3 \right) \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}}$$

$$=\frac{\sqrt{3}}{4}-\frac{1}{3}$$



$$\text{Sol.} \qquad T_{r+1} = {}^{16}C_r {\left(\frac{x}{\cos\theta}\right)}^{16-r} {\left(\frac{1}{x\sin\theta}\right)}^r$$

for r = 8 term is free from 'x

$$T_9 = {}^{16}C_8 \frac{1}{\sin^8 \theta \cos^8 \theta}$$

$$T_9 = {}^{16}C_8 \frac{2^8}{(\sin 2\theta)^8}$$

In 
$$\theta \in \left[\frac{\pi}{8}, \frac{\pi}{4}\right]$$
,  $L_1 = {}^{18}C_8 \, 2^8 \quad \therefore \text{ (Min value of } L_1 \text{ at } \theta = \frac{\pi}{4}\text{)}$ 

In 
$$\theta \in \left[\frac{\pi}{16}, \frac{\pi}{8}\right]$$
,  $L_1 = {}^{16}C_8 \frac{2^8}{\left(\frac{1}{\sqrt{2}}\right)^8} = {}^{16}C_8.2^8.2^4 \ (\because \text{ min value of } L_2 \text{ at } \theta = \frac{\pi}{8})$ 

$$\frac{L_2}{L_1} = \frac{^{16}C_8.2^8 \, 2^4}{^{16}C_8.2^8} = 16$$

- 63. Bonus
- Sol. Case I : Exactly two box contain 2, 3 balls and other two box does not contains 2, 3 balls equals to  ${}^4C_2$

$$^{4}C_{2}\times2\times{}^{10}C_{2}\times{}^{8}C_{3}\times\left(2^{5}-\frac{5!}{2!3!}\times2!\right)$$

$$=2^4\times 3^2\times 45\times 8\times 7=2^7\times 3^4\times 5\times 7$$

Case - II: Two box contains 2 balls each and two box contain 3 balls each equals to

$$\frac{10!}{2!3!2!3!2!2!} \times 4!$$

$$=2^5\times3^3\times5^2\times7$$

$$\Rightarrow \text{ probability } = \frac{2^5 \times 3^3 \times 5 \times 7 \left(12 + 5\right)}{4^{10}} = \frac{3^3 \times 5 \times 7 \times 17}{2^{15}}$$

Sol. 
$$A = \{x : x \in (-2,2)\}$$

$$B = \{x : x \in (-\infty, -1] \cup [5, \infty)\}$$

$$A \cap B = \left\{ x : x \in \left(-2, -1\right] \right\}$$

$$A \cup B = \{x : x \in (-\infty, 2) \cup [5, \infty)\}$$

$$A - B = \{x : x \in (-1,2)\}$$

$$B-A=\left\{x:x\in\left(-\infty,-2\right]\cup\left[5,\infty\right)\right\}$$

Sol. Use 
$$R_1 \rightarrow R_1 + R_3 - 2R_2$$

$$f(x) = \begin{vmatrix} 1 & 0 & 0 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$$

Sol. Given that 
$$f(g(x)) = x$$

$$\Rightarrow f'(g(x)).g'(x) = 1$$

Put 
$$x = a$$

$$\Rightarrow$$
 f'(g(a))g'(a) = 1

$$\Rightarrow$$
 f'(b)×5=1

$$\Rightarrow$$
 f'(b) =  $\frac{1}{5}$ 

Sol. Given 
$$2at_1 = -2 \Rightarrow t_1 = \frac{-1}{2}$$
  
Also  $t_1t_2 = -1 \Rightarrow t_2 = 2$ 

Equation of tangent is  $t2y = x + at_2^2$  $\Rightarrow 2y = x + 8$ 

Sol. 
$$\frac{dx}{d\theta} = 2\cos\theta - 2\cos2\theta$$

$$\frac{dy}{d\theta} = -2\sin\theta + 2\sin2\theta$$

$$\frac{dy}{dx} = \frac{\sin2\theta - \sin\theta}{\cos\theta - \cos2\theta} = \cot\frac{3\theta}{2}$$

$$\frac{d^2y}{dx^2} = \frac{-3}{2}\csc^2\frac{3\theta}{2}.\left(\frac{d\theta}{dx}\right)$$

$$= \frac{-3}{2}\csc^2\left(\frac{3\theta}{2}\right).\frac{1}{(2\cos\theta - 2\cos2\theta)}$$

