



Introduction to Query Optimization

Abdu Alawini

University of Illinois at Urbana-Champaign

CS411: Database Systems



Optimization

- *So far, we talked about physical implementations. Next step: how do we use them?*
- At the heart of the database engine
- Step 1: convert the SQL query to a logical plan
- Step 2: find a better logical plan, find an associated physical plan
- (Feed the physical plan into the query processor.)



Converting from SQL to Logical Plans

Need to start someplace..

The easy cases:

Select a_1, \dots, a_n
From R_1, \dots, R_k
Where C

$$\pi_{a_1, \dots, a_n}(\sigma_C(R_1 \times R_2 \times \dots \times R_k))$$

Select $a_1, \dots, a_n, \text{aggs}$
From R_1, \dots, R_k
Where C
Group by b_1, \dots, b_l

Uses “extended” relational algebra, with gamma and delta

$$\pi_{a_1, \dots, a_n}(\gamma_{b_1, \dots, b_l, \text{aggs}}(\sigma_C(R_1 \times R_2 \times \dots \times R_k)))$$

In most of these cases, the \times will be a \bowtie



Optimization: Logical Query Plan

- Now we have one logical plan. Let's try to make it better.
- Ingredient 1: **Algebraic laws**: what are the ways in which an expression or tree may be rewritten without changing the meaning
- Ingredient 2: **Optimizations**: if there are multiple ways to write the same query, which one to choose.
 - Rule-based (heuristics): apply laws that seem to result in cheaper plans
 - Cost-based: estimate size and cost of intermediate results, search systematically for best plan



The three components of an optimizer

- Algebraic laws
- A cost estimator
- Optimization
 - Rule based
 - Cost based



Query Optimization: RA Equivalence Rules

Abdu Alawini

University of Illinois at Urbana-Champaign

CS411: Database Systems



Algebraic Laws

Hold independent of set or bag..

- Commutative and [Associative Laws](#)
 - $R \cup S = S \cup R$, $R \cup (S \cup T) = (R \cup S) \cup T$
 - $R \cap S = S \cap R$, $R \cap (S \cap T) = (R \cap S) \cap T$
 - $R \bowtie S = S \bowtie R$, $R \bowtie (S \bowtie T) = (R \bowtie S) \bowtie T$
- Distributive Laws
 - $R \bowtie (S \cup T) = (R \bowtie S) \cup (R \bowtie T)$



Algebraic Laws

- Laws involving selection (set semantics):
 - $\sigma_{C \text{ AND } C'}(R) = \sigma_C(\sigma_{C'}(R)) = \sigma_C(R) \cap \sigma_{C'}(R)$
 - $\sigma_{C \text{ OR } C'}(R) = \sigma_C(R) \cup \sigma_{C'}(R)$
 - $\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie S$
 - When is this true?
 - Certainly true when C involves only attributes of R
 - What if it involves attributes of R and S?
 - For example: R(X, Y), S(Y, Z)
 - Say: $Y = 3; X = 3 \wedge Z = 5$



Laws involving selection (set semantics) Cont.

- $\sigma_C(R - S) = \sigma_C(R) - S$
 - When is this true?
- $\sigma_C(R \cup S) = \sigma_C(R) \cup \sigma_C(S)$
- $\sigma_C(R \cap S) = \sigma_C(R) \cap S$



Algebraic Laws

- Example: $R(A, B, C, D), S(E, F, G)$
 - $\sigma_{F=3}(R \bowtie_{D=E} S) = ?$
 - $\sigma_{A=5 \text{ AND } G=9}(R \bowtie_{D=E} S) = ?$
- Simplify as much as possible by pushing down predicates
 - As close to the relations as possible



Algebraic Laws

- Example: $R(A, B, C, D), S(E, F, G)$
 - $\sigma_{F=3}(R \bowtie_{D=E} S) = R \bowtie_{D=E} (\sigma_{F=3}(S))$
 - $\sigma_{A=5 \text{ AND } G=9}(R \bowtie_{D=E} S) = (\sigma_{A=5}(R)) \bowtie_{D=E} (\sigma_{G=9}(S))$



Algebraic Laws

- Laws involving selection (set semantics):
 - $\sigma_{C \text{ AND } C'}(R) = \sigma_C(\sigma_{C'}(R)) = \sigma_C(R) \cap \sigma_{C'}(R)$
 - $\sigma_{C \text{ OR } C'}(R) = \sigma_C(R) \cup \sigma_{C'}(R)$ ↪ *what about this one?*
 - $\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie S$
 - Only when C involves only attributes of R
 - $\sigma_C(R - S) = \sigma_C(R) - S$
 - $\sigma_C(R \cup S) = \sigma_C(R) \cup \sigma_C(S)$
 - $\sigma_C(R \cap S) = \sigma_C(R) \cap S$

*Exercise: Think about which
of these hold for bag semantics....*



Algebraic Laws

- Laws involving selection (bag semantics??):
 - $\sigma_{C \text{ OR } C'}(R) = \sigma_C(R) \cup \sigma_{C'}(R)$ ↪ what about this one?



