

The ADT Stack

The Stack Concept

- Stack Characteristics

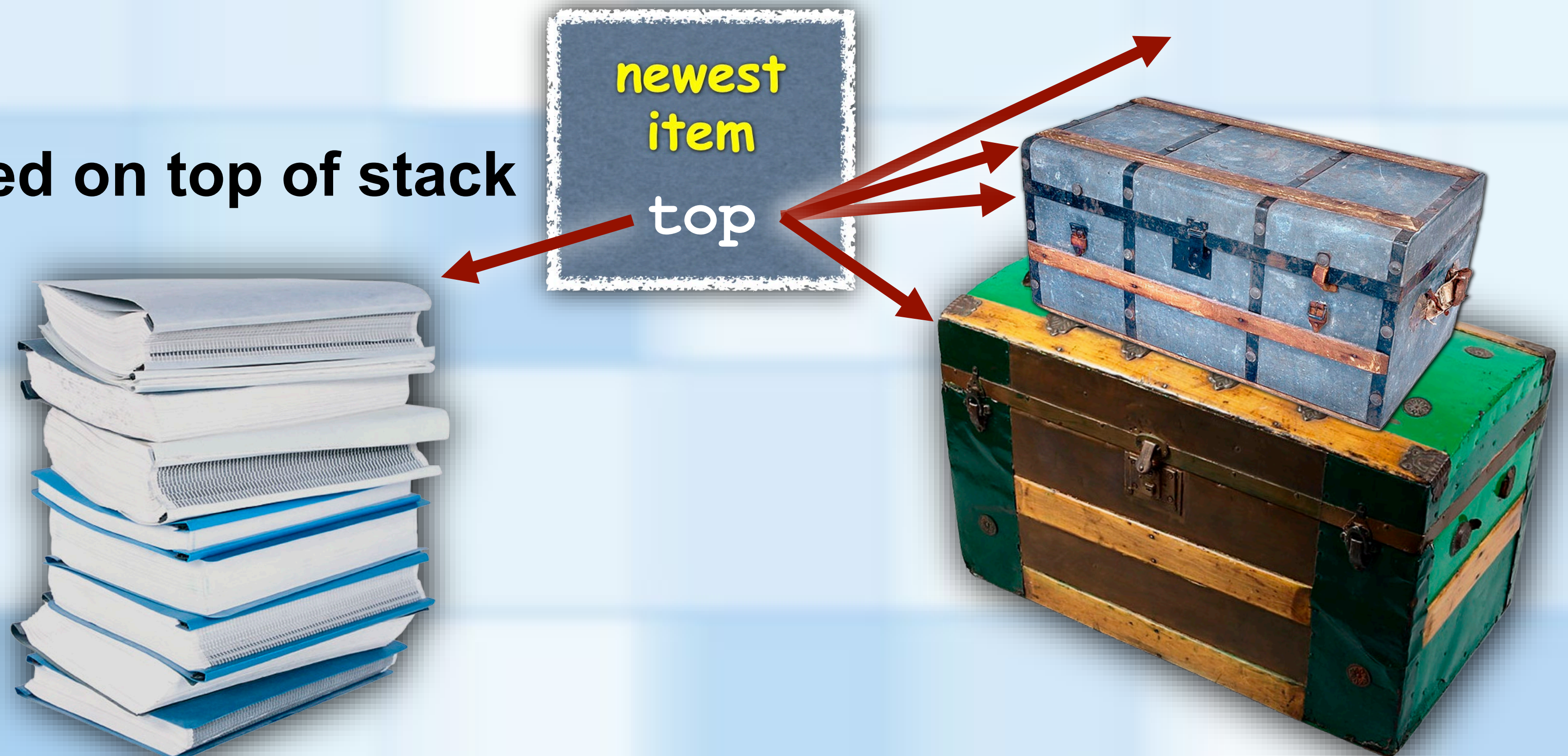
- Last-in, first-out (LIFO) property
- Last item placed on stack will be first item removed
- Items placed and removed on top of stack

