

True/False Questions MATH-2551

Question: In the spherical coordinate system, a point is represented by an ordered triple (ρ, θ, ϕ) where ρ is the distance from the origin and satisfies $\rho \neq 0$. True or False?

Answer: False

Question:

$\lim_{t \rightarrow a} \|r(t) - L\| = 0$ is a sufficient condition for TRUE. r approaches the limit L as t approaches a , provided that the above equation holds.

Answer: False

Question: True or False: The derivative of a vector-valued function exists at every point where the limit $\lim_{\Delta t \rightarrow 0} \frac{r(t + \Delta t) - r(t)}{\Delta t}$ exists, and the function is differentiable over an interval if its derivative exists at every point within that interval.

Answer: False

Question: True or False: A principal unit tangent vector at t is always perpendicular to the curve C when $t = t_0$

Answer: False

Question: $\int [f(t)i + g(t)j]dt = [\int f(t)dt]i + [\int g(t)dt]j$ is true for any integrable real-valued functions f , g , and h over the closed interval $[a, b]$.

Answer: False

Question: Is it true that the curvature k of a smooth curve $r(s)$ at s is given by the magnitude of the derivative $T(s)$?

Answer: True

Question: The principal unit normal vector at t is always perpendicular to the binormal vector at t .

Answer: True

Question: The acceleration vector is equal to the derivative of velocity.

Answer: True

Question: Is the set of points satisfying the equation $f(x, y) = c$ a level curve of a function of two variables for every value c ?

Answer: False

Question: True or False: A vertical trace of a function $z=f(x,y)$ can only be obtained by solving the equation $f(a,y)=z$ for a given constant $x=a$.

Answer: False

Question: True or False: A level surface of a function of three variables is defined as the set of points satisfying $f(x,y,z)=c$ for some number c in the range of f .

Answer: True

Question: Every δ disk in R^2 is closed under addition.

Answer: False

Question: An interior point of a set S in R^2 is always a boundary point of S . (True/False)

Answer: False

Question: Let S be a subset of R^2 (Figure 4.17).

Every point in an open set is necessarily a boundary point.

True or False?

Answer: False

Question: True or False: A set S is a region if it is not open.

Answer: False

Question: The definition is converted to a conceptual true or false question as follows:

Is the following statement true: For any $\epsilon > 0$, there exists a number $\delta > 0$ such that $|f(x,y) - L| < \epsilon$ whenever $(x-a)^2 + (y-b)^2 < \delta$.

Answer: True

Question: True or False: A function $f(x,y)$ is continuous at a point (a,b) in its domain if it exists at that point, and the limit as (x,y) approaches (a,b) equals the value of the function at (a,b) .

Answer: True

Question: The partial derivative $\frac{\partial f}{\partial x}$ is defined as the limit of the average rate of change of f as x approaches a certain value.

Answer: False

Question: True or False: The partial derivative of a function with respect to one variable is defined as the limit of the difference quotient as the change in that variable approaches zero.

Answer: True

Question: Let (x_0, y_0, z_0) be a point on a surface S , and let C be any curve passing through (x_0, y_0, z_0) and lying entirely in S . True or False: The tangent lines to all such curves C at (x_0, y_0, z_0) lie in the same plane.

Answer: False

Question: The equation of the tangent plane to a surface defined by $z = f(x, y)$ at a point (x_0, y_0) is given by:

$$z = f(x_0, y_0) + f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0).$$

True or False?

Answer: True

Question: The linear approximation of a function at a point is always given by the equation:
 $f(x_0, y_0) + f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0)$.

Answer: True

Question: True or False: A function is differentiable at a point if it can be written as a linear combination of its coordinates plus an error term that approaches zero faster than the distance from the point.

Answer: False

Question: When a function $f(x, y)$ is differentiable at (x_0, y_0) , then the total differential dz can be expressed as TRUE?

Answer: False

Question: A function is differentiable at a point if it can be written as the sum of the value of the function at that point, plus linear terms in the variables, plus an error term that goes to zero faster than the distance from the point.

Answer: True

Question: The directional derivative of a function $f(x, y)$ in the direction of $\mathbf{u} = \cos\theta\mathbf{i} + \sin\theta\mathbf{j}$ is determined by the limit:

$$\lim_{h \rightarrow 0} \frac{f((a, b) + h\mathbf{u}) - f(a, b)}{h}$$

True or False?

Answer: True

Question: The gradient of a function $f(x, y)$ is always written as $\text{grad } f$.

True or False?

Answer: False

Question: The gradient of a function $f(x, y, z)$ can also be written as True or False ?

Answer: False

Question: The directional derivative of a function f at (x_0, y_0, z_0) in the direction of $\mathbf{u} = \cos\alpha\mathbf{i} + \cos\beta\mathbf{j} + \cos\gamma\mathbf{k}$ is given by $\lim_{t \rightarrow 0} \frac{f(x_0 + t \cos\alpha, y_0 + t \cos\beta, z_0 + t \cos\gamma) - f(x_0, y_0, z_0)}{t}$, provided the limit exists.

