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ECE 3150: Microelectronics

Spring 2015

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Homework 1

Due on Jan. 29, 2015 at 5:00 PM

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**Suggested Readings:**

a) Lecture notes

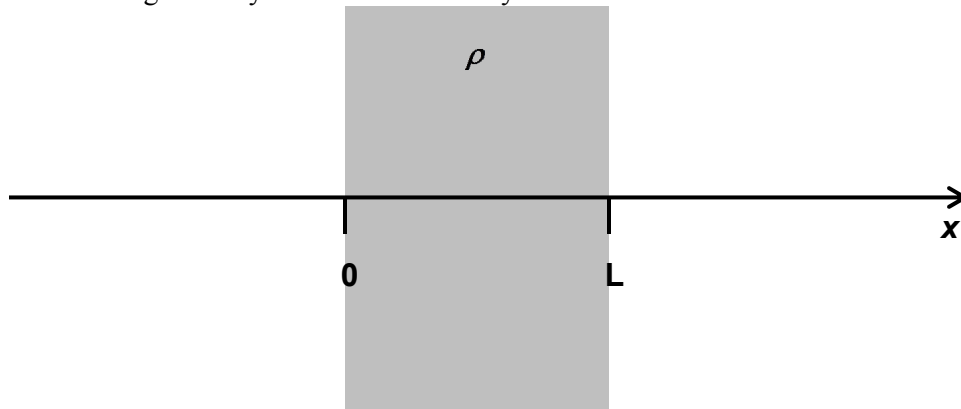
**Important Note:**

**MAKE SURE THAT YOU INDICATE THE UNITS ASSOCIATED WITH YOUR NUMERICAL ANSWERS. OTHERWISE NO POINTS WILL BE AWARDED. Graders please make note.**

**Unless noted otherwise, always assume room temperature.**

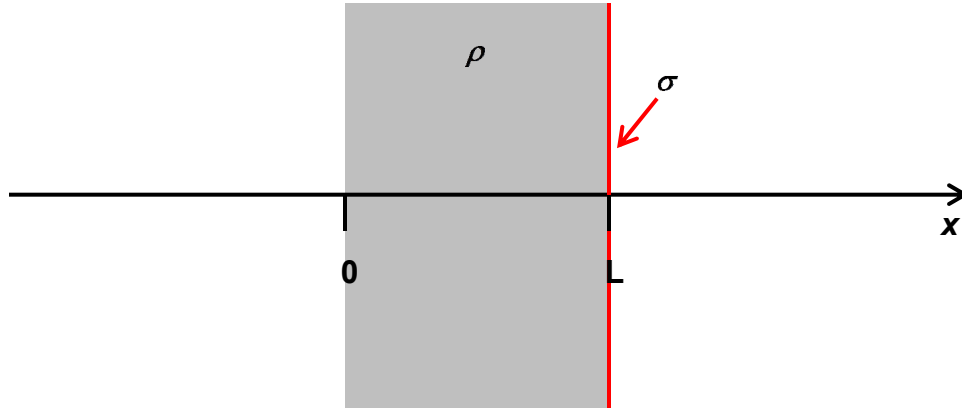
**Problem 1.1: (Review of electrostatics)**

Consider a region of space between  $x=0$  and  $x=L$  containing a uniform volume charge density of  $\rho$  (Coulombs/m<sup>3</sup>), as shown below. The dielectric constant everywhere is  $\epsilon_0$ . This is a 1D problem. Assume the region with the charge density to be infinite in the  $y$  and  $z$  directions.



Suppose the electrostatic potential and the electric field at  $x=0$  are known and are  $\phi(x=0)$  and  $E_x(x=0)$ , respectively.

- a) In terms of the given quantities, find the electrostatic potential and the electric field for  $0 < x < L$ .
- b) In terms of the given quantities, find the electrostatic potential and the electric field for  $x > L$ .
- c) The above problem is now slightly modified. A charge sheet with a surface charge density of  $\sigma$  (Coulombs/m<sup>2</sup>) is added in the  $y$ - $z$  plane at  $x = L$ , as shown below. In terms of the given quantities, find the electrostatic potential and the electric field for  $x > L$ .



### Problem 1.2: (Semiconductors in equilibrium)

Consider the following three samples of silicon, each of which has different dopants and different doping levels:

