

550.400: Mathematical Modeling and Consulting

Lecture Notes

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Outline

FAQ

Causality & Spurious Correlation & Math Modeling

Adobe Connect

<https://connect.johnshopkins.edu/meeting550400/>

Announcement

- HW *SET 1* due on Monday Oct 8
- Marked Work Statement is returned on Monday Oct 8
- Check the blackboard frequently for updates
- Ask non-sensitive questions on Blackboard Discussion Forum FAQ

Git FAQ

<http://gitref.org/index.html>

Vim FAQ

In Vim, how do you

- start, save, quit Vim?
- show numbers on the side?
- change the color theme?
- move around?
- spell check?
- find particular words?
- save typing while coding these \LaTeX commands?
- install plugins?

Vim FAQ

Vim is a *highly customizable* text editor

1. \LaTeX , R, C/C++, Java, Python, Git and etc.
2. Regular expression, syntax coloring, auto-completion
3. \<ESC> -mode
 - $\text{\texttt{:}}$ -mode, aka., the last line mode
 - $\text{\texttt{i}}$ -mode, aka., the insert mode

Vim FAQ

- Download & Install GVim or MacVim
- Download & Install tetris.vim
- Download & Install minibufexpl.vim
- Download & Install Gundo
- Download & Install Vim-LaTeX

Vim FAQ

version 1.1

April 1st, 06

vi/vim lesson 1 - basic editing

motion

curves the cursor, or defines the range for an operator

command

direct action command, if red, it enters insert mode

Esc

normal mode

\$ eol

^ "soft" bol

0 "hard" bol

W next word

E end word

R replace mode

w next word

e end word

U undo

I insert mode

A append at eol

• ex cmd line

h ←

j ↓

k ↑

l →

X backspace

x delete char

B prev word

b prev word

Basics:

h j k l are vi/vim cursor keys – use them as they are much closer than regular cursor keys!

Use **[** to enter insert mode, cursor turns from a block into a vertical line, and you can type in text. Use **Esc** to return to normal mode.

Use **x** to delete the current character, or **X** to delete the one to the left

Use **A** to insert text at the end of the line (wherever you are in the line!)

(Note: insert mode is actually very similar to a regular editor, you can use cursor/navigation keys, backspace, delete...)

Extras:

U to undo the last action – traditional vi has a single level, while vim supports unlimited undo (CTRL-**R** to redo)

0 jumps directly to the beginning of the line, **\$** to the end, and **^** to the first non-blank

Use **W b e** to move along 'words'. A 'word' is a sequence of all alphanumeric or punctuation signs: **muux{foo} bar, baz!**

Use **W B E** to move along WORDS. A 'WORD' is a sequence of any non-blank characters: **muux{foo} bar, baz!**

Use **R** to enter insert mode with an overstrike cursor, which types over existing characters.

: w and press enter to save. **:** q and enter to quit.

For the rest of the tutorial & a full cheat sheet, go to www.viemu.com - home of ViEmu, vi/vim emulation for Microsoft Visual Studio

L^AT_EX FAQ

How do you add a figure in \LaTeX ?

```
\begin{figure}
\caption{<+caption text+>}
\begin{center}
\includegraphics[width= <+number+>\textwidth]{<+filename+>}
\end{center}
\end{figure}
```

Here, $\langle + \dots + \rangle$ denotes a thing that you need to fill in.

But you will need this in the preamble part of your \LaTeX :

```
\usepackage{graphicx}
```

To save yourself from unnecessary glitches, insert png, jpeg, pdf files only.

L^AT_EX FAQ

How can I code a beamer?

```
\documentclass[hyperref={colorlinks=false},handout,10pt]{beamer}
\usetheme{Singapore}
\usecolortheme{lily}
\usefonttheme[onlymath]{serif} % What does this do?
```

OR

```
\documentclass[hyperref={colorlinks=false},handout,10pt]{beamer}
\usetheme{Berlin}
\usecolortheme{wolverine}
\usefonttheme[onlymath]{serif} % What does this do?
```

For a more complete array of themes, go to:

<http://www.hartwork.org/beamer-theme-matrix/>

L^AT_EX FAQ

How can I code a beamer?: a single side with no block

```
\begin{document}
  \begin{frame} # one frame per one slide
    \frametitle{hello world} # optional but you want one
    \begin{itemize}
      \item apple
      \item orange
    \end{itemize}
  \end{frame}
\end{document}
```

How can I code a beamer?: a single side with one block

```
\begin{document}
  \begin{frame} # one frame per one slide
    \frametitle{hello world} # optional but you want one
    \begin{block}{hey world}
      Bob!
    \end{block}
  \end{frame}
\end{document}
```

