

One of the many powers that C++ gives the programmer is the ability to work with the individual bits of an integer field. The purpose of this appendix is to give an overview of how integer data types are stored in binary and explain the bitwise operators that the C++ offers. Finally, we will look at bit fields, which allow us to treat the individual bits of a variable as separate entities.

#### **Integer Forms**

The integer types that C++ offers are as follows:

```
char
int
short
long
unsigned char
unsigned (same as unsigned int)
unsigned short
unsigned long
```

When you assign constant values to integers in C++, you may use decimal, octal, or hexadecimal. Placing a zero in the first digit creates an octal constant. For example, 0377 would be interpreted as an octal number. Hexadecimal constants are created by placing 0x or 0X (zero-x, not O-x) in front of the number. The number 0X4B would be interpreted as a hex number.

## **Binary Representation**

Regardless of how you express constants, integer values are all stored the same way internally—in binary format. Let's take a quick review of binary number representation.

Let's assume we have a one-byte field. The following diagram shows our field broken into its individual bits.

Bit	Bit	Bit	Bit	Bit	Bit	Bit	Bit			
7	6	5	4	3	2	1	0			
High Order> Low Order										

The leftmost bits are called the *high order* bits and the rightmost bits are called the *low order* bits. Bit number 7 is the highest order bit, so it is called the *most significant* bit.

Each of these bits has a value assigned to it. The following diagram shows the values of each bit.

	Bit								
	7	6	5	4	3	2	1	0	
Values ->	128	64	32	16	8	4	2	1	

These values are actually powers of two. The value of bit 0 is  $2^0$  which is 1. The value of bit 1 is  $2^1$ , which is 2. Bit 2 has the value  $2^2$ , which is 4. It progresses to the last bit.

When a number is stored in this field, the bits may be set to either 1 or 0. Here is an example.

	Bit								
	7	6	5	4	3	2	1	0	
	0	1	1	0	0	1	1	0	
Values ->	128	64	32	16	8	4	2	1	•

Here, bits 1, 2, 5, and 6 are set to 1. To calculate the overall value of this bit pattern, we add up all of the bit values of the bits that are set to 1.

Bit 1's value	2	
Bit 2's value	4	
Bit 5's value	32	
Bit 6's value	64	
	Overall Value	102

The bit pattern 01100110 has the decimal value 102.

# **Negative Integer Values**

One way that a computer can store a negative integer is to use the leftmost bit as a sign bit. When this bit is set to 1, it would indicate a negative number, and when it is set to 0 the number would be positive. The problem with this, however, is that we would have two bit patterns for the number 0. One pattern would be for positive 0, the other would be for negative 0. Because of this, most systems use two's complement representation for negative integers.

To calculate the two's complement of a number, first you must get the one's complement. This means changing each 1 to a 0, and each 0 to a 1. Next, add 1 to the resulting number. What you have is the two's complement. Here is how the computer stores the value -2.

2 is stored as	0000010
Get the one's complement	11111101
Add 1	1
And the result is	11111110

As you can see, the highest order bit is still set to 1, indicating not only that this is a negative number, but it is stored in two's complement representation.

#### **Bitwise Operators**

C++ provides operators that let you perform logical operations on the individual bits of integer values, and shift the bits right or left.

#### **The Bitwise Negation Operator**

The bitwise negation operator is the ~ symbol. It is a unary operator that performs a negation, or one's complement on each bit in the field. The expression

```
~val
```

returns the one's complement of val. It does not change the contents of val. It could be used in the following manner:

```
negval = ~val;
```

This will store the one's complement of val in negval.

#### The Bitwise AND Operator

The bitwise AND operator is the & symbol. This operator performs a logical AND operation on each bit of two operands. This means that it compares the two operands bit by bit. For each position, if both bits are 1, the result will be 1. If either or both bits are 0, the results will be 0. Here is an example:

```
andval = val & 0377;
```

The result of the AND operation will be stored in andval. There is a combined assignment version of this operator. Here is an example:

```
val &= 0377;
This is the same as:
    val = val & 0377;
```

## **The Bitwise OR Operator**

The bitwise OR operator is the | symbol. This operator performs a logical OR operation on each bit of two operands. This means that it compares the two operands bit by bit. For

each position, if either of the two bits is 1, the result will be 1. Otherwise, the results will be 0. Here is an example:

```
orval = val | 0377;
```

The result of the OR operation will be stored in orval. There is a combined assignment version of this operator. Here is an example:

```
val |= 0377;
```

