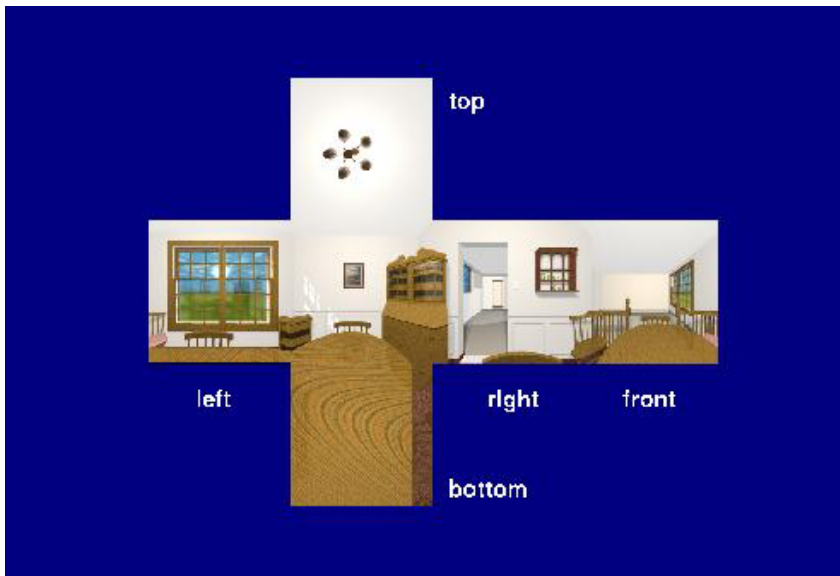


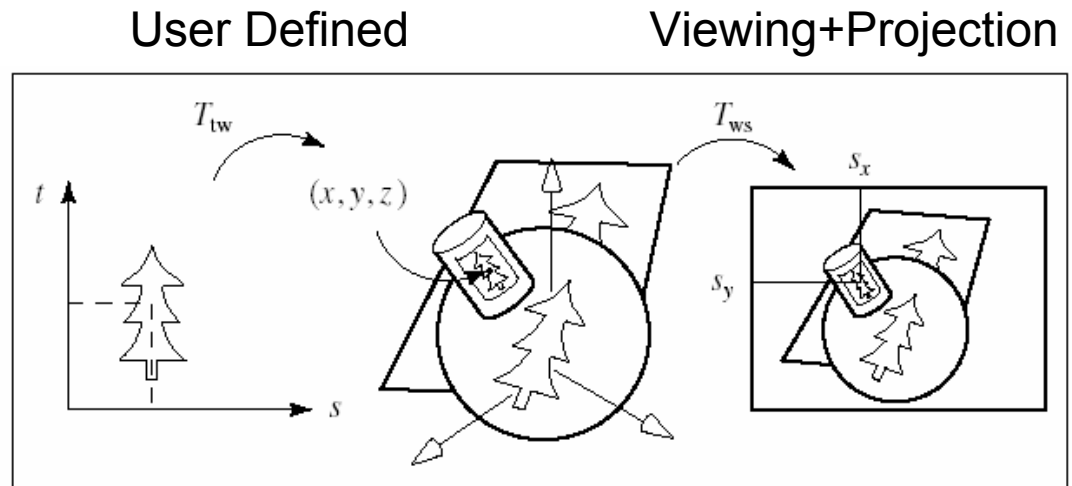
# Texture Mapping

*Pasting textures on surfaces: Hill 8.5*



# Systems involved

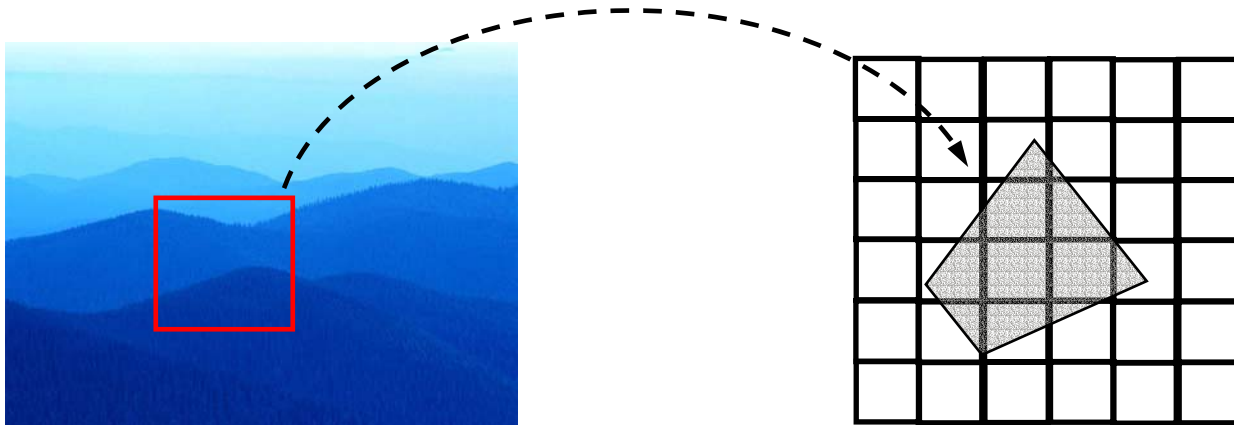
**FIGURE 8.35** Drawing texture on several objects of different shape.



