Problem 2: Threads Synchronisation and Communication

Consider an application with two cooperating user threads A and B. Each consists of a sequence of three function calls whose execution is dependent as shown in Figure 2.1. The threads share access to the integer variables: Ai, Bi.



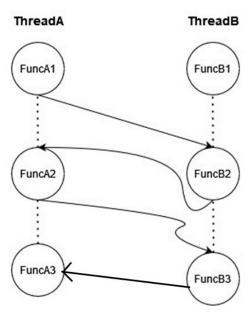


Figure 2.1

Hypothetically, we assume that the thread functions update the shared variables Ai and Bi as follows:

- FuncA1: A1= $\sum_{i=0}^{i=500} i$
- FuncB1: B1= $\sum_{i=0}^{i=250} i$
- FuncB2: B2= A1+ $\sum_{i=0}^{i=200} i$
- FuncA2: A2= $B2 + \sum_{i=0}^{i=300} i$
- FuncB3: B3= $A2 + \sum_{i=0}^{i=400} i$
- FuncA3: A3= B3 + $\sum_{i=0}^{i=400} i$
- a) Using the mathematical expressions of the functions and their execution dependence as shown in Figure 2.1, give the final correct values of the shared variables¹
- b) Give the additional synchronization code needed to implement the thread functions execution

 $^{^{1}\}sum_{i=0}^{n} i = n * (n+1)/2$

- dependence irrespective of the Operating System's threads scheduling. Active wait (i.e. while(!cond){} which wastes CPU cycles) or Thread sleep method should not be used in your solution. Explain in detail your answer.
- c) Using Java, code the application with your additional synchronisation code given in your answer to (b). The sum $\sum_{i=0}^{n} i$ should be collected from a static method in a dedicated utility class and should be coded using a loop.
- **d)** Extend the main() function code to run the two threads for a high number of iterations to verify the correctness of the implementation. Explain your answer.

What to submit

- Your java programs
- A report explaining the implementation of the synchronisation with reference to the relevant lines of your code along with the testing result. Maximum 3 pages.