L^AT_EX FAQ

How can I code a beamer?: two slides

```
\begin{document}
  \begin{frame} # one frame per one slide
    \frametitle{hello world} # optional but you want one
    \begin{itemize}
      \item apple
      \item orange
    \end{itemize}
  \end{frame}
  \begin{frame} # one frame per one slide
    \frametitle{hello world} # optional but you want one
    \begin{block}{hey world}
      Bob!
    \end{block}
  \end{frame}
\end{document}
```

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L^AT_EX FAQ

How can I code a beamer?: a single frame with two columns

```
\begin{document}
  \begin{frame} # one frame per one slide
    \frametitle{hi world} # optional but you want one
    \begin{columns}
      \begin{column}{0.5\textwidth}
        \begin{itemize}
          \item Alice!
        \end{itemize}
      \end{column}
      \begin{column}{0.5\textwidth}
        \begin{block}{hey world}
          Bob!
        \end{block}
      \end{column}
    \end{columns}
  \end{frame}
\end{document}
```

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L^AT_EX FAQ

How can I code a beamer?: with a table of contents

```
\begin{document}

  \begin{frame}
    \frametitle{Outline}
    \tableofcontents
  \end{frame}

  \section{Hello World} # optional
  \subsection{hello world} # optional
  \begin{frame} # one frame per one slide
    \frametitle{hi world} # optional but you want one
  \end{frame}

  \section{Hello New World}
  \begin{frame} # one frame per one slide
    \frametitle{hi new world} # optional but you want one
  \end{frame}
\end{document}
```

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L^AT_EX FAQ

SO, how to put a code in the slide? and it looks like codes?

<pre>\begin{lstlisting} require(tikzDevice) x = rnorm(100) plot.ts(x) dev.off() \end{lstlisting}</pre>	<pre>require(tikzDevice) x = rnorm(100) plot.ts(x) dev.off()</pre>
--	--

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LaTeX FAQ

But, this requires the following in the preamble portion of your tex file:

```
\usepackage{listings}
\lstset{
  basicstyle=\footnotesize\ttfamily,
  numbers=left,
  frame=bottomline,
  framextopmargin=50pt,
}
```

Where to get more help:

<http://en.wikibooks.org/wiki/LaTeX/Presentations>

R FAQ

How to do software documentation (via R)

```
myfun <- function(x) {x^2}
package.skeleton(name='MYPAC',
  list='myfun',
  path='~/')

#Do the documentation
system('R CMD check ~/MYPAC')
system('R CMD build ~/MYPAC')
system('R CMD install MYPAC')
```

R FAQ I

Using R to do Bash Stuff

```
for(itr in 1:8) {
  stanzaname = paste("stanza",itr,sep="")
  gitaddress = paste("git://github.com/nhlee/550400.",
    stanzaname, ".git", sep="")
  bashcommand = paste("git remote add ",
    stanzaname, " ", gitaddress, sep="")
  system(bashcommand)
}
```

- 1:8 creates a vector that ...
- X = 1 assigns 1 to X
- X <- 1 also assigns 1 to X
- lots of things are done through function
- paste and system are functions that ...

R FAQ II

- functions has none or more arguments
- arguments are implicitly ordered but the order can be overridden

```
system(`ls -ld .*`)
system(`cat .Rprofile`)
system(`cat .bashrc`)
system(`cat .gitignore`)
system(`cat .vimrc`)
```

- .xxx files are hidden
- ls -ld .* show the hidden files
- .Rprofile set up your R behavior
- .bashrc set up your bash behavior
- .gitignore set up your git behavior
- .vimrc set up you vim behavior

R FAQ III

- these files are equivalent to Preference part of your GUI software

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Assessing Causality (WMA, 527)

- Consistency of association:
The association is observed in several different populations using different types of study design.
- Strength of association
A bigger difference in outcomes between cases with and without the purported causal factor indicates a stronger association.
- Temporal relationship
The cause preceded the effect. A correlation between two variables measured at the same time gives weaker evidence than one measuring the relationship between changes in the supposed cause and subsequent responses in the outcome.
- Mechanism
There is a plausible means by which the alleged cause could affect the outcome.

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Spurious Causality I

Is there a plausible means by which the alleged cause could affect the outcome?

Chocolate Consumption Vs. Electricity Production

```
cbe.loc<-'http://www.massey.ac.nz/~pscowper/ts/cbe.dat';
cbe <- read.table(cbe.loc,header=T);
plot(cbe[,1],cbe[,3]);
```

Euro & UK Pound Exchange Rate against US Dollar

```
xrate.loc <- 'http://www.massey.ac.nz/~pscowper/ts/us_rates.dat';
xrates <- read.table(xrate.loc,header=T);
plot(xrates$UK,xrates$EU,pch=4);
```

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Spurious Causality II

How about when there is no context goes with the variables? That is, you just have numbers.

