

# Title Here

by

Author Name

Department of Mechanical Engineering  
McGill University, Montreal  
December, 2019

A thesis submitted to McGill University  
in partial fulfillment of the requirements of the degree of  
Master of Engineering

Supervisor:

Professor James Richard Forbes

Author Name  
first.last@mail.mcgill.ca

© Author Name 2019

---

All Rights Reserved

*To my family for their steadfast support and love.*

## Abstract

Abstract in English.

## Résumé

Résumé en Français.

## Acknowledgements

Acknowledgements here.

## Preface

The contributions of this thesis that are original to the author’s knowledge are as follows.

- Chapter 1
  - Solving the batch SLAM problem using a right-invariant framework while explicitly considering bias states.

# Table of Contents

Dedication . . . . . ii

Abstract . . . . . iii

Acknowledgements . . . . . v

Preface . . . . . vi

List of Figures . . . . . ix

List of Tables . . . . . x

List of Abbreviations . . . . . xi

List of Symbols . . . . . xii

Chapter

1. Introduction . . . . . 1

1.1 Thesis Objective . . . . . 1

1.2 Thesis Overview . . . . . 1

1.3 TEMPLATE: Using `cleverref` and `acronym` . . . . . 2

2. Preliminaries . . . . . 3

3. Closing Remarks and Future Work . . . . . 4

3.1 Conclusions . . . . . 4

3.2 Future Work . . . . . 4

Appendices . . . . . 5

A. Appendix 1 . . . . . 6



A.1	Section 1 . . . . .	6
A.2	Section 2 . . . . .	6
<b>B.</b>	<b>Appendix 2 . . . . .</b>	<b>7</b>
B.1	Section 1 . . . . .	7
B.2	Section 2 . . . . .	7

## List of Figures

Figure

## List of Tables

Table

## List of Abbreviations

**SLAM**      Simultaneous Localization and Mapping

## List of Symbols

$\ \cdot\ $	the Euclidian norm of a physical vector
$\mathbb{R}^n$	the vector space of real $n$ -dimensional vectors
$\mathbb{R}^{m \times n}$	the space of real $m \times n$ -dimensional matrices
$(\cdot)^\top$	transpose
$(\cdot)^\times$	cross operator for $\mathfrak{so}(3)$
$(\cdot)^\wedge$	operator mapping an element of $\mathbb{R}^d$ to $\mathfrak{g}$
$(\cdot)^\vee$	operator mapping an element of $\mathfrak{g}$ to $\mathbb{R}^d$
$\mathbf{0}$	zero matrix
$\mathbf{1}$	identity matrix
$\text{diag}(\mathbf{M}_1, \dots, \mathbf{M}_n)$	block diagonal matrix with $\mathbf{M}_1, \dots, \mathbf{M}_n$ on diagonals, and zeros elsewhere
$\underline{\mathcal{F}}_i$	reference frame
$\underline{r}$	a physical vector
$\underline{r}^{zw}$	the position of point $z$ relative to point $w$
$\underline{r}^{\bullet a}$	the time derivative of $\underline{r}$ with respect to $\underline{\mathcal{F}}_a$
$\underline{r}^{zw \bullet a} = \underline{v}^{zw/a}$	velocity of point $z$ relative to point $w$ with respect to $\underline{\mathcal{F}}_a$
$\underline{\mathcal{F}}_a$	a vectrix, that is a matrix of unit length physical vectors that form a basis for $\underline{\mathcal{F}}_a$ , where $\underline{\mathcal{F}}_a^\top = [\underline{a}^1 \quad \underline{a}^2 \quad \underline{a}^3]$
$\mathbf{r}_a$	the physical vector $\underline{r}$ resolved in $\underline{\mathcal{F}}_a$
$\mathbf{C}_{ab}$	a DCM parameterizing the attitude of $\underline{\mathcal{F}}_a$ relative to $\underline{\mathcal{F}}_b$

$\underline{\omega}^{ba}$ 

angular velocity of  $\underline{\mathcal{F}}_b$  relative to  $\underline{\mathcal{F}}_a$

# Chapter 1

## Introduction

High-level introduction to the field of research.

### 1.1 Thesis Objective

### 1.2 Thesis Overview

This thesis is structured as follows.

Chapter 2 summarizes mathematical concepts and notation that are used throughout this thesis.

\Cref{chap:iekf}> outlines the IEKF. The relevant theorems and proofs are presented in continuous and discrete-time. The left-invariant extended Kalman filter and right-invariant extended Kalman filter are then detailed.

In \cref{chap:SE3}>, several examples of the IEKF are presented to illustrate how to practically implement an IEKF and to compare its performance to that of a standard multiplicative extended Kalman filter (MEKF).

In \cref{chap:batch}>, a solution to the SLAM problem in the invariant framework is presented. Simulation results are shown comparing the novel formulation to more traditional batch-based solutions to the SLAM problem.

This thesis is concluded in Chapter 3, where a summary of the findings are presented, along with recommended future work.

### 1.3 TEMPLATE: Using `cleveref` and `acronym`

A system of equations is given by

$$\mathbf{Ax} = \mathbf{b}. \tag{1.1}$$

Use `\cref` to reference a label (equation, figure, table, chapter, e.t.c.) in the middle of a sentence, and use `\Cref` to reference a label at the beginning of the sentence.

For example, (1.1) is an important equation. Equation (1.1) is used extensively in estimation theory (note how ‘Equation’ is automatically added when using `\Cref`).

The `acronym` package handles acronyms well using `\Ac` (at the beginning of the sentence) and `\ac` (otherwise). The package will take care of expanding the acronym when it’s first used, and then uses the abbreviation/short-name afterwards.

For example, Simultaneous Localization and Mapping (SLAM) is an interesting field of research. Probability is extensively used in SLAM. The upper-case/lower-case rules of the long names (defined in `abbreviations.tex`) should be consistent for all acronyms.



# Chapter 2

## Preliminaries

## Chapter 3

# Closing Remarks and Future Work

### 3.1 Conclusions

### 3.2 Future Work

# Appendices

## Appendix 1

## Appendix 1

**A.1 Section 1**

**A.2 Section 2**

## Appendix 2

## Appendix 2

B.1 Section 1

B.2 Section 2