$$(s_x, s_y) = T_{ws}(T_{tw}(s, t))$$



# Texture to Screen

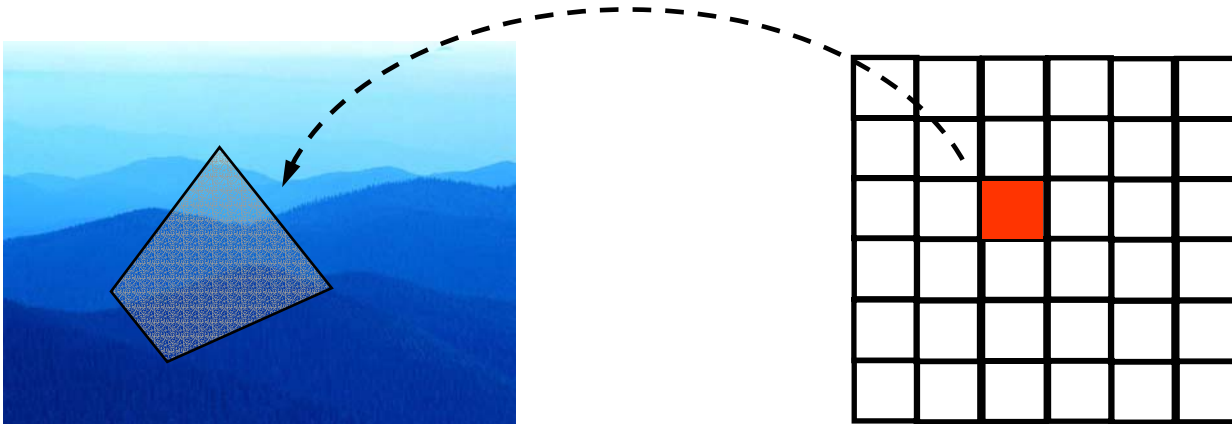


$$(sx, sy) = Tws(Ttw(s, t))$$

We would have to calculate pixel coverages

# Screen to texture

*Better approach*

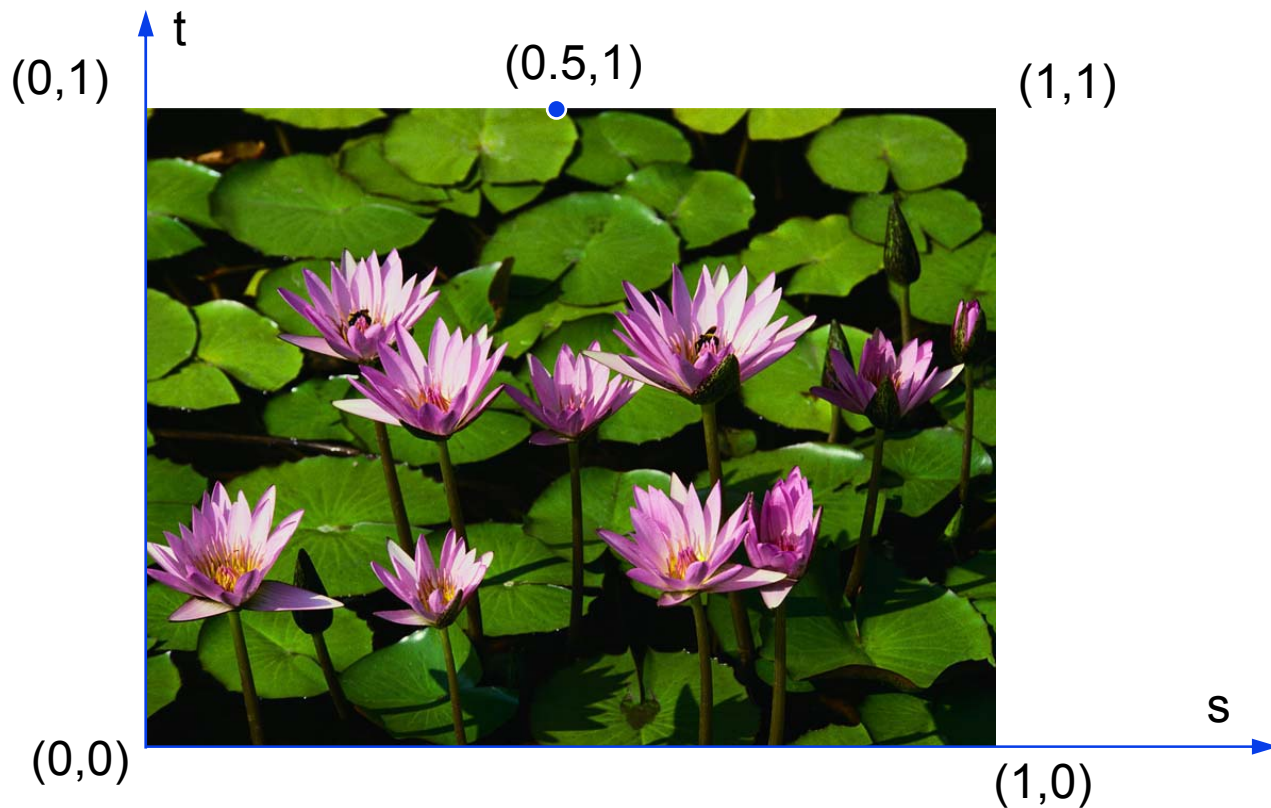


$$(s,t) = \text{Twt}(\text{Tsw}(sx,sy))$$

Requires inverting the  
projection matrix

# Textures are always images

They are always assigned the shown parametric coordinates  $(s,t)$ .



# From texture to world (object)

*To apply a texture to an object we have to find a correspondance between  $(s,t)$  and some object coordinate system.*

- Mapping via a parametric representation of the object space (points).
- By hand.

# Mapping from texture to a parametric representation of the object space

## *Linear transformation*

### *Texture space (s,t) to object space (u,v)*

$$u = u(s,t) = a_u s + b_u t + c_u$$

$$v = v(s,t) = a_v s + b_v t + c_v$$

$$s \text{ in } [0,1]$$

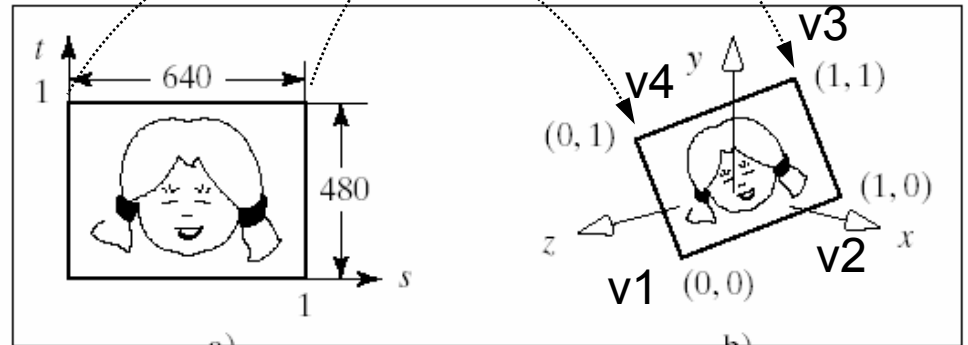
$$t \text{ in } [0,1]$$

# Example: Image to a quadrilateral

*Simply*

$$u = u(s,t) = s$$

$$v = v(s,t) = t$$



```
glTexCoord2f(0,0) ; glVertex3dv(v1) ;
```

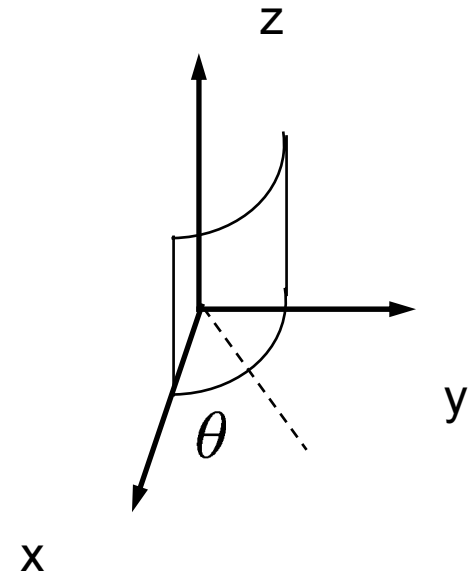
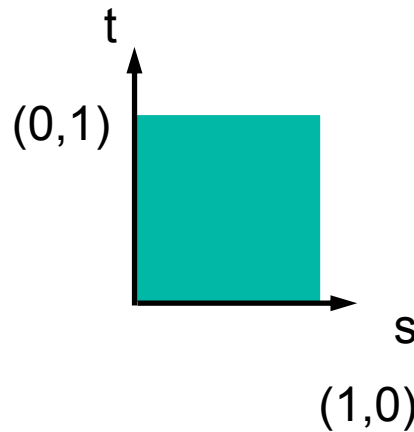
```
glTexCoord2f(1,0) ; glVertex3dv(v2) ;
```

```
glTexCoord2f(1,1) ; glVertex3dv(v3) ;
```

```
glTexCoord2f(0,1) ; glVertex3dv(v4) ;
```



# Example: Square texture to cylinder



*Parametric form :*

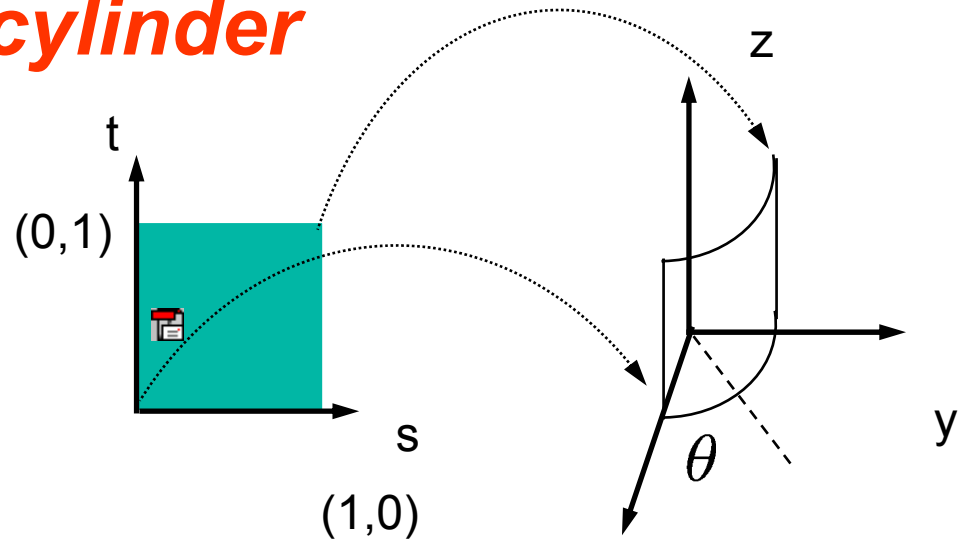
$$x = r \cos \theta, \quad y = r \sin \theta, \quad z$$

