

# DECISION TREES



Churn  $\Rightarrow$  Jio, Airtel  $\Rightarrow$  Employee

- ① Retaining :-  $\uparrow$  Salary, promotion
- ② Hiring :- training time + Cost + Misfit

Churn of an employee  
leaving.

Classification : Solved

Identify those important  
factors which are leading to  
employee attrition.

Solved : Model interpret &  
feature importance

DS

① Data Ingestion

② EDA

- preprocess / clean ✓
- plot distribution ✓
- Encoding
- Imbalance
- Scaling
- Outliers
- Dimensionality Reduction [if required]
- feature engineering

$\Rightarrow$  Stays  
 $\Rightarrow$  leaves.

log Reg  $\Rightarrow$  lead to a complex model  
Overfitting

KNN  $\Rightarrow$  slow

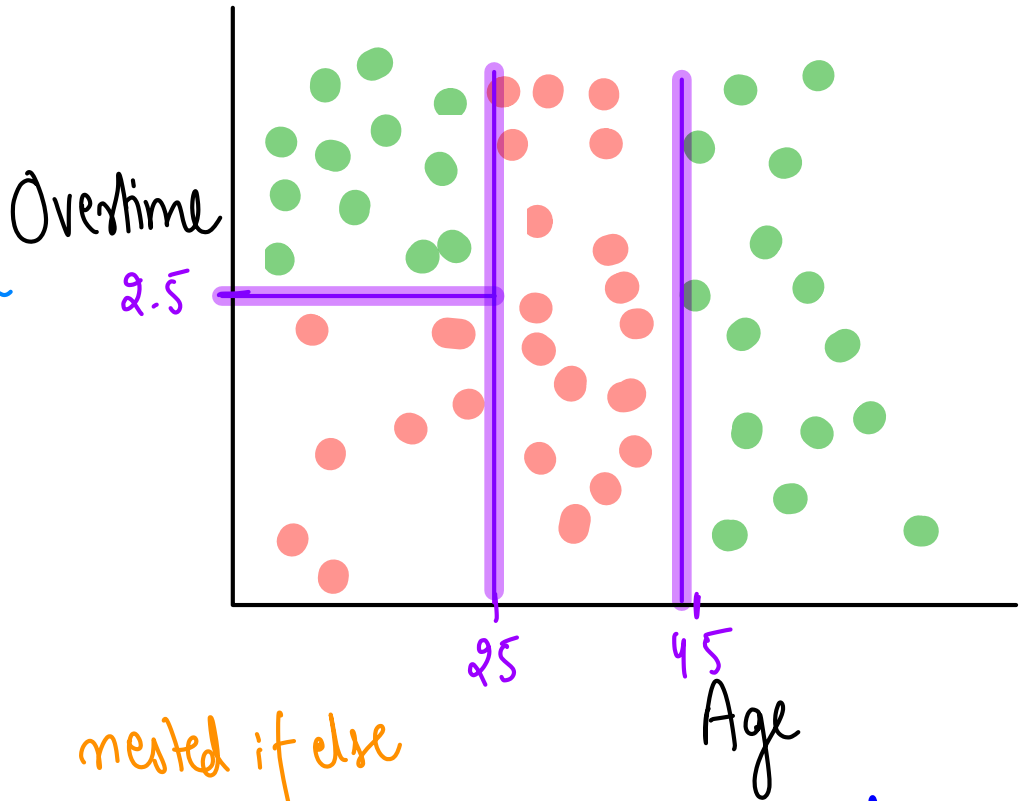
if age  $> 45$   
 $\Rightarrow$  leave

else if age  $> 25$   
 $\Rightarrow$  stay

else if overtime  $> 2.5$   
 $=$  leaves

nested if else  
conditions

else  
 $\Rightarrow$  stays.