Answer: True

Question: f is a function of two variables that has a critical point (x_0, y_0) if either $f_x(x_0, y_0) = 0$ or $f_y(x_0, y_0) = 0$, or neither partial derivative exists. True or False?

Answer: False

Question: True or False: A function f has a local maximum at a point (x_0, y_0) if $f(x_0, y_0)$ is greater than or equal to its value at every point within some disk centered at (x_0, y_0) .

Answer: False

Question: Is a point a saddle point for a function if it is critical in both x and y directions but is not a local extremum?

Answer: False

Question: The double integral of a function $f(x, y)$ over a rectangular region R can be evaluated using an infinite sum of area elements ΔA .

$$\text{True or False : } \lim_{m, n \rightarrow \infty} \sum_{i=1}^m \sum_{j=1}^n f(x_i^*, y_j^*) \Delta A = \int_R f(x, y) dA$$

Answer: True

Question: True or False: The iterated integral of a function $f(x, y)$ over a rectangular region can be evaluated in either order (i.e., $\int_a^b \int_c^d f(x, y) dy dx = \int_a^b \left[\int_c^d f(x, y) dy \right] dx$ or $\int_c^d \int_a^b f(x, y) dx dy = \int_c^d \left[\int_a^b f(x, y) dx \right] dy$).

Answer: True

Question: The area of a region is given by $\int_R 1 dA$.

True or False?

Answer: False

Question: The average value of a function of two variables over a region R is always given by $\frac{1}{|R|} \iint_R f(x, y) dA$,

True or False?

Answer: False

Question: Is a region in the (x, y) -plane of Type I if it is bounded by two vertical lines and the graphs of two continuous functions?

Answer: False

Question: The area of a plane-bounded region is equal to the single integral $\int_D 1 dA$.

True or False?

Answer: False

Question: Here is the converted conceptual true or false question:

Is it true that if a function $f(x, y)$ is integrable over a plane-bounded region D with positive area $\int_D 1 dA$, then the average value of the function is given by $\frac{1}{\int_D 1 dA} \iint_D f(x, y) dA$?

Answer: True

Question: The joint density function of two continuous random variables satisfies the inequality $f(x, y) \geq 0$ and the equation $\int \int_{R^2} f(x, y) dA = 1$. TRUE or FALSE?

Answer: TRUE

Question: The variables XX and YY are said to be independent random variables if their joint density function is equal to the product of their individual density functions: True or False

Answer: False

Question: The expected values $E(X)$ and $E(Y)$ denote the most likely outcomes of the events. True or False?

Answer: False

Question: The double integral of a function over a polar rectangular region can be evaluated by summing up values of the function at discrete points multiplied by the area of each subregion.

Answer: False

Question: True or False: The triple integral of a function $f(x, y, z)$ over a rectangular box B is defined as the limit of a Riemann sum of the function evaluated at specific points within the region.

Answer: True

Question: A triple integral in cylindrical coordinates can always be defined as the limit of a triple Riemann sum.

Answer: True

Question: The triple integral in spherical coordinates is a limit of a triple Riemann sum.

Answer: False

Question: A transformation $T: G \rightarrow R, T: G \rightarrow R$, defined as $T(u, v) = (x, y), T(u, v) = (x, y)$, is a one-to-one transformation if TRUE no two points map to the same image point.

Answer: False

Question: Here is the conceptual true or false question:

The Jacobian of a transformation $(u, v) \mapsto (g(u, v), h(u, v))$ can always be expressed as a 2×2 determinant involving partial derivatives.

Answer: True

Question: A vector field is an assignment of a three-dimensional vector to each point of its domain. True or False?

Answer: True

Question: Is a vector field F in R^2 or R^3 necessarily a gradient field if there exists a scalar function f such that $\nabla f = \mathbf{F}$?

Answer: False

Question: The scalar line integral of a function along a curve can be approximated by the sum of function values at discrete points on the curve.

Answer: True

Question: True or False: The flux of a vector field F across a curve C is equal to the line integral of the dot product of F with the unit tangent vector n multiplied by the magnitude of the unit tangent vector, over the entire length of the curve.

Answer: True

Question: A closed curve can traverse itself exactly once. False: (a, b)

Let me know if this meets your requirements!

Answer: False

Question: A simply connected region is a region that has at least one hole.

Answer: False

Question: Is a vector field F path independent if for any two paths C_1 and C_2 in its domain D with the same initial and terminal points, the line integral of F over C_1 is equal to the line integral of F over C_2 ?

Answer: True

Question: The curl of a vector field is a scalar.

Answer: False

Question: True or False: The parameter domain of a surface parameterization is always contained within the uv -plane.

Answer: False

Question: Is a parameterization $r(u, v) = \langle x(u, v), y(u, v), z(u, v) \rangle$ regular if the product $r_u \times r_v$ is zero for at least one point (u, v) in the domain?

Answer: False

Question: A surface parameterization $r(u, v)$ is smooth if it has non-zero tangent plane at every point (u, v) in its domain. True or False?

