

IMA204_TP_DEFMODEL_IMA201_2022-23-STUDENTS

January 7, 2023

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
from IPython.display import HTML
from matplotlib import animation, rc

from skimage.color import rgb2gray
from skimage import data
from skimage.filters import gaussian
from skimage.segmentation import active_contour # For active_contour function

# For active_contour function
from skimage.segmentation import chan_vese, morphological_chan_vese, ↵
    ↵checkerboard_level_set, morphological_geodesic_active_contour

# For some image filtering
from skimage.morphology import white_tophat, black_tophat, disk

import skimage.io

from IPython.core.interactiveshell import InteractiveShell
InteractiveShell.ast_node_interactivity = "all"
```

```
[ ]: def edge_map(img, sigma):
    blur = skimage.filters.gaussian(img, sigma)
    return skimage.filters.sobel(blur)

def edge_map2(img, sigma):
    blur = skimage.filters.gaussian(img, sigma)
    return skimage.filters.scharr(blur)

def subtract_background(image, radius=5, light_bg=False):
    str_el = disk(radius)
    if light_bg:
        return black_tophat(image, str_el)
    else:
        return white_tophat(image, str_el)
```

```

def define_initial_circle(R0,r0,c0,Nber_pts=400):
    # Define initial contour shape
    s      = np.linspace(0, 2*np.pi, Nber_pts)
    Radius = R0
    r      = r0 + Radius*np.sin(s)
    c      = c0 + Radius*np.cos(s) #col
    init   = np.array([r, c]).T
    return init

## Create slides for animation
def animate_cv(image, segs, interval=1000):
    fig, ax = plt.subplots(figsize=(8, 8))
    ax.imshow(image, cmap='gray');
    im = ax.imshow(segs[0], alpha=0.5, cmap='inferno');
    ax.axis('off')

    def init():
        im.set_data(segs[0])
        return [im]

    def animate(i):
        im.set_array(segs[i])
        return [im]

    anim = animation.FuncAnimation(fig, animate, init_func=init,
                                   frames=len(segs), interval=1000, blit=True);
    return anim

def animate_snake(image, segs, interval=500):
    fig, ax = plt.subplots(figsize=(6, 6))
    ax.imshow(image, cmap='gray');
    # im = ax.imshow(segs[0], alpha=0.5, cmap='inferno');
    #ax.plot(segs[0][:, 1], segs[0][:, 0], '--r', lw=3)
    ax.axis('off')
    line, = ax.plot([], [], '-r', lw=2)

    def init():
        line.set_data(segs[0][:, 1], segs[0][:, 0])
        return [line,]

    def animate(i):
        line.set_data(segs[i][:, 1], segs[i][:, 0])
        return [line,]

```

```

anim = animation.FuncAnimation(fig, animate, init_func=init,
                               frames=len(segs), interval=1000, blit=True);

return anim

#####
def store_evolution_in(lst):
    """Returns a callback function to store the evolution of the level sets in
    the given list.
    """

    def _store(x):
        lst.append(np.copy(x))

    return _store

```

1 Read images

This cell reads a series of images that you can then use in various tests. Note that some images are provided with ground-truth masks of structures of interest: 1. OCT_myocardium/case272.tif [one image] 2. images_blood_cells/000016.png [several images available]

```

[ ]: # import warnings
# warnings.filterwarnings( "ignore", module = "matplotlib\.*" )

img_star      = skimage.io.imread('./images_misc/smooth_star.png', as_gray=
    ↪ True)
img_star_noisy = skimage.io.imread('./images_misc/smooth_star_noisy.png',
    ↪ as_gray = True)

img_hela      = skimage.io.imread('./images_misc/hela_big_gt.png', as_gray = True)
edge_hela     = edge_map(img_hela, sigma=2)

img_pepper    = skimage.io.imread('./images_misc/peppers_gt.png', as_gray = True)
edge_pepper   = edge_map(img_pepper, sigma=2)
img_pepper    = img_pepper.astype('float64')

img_MRIB      = skimage.io.imread('./images_misc/MRI_brain_sag.png', as_gray = True)
edge_MRIB     = edge_map(img_MRIB, sigma=2)
img_MRIf      = skimage.io.imread('./images_misc/MRI_fetus.png', as_gray = True)
edge_MRIf     = edge_map(img_MRIf, sigma=2)

img_cell      = skimage.io.imread('./images_blood_cells/000016.png', as_gray = True)
edge_cell     = edge_map(img_cell, sigma=2)

```