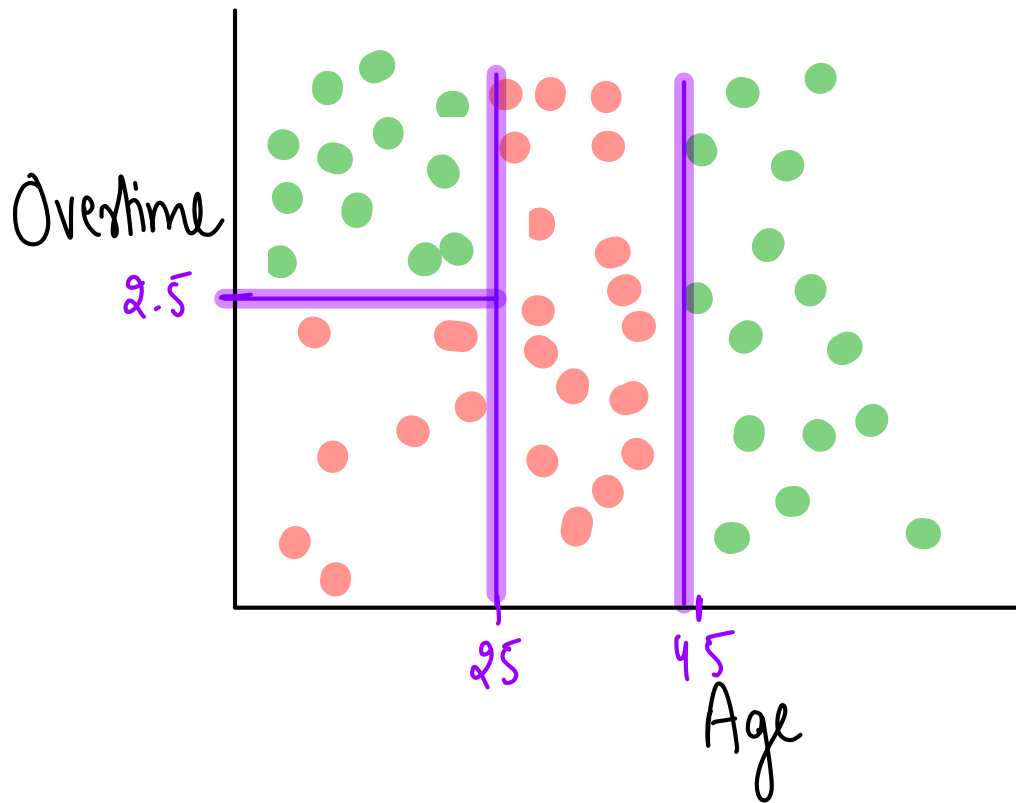
Axis parallel  
Decision Boundaries.

if age < 25  
if overtime > 2.5  
⇒ leave

else ⇒ stay

else if age > 45  
⇒ leave

else ⇒ stay.