*Surface parameters :*  $u = \theta, v = z$

*with*  $0 \leq u \leq \pi/2, \quad 0 \leq v \leq 1$

# Example : Square texture to cylinder

## *Square texture to cylinder*

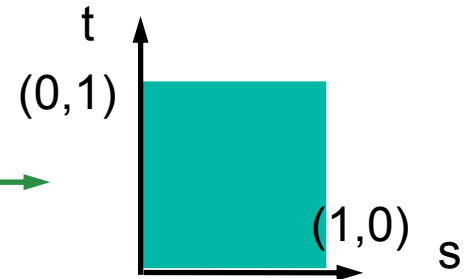
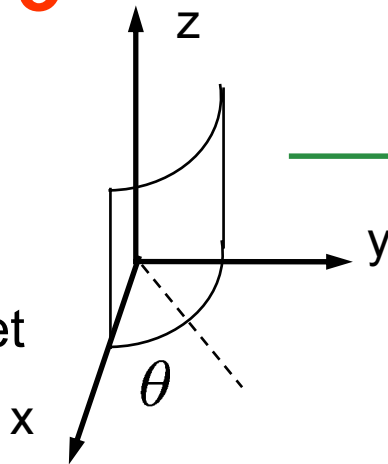
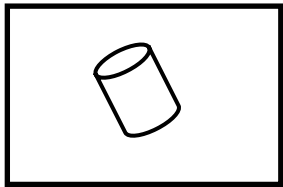


We pick the following linear transformation that maps  $(s, t) = (0, 0)$  to  $(x, y, z) = (r, 0, 0)$  and  $(s, t) = (1, 1)$  to  $(x, y, z) = (0, r, r)$ .

$$u = s\pi/2, \quad v = t$$

# Example : Square texture to cylinder

## From screen to texture



1. Inverse transform  $(sx, sy)$  to get world position  $(x, y, z)$ .
2. Then having  $(x, y, z)$

$$u = \tan^{-1}(y/x), \quad v = z$$

$$s = 2u/\pi, \quad t = v$$

$$\text{Reminder : } u = s\pi/2, \quad v = t$$

$$x = r\cos\theta, \quad y = r\sin\theta, \quad z$$

$$\text{Surface parameters : } u = \theta, v = z$$

# How does that work with the graphics pipeline?

*Only polygons*

*Only vertices go down the graphics pipeline.*

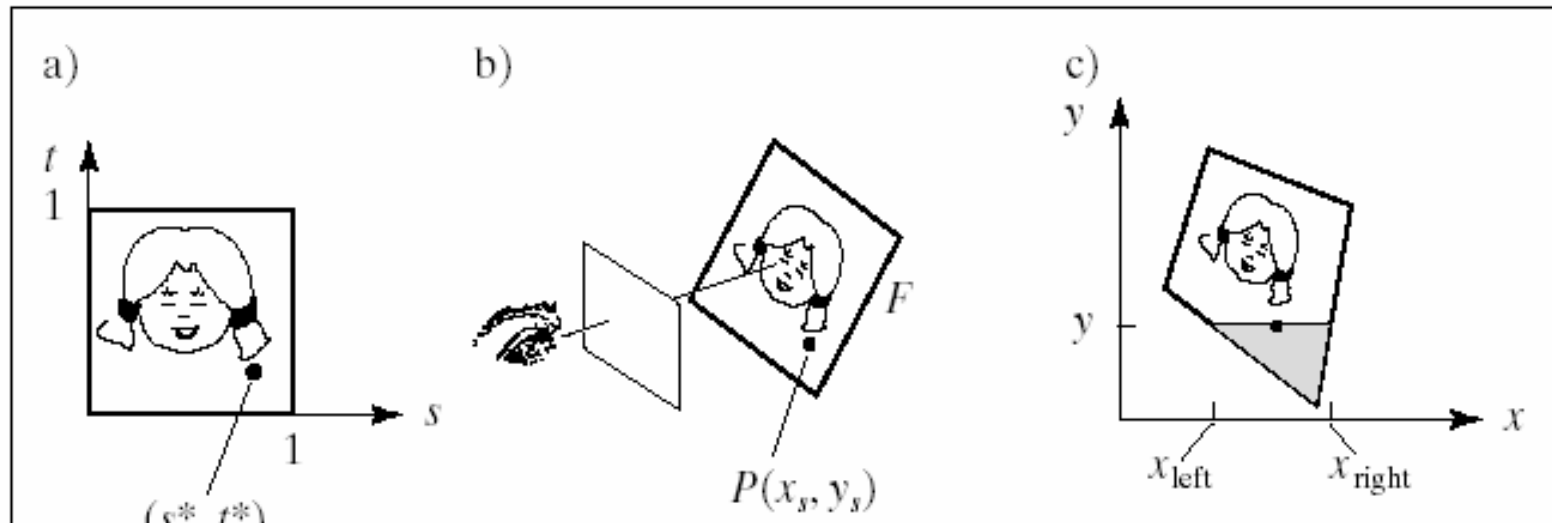
Interior points?