```

#skimage.io.imshow(img_cell)

img_mask = skimage.io.imread('./masks_blood_cells/000016.png', as_gray = True)
edge_mask = edge_map(img_mask, sigma=2)
# skimage.io.imshow(img_mask)

img_OCT = skimage.io.imread('./OCT_myocardium/case272.tif', as_gray = True)
edge_OCT = edge_map(img_OCT, sigma=2)
labels_OCT = skimage.io.imread('./OCT_myocardium/case272_label.tiff', as_gray = True)

img_nodule = skimage.io.imread('./thyroid_nodule/1074.png', as_gray = True)
edge_nodule = edge_map(img_nodule, sigma=2)
labels_nodule = skimage.io.imread('./thyroid_nodule/1074_mask.png', as_gray = True)

fig, axes = plt.subplots(4,4, figsize=(16, 8))
ax = axes.ravel()
ax[0].imshow(img_cell, cmap=plt.cm.gray);
ax[1].imshow(edge_cell, cmap=plt.cm.gray);
ax[2].imshow(img_mask, cmap=plt.cm.gray);
ax[3].imshow(edge_mask, cmap=plt.cm.gray);
ax[4].imshow(img_pepper, cmap=plt.cm.gray);
ax[5].imshow(edge_pepper, cmap=plt.cm.gray);
ax[6].imshow(img_MRIB, cmap=plt.cm.gray);
ax[7].imshow(edge_MRIB, cmap=plt.cm.gray);
ax[8].imshow(img_MRIF, cmap=plt.cm.gray);
ax[9].imshow(edge_MRIF, cmap=plt.cm.gray);
ax[10].imshow(img_OCT, cmap=plt.cm.gray);
ax[11].imshow(edge_OCT, cmap=plt.cm.gray);
ax[12].imshow(labels_OCT, cmap=plt.cm.gray);
ax[13].imshow(img_nodule, cmap=plt.cm.gray);
ax[14].imshow(edge_nodule, cmap=plt.cm.gray);
ax[15].imshow(labels_nodule, cmap=plt.cm.gray);

```

2 Image properties:

2.1 Range of values and data type matter ...

Some routines won't work if your image type is int8 or uint8... Here is how to check your image data type

And regularly check your image content in terms of: * intensities range of values * distributions of intensities via its histogram

```
[ ]: img_test = img_cell
Sigma_val = 1
edge_test = edge_map(img_test, sigma=Sigma_val)

## Print some basic image properties
print(img_test.dtype)
print(np.min(img_test))
print(np.max(img_pepper))

## Show Hist
hist_test, bins_test = np.histogram(img_test.flatten(), bins=256)
hist_edge_test, bins_edges_test = np.histogram(edge_test.flatten(), bins=256)

fig, axes = plt.subplots(2,2, figsize=(4, 4))
ax = axes.ravel()
ax[0].imshow(img_test, cmap=plt.cm.gray);
ax[0].set_title("Original Im", fontsize=6);
ax[1].plot(bins_test[0:-1], hist_test);
ax[1].set_title("Hist Im", fontsize=6);
ax[2].imshow(edge_test, cmap=plt.cm.gray);
ax[2].set_title("Edge Map Im", fontsize=6);
ax[3].plot(bins_edges_test[0:-1], hist_edge_test);
ax[3].set_title("Hist Edge map", fontsize=6);
fig.tight_layout()
plt.show();
```

3 Edge maps

Deformable models rely on edge maps. Most routines have their own strategy coded to compute the edge map.

- Edge maps usually involve smoothing of the image, to be robust to noise. Make sure you understand how this is controlled in the routine you use.
- Edge maps usually show pixels with high gradient magnitudes in white (high values)
- Most deformable model routines can be fed directly with an Edge Map rather than the original image as its input
- Some routine expect to be fed with an inverse edge map where high gradient locations have small values, to stop the contour via a velocity set to ~zero.

```
[ ]: img_to_test = img_pepper

# Classic Edge map with Gaussian smoothing controled by sigma
edge_test1 = edge_map(img_to_test, sigma=1)
edge_test1_l = np.log2(edge_test1)
edge_test2 = edge_map(img_to_test, sigma=2)
```

```

edge_test2_1      = np.log2(edge_test2)

# Inversed Edge map
# Returns Edge map = 1.0 / np.sqrt(1.0 + alpha * gradnorm)
edge_inv_test     = skimage.segmentation.inverse_gaussian_gradient(img_to_test,
    ↪alpha=1.0, sigma=1.0)

fig, axes = plt.subplots(2,3, figsize=(6, 6))
ax = axes.ravel()

ax[0].imshow(img_to_test, cmap=plt.cm.gray);
ax[1].imshow(edge_inv_test, cmap=plt.cm.gray);
ax[1].set_title("Edge map inversed", fontsize=6);
ax[2].imshow(edge_test1, cmap=plt.cm.gray);
ax[2].set_title("Edge map sigma = 1", fontsize=6);
ax[3].imshow(edge_test2, cmap=plt.cm.gray);
ax[3].set_title("Edge map sigma = 2", fontsize=6);
ax[4].imshow(edge_test1_1, cmap=plt.cm.gray);
ax[4].set_title("Log Edge map sigma = 1", fontsize=6);
ax[5].imshow(edge_test2_1, cmap=plt.cm.gray);
ax[5].set_title("Log Edge map sigma = 2", fontsize=6);

for i in range(0,6):
    ax[i].set_xticks([]), ax[i].set_yticks([]);

fig.tight_layout()
plt.show();

```

4 Test some image manipulations

Let you test some image transformations based on morphological operators and histogram manipulation. When transforming image contrast, it is always interesting to look at the differences between the original image and the transformed version.

