

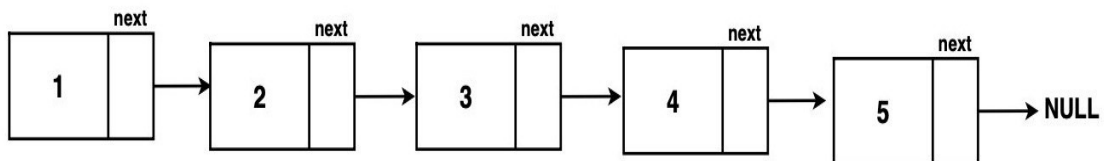
Find middle element in a Linked List

**Problem Statement:** Given the head of a linked list of integers, determine the middle node of the linked list. However, if the linked list has an even number of nodes, return the second middle node.

### Examples

#### Example 1:

**Input:** LL: 1 2 3 4 5

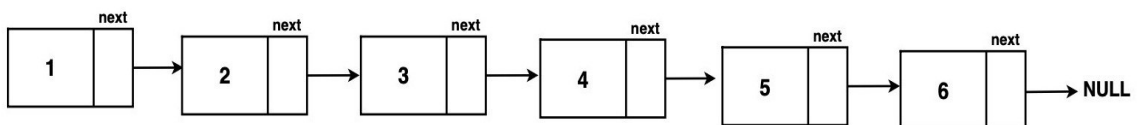


**Output:** 3

**Explanation:** Node with value 3 is the middle node of this linked list.

#### Example 2:

**Input:** LL: 1 2 3 4 5 6



**Output:** 4

**Explanation:** In this example, the linked list has an even number of nodes hence we return the second middle node which is 4.

## Brute Force Approach

### Algorithm / Intuition

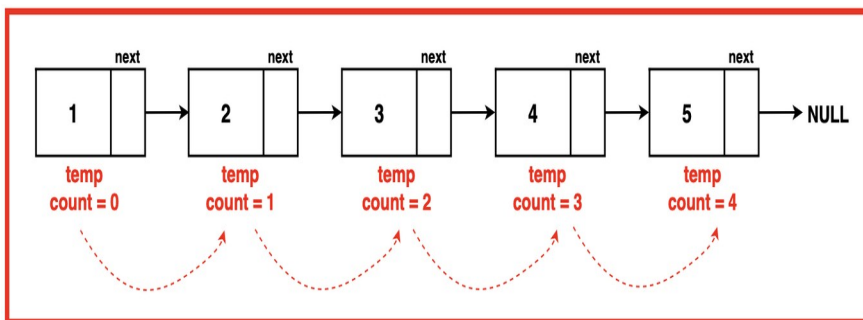
Using the brute force approach, we can find the middle node of a linked list by traversing the linked list and finding the total number of nodes as `count`. Then we reset the traversal pointer and traverse to the node at the  $\lfloor \text{count}/2 + 1 \rfloor$ th position. That will be the middle node.

### Algorithm:

**Step 1:** Initialise pointer temp to the head of the linked list and a variable to count to hold the number of nodes in the linked list. Using temp traverse the linked list, increasing the value of count by one at each node till temp becomes null. The final value of count will represent the length of the linked list.

**Step 2:** Calculate mid as  $\text{count}/2 + 1$  where count is the length of the linked list. Mid represents the position of the middle node.

**Step 3:** Reset temp pointer back to the head and traverse the list by iteratively moving temp mid number of times. The node pointed to by current after this traversal is the middle node of the linked list.