$$\frac{d^2y}{dx^2} = \frac{1}{2}\cos^2\left(\frac{3\theta}{2}\right) \cdot \frac{1}{(2\cos\theta - 2\cos2\theta)}$$

$$\frac{d^2y}{dx^2} = \frac{1}{2}\cos^2\left(\frac{3\theta}{2}\right) \cdot \frac{1}{4\sin\left(\frac{3\theta}{2}\right)\sin\left(\frac{\theta}{2}\right)}$$

$$= +\frac{3}{8}$$

69. C  
Sol. 
$$y = mx + c$$
, compare with  $x + 6y = 8$   

$$\Rightarrow m = \frac{-1}{6}$$

$$c^2 = a^2m^2 + b^2$$

$$\Rightarrow \frac{16}{9} = \frac{a^2}{36} + \frac{4}{3}$$

$$\Rightarrow a^2 = 16$$

$$e = \sqrt{1 - \left(\frac{b}{a}\right)^2} = \sqrt{\frac{11}{12}}$$

70. A 
$$\begin{vmatrix} 7 & 6 & -2 \\ 3 & 4 & 2 \\ 1 & -2 & -6 \end{vmatrix}$$

$$= 7(-20) - 6(-20) - 2(-10)$$
$$= -140 + 120 + 20 = 0$$

So infinite non - trivial solution exist

71. 36

Sol. Two circles touches each other if  $C_1C_2 = |r_1 \pm r_2|$ 

Distance between  $C_2(3,0)$  and  $C_1(0,4)$  is either  $\sqrt{k}+1=5$  or  $|\sqrt{k}-1|=5$ 

$$\Rightarrow$$
 k = 16 or k = 36

⇒ maximum value of k is 36

72. 51

$$\begin{split} \text{Sol.} \qquad & \sum_{r=0}^{25} \left(4r+1\right)^{25} C_r = 4 \sum_{r=0}^{25} r^{25} C_r + \sum_{r=0}^{25} {}^{25} C_r \\ & = 4 \sum_{r=1}^{25} r \times \frac{25}{r} {}^{24} C_{r-1} + 2^{25} = 100 \sum_{r=1}^{25} {}^{24} C_{r-1} + 2^{25} \\ & = 100.2^{24} + 2^{25} = 2^{25} \left(50+1\right) = 51.2^{25} \\ & \text{So } k = 51 \end{split}$$

73. 30

Sol. 
$$\vec{b} \cdot \vec{c} = 10 \Rightarrow |\vec{b}| |\vec{c}| \cos\left(\frac{\pi}{3}\right) = 10 \Rightarrow$$

$$5 \cdot |\vec{c}| \cdot \frac{1}{2} = 10 \Rightarrow |\vec{c}| = 4$$
Also,  $\vec{a} \cdot (\vec{b} \times \vec{c}) = 0$ 

$$|\vec{a} \times (\vec{b} \times \vec{c})| = |\vec{a}| |\vec{b} \times \vec{c}| \sin\left(\frac{\pi}{2}\right)$$

$$\sqrt{3} \times |\vec{b}| |\vec{c}| \sin\frac{\pi}{3} \times 1 = \sqrt{3} \times 5 \times 4 \times \frac{\sqrt{3}}{2} = 30$$

74. 3

Sol. Lines must be intersecting

$$\Rightarrow (2s-1, 4s+3, 3s-1) = (2t-3, 6t-2, \lambda t+1)$$

$$2s-1 = 2t-3, 4s+3 = 6t-2, 3s-1 = \lambda t+1$$

$$\Rightarrow t = \frac{1}{2}, s = -\frac{1}{2}, \lambda = -7$$

distance of plane contains given lines from given plane is same as distance between point (-3, -2, 1) from given plane.

Required distance equal to 
$$\frac{\left|-69+20-2+48\right|}{\sqrt{529+100+4}} = \frac{3}{\sqrt{633}} = \frac{k}{\sqrt{633}} \Rightarrow k = 3$$

#### JEE-MAIN-2020 (9<sup>th</sup> Jan-Second Shift)-PCM-36

75. 14
Sol. First common term = 23
common difference =  $7 \times 4 = 28$ Last term  $\leq 407$   $\Rightarrow 23 + (n-1) \times 28 \leq 407$   $\Rightarrow (n-1) \times 28 \leq 384$   $\Rightarrow n \leq 13.71 + 1$   $n \leq 14.71$ So n = 14