#### **ECE 3150: Microelectronics**

### Spring 2015

#### Homework 8

Due on April 09, 2015 at 5:00 PM

## **Suggested Readings:**

a) Lecture notes

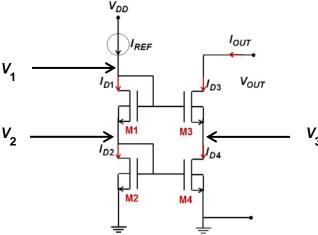
#### **Important Notes:**

1) MAKE SURE THAT YOU INDICATE THE UNITS ASSOCIATED WITH YOUR NUMERICAL ANSWERS. OTHERWISE NO POINTS WILL BE AWARDED.

2) Unless noted otherwise, always assume room temperature.

#### **Problem 8.1: (A cascode current source/mirror)**

Consider the following cascade current source/mirror:



Assume that all NFETs are identical and their characteristics are given by:

$$W = 10 \mu \text{m}$$
  
 $L = 1 \mu \text{m}$   
 $\mu_n C_{0x} = 200 \mu \text{A}/\text{V}^2$   
 $\lambda_n = 0.11/\text{V}$   
 $V_{DD} = 5.0 \text{ V}$   
 $V_{TN} = 0.5 \text{ V}$ 

$$I_{REF} = 1 \, mA$$

a) Find the voltages  $V_1$  and  $V_2$ .

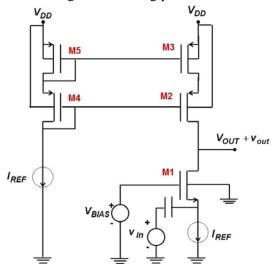
b) What is the relationship between voltages  $V_3$  and  $V_{OUT}$ ?

It might be obvious that if  $V_{OUT} = V_1$  then  $I_{OUT} = I_{REF}$ . However, when  $V_{OUT} \neq V_1$  then  $I_{OUT} \neq I_{REF}$ .

- c) What is the lowest value of  $V_{OUT}$  at which at least one NFET goes into the linear region? Which NFET?
- d) Using the values of voltages  $V_1$  and  $V_2$  found in part (a), calculate and plot (not sketch)  $I_{OUT}$  vs  $V_{OUT}$  with  $V_{OUT}$  in the range 0 and 5 Volts.
- e) Draw a small signal circuit of the current source when looking in from the output terminals.
- f) Use the small signal circuit of part (e) to find and expression for the output resistance  $r_{oc}$  of the current source.
- g) Assuming  $V_{OUT} = V_1$ , find the actual numerical value of the output resistance  $r_{OC}$  using the expression found in part (f).

## Problem 8.2: (A common gate amplifier)

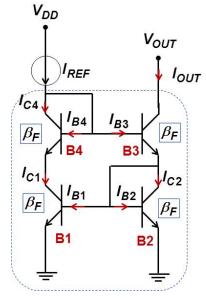
Consider the following FET common gate amplifier. The two current sources shown have output resistances equal to  $r_{oc}$ . In answering the following parts, DO NOT MAKE ANY APPROSIMATIONS.



- a) Find the open circuit voltage gain  $A_V = V_{out}/V_{in}$ .
- b) Find the input resistance  $R_{in}$  assuming a load resistor  $R_L$  is connected at the output.
- c) Find the output resistance  $R_{out}$  assuming that the input voltage source  $v_{in}$  is replaced by a voltage source  $v_s$  is in series with a resistor  $R_s$ .

## **Problem 8.3: (Double Wilson BJT current source/mirror)**

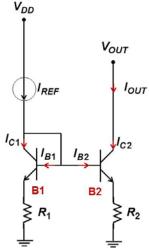
Consider the following BJT current source. All BJTs are identical and their  $V_{BE-ON}$  and  $V_{CE-SAT}$  are known.



- a) Find an expression for the small signal output resistance  $r_{oc}$  of the current source.
- b) What is the lowest voltage value  $V_{OUT}$  can take before at least one of the BJTs goes into the saturation region?

# Problem 8.4: (A BJT current source)

Consider the following BJT current source. All BJTs are identical and their  $V_{BE-ON}$  and  $V_{CE-SAT}$  are known.



a) Find an expression for the small signal output resistance  $r_{oc}$  of the current source.

b) What is the lowest voltage value $V_{OUT}$ can take before at least one of the BJTs goes into the saturation region (your answer could depend on $I_{OUT}$ )?