



# Database Design: Boyce-Codd Normal Form

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CS411: Database Systems

# Normal Forms

**First Normal Form** = all attributes are atomic

**Second Normal Form (2NF)** = old and obsolete

**Boyce Codd Normal Form (BCNF)**

**Third Normal Form (3NF)**

Others...



# Learning Objectives

After this lecture, you should be able to:

- Decompose a database schema into a set of relations obeying BCNF

# Eliminating Anomalies

Main idea:

- $X \rightarrow A$  is OK, if  $X$  is a (super)key
- $X \rightarrow A$  is NOT OK, otherwise
  - Need to decompose the table, but how?

Boyce-Codd Normal Form (BCNF)

# Boyce-Codd Normal Form

**Definition.** A relation R is in BCNF if and only if:

Whenever there is a nontrivial FD:  $A_1A_2\dots A_n \rightarrow B$ ,  
then  $A_1A_2\dots A_n$  is a superkey for R.

**There are no “bad” FDs: whenever there is a nontrivial FD, its left side must be a superkey**

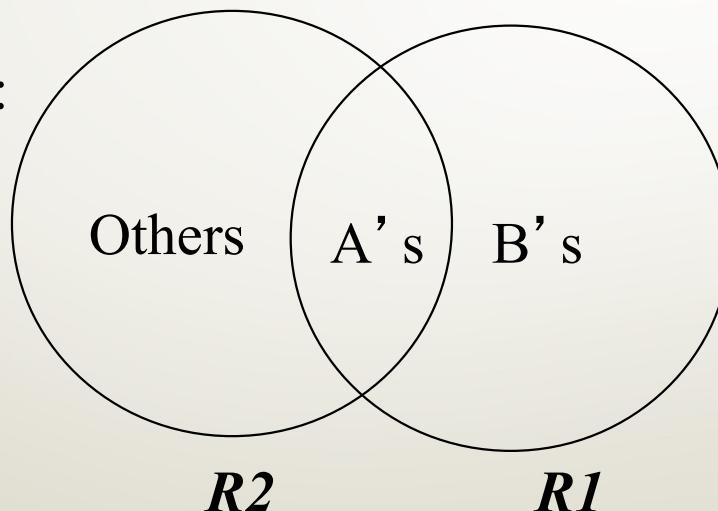
# BCNF Decomposition

Find a dependency that violates the BCNF condition:

$$A_1, A_2, \dots, A_n \longrightarrow B_1, B_2, \dots, B_m$$

Heuristic : choose  $B_1, B_2, \dots, B_m$  “as large as possible”

Decompose:



Continue until  
there are no  
BCNF violations  
left.

# Example Decomposition

Person:

Name	SSN	Age	EyeColor	Phone

Functional dependencies:

$$\text{SSN} \rightarrow \text{Name, Age, Eye Color}$$

BCNF: Person1(SSN, Name, Age, EyeColor),  
Person2(SSN, Phone)

# BCNF Decomposition: The Algorithm

Input: relation R, set S of FDs over R

- 1) Check if R is in BCNF, if not:
  - a) pick a violation FD  $f: A \rightarrow B$
  - b) compute  $A^+$
  - c) create  $R_1 = A^+, R_2 = A \text{ union } (R - A^+)$
  - d) compute all FDs over  $R_1$ , using R and S. Repeat similarly for  $R_2$ . (**See Algorithm 3.12**)
  - e) Repeat Step 1 for  $R_1$  and  $R_2$
- 2) Stop when all relations are BCNF, or are two-attributes

(Two attribute relations are always in BCNF,  
see E.g. 3.17 (pg. 89) for proof and examples)

# Another Example

- Person (Name, SSN, Age, EyeColor, Phone, HairColor)
- FD 1: SSN → Name, Age, EyeColor
- FD 2: Age → HairColor

**FD 1 and 2 imply: SSN → Name, Age, EyeColor, HairColor**

**Iteration 1:** Split based on SSN → Name, Age, EyeColor, HairColor

- Person(SSN, Name, Age, EyeColor, HairColor)
- Phone(SSN, Phone)

**Iteration 2:** Split based on Age → HairColor

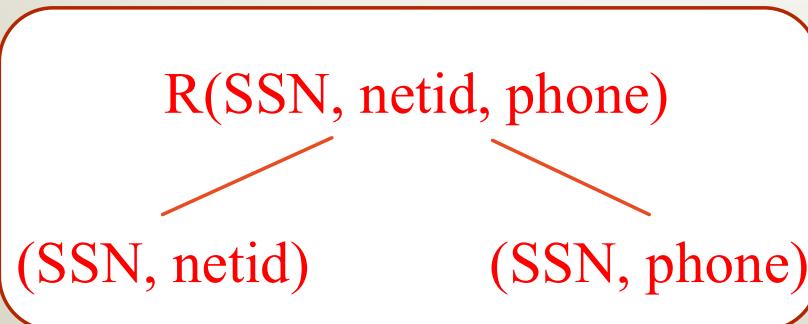
- Person(SSN, Name, Age, EyeColor)
- Hair(Age, HairColor)
- Phone(SSN, Phone)

# Q: Is BCNF Decomposition unique?

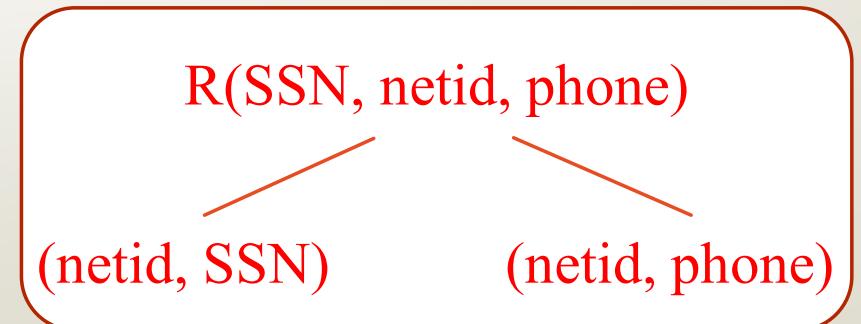
- $R(\text{SSN}, \text{netid}, \text{phone})$ .
  - FD1:  $\text{SSN} \rightarrow \text{netid}$
  - FD2:  $\text{netid} \rightarrow \text{SSN}$
- Each of these two FDs violates BCNF.

*Can you tell me two different BCNF decomp for R?*

Pick FD1



Pick FD2



# Properties of BCNF

- BCNF removes certain types of redundancies
  - All redundancies based on FDs are removed.
- BCNF Decomposition avoids information loss
  - You can construct the original relation instance from the decomposed relations' instances.

## Desirable Properties of Schema Refinement

- ✓ 1) minimize redundancy
- ✓ 2) avoid info loss
- 3) preserve dependency
- 4) ensure good query performance