Code

```
import java.util.*;

// Node class represents a node in a linked list
class Node {
    // Data stored in the node
    int data;
    // Pointer to the next node in the list
    Node next;

    // Constructor with both data
    // and next node as parameters
    Node(int data, Node next) {
        this.data = data;
        this.next = next;
    }

    // Constructor with only data as
    // a parameter, sets next to null
    Node(int data) {
        this.data = data;
        this.next = null;
    }
}

public class FindMiddleOfLinkedList {

    // Function to find the middle node of a linked list
```

```

static Node findMiddle(Node head) {
    // If the list is empty or has
    // only one element, return the head as
    // it's the middle.
    if (head == null || head.next == null) {
        return head;
    }

    Node temp = head;
    int count = 0;

    // Count the number of nodes
    // in the linked list.
    while (temp != null) {
        count++;
        temp = temp.next;
    }

    // Calculate the position of the middle node.
    int mid = count / 2 + 1;
    temp = head;

    while (temp != null) {
        mid = mid - 1;

        // Check if the middle
        // position is reached.
        if (mid == 0){
            // break out of the loop
            // to return temp
            break;
        }
        // Move temp ahead
        temp = temp.next;
    }

    // Return the middle node.
    return temp;
}

public static void main(String[] args) {
    // Creating a sample linked list:
    Node head = new Node(1);
    head.next = new Node(2);
    head.next.next = new Node(3);
    head.next.next.next = new Node(4);
    head.next.next.next.next = new Node(5);

    // Find the middle node
    Node middleNode = findMiddle(head);

    // Display the value of the middle node
    System.out.println("The middle node value is: " + middleNode.data);
}

```

**Output:** The middle node value is: 3

## Complexity Analysis

**Time Complexity:  $O(N+N/2)$**  The code traverses the entire linked list once and half times and then only half in the second iteration, first to count the number of nodes then then again to get to the middle node. Therefore, the time complexity is linear,  $O(N + N/2) \sim O(N)$ .

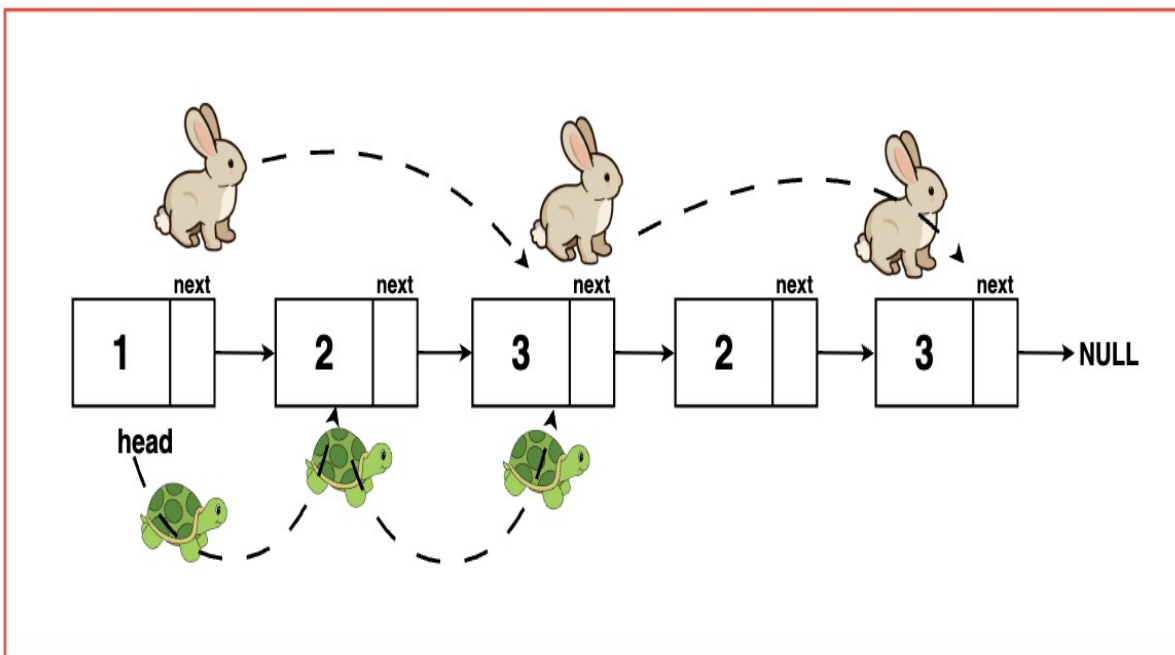
**Space Complexity :  $O(1)$**  There is constant space complexity because it uses a constant amount of extra space regardless of the size of the linked list. We only use a few variables to keep track of the middle position and traverse the list, and the memory required for these variables does not depend on the size of the list.