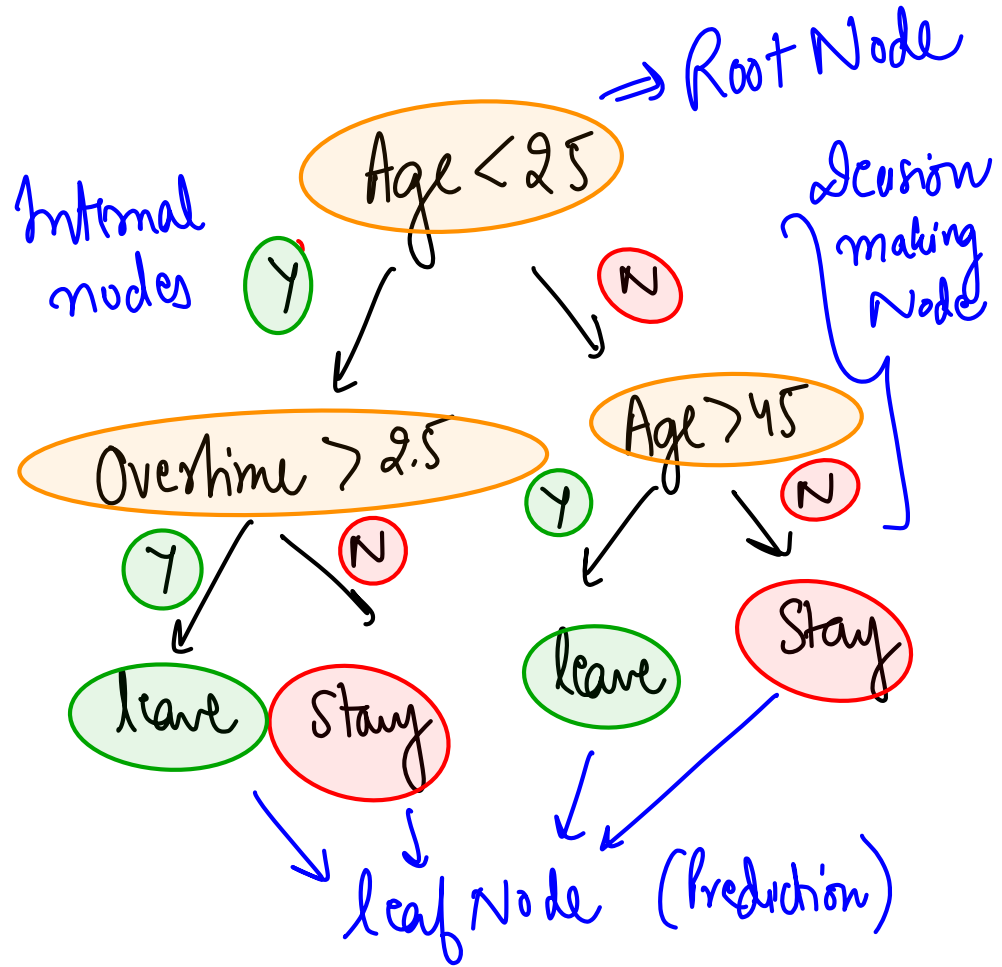


if age < 25  
if overtime > 2.5  
⇒ leave

else ⇒ stay

else if age > 45  
⇒ leave

else  
⇒ stay.



# Quiz time!

🕒 Time Left: 7s

## Quiz - 1 Try it out

What is the main disadvgne of KNN ?

41 users have participated



- |   |   |     |
|---|---|-----|
| A | It becomes computationally expensive for large datasets | 83% |
| B | Not suitable to handle categorical features             | 5%  |
| C | Can't be used for regression                            | 0%  |
| D | Non parametric algo so difficult to train.              | 12% |

[End Quiz Now](#)

# Quiz time!

🕒 Quiz Ended!

Statement I : Topmost node is called leaf node Statement II: Topmost node is called root node. Statement III: Bottom nodes are called root nodes. Statement IV: Nodes in between root and leaf are called decision nodes/ internal nodes.

Which of the following statements are true ?