- Some Real Life Stacks

- Books on a desk
- Dishes in a Cafeteria
- Boxes in an attic

push ()

pop ()



The ADT Stack

- Collection of objects in reverse chronological order with same data type

- ADT Stack operations

- Add a new item to the stack

push (ItemType someItem)

- Remove item that was added most recently

pop ()

- Retrieve item that was added most recently

ItemType peek ()

- Determine whether a stack is empty

boolean isEmpty ()

push (



)

peek ()



Stack

```
+push(someItem: T): void  
+pop(): void  
+peek(): T  
+isEmpty(): boolean  
+clear(): void
```



The ADT Stack

Stack

```
+push(someItem: T): void  
+pop(): void  
+peek(): T  
+isEmpty(): boolean  
+clear(): void
```

```
/** @file StackInterface.h */
```

```
#ifndef STACKINTERFACE  
#define STACKINTERFACE
```

```
template<class ItemType>
```

```
class StackInterface
```

```
{  
public:
```

```
    virtual bool isEmpty() const = 0;
```

```
    virtual bool push(const ItemType& someItem) = 0;
```

```
    virtual bool pop() = 0;
```

```
    virtual ItemType peek() const = 0;
```

```
    virtual ~StackInterface() { }
```

```
}; // end StackInterface
```

```
#endif
```


Using the ADT Stack

```
template<class ItemType>
class StackInterface {
public:
    virtual bool isEmpty() const = 0;
    virtual bool push(const ItemType& someItem) = 0;
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/** @file StackInterface.h */
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#define STACKINTERFACE
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template<class ItemType>
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    virtual bool isEmpty() const = 0;
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    virtual bool push(const ItemType& someItem) = 0;
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    virtual bool pop() = 0;
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```
    virtual ItemType peek() const = 0;
```

```
    virtual ~StackInterface() { }
```

```
}; // end StackInterface
```

```
#endif
```

Using the ADT Stack



Jokha is at the top of the stack.
Jokha is removed from the stack.
Jane is at the top of the stack.
Jane is removed from the stack.

```
template<class ItemType>
class StackInterface {
public:
    virtual bool isEmpty() const = 0;
    virtual bool push(const ItemType& someItem) = 0;
    virtual bool pop() = 0;
    virtual ItemType peek() const = 0;
    virtual ~StackInterface() { }
}; // end StackInterface
```

```
Stack<std::string>* stringStack = new Stack<std::string>();
stringStack->push("Jeet");
stringStack->push("Juan");
stringStack->push("Jachin");
stringStack->push("Jane");
stringStack->push("Jokha");

std::string top = stringStack->peek();
std::cout << top << " is at the top of the stack.\n";

if (stringStack->pop())
    std::cout << top << " is removed from the stack.\n";

top = stringStack->peek();
std::cout << top << " is at the top of the stack.\n";

if (stringStack->pop())
    std::cout << top << " is removed from the stack.\n";
```

Balanced Expressions

Balanced Expressions

- **Checking for Balanced Expressions**

- **Scan expression:**

- Ignore characters that are not delimiters

- **When open delimiter is encountered**

- **push** it on the stack

- **When close delimiter is encountered**

- check to see if it matches top of stack
- if yes, **pop** off top of stack

if not, expression is not balanced

Balanced

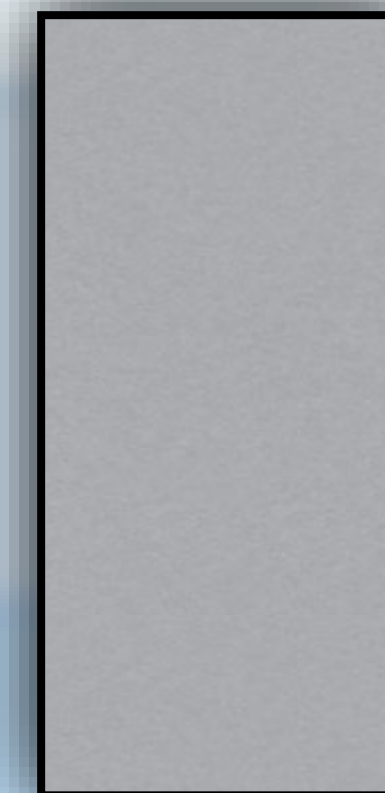
{ [() ()] () }

Not Balanced

[(])