*Calculate texture coordinates by interpolation along scanlines.*

# Rendering the texture

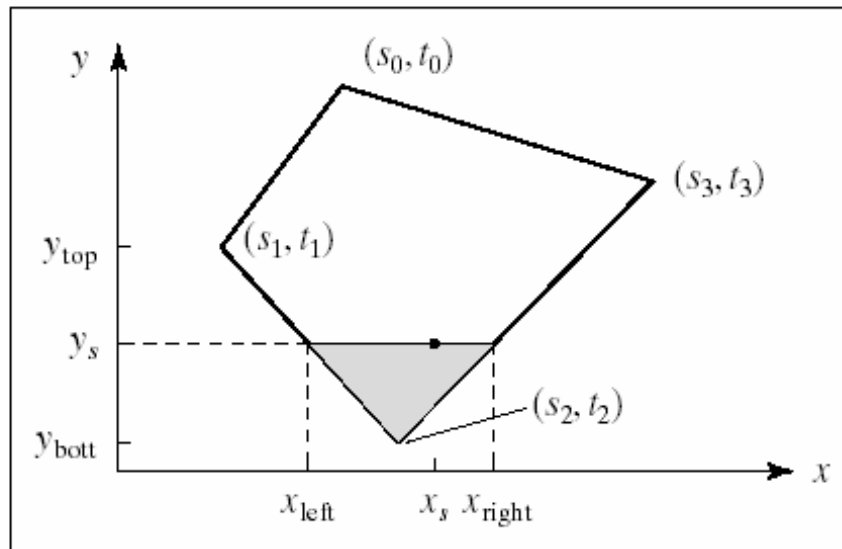
## *Scanline in screen space*

- Generating  $s, t$  coordinates for each pixel



**FIGURE 8.39** Rendering a face in a camera snapshot.

# Interpolation of texture coordinates

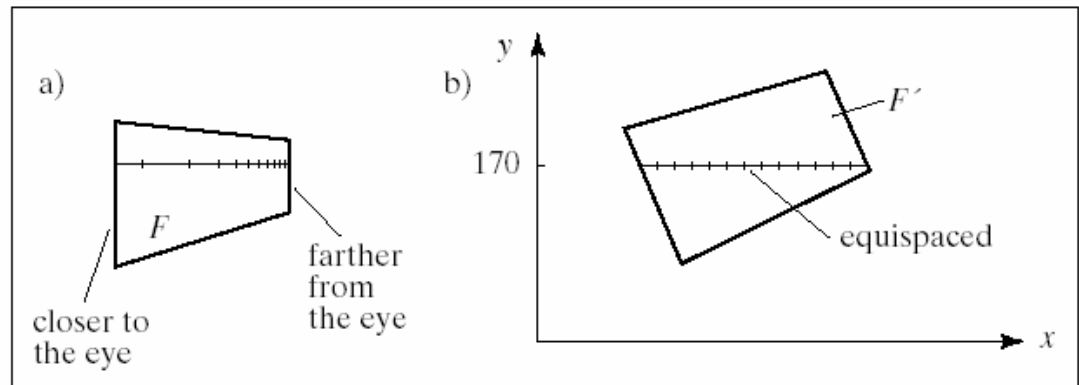
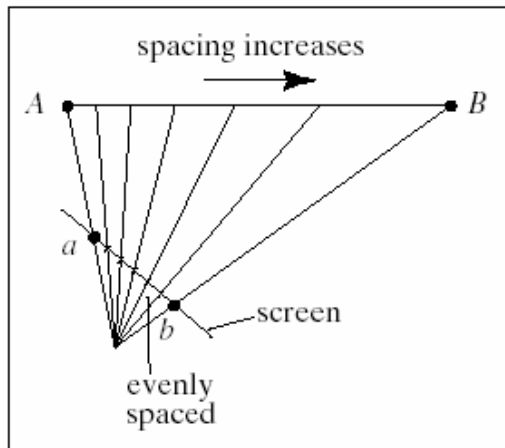


**FIGURE 8.40** Incremental calculation of texture coordinates.

# Problem

## *Perspective forshortening*

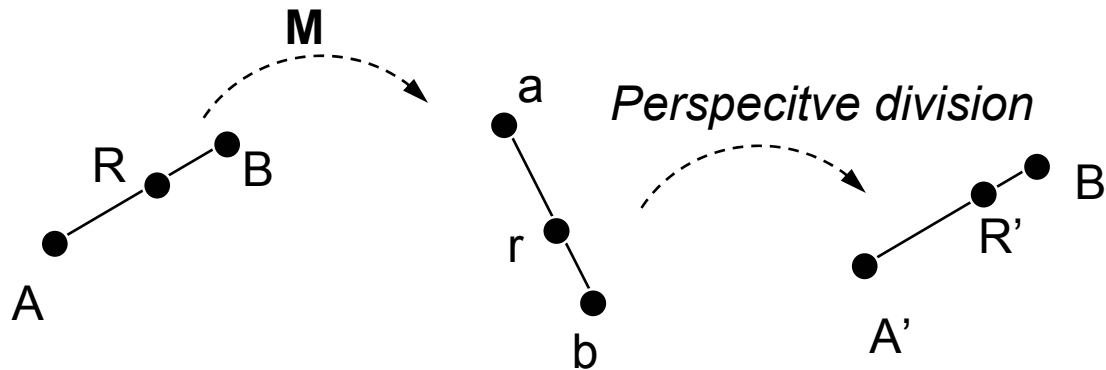
- Scanconversion takes equal steps along scanline (screen space)
- Equal steps in screen space not equal steps in world space



**FIGURE 8.41** Spacing of samples with linear interpolation.

# Inbetween points

*How do points on lines transform?*



$$R(g) = (1-g)A + gB$$

$$r = MR$$

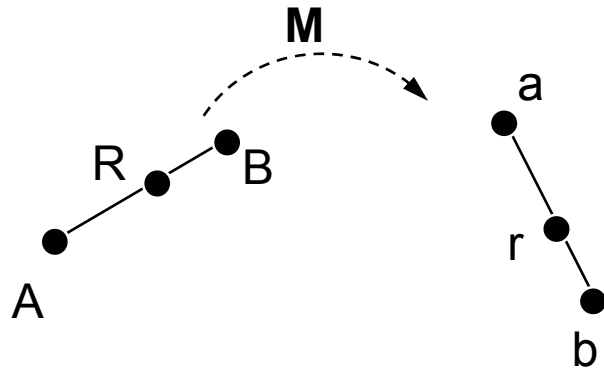
$$R'(f) = (1-f)a' + fb' \text{ in cartesian coordinates}$$

What is the relationship between  $g$  and  $f$ ?



# First step

*World to homogeneous space (4D)*



$$R = (1 - g)A + gB$$

$$r = MR = M[(1 - g)A + gB] = (1 - g)MA + gMB \Rightarrow$$

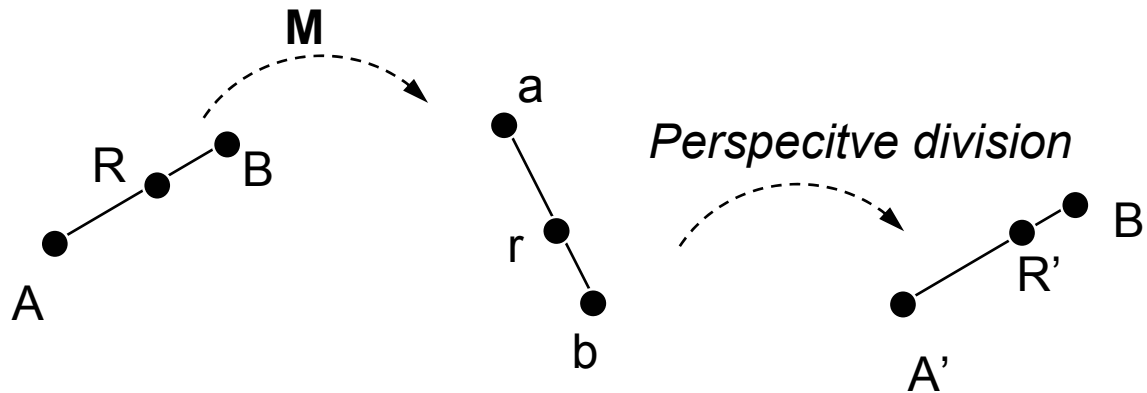
$$r = (1 - g)a + gb$$

$$a = MA = (a_1, a_2, a_3, a_4)$$

$$b = MB = (b_1, b_2, b_3, b_4)$$

# Second step

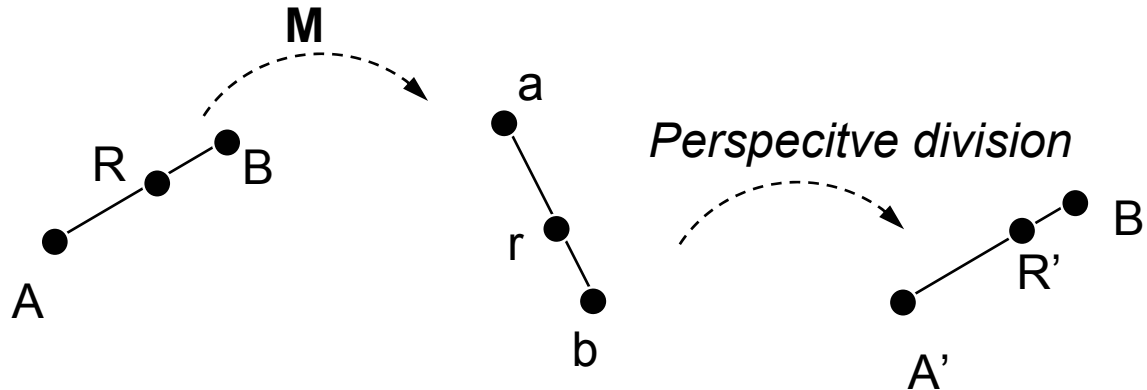
## Perspective division



$$\left\{ \begin{array}{l} r = (1 - g)a + gb \\ a = (a_1, a_2, a_3, a_4) \\ b = (b_1, b_2, b_3, b_4) \end{array} \right\} \Rightarrow$$

$$R'_1 = \frac{r_1}{r_4} = \frac{(1 - g)a_1 + gb_1}{(1 - g)a_4 + gb_4}$$

# Putting all together



$$R'_1 = \frac{(1 - g)a_1 + gb_1}{(1 - g)a_4 + gb_4} = \frac{lerp(a_1, b_1, g)}{lerp(a_4, b_4, g)}$$