40 users have participated

A	All statements are true	5%
B	II & IV	83%
C	I & III	2%
D	III & IV	10%

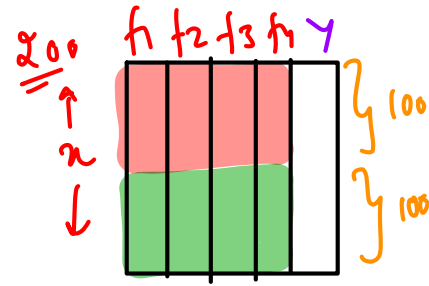
I X  
II ✓  
III X  
IV ✓



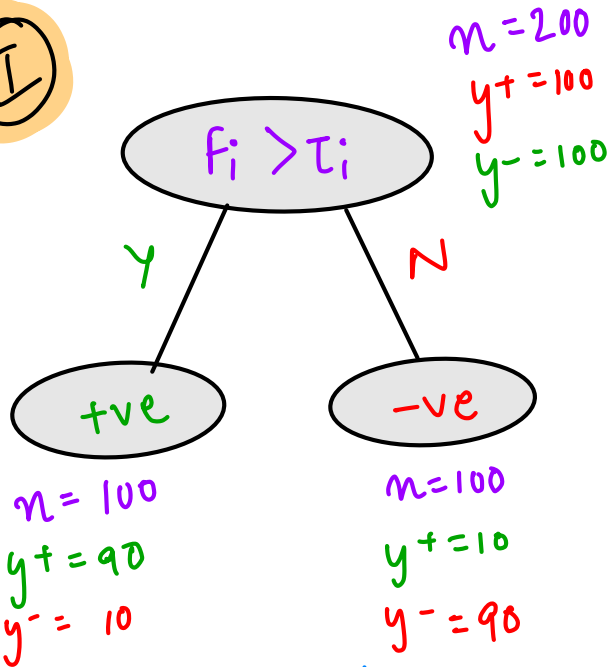
To learn

Data: 200

$$y^+ = 100$$
$$y^- = 100$$

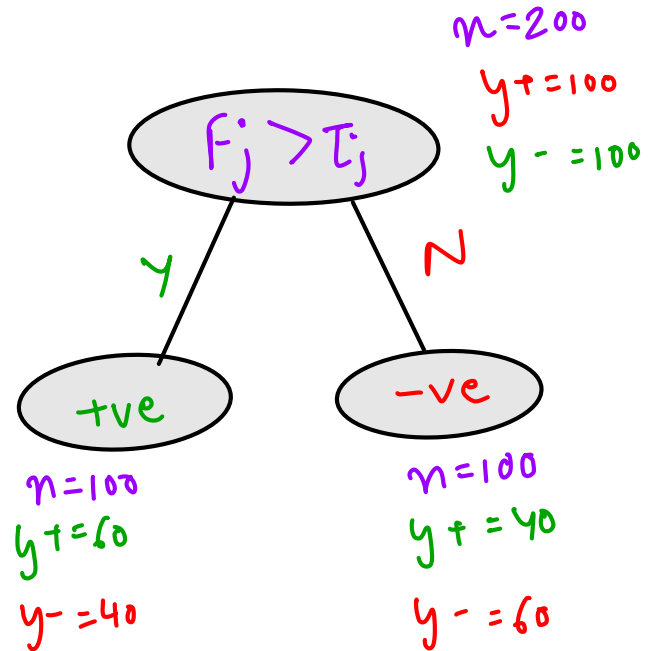


I



# misclassified = 20

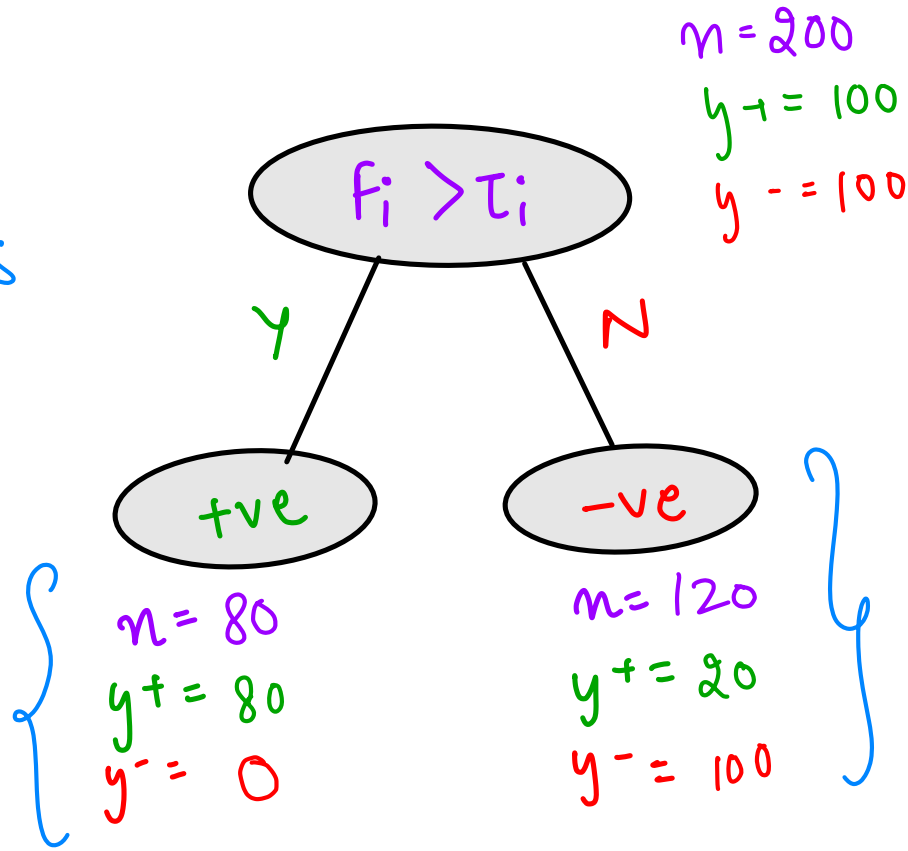
II



# misclassification = 80

HOMOGENEOUS

PURE  
NODE



OBJECTIVE:

find out those conditions which lead to  
creation of PURE NODES / HOMOGENEOUS  
REGIONS.

↳ Quantifiable measure  
measurement of purity of  
nodes.

# Entropy

⇒ Randomness

⇒ Basics of probability

⇒ Information theory

⇒ Measure of "Impurity"

Impurity  $\uparrow \Rightarrow$  Heterogeneity  $\uparrow \Rightarrow$  Entropy  $\uparrow \Rightarrow$  Purity  $\downarrow\downarrow$   
 $Y \Rightarrow$  discrete RV  $\in \{y_1, y_2, y_3, y_4\}$

$$H(Y) = - \sum_{i=1}^k P(y_i) \log_2 P(y_i)$$

Entropy for binary classification

$y \in \{0, 1\}$

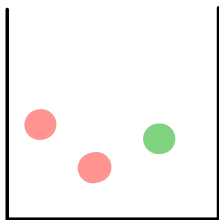