This is the same as

#### The Bitwise EXCLUSIVE OR Operator

The bitwise EXCLUSIVE OR operator is the ^ symbol. This operator performs a logical XOR operation on each bit of two operands. This means that it compares the two operands bit by bit. For each position, if one of the two bits is 1, but not both, the result will be 1. Otherwise, the results will be 0. Here is an example:

```
xorval = val ^ 0377;
```

The result of the XOR operation will be stored in xorval. There is a combined assignment version of this operator. Here is an example:

```
val ^= 0377;
```

This is the same as:

## **Using Bitwise Operators with Masks**

Suppose we have the following variable declarations:

The binary pattern for each of these two variables will be as follows:

value>	0	1	1	0	1	1	1	0	= 110
cloak>	0	0	0	0	0	0	1	0	= 2

The operation

will perform a logical bitwise AND on the two variables value and cloak. The result will be stored in value. Remember a bitwise AND will produce a 1 only when both bits are set to 1. Here is a diagram showing the result of the AND operation.

value>	0	1	1	0	1	1	1	0	
AND									
cloak>	0	0	0	0	0	0	1	0	

equals

result>	0	0	0	0	0	0	1	0

The 0's in the cloak variable "hide" the values that are in the corresponding positions of the value variable. This is called *masking*. When you mask a variable, the only bits that will "show through" are the ones that correspond with the 1's in the mask. All others will be turned off.

## **Turning Bits On**

Sometimes you may want to turn on selected bits in a variable and leave all of the rest alone. This operation can be performed with the bitwise OR operator. Let's see what happens when we OR the value and cloak variables we used before, but using a different value for cloak.

```
char value = 110, cloak = 16;
value |= mask;
```

This diagram illustrates the result of the OR operation:

value>	0	1	1	0	1	1	1	0
OR								
cloak>	0	0	0	1	0	0	0	0
Equals								
result>	0	1	1	1	1	1	1	0

This caused bit 4 to be turned on and all the rest to be left alone.

# **Turning Bits Off**

Suppose that instead of turning specific bits on, you wish to turn them off. Assume we have the following declaration:

```
char status = 127, cloak = 8;
```

Bit 3 of cloak is set to 1, and all the rest are set to 0. If we wish to set bit 3 of status to 0 we must AND it with the negation of cloak. In other words, we must get the one's complement of cloak, then AND it with status. The statement would look like this:

```
status &= ~cloak;
```

Here is what cloak's bit pattern looks like:

cloak>	0	0	0	0	1	0	0	0
	•		•	•	_	•	1	

And here is the one's complement of cloak:

~cloak>	1	1	1	1	0	1	1	1	

Here is what we get when we AND status and the one's complement of cloak:

status>	0	1	1	1	1	1	1	1
---------	---	---	---	---	---	---	---	---

AND								
~cloak>	1	1	1	1	0	1	1	1
Equals								
result>	0	1	1	1	0	1	1	1

Bit 3 of status is turned off, and all other bits were left unchanged.

# **Toggling Bits**

To toggle a bit is to flip it off when it is on, and on when it is off. This can be done with the EXCLUSIVE OR operator. We will use the following variables to illustrate.

```
char status = 127, cloak = 8;
```

Our objective is to toggle bit 3 of status, so we will use the XOR operator.

```
status ^= cloak;
```

Here is the diagram of the operation:

status>	0	1	1	1	1	1	1	1
XOR								
cloak>	0	0	0	0	1	0	0	0
Equals								
result>	0	1	1	1	0	1	1	1

Bit 3 of status will be set to 0. If we repeat this operation with the new value of status, this is what will happen:

status>	0	1	1	1	0	1	1	1
XOR								
cloak>	0	0	0	0	1	0	0	0
equals								
result>	0	1	1	1	1	1	1	1

Bit 3 of status will be toggled again, restoring it to its previous state.

## Testing the Value of a Bit

To test the value of an individual bit, you must use the AND operator. For example, if we want to test the variable bitvar to see if bit 2 is on, we must use a mask that has bit 2 turned on. Here is an example of the test:

```
if ((bitvar & 4) == 4)
  cout << "Bit 2 is on.\n";</pre>
```

Remember that ANDing a value with a mask will produce a value that hides all of the bits but the ones turned on in the mask. If bit 2 of bitvar is on, the expression bitvar & 4 will return the value 4.

The parentheses around bitvar & 4 are necessary because the == operator has higher precedence than the & operator.

## The Bitwise Left Shift Operator

The bitwise left shift operator is two less-than signs (<<). It takes two operands. The operand on the left is the one to be shifted, and the operand on the right is the number of places to shift. When the bit values are shifted left, the vacated positions to the right are filled with 0's and the bits that shift out of the field are lost. Suppose we have the following variables:

```
char val = 2, shiftval;
```

The following statement will store in shiftval the value of val shifted left 2 places.