## Optimal Approach

### Algorithm / Intuition

The previous method requires the traversal of the linked list twice. To enhance efficiency, the Tortoise and Hare Algorithm is introduced as an optimization where the middle node can be found in just one traversal.

The Tortoise and Hare algorithm leverages two pointers, 'slow' and 'fast', initiated at the beginning of the linked list. The 'slow' pointer advances one node at a time, while the 'fast' pointer moves two nodes at a time.



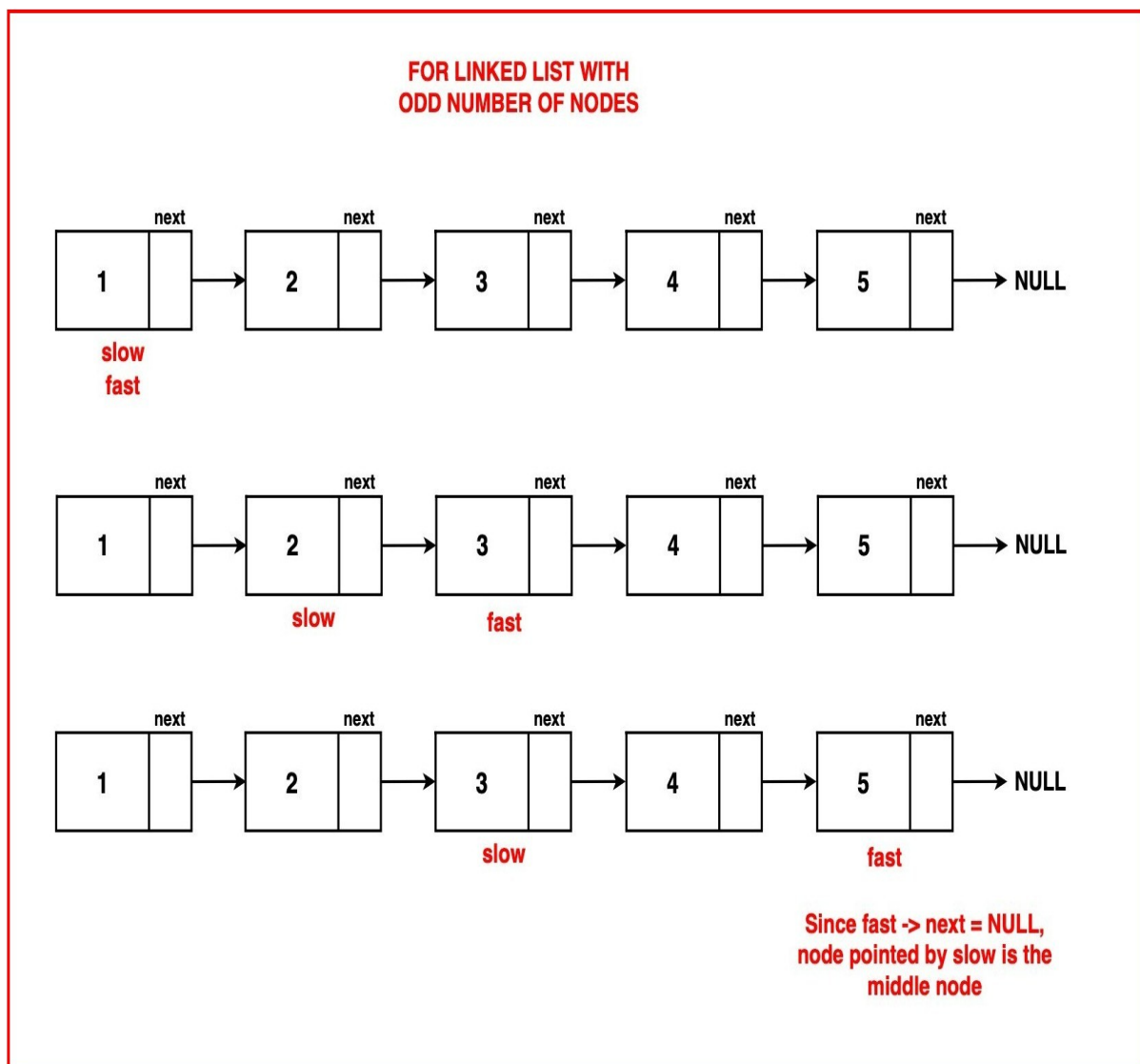
The Tortoise and Hare algorithm works because the fast-moving hare reaches the end of the list in exactly the same time it takes for the slow-moving tortoise to reach the middle. When the hare reaches the end, the tortoise is guaranteed to be at the middle of the list.