$$H(y) = - [ P(0) \cdot \log P(0) + P(1) \log P(1) ]$$

$$P(0) = p \quad P(1) = 1-p$$

$$H(y) = - [ p \log p + (1-p) \log(1-p) ]$$

looks similar to log loss.

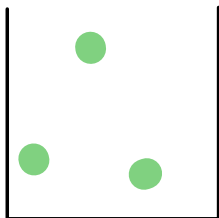
$$\text{log loss} = - \left[ \underbrace{y}_{\text{actual}} \log \underbrace{\hat{y}}_{\text{predicted}} + (1-y) \log(1-\hat{y}) \right]$$



$$P(R) = 1/2$$
$$P(G) = 1/2$$

$$H(Y) = 1$$

$$H(Y) = -[P(G) \log P(G) + P(R) \log P(R)]$$



$$P(R) = 1/6$$
$$P(G) = 5/6$$

$$H(Y) = 0.65$$

```
In [10]: def calc_entropy(p_g, p_r):  
         return -((p_g*np.log2(p_g)) + (p_r*np.log2(p_r)))
```

```
In [11]: calc_entropy(p_g=1/2, p_r=1/2)
```

```
Out[11]: 1.0
```

```
In [15]: calc_entropy(p_g=10e-100, p_r=1).round(2)
```

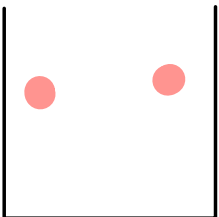
```
Out[15]: 0.0
```

```
In [16]: calc_entropy(p_g=1, p_r=10e-100).round(2)
```

```
Out[16]: 0.0
```

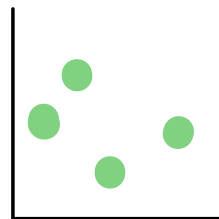
```
In [17]: calc_entropy(p_g=5/6, p_r=1/6)
```

```
Out[17]: 0.6500224216483541
```