Let's see what is happening behind the scenes with the value in vals.

Before shift	0	0	0	0	0	0	1	0
After shift	0	0	0	0	1	0	0	0

Realize, however that val itself is not being shifted. The variable shiftval is being set to the value of val shifted left 2 places. If we wanted to shift val itself, we could use the combined assignment version of the left shift operator.

Shifting a number left by n places is the same as multiplying it by  $2^n$ . So, this example is the same as:

The bitwise shift will almost always work faster, however.

## The Bitwise Right Shift Operator

The bitwise right shift operator is two greater-than signs (>>). Like the left shift operator, it takes two operands. The operand on the left is the one to be shifted, and the operand on the right is the number of places to shift. When the bit values are shifted right, and the variable is signed, what the vacated positions to the left are filled with depends on the machine. They could be filled with 0s, or with the value of the sign bit. If the variable is unsigned, the places will be filled with 0s. The bits that shift out of the field are lost. Suppose we have the following variables:

The following statement will store in shiftval the value of val shifted right 2 places.

Let's see what is happening behind the scenes with the value in val.

Before shift	0	0	0	0	1	0	0	0
After shift	0	0	0	0	0	0	1	0

As before, val itself is not being shifted. The variable shiftval is being set to the value of val shifted right 2 places. If we wanted to shift val itself, we could use the combined assignment version of the right shift operator.

```
val >>= 2;
```

Shifting a number right by n places is the same as dividing it by  $2^n$  (as long as the number is not negative). So, the example is the same as

```
val \neq 4;
```

The bitwise shift will almost always work faster, however.

#### **Bit Fields**

C++ allows you to create data structures that use bits as individual variables. Bit fields must be declared as part of a structure. Here is an example.

```
struct {
   unsigned field1 : 1;
   unsigned field2 : 1;
   unsigned field3 : 1;
   unsigned field4 : 1;
   } fourbits;
```

The variable fourbits contains 4 bit fields: field1, field2, field3, and field4. Following the colon after each name is a number that tells how many bits each field should be made up of. In this example, each field is 1 bit in size. This structure is stored in memory in a regular unsigned int. Since we are only using 4 bits, the remaining ones will go unused.

Values may be assigned to the fields just as if it were a regular structure. In this example, we assign the value 1 to the field1 member:

```
fourbits.field1 = 1;
```

Because these fields are only 1 bit in size, we can only put a 1 or a 0 in them. We can expand the capacity of bit fields by making them larger, as in the following example:

```
struct {
  unsigned field1 : 1;
  unsigned field2 : 2;
  unsigned field3 : 3;
  unsigned field4 : 4;
} mybits;
```

Here, mybits.field1 is only 1 bit in size, but others are larger. mybits.field2 occupies 2 bits, mybits.field3 occupies 3 bits, and mybits.field4 occupies 4 bits. Here is a table that shows the maximum values of each field:

Field Name	Number of Bits	Maximum Value
mybits.field1	1	1
mybits.field2	2	3
mybits.field3	3	7
mybits.field4	4	15

This data structure uses a total of 10 bits. If you create a bit field structure that uses more bits than will fit in an int, the next int sized area will be used. Suppose we define the following bit field structure on a system that has 16 bit integers.

```
struct {
  unsigned tiny : 1;
  unsigned small : 4;
  unsigned big : 6;
  unsigned bigger : 8;
  unsigned biggest : 9;
  } flags;
```

The problem that occurs here is that flags.bigger will straddle the boundary between the first and second integer area. The compiler won't allow this to happen. flags.tiny, flags.small, and flags.big will occupy the first integer area, and flags.bigger will reside in the second integer area. There will be 5 unused bits in the first. Likewise, since flags.bigger and flags.biggest cannot fit within one integer area, flags.biggest will reside in a third area. There will be 8 unused bits in the second area, and 7 unused bits in the third.

You can force a field to be aligned with the next integer area by putting an unnamed bit field with a length of 0 before it. Here is an example:

The unnamed fields with the 0 width force scattered.second and scattered.third to be aligned with the next int area.

You can create unnamed fields with lengths other than 0. This way you can force gaps to exist at certain places. Here is an example.

This will cause a 2-bit gap to come between gaps.first and gaps.second, and a 3-bit gap to come between gaps.second and gaps.third.

Bit fields are not very portable when the physical order of the fields and the exact location of the boundaries are used. Some machines order the bit fields from left to right, but others order them from right to left.