### Algorithm

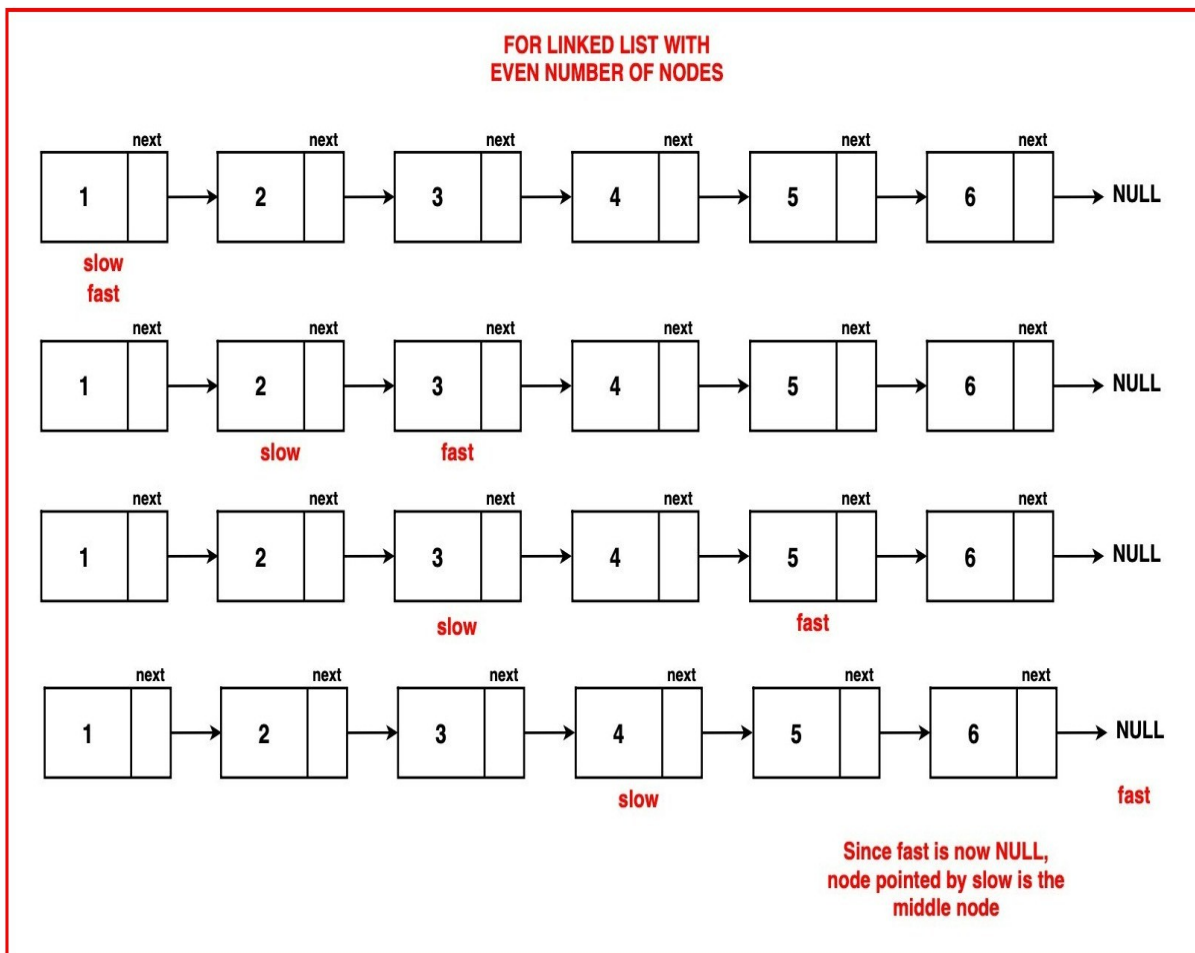
**Step 1:** Initialise two pointers, 'slow' and 'fast', to the head of the linked list. 'slow' will advance one step at a time, while 'fast' will advance two steps at a time. These pointers will move simultaneously.