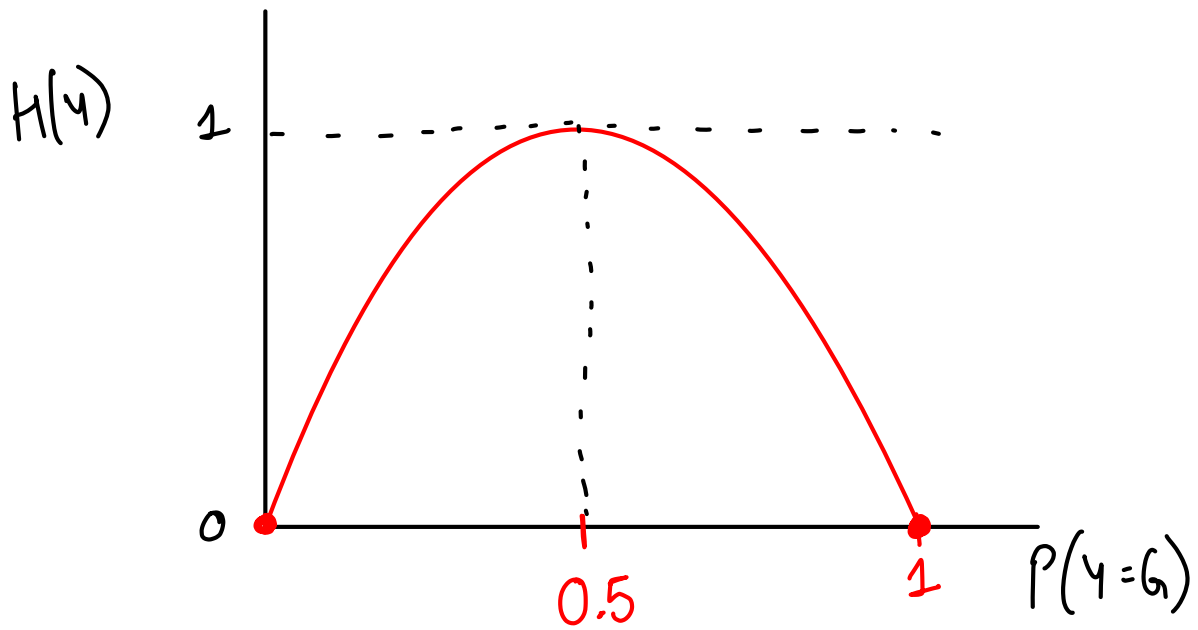
$$P(R) = 6/6 = 1$$
$$P(G) = 0/6 = 0$$

$$H(Y) = 0$$



$$P(R) = 0/6 = 0$$
$$P(G) = 6/6 = 1$$

$$H(Y) = 0$$



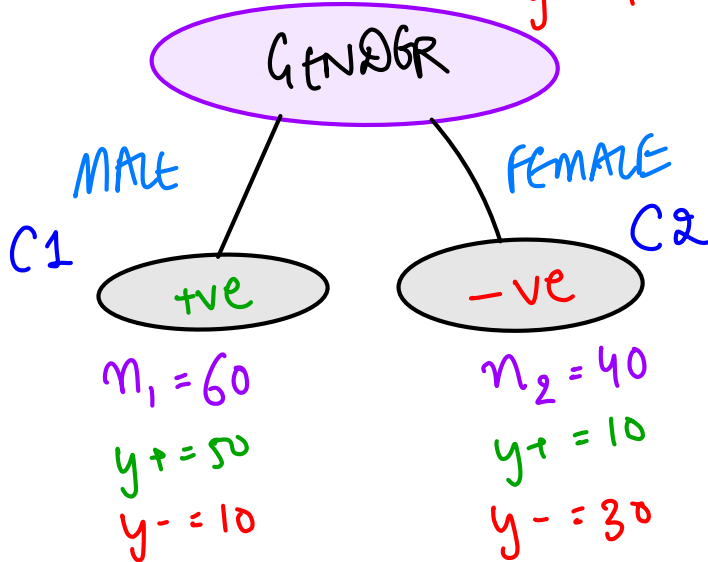
# Decision Trees

features

Gender, Education

$$H_{\text{parent}} = 0.97$$

$$\begin{aligned} n &= 100 \\ y^+ &= 60 \\ y^- &= 40 \end{aligned}$$

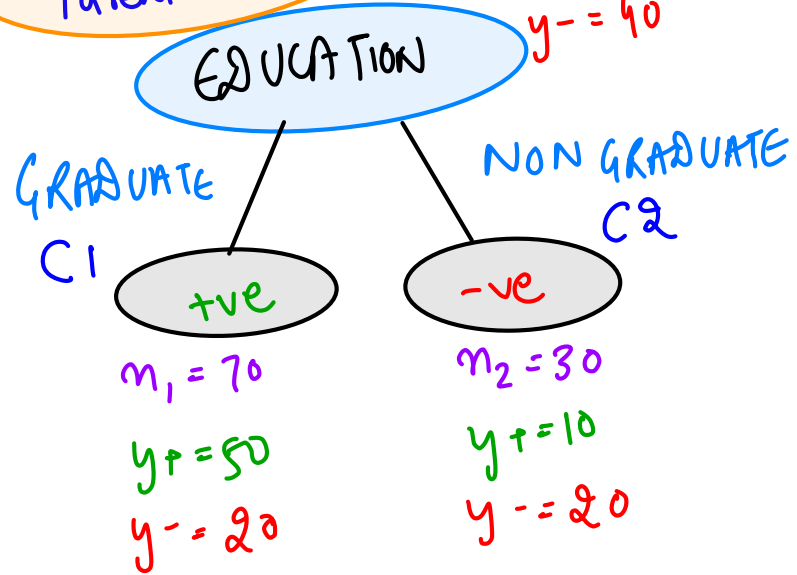


$$H_{C1} = 0.65$$

$$H_{C2} = 0.81$$

$$H_{\text{Parent}} = 0.97$$

$$\begin{aligned} n &= 100 \\ y^+ &= 60 \\ y^- &= 40 \end{aligned}$$



$$H_{C1} = 0.86$$

$$H_{C2} = 0.91$$



## Information Gain

```
In [18]: ## Left  
## Parent  
calc_entropy(p_g=0.6,p_r=0.4)
```

Out[18]: 0.9709505944546686

```
In [19]: ## Left  
## Child 1  
calc_entropy(p_g=5/6,p_r=1/6)
```

Out[19]: 0.6500224216483541

```
In [20]: ## Left  
## Child 2  
calc_entropy(p_g=1/4,p_r=3/4)
```

Out[20]: 0.8112781244591328