At the same time :

$$R' = (1 - f)A' + fB' \Rightarrow$$

$$R'_1 = (1 - f)\frac{a_1}{a_4} + f\frac{b_1}{b_4} = lerp(\frac{a_1}{a_4}, \frac{b_1}{b_4}, f)$$



# Relation between the fractions

$$\left. \begin{aligned} R1(f) &= \frac{\text{lerp}(a1, b1, g)}{\text{lerp}(a4, b4, g)} \\ R1(f) &= \text{lerp}\left(\frac{a1}{a4}, \frac{b1}{b4}, f\right) \end{aligned} \right\} \Rightarrow g = \frac{f}{\text{lerp}\left(\frac{b4}{a4}, 1, f\right)}$$

substituting this in  $R(g) = (1 - g)A + gB$  yields

$$R1 = \frac{\text{lerp}\left(\frac{A1}{a4}, \frac{B1}{b4}, f\right)}{\text{lerp}\left(\frac{1}{a4}, \frac{1}{b4}, f\right)}$$

**THAT MEANS:** For a given  $f$  in **screen space** and  $A, B$  in **world space** we can find the corresponding  $R$  (or  $g$ ) in **world space** using the above formula.

“ $A$ ” can be texture coordinates, position, color, normal etc.

# Rendering images incrementally

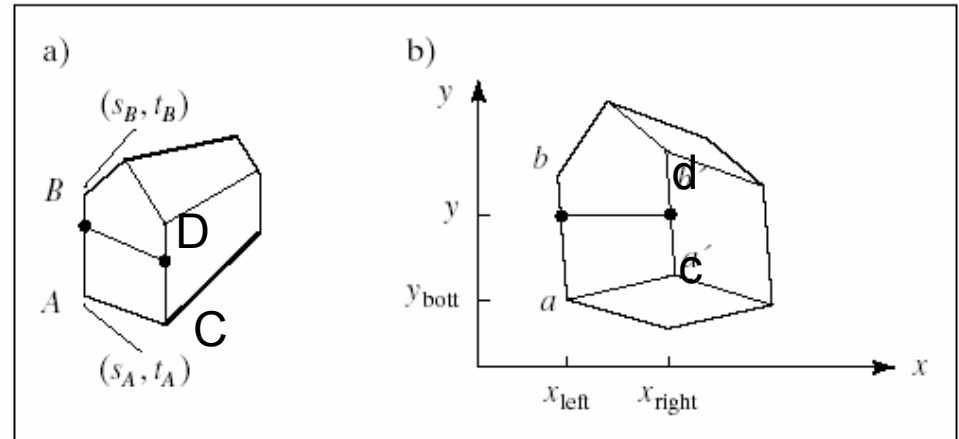
*A maps to a (homogeneous)*

*B maps to b*

*C maps to c*

*D maps to d*

*For scanline y:*



$$f = (y - y_{bott}) / (y_{top} - y_{bott})$$

$$s_{left}(y) = \frac{\text{lerp}(\frac{s_A}{a_4}, \frac{s_B}{b_4}, f_l)}{\text{lerp}(\frac{1}{a_4}, \frac{1}{b_4}, f_l)}, s_{right}(y) = \frac{\text{lerp}(\frac{s_C}{c_4}, \frac{s_D}{d_4}, f_r)}{\text{lerp}(\frac{1}{c_4}, \frac{1}{d_4}, f_r)}$$

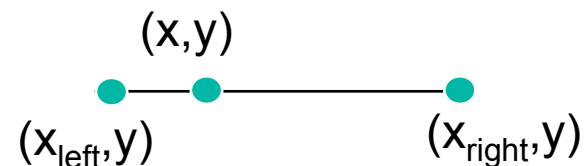
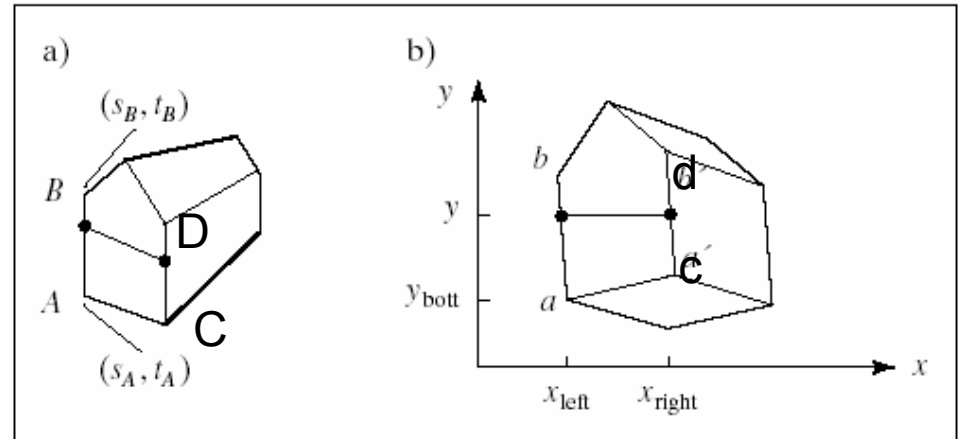
*Once we have  $s_{left}$  and  $s_{right}$  another hyperbolic interpolation fills in the scanline*

# Interpolation along the scanline

$$s_{left}(y) = \frac{\text{lerp}(\frac{s_A}{a_4}, \frac{s_B}{b_4}, f_l)}{\text{lerp}(\frac{1}{a_4}, \frac{1}{b_4}, f_l)}$$

$$s_{right}(y) = \frac{\text{lerp}(\frac{s_C}{c_4}, \frac{s_D}{d_4}, f_r)}{\text{lerp}(\frac{1}{c_4}, \frac{1}{d_4}, f_r)}$$

$$s(x, y) = \frac{\text{lerp}(\frac{s_{left}}{h_{left}}, \frac{s_{right}}{h_{right}}, f)}{\text{lerp}(\frac{1}{h_{left}}, \frac{1}{h_{right}}, f)}$$



What are the f, and h's?

# Interpolation along the scanline

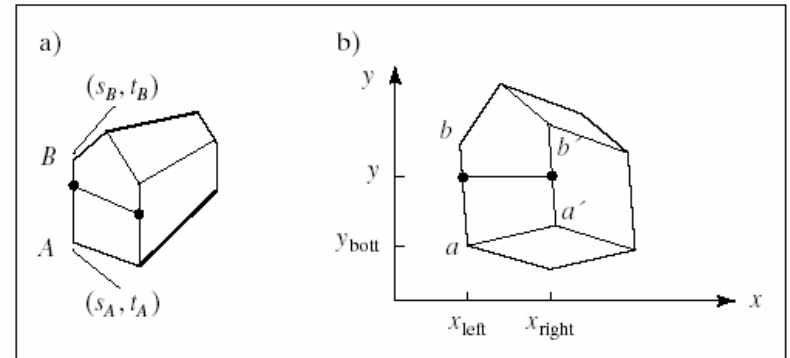
$$s_{left}(y) = \frac{\text{lerp}(\frac{s_A}{a_4}, \frac{s_B}{b_4}, f_l)}{\text{lerp}(\frac{1}{a_4}, \frac{1}{b_4}, f_l)}, s_{right}(y) = \frac{\text{lerp}(\frac{s_C}{c_4}, \frac{s_D}{d_4}, f_r)}{\text{lerp}(\frac{1}{c_4}, \frac{1}{d_4}, f_r)}$$

$$s(x, y) = \frac{\text{lerp}(\frac{s_{left}}{h_{left}}, \frac{s_{right}}{h_{right}}, f)}{\text{lerp}(\frac{1}{h_{left}}, \frac{1}{h_{right}}, f)}$$