a { b [c (d + e) / 2 - f] + 1 }



delimiterStack

Balanced Expressions

- **Checking for Balanced Expressions**

- **Scan expression:**

- Ignore characters that are not delimiters

- **When open delimiter is encountered**

- **push** it on the stack

- **When close delimiter is encountered**

- check to see if it matches top of stack
- if yes, **pop** off top of stack

if not, expression is not balanced

Balanced

{ [() ()] () }

Not Balanced

[(])



a {{ b [c (d + e] / 2 - f) + 1 }



Check Balance Implementation

```
bool checkBalance(string expression) {
    Stack<char> openDelimiterStack = new Stack<char>();
    int characterCount = expression.length();
    bool isBalanced = true;
    int index = 0;
    char nextCharacter = ' ';
```

```
while (isBalanced && (index < characterCount)) {
    nextCharacter = expression.charAt(index);
    switch (nextCharacter){
        case '(': case '[': case '{':
            openDelimiterStack->push(nextCharacter);
            break;
        case ')': case ']': case '}':
            if (openDelimiterStack->isEmpty())
                isBalanced = false;
            else
            {
                char openDelimiter = openDelimiterStack->pop();
                openDelimiterStack->pop();
                isBalanced = isPaired(openDelimiter, nextCharacter);
            } // end if
            break;
        default:
            break;
    } // end switch
    index++;
} // end while
if (!openDelimiterStack->isEmpty())
    isBalanced = false;
return isBalanced;
} // end checkBalance
```

```
// Returns true if the given characters, open and close,
//form a pair of parentheses, brackets, or braces.
bool isPaired(char open, char close)
{
    return (open == '(' && close == ')') ||
           (open == '[' && close == ']') ||
           (open == '{' && close == '}');
} // end isPaired
```


Algebraic Expressions

Algebraic Expressions

- **Operator Precedence**

- () Parenthesis
- + Unary
- ^ Exponentiation
- * / % Multiplicative
- + - Additive

- **Binary Operators**

- Require two operands

4 + 5

- **Unary Operators**

- Single operand

-6

- *Infix*

- *Common Notation*

5 + 6

5 + 6 * 7

(5 + 6) * 7

20 - 26 * 8 ^ 3

5 + 6 * 7

5 + 6 * 7

- *Prefix*

- *Functional Languages*

+ 5 6

+ * 7 6 5

* + 5 6 7

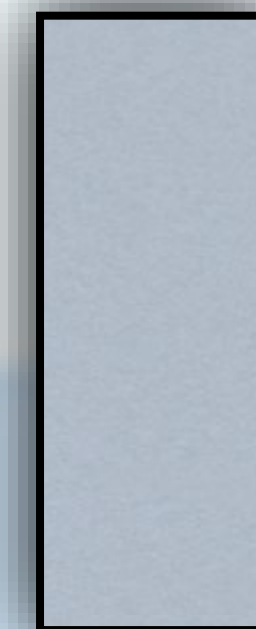
- *Postfix*

- *Reverse Polish Notation*

5 6 +

5 6 7 * +

7 5 6 + *



operatorStack

Evaluating Postfix Expressions

- Scan characters in the Postfix Expression
 - When an *operand* is encountered,
 - **push** it onto the operandStack
 - When an *operator* is encountered,
 - apply it to the top two *operands* of the operandStack
 - **pop** the *operands* from the operandStack
 - **push** the result of the operation onto the operandStack