**Step 2:** Traverse the linked list with the 'slow' and 'fast' pointers. While traversing, repeatedly move 'slow' one step and 'fast' two steps at a time.

**Step 3:** Continue this traversal until fast reaches the end of the list (i.e., fast or fast.next is null), the slow pointer will be at the middle of the list.



When the linked list has an odd number of nodes, fast.next ensures that the fast pointer doesn't go past the end of the list. In this case, fast reaches the last node, and fast.next becomes null, signalling the end of the traversal.



When the linked list has an even number of nodes, fast will reach the end of the list and be null, which still signifies the end of the traversal.

Code

```
import java.util.*;

// Node class represents a node in a linked list
class Node {
    // Data stored in the node
    int data;
    // Pointer to the next node in the list
    Node next;

    // Constructor with both data
    // and next node as parameters
    Node(int data, Node next) {
        this.data = data;
        this.next = next;
    }

    // Constructor with only data as
    // a parameter, sets next to null
    Node(int data) {
        this.data = data;
        this.next = null;
    }
}

public class FindMiddleOfLinkedList {
```

```

static Node findMiddle(Node head) {
    // Initialize the slow pointer to the head.
    Node slow = head;

    // Initialize the fast pointer to the head.
    Node fast = head;

    // Traverse the linked list using
    // the Tortoise and Hare algorithm.
    while (fast != null && fast.next != null && slow != null) {
        // Move fast two steps.
        fast = fast.next.next;
        // Move slow one step.
        slow = slow.next;
    }
    // Return the slow pointer,
    // which is now at the middle node.
    return slow;
}

public static void main(String[] args) {
    // Creating a sample linked list:
    Node head = new Node(1);
    head.next = new Node(2);
    head.next.next = new Node(3);
    head.next.next.next = new Node(4);
    head.next.next.next.next = new Node(5);

    // Find the middle node
    Node middleNode = findMiddle(head);

    // Display the value of the middle node
    System.out.println("The middle node value is: " + middleNode.data);
}
}

```

**Output:** The middle node value is: 3

### Complexity Analysis

**Time Complexity:  $O(N/2)$**  The algorithm requires the 'fast' pointer to reach the end of the list which it does after approximately  $N/2$  iterations (where  $N$  is the total number of nodes). Therefore, the maximum number of iterations needed to find the middle node is proportional to the number of nodes in the list, making the time complexity linear, or  $O(N/2) \sim O(N)$ .

**Space Complexity :  $O(1)$**  There is constant space complexity because it uses a constant amount of extra space regardless of the size of the linked list. We only use a few variables to keep track of the middle position and traverse the list, and the memory required for these variables does not depend on the size of the list.