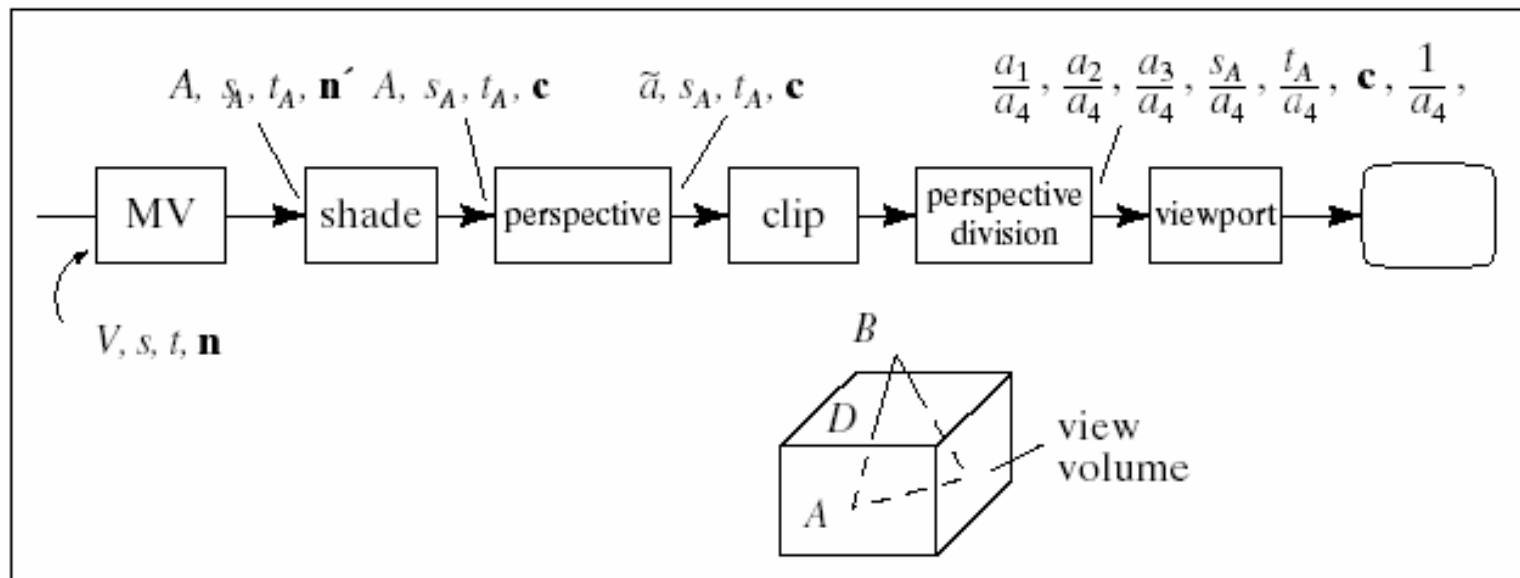
$$h_{left} = \text{lerp}(a_4, b_4, f_l)$$

$$h_{right} = \text{lerp}(c_4, d_4, f_r)$$

$$f = (x - x_{left}) / (x_{right} - x_{left})$$



# Pipeline with hyperbolic interpolation





# What does the texture do?

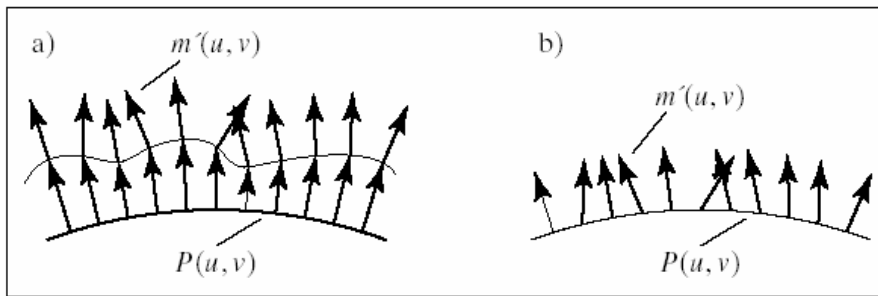
## *Replace*

- $I_r = \text{texture\_r}(s,t)$
- `glTexEnvf(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_DECAL) ;`

## *Modulate*

- $I = \text{texture}(s,t)[I_{aka} + I_{dkd} \times \text{lambert}] + I_{sks} \times \text{phong}$
- `glTexEnvf(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_MODULATE) ;`

# Bump Mapping



**FIGURE 8.50** On the nature of bump mapping.

$$P'(u,v) = P(u,v) + \text{texture}(u,v)m(u,v)$$

Approximation by Blinn

$$m'(u,v) = m(u,v) + [(m \times P\_v) \text{texture\_u} - (m \times P\_u) \text{texture\_v}]$$

Where  $\_$  indicates partial derivative.

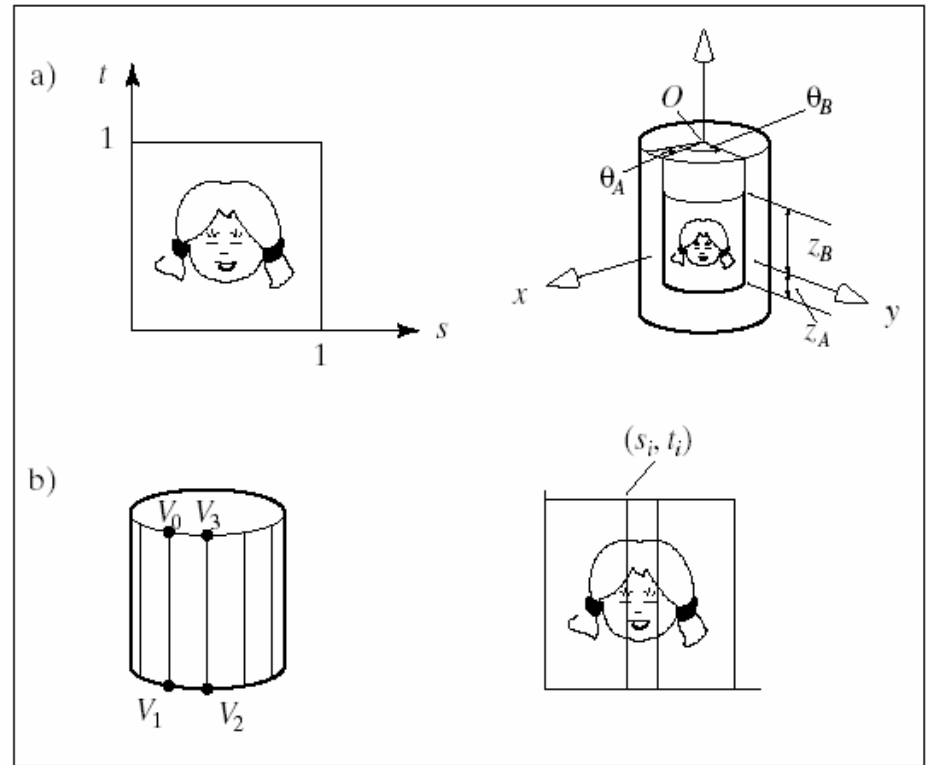
All functions evaluated at  $(u,v)$ .

# Example



# Calculating texture coordinates

# Wrapping textures on curved surfaces



$$s = \frac{\theta - \theta_a}{\theta_b - \theta_a}, t = \frac{z - z_a}{z_b - z_a}$$

Cylinder with  $N$  faces

Left edge at azimuth  $\theta = 2\pi i / N$

Upper left vertex texture coordinates  $s_i = \frac{2\pi i / N - \theta_a}{\theta_b - \theta_a}, t_i = 1$ .