Answer: False

Question: The surface area of a smooth parameterization S is given by $\int \int_D \|t_u \times t_v\| dA$.

True or False?

Answer: False

Question: True or False: The surface integral of a scalar-valued function over a piecewise smooth surface is equal to the limit of the sum of the function's values at a set of discrete points on the surface.

Answer: True

Question: When evaluating the surface integral of a continuous vector field F over an oriented surface S with unit normal vector N , True or False: $\iint_S F \cdot dS = \iint_S F \cdot NdS$?

Answer: False

Question: A second-order differential equation is always linear if it can be written in the form $a_2(x)y'' + a_1(x)y' + a_0(x)y = r(x)$ where $a_2(x)$, $a_1(x)$, and $a_0(x)$ are real-valued functions.

Answer: True

Question: For a set of functions $f_1(x), f_2(x), \dots, f_n(x)$ to be linearly dependent, it is true that there exist constants c_1, c_2, \dots, c_n , not all zero, such that $c_1 f_1(x) + c_2 f_2(x) + \dots + c_n f_n(x) = 0$ for all x over the interval of interest.

Answer: True

Question: When solving a differential equation, the characteristic equation is always True .
 $a\lambda^2 + b\lambda + c = 0$.

Answer: False

Question: A particular solution to a differential equation is always accompanied by an arbitrary constant. *True or False*

Answer: True

Question: True or False: If x and y are continuous functions of t on an interval I , then the equations $x = x(t)$ and $y = y(t)$ are called trigonometric equations and t is called the period.

Answer: False

Question: A parabola is a set of points whose distance from the focus is always greater than its distance from the directrix.

(True or False?)

Answer: False

Question: Is it always true that for any point on an ellipse, the sum of its distances from two fixed points (the foci) is constant? True or False

Answer: True

Question: True or False: A hyperbola is the set of all points where the difference between their distances from two fixed points (the foci) is constant.

Answer: True

Question: If $e=0, e=0$, then the conic section is a ?

Answer: False

Question: True or False: A vector is a quantity with only magnitude.

Answer: False

Question: True or False: Two vectors with the same magnitude but opposite direction are equivalent.

Answer: True

Question: When multiplying a vector \mathbf{v} by a scalar k , the resulting vector has a magnitude that is times the magnitude of \mathbf{v} .

Answer: True

Question: When constructing the sum of two vectors \mathbf{v} and \mathbf{w} graphically, placing the initial point of \mathbf{w} at the terminal point of \mathbf{v} ensures that the resulting vector sum $\mathbf{v} + \mathbf{w}$ has an initial point coinciding with the initial point of \mathbf{v} and a terminal point coinciding with the terminal point of \mathbf{w} .

True or False?

Answer: True

Question: The vector $\langle x, y \rangle$ can always be written in component form as $v = \langle x, y \rangle$.

Answer: True

Question: Scalar multiplication of a vector by a non-zero scalar results in a vector with opposite direction.

Answer: False

Question: In three-dimensional space, the origin is located at the point of intersection (0) between the x , y , and z axes. True or False?

Answer: False

Question: A sphere is the set of all points equidistant from a fixed point, the center of the sphere.

Answer: True

Question: The dot product of two vectors $\vec{u} = \langle u_1, u_2, u_3 \rangle$ and $\vec{v} = \langle v_1, v_2, v_3 \rangle$ can be computed by summing the products of their components.

Answer: False

Question: The direction angles for a nonzero vector and its coordinate axes can only have cosine values equal to 0 or 1. True or False?

Answer: False

Question: The length of the vector projection of \mathbf{v} onto \mathbf{u} is equal to $\|\mathbf{v}\| \cos \theta = |\mathbf{u} \cdot \mathbf{v}| / \|\mathbf{u}\|$. True or False

Answer: True

Question: The cross product $\mathbf{u} \times \mathbf{v} = \langle u_2v_3 - u_3v_2, -(u_1v_3 - u_3v_1), u_1v_2 - u_2v_1 \rangle$ depends only on the magnitudes of u and v , not their directions.

Answer: False

Question: The triple scalar product of three vectors is equal to $\boxed{\text{True}}$ $\mathbf{u} \cdot (\mathbf{v} \times \mathbf{w})$.

Answer: True

Question: True or False: Torque is equal to the dot product of the position vector \mathbf{r} and force vector \mathbf{F} .

Answer: False

Question: The vector equation $\boxed{\text{True}}$ $\mathbf{n} \cdot \overrightarrow{PQ} = 0$ forms a plane and represents the set of all points Q satisfying the equation.

Answer: False

Question: True or False: A set of lines parallel to a given line passing through a given curve is not known as a cylindrical surface, or cylinder.

Answer: False

Question: The traces of a surface are always two-dimensional. True or False?

Answer: False

Question: Here is the converted conceptual true or false question:

All quadric surfaces can be expressed as the graph of an equation of the form $Ax^2 + By^2 + Cz^2 + Dxy + Exz + Fyz + Gx + Hy + Jz + K = 0$.

(Note: I've used LaTeX syntax to ensure proper compilation)

Answer: False