In [ ]:

```
In [ ]: ## Right  
## Parent  
calc_entropy(p_g=0.6,p_r=0.4)
```

```
In [21]: ## Right  
## Child 1  
calc_entropy(p_g=5/7,p_r=2/7)
```

Out[21]: 0.863120568566631

```
In [22]: ## Right  
## Child 2  
calc_entropy(p_g=1/3,p_r=2/3)
```

Out[22]: 0.9182958340544896

Weighted Entropies of children.

$$\frac{n_1}{n} H(C_1) + \frac{n_2}{n} H(C_2)$$

I

Gender

II

Education

$$H_{\text{parent}} = 0.97$$

$$H_{\text{children}} = 0.714$$

$$H_{\text{parent}} = 0.97$$

$$H_{\text{children}} = 0.875$$

# Information Gain

$$\begin{aligned} IG_I &= H_{\text{parent}} - H_{\text{children}}^{\text{Gender}} \\ &= 0.97 - 0.71 = 0.26 \end{aligned}$$

$$\begin{aligned} IG_{II} &= H_{\text{parent}} - H_{\text{children}}^{\text{education}} \\ &= 0.97 - 0.875 = 0.095 \end{aligned}$$

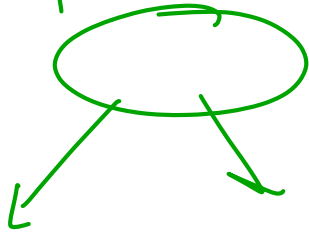
$$IG_1 > IG_2$$

We will split on Gender.