# Automatic calculation of Texture Coordinates

```
glEnable(GL_TEXTURE_GEN_S);
```

```
glEnable(GL_TEXTURE_GEN_T);
```

```
glTexGeni(GL_S, GL_TEXTURE_GEN_MODE,  
          GL_OBJECT_LINEAR);
```

```
Glfloat coeff[4] = {1,0,0,0} ;
```

```
glTexGenfv(GL_S, GL_OBJECT_PLANE, coeff);
```

Same for T

# GL\_OBJECT\_LINEAR

## *Linear combination of coordinates*

$$S \text{ or } T = p_0 * x + p_1 * y + p_2 * z + p_4 * w$$

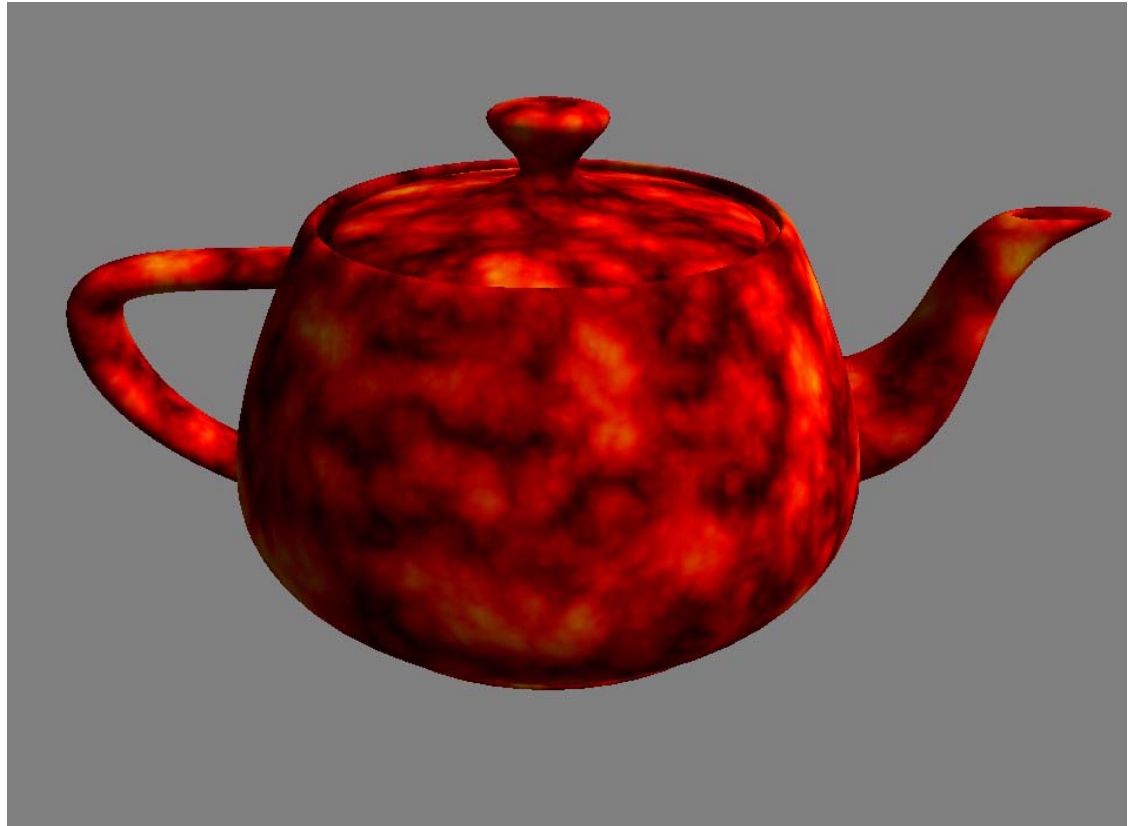
If  $(p_0, p_1, p_2, p_3)$  correctly normalized then  
distance to plane  $(p_0, p_1, p_2, p_3)$

E.g.  $(1, 0, 0, 0)$  distance from plane  $x = 0$ .