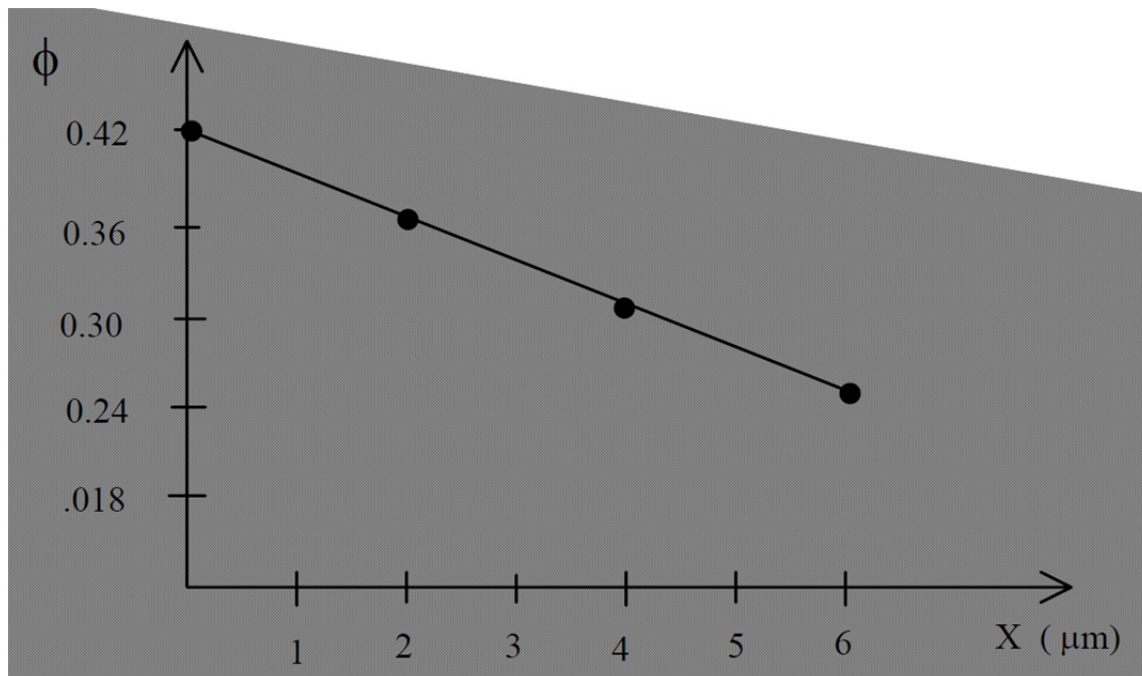
- Sample A:  $10^{17} \text{ cm}^{-3}$  Arsenic dopant  
 Sample B:  $10^{16} \text{ cm}^{-3}$  Boron dopant AND  $5 \times 10^{15} \text{ cm}^{-3}$  Phosphorous dopant  
 Sample C: Intrinsic (no dopants)

Complete a table like that shown below for these three samples. Assume that at room temperature the electron mobility,  $\mu_n$ , is  $1600 \text{ cm}^2/\text{V-s}$ , the hole mobility,  $\mu_p$ , is  $600 \text{ cm}^2/\text{V-s}$ , and the room temperature intrinsic carrier concentration in silicon,  $n_i$ , is  $10^{10} \text{ cm}^{-3}$ .

	Type (N or P)	$n_o$	$p_o$	Resistivity $\rho$	Potential $\phi_n$ or $\phi_p$ in Volts
Sample A					
Sample B					
Sample C					

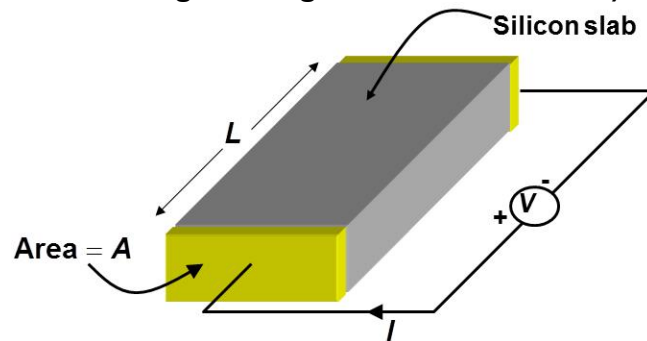
### Problem 1.3: (Currents in semiconductors)

Consider a doped semiconductor in thermal equilibrium in which the electrostatic potential (with respect to intrinsic silicon) has been measured and found to be as indicated in the figure below. Assume that  $\mu_n = 1000 \text{ cm}^2/\text{V-s}$  and  $\mu_p = 500 \text{ cm}^2/\text{V-s}$ .



- Plot the electron and hole concentrations (with units) vs  $x$  for  $0 \leq x \leq 6 \mu\text{m}$ .
- Plot the electric field (with units) vs  $x$  for  $0 \leq x \leq 6 \mu\text{m}$ .
- Calculate and plot the electron drift current density (with units) vs  $x$  for  $0 \leq x \leq 6 \mu\text{m}$ .
- Calculate and plot the electron diffusion current density (with units) vs  $x$  for  $0 \leq x \leq 6 \mu\text{m}$ .

#### Problem 1.4: (Resistance engineering in semiconductors)



- Consider a piece of P-doped silicon with an area  $A$  equal to  $1.0 \text{ sq-}\mu\text{m}$  and length  $L$  equal to  $10 \mu\text{m}$ . It is required that the resistance of this piece be  $100 \Omega$ . If the hole diffusivity is  $D_p$  is  $27 \text{ cm}^2/\text{s}$ , find the p-doping necessary to achieve the desired resistance value.