Numerical simulation: presence of confounding variable

```
x <- y <- mu <- rep(0,1000);
for(i in 2:1000)
  mu[i] <- mu[i-1] + rnorm(1);
x <- mu + rnorm(1000);
y <- mu + rnorm(1000);
```

Numerical simulation: presence of "stochastic trend"

```
set.seed(10); x <- rnorm(100); y <- rnorm(100);
for(i in 2:100) {
  x[i] <- x[i-1] + rnorm(1);
  y[i] <- y[i-1] + rnorm(1);
}
```

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Spurious Causality III

Working with a model under “stochastic trend” is a tricky business.

A procedure of testing for confounding stochastic trend

```
require(tseries);
adf.test(x)$p.value; #this tests for stochastic trend in x
adf.test(y)$p.value; #so does this but in y
po.test(cbind(x,y)); #this tests for confounding factors in x and y
```

Are two exchange-rates confounded? “co-integrated”?

```
pp.test(xrates$UK)
pp.test(xrates$EU)
po.test(cbind(xrates$UK,xrates$EU))
ukeu.lm <- lm(xrates$UK ~ xrates$EU)
ukeu.res <- resid(ukeu.lm)
```

Apropos

Two non-stationary time series X_t and Y_t are *cointegrated* if some linear combination $aX_t + bY_t$, with a and b constant, is a stationary series.

- Have you heard of p -value?
- How about null and alternative hypotheses?
- Again, what do you mean by “stochastic trend”?
- What do you mean by “stationary processes”?

Time Series Model

Is there a plausible means by which the alleged cause could affect the outcome?

A time series model is a *descriptive model*

- its primary goal is to describe quantitative relationship between variables,
- it need not provide the underlying mechanism/context,
- it need not be a generative model.

Time Series Model

A sequence $\{X_i : i = 0, \pm 1, \pm 2, \dots\}$ of random variables taking values in \mathbb{R} is said to be a “white noise” sequence if

- X_i and X_j are statistically independent,
- X_i and X_j are statistically identical,
- its mean is zero and its variance is positive.

A white noise sequence is normal/Gaussian if its common likelihood function (aka. density) is normal/Gaussian, i.e.,

$$P(x \leq X_i \leq x + dx) \approx f(x)dx,$$

where

$$f(x) = \frac{1}{\sqrt{2\sigma}} \exp\left(-\frac{x^2}{2\sigma^2}\right).$$

Time Series Model

AR(p) model:

- AR stands for *autoregressive*
- in words, the current value is a function of past values plus some random noise
- for $p = 1, 2, \dots$,

$$X(t) = \beta_0 + \beta_1 X_{t-1} + \dots + \beta_p X_{t-p} + \varepsilon_t$$

- for example, X_t and Y_t defined below are AR(1) models,

$$X_t = X_{t-1} + \varepsilon_t,$$

$$Y_t = 0.5Y_{t-1} + w_t$$

Time Series Model

VAR(p) model:

- VAR(p) stands for *vector autoregressive*
- for example,

$$X_t = 0.5X_{t-1} + Y_{t-1} + \varepsilon_t,$$

$$Y_t = X_{t-1} + 0.5Y_{t-1} + w_t.$$

- more generally, for $p \times p$ matrix A ,

$$X_t = AX_{t-1} + W_t.$$

Time Series Model

Example on Page 222

```
require(tseries);

data(USEconomic);
myts = cbind(GNP,M1);
plot(myts);

fittedmodel = ar(myts, order.max=1, method='ols', dmean = F, intercept = T);

print(fittedmodel);
```

-
- USEconomic contains a quarterly US economic series from 1954 till 1987
 - GNP denotes the gross national product
 - M1 denotes “real money”, which means income adjusted by inflation

Time Series Model

Example on Page 224

```
require(vars);

fittedmodel <- VAR(myts,p=1,type='trend');

print(fittedmodel);
```

-
- Yet another way to fit a VAR(1) model in R
 - VAR function from vars package is somewhat general than ar function in that you can have linear term, i.e., for type='both', the RHS of the VAR(1) formula contains

$$\alpha_0 + \alpha_1 t$$

Granger Causality

The cause preceded the effect. A correlation between two variables measured at the same time gives weaker evidence than one measuring the relationship between changes in the supposed cause and subsequent responses in the outcome.