⇒ Minimise Entropy

⇒ Maximise Information Gain.

$$H_{\text{parent}} = 0.97$$



$$IG = 1$$

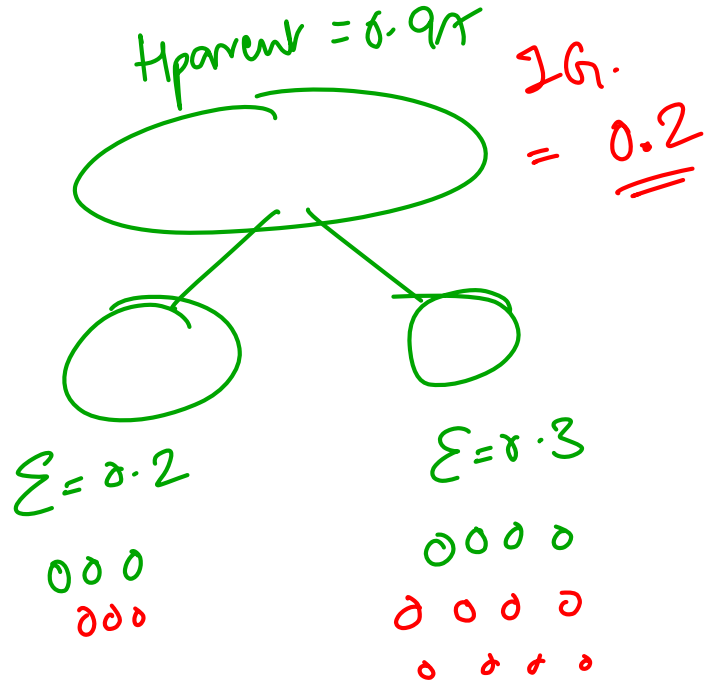
$$\underline{\underline{0.97}}$$

$$\underline{\underline{\epsilon = 0}}$$

0 0  
0 0 0  
0 0

$$\epsilon = 0$$

0 0 0  
0 0 0  
0 0



$$H_{\text{parent}} = 0.97$$

$$IG = \underline{\underline{0.2}}$$

$$\epsilon = 0.2$$

0 0 0  
0 0 0

$$\epsilon = 0.3$$

0 0 0 0  
0 0 0 0  
0 0 0 0

# Quiz time!

Quiz Ended!

Quiz3 - Check your understanding Which of the following statement is false ?

28 users have participated

A	Purer the node, more confidence we are in our prediction	21%
B	For making prediction, DT takes majority vote of class.	25%
C	More homogenous the data is at the node, more confident we are about our prediction	25%
✓ D	None of the above	29%

# Quiz time!

🕒 Quiz Ended!

Quiz5 - Check your understanding What will the value of entropy for following distribution of datapoints in node: Positive class: 50  
Negative class: 0

29 users have participated

A	0.33	7%
B	1	21%
C	-1	7%
✓ D	0	65%

} 9 }  
} 20 }

+ve = 50  
-ve = 0

## Quiz time!

🕒 Time Left: 7s

$$f_1 = 0.3$$

$$f_2 = 0.03$$

$$f_3 = 0.2$$

**Quiz 6 - Check your understanding We calculated information gain for 3**

**features which is as follows: Feature 1 : 0.3**

**Feature 2 : 0.03**

**Feature 3: 0.2 Which feature would you pick for splitting the node ?**

28 users have participated



A

Feature 1

79%

B

Feature 2

11%

C

Feature 3

11%

[End Quiz Now](#)

307