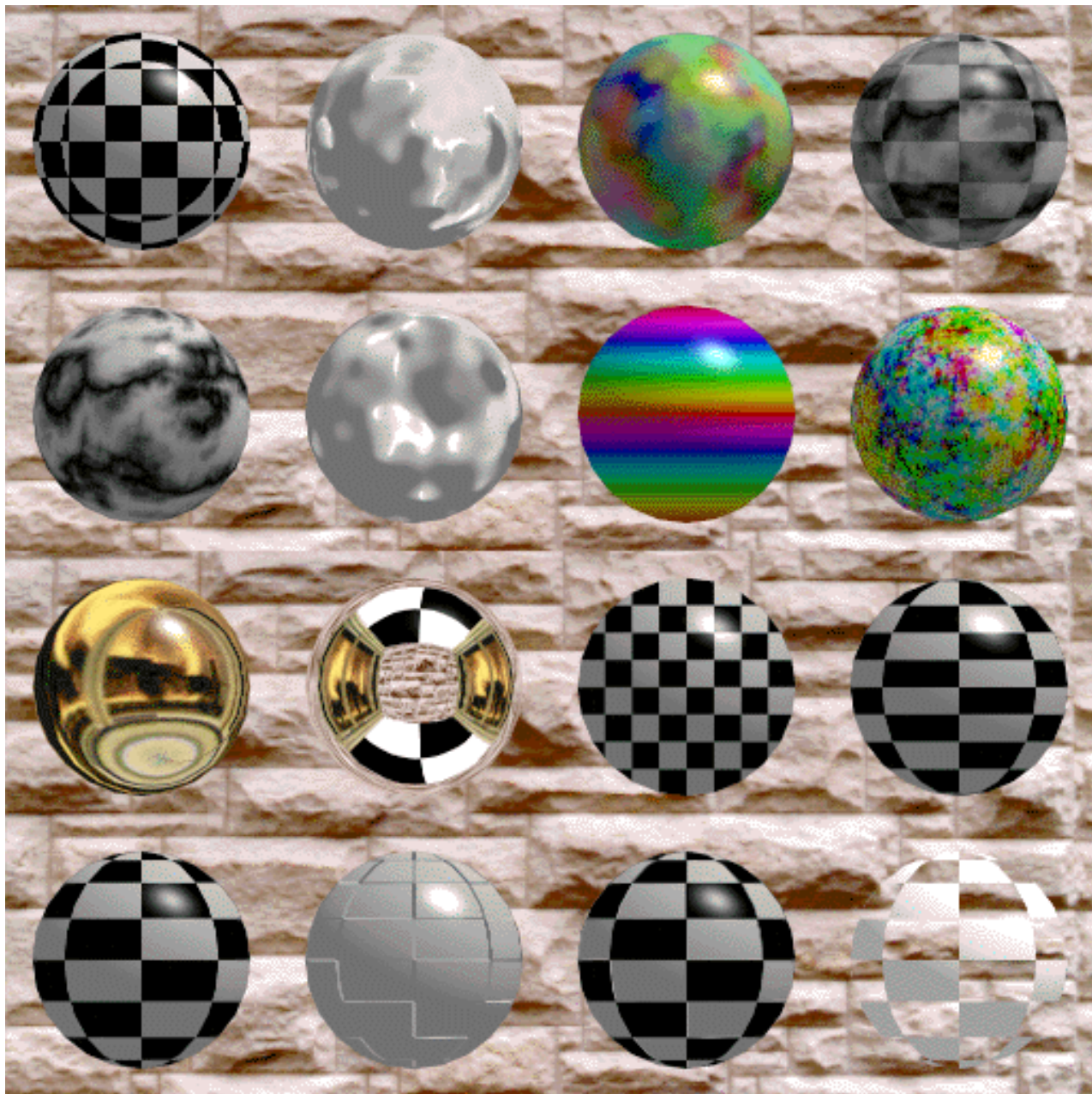
# Procedural texture

Volumetric textures

$$C = B(x,y,z)$$

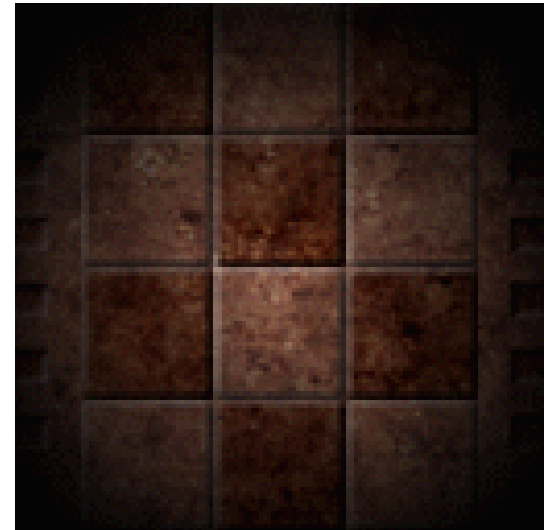
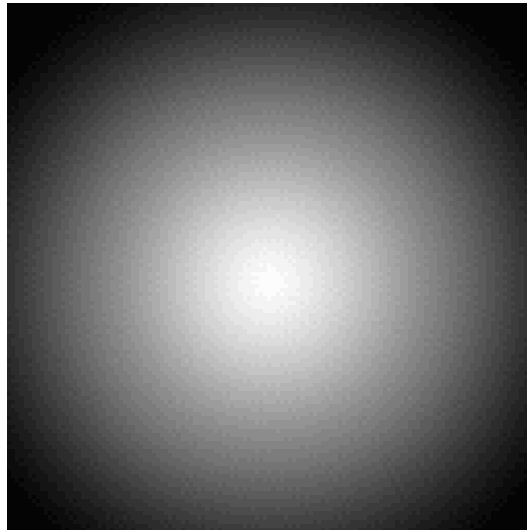
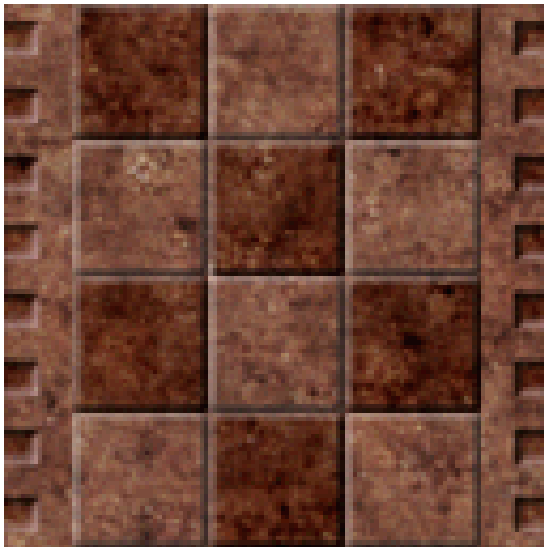






# Light maps

## *Static objects*



# Texture filtering

*Texture images consist of pixels (texels).*

*Therefore:*

- *Magnification*: a pixel on the screen may cover only part of a texel.
- *Minification*: a pixel on the screen may cover more than one texels.

*Solution: Filtering*

# Texture filtering in OpenGL

```
glTexParameteri(GL_TEXTURE_2D,  
    GL_TEXTURE_MAG_FILTER, GL_NEAREST) ;
```

```
glTexParameteri(GL_TEXTURE_2D,  
    GL_TEXTURE_MIN_FILTER, GL_NEAREST) ;
```

GL\_TEXTURE\_MAG\_FILTER: GL\_NEAREST or GL\_LINEAR

GL\_TEXTURE\_MIN\_FILTER: GL\_NEAREST, GL\_LINEAR,  
 GL\_NEAREST\_MIPMAP\_NEAREST,  
 GL\_LINEAR\_MIPMAP\_NEAREST,  
 GL\_LINEAR\_MIPMAP\_LINEAR,

# Texture mapping in OpenGL

```
void glTexImage2D(  
    GLenum target,    // must be GL_TEXTURE_2D  
    GLint level,  
    GLint internalformat, // e.g. 3  
    GLsizei width,  
    GLsizei height,  
    GLint border,  
    GLenum format,    // e.g. GL_RGB  
    GLenum type,      // e.g. GL_UNSIGNED_BYTE  
    const GLvoid *pixels // size powers of 2 !!  
);
```

# Texture Parameters

```
void glTexParameterf(  
    GLenum target,          // e.g. GL_TEXTURE_2D  
    GLenum pname,          // GL_WRAP_S  
    GLfloat param           // value e.g. GL_CLAMP  
);
```

# Texture effect

```
void glTexEnvf(  
    GLenum target,      // GL_TEXTURE_ENV  
    GLenum pname,      // GL_TEXTURE_ENV_MODE  
    GLfloat param       // GL_MODULATE, GL_DECAL,  
                        // and GL_BLEND  
);
```

# Enabling texture mapping

*glEnable(GL\_TEXTURE\_2D) ;*

*glDisable(GL\_TEXTURE\_2D) ;*



# Texture mapping example

```
void initTexture(void) {  
    glTexImage2D(GL_TEXTURE_2D, 0, 3, Img.m_width,  
        Img.m_height, 0, GL_RGB, GL_UNSIGNED_BYTE,  
        Img.m_data);  
    glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S,  
        GL_REPEAT);  
    glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T,  
        GL_REPEAT);  
    glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_NEAREST);  
    glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,  
        GL_NEAREST);  
    glTexEnvf(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE,  
        GL_DECAL);  
    glEnable(GL_TEXTURE_2D);  
}
```

# Texture Objects

*Copying an image from main memory to video memory is very expensive (glTexImage2D) .*

- *Create texture names*
- *Bind (create) texture objects to texture data:*
  - *Image arrays + texture properties*
- *Bind and rebind texture objects.*

# Naming texture objects

```
void glGenTextures(GLsizei n, GLuint  
    *textureNames) ;
```

**Returns** *n* unused names `textureNames[0]...[n]`).

```
GLboolean glIsTexture(GLuint textureName) ;
```

# Creating Texture Objects

```
glBindTexture(GLenum target, GLuint  
textureName) ;
```

## *Three things:*

- If textureName > 0 and not already assigned a new texture object is created.
- If textureName assigned, the textureObject becomes active.
- If textureName is 0 OpenGL stops using textures and returns to the default unnamed texture.

# Initial creation

```
glBindTexture(Glenum target, GLuint  
textureName) ;
```

**Target:**

```
GL_TEXTURE_1D, GL_TEXTURE_2D , GL_TEXTURE_3D,  
GL_TEXTURE_CUBE_MAP.
```

# Example: Creating the textures

```
void init(void) {
    glGenTextures(2, texName) ;
    glBindTexture(GL_TEXTURE_2D, texName[0]) ;
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S,
GL_CLAMP);
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T,
GL_CLAMP);
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER,
GL_NEAREST);
    glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,
GL_NEAREST);
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA,
GL_UNSIGNED_BYTE, image1) ;

    glBindTexture(GL_TEXTURE_2D, texName[1]) ;
    ...
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA,
GL_UNSIGNED_BYTE, image2) ;

}
```

# Example: Using the textures

```
void display(void) {  
    ...  
    glBindTexture(GL_TEXTURE_2D, texName[0]) ;  
    glBegin(GL_QUADS) ;  
    glTexCoord2f(0.0,0.0) ;  
    ...  
    glEnd() ;  
  
    glBindTexture(GL_TEXTURE_2D, texName[1]) ;  
    glBegin(GL_QUADS) ;  
    glTexCoord2f(0.0,0.0) ;  
    ...  
    glEnd() ;  
}
```