Algebraic Laws

- Laws involving projections
 - $\Pi_M(\Pi_N(R)) = \Pi_{M \cap N}(R)$
 - $\Pi_M(R \bowtie S) = \Pi_N(\Pi_P(R) \bowtie \Pi_Q(S))$
 - Where N, P, Q are appropriate subsets of attributes of M that are “needed afterwards”
- Example R(A,B,C,D), S(E, F, G)
 - $\Pi_{A,B,G}(R \bowtie_{D=E} S) = \Pi_? (\Pi_?(R) \bowtie \Pi_?(S))$



Query Optimization: Rule-Based Optimization

Abdu Alawini

University of Illinois at Urbana-Champaign

CS411: Database Systems



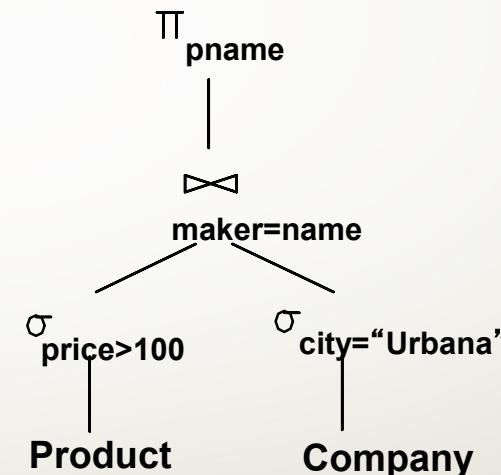
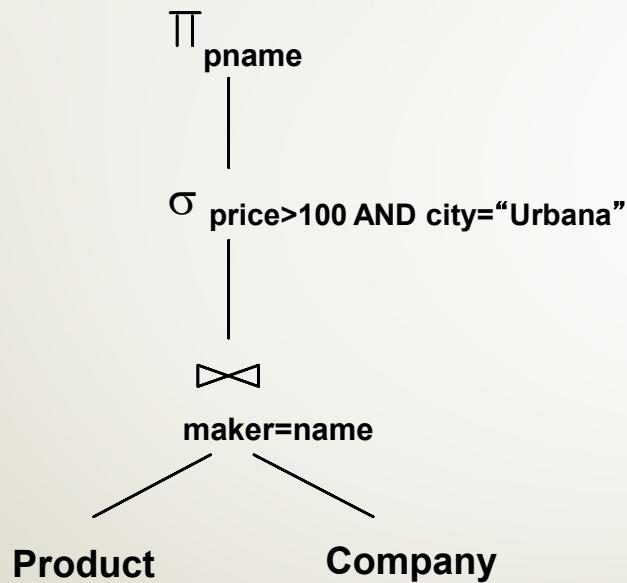
Heuristic Based Optimizations

- Rewriting of logical plan based on specific algebraic laws
- Results in better execution plans most of the time



Heuristic 1: Push selections down

Uses $\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie \sigma_C(S)$

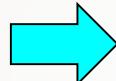


The earlier we process selections, less tuples we need to manipulate higher up in the tree



Pushing selection down: More complex Settings

```
Select y.name, Max(x.price)  
From product x, company y  
Where x.maker = y.name  
GroupBy y.name  
Having Max(x.price) > 100
```



```
Select y.name, Max(x.price)  
From product x, company y  
Where x.maker=y.name and  
x.price > 100  
GroupBy y.name
```

- ⑩ For each company, find the maximum price among its products.
- ⑩ But only display (company, maxprice) pair if maxprice > 100
- ⑩ Advantage: the size of the join will be smaller.
- ⑩ Requires transformation rules specific to the grouping/aggregation operators.
- ⑩ Won't work if we replace Max by Avg.

Heuristic 2

- (In some cases) push selections up, then down
- But ultimately pushed down
- $\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie \sigma_C(S)$

Typically: apply selections as close to the relations as possible so as to reduce size of intermediate results



Pushing selection up?

Bargain view: for categories with some price<5, find the company that makes the cheapest product in that category, and that price

```
Select V2.name, V2.price  
From V1, V2  
Where V1.category = V2.category and  
V1.minprice = V2.price
```

```
Create View V1 AS  
Select x.category,  
Min(x.price) AS minprice  
From product x  
Where x.price < 5  
GroupBy x.category
```

```
Create View V2 AS  
Select y.name, x.category, x.price  
From product x, company y  
Where x.maker=y.name
```



Pushing selection up ...

Bargain view: for categories with some price <5 , find the company that makes the cheapest product in that category, and that price

```
Select V2.name, V2.price  
From V1, V2  
Where V1.category = V2.category and  
V1.minprice = V2.price AND V1.minprice < 5
```

```
Create View V1 AS  
Select x.category,  
Min(x.price) AS minprice  
From product x  
Where x.price < 5  
GroupBy x.category
```

```
Create View V2 AS  
Select y.name, x.category, x.price  
From product x, company y  
Where x.maker=y.name
```



... and then down

Bargain view: for categories with some price<5, find the company that makes the cheapest product in that category, and that price

```
Select V2.name, V2.price  
From V1, V2  
Where V1.category = V2.category and  
V1.minprice = V2.price AND V1.minprice < 5
```

```
Create View V1 AS  
Select x.category,  
Min(x.price) AS minprice  
From product x  
Where x.price < 5  
GroupBy x.category
```

```
Create View V2 AS  
Select y.name, x.category, x.price  
From product x, company y  
Where x.maker=y.name AND x.price < 5
```