```

[ ]: img_ori_to_test = img_cell
img_to_test         = img_ori_to_test

PRE_ENHANCE         = 1
OPTION_ENHANCE      = 0 # can be 0 (nothing) to 4

# Run all OPTION_ENHANCE for display here
gamma_corrected      = skimage.exposure.adjust_gamma(img_to_test, 2)
logarithmic_corrected = skimage.exposure.adjust_log(img_to_test, gain=
    ↪1, inv=True)

```

```

img_open          = skimage.morphology.diameter_opening(img_to_test, 40,
↳connectivity=2)
img_adapteq       = skimage.exposure.equalize_adapthist(img_to_test,
↳clip_limit=0.03)

# PRE ENHANCEMENT OPTIONS:
if PRE_ENHANCE==1:
    if OPTION_ENHANCE==1:
        # Gamma
        img_to_test = gamma_corrected
    elif OPTION_ENHANCE==2:
        # Logarithmic (O = gain*log(1 + I)) or if Inv (O = gain*(2**I - 1))
        img_to_test = logarithmic_corrected
    elif OPTION_ENHANCE==3:
        # Morpho Opening
        img_to_test = img_open
elif OPTION_ENHANCE==4:
    # Contrast Limited Adaptive Histogram Equalization (CLAHE).
    img_to_test = img_adapteq

# Enhance details either dark around light background of vice versa with the
↳Top-Hat transform
Radius_val = 5
img_test1 = subtract_background(img_to_test, radius=Radius_val, light_bg=False)
img_test2 = subtract_background(img_to_test, radius=Radius_val, light_bg=True)

# SHOW OUTPUTS
fig, axes = plt.subplots(2,5, figsize=(10, 4),constrained_layout=True)
ax        = axes.ravel()
Shrink_factor_colormap = 0.5
ax[0].imshow(img_ori_to_test, cmap=plt.cm.gray);
ax[0].set_title("Ori", fontsize=6);

ax[1].imshow(img_open, cmap=plt.cm.gray);
ax[1].set_title("Opening", fontsize=6);
ax[2].imshow(gamma_corrected, cmap=plt.cm.gray);
ax[2].set_title("Gamma correction", fontsize=6);
ax[3].imshow(logarithmic_corrected, cmap=plt.cm.gray);
ax[3].set_title("Log correction", fontsize=6);
ax[4].imshow(img_adapteq, cmap=plt.cm.gray);
ax[4].set_title("Adapt Hist Eq", fontsize=6);

ax[5].imshow(img_test1, cmap=plt.cm.gray);
ax[5].set_title("Tophat Dark bkg", fontsize=6);
ax[6].imshow(img_test2, cmap=plt.cm.gray);
ax[6].set_title("Tophat Light bkg", fontsize=6);

```

```

tmp_show = ax[7].imshow(img_to_test-img_test2, cmap=plt.cm.gray);
ax[7].set_title("Diff: (Ori-Light bkg)", fontsize=6);
plt.colorbar(tmp_show,ax=ax[7], shrink=Shrink_factor_colormap, location='right')

tmp_show = ax[8].imshow(abs(img_to_test-img_test2), cmap=plt.cm.gray);
ax[8].set_title("Diff: abs(Ori-Light bkg)", fontsize=6);
plt.colorbar(tmp_show,ax=ax[8], shrink=Shrink_factor_colormap, location='right')

tmp_show = ax[9].imshow(np.log2(abs(img_to_test-img_test2)), cmap=plt.cm.gray);
ax[9].set_title("Diff: log(abs(Ori-Light bkg))", fontsize=6);
plt.colorbar(tmp_show,ax=ax[9], shrink=Shrink_factor_colormap, location='right')

#fig.tight_layout() # not compatible with option constrained_layout=True in plt.
#↳subplots needed to display the colorbar
plt.show();

```

5 Seg #1:

5.0.1 Snake on a binary shape

Based on the routine **active_contour** from skimage. Default **parameter values** are: * $\alpha=0.01$ (Snake length shape parameter. Higher values makes snake contract faster.) * $\beta=0.1$ (Snake smoothness shape parameter. Higher values makes snake smoother.) * $\gamma=0.01$ (Explicit time stepping parameter - Equivalent to the viscosity of the environment) * $\max_px_move=1.0$

There are two **other parameters** that define the final image information used to define external forces used to define regions. $img = w_line \times img + w_edge \times edge$: * $w_line_val=0$ (default) | $=1$ if want to input img directly. Use negative values to attract toward dark * $w_edge_val=1$ (default) | $=0$ if do not want to use internal edge map. Use negative values to repel snake from edges

5.1 TODO:

1. Run the cell for **img_to_seg=img_mask** with the sets of parameter values provided. 1st set uses values by default, 2nd-3rd sets use custom values to help improve the smoothness of the final contour.
 1. Comment on defaults seen on the obtained initial segmentations.
 2. Explain why you think increasing the γ_val has better helped smooth the final contour.
2. Test now by using a small initial circle inside the white shape. What is happening and what additional force seen in the class could help fixing this issue?
3. Now run the segmentation on the **img_to_seg=img_star** or **img_to_seg=img_star_noisy**. Try the same parameter values adjustments as before to get a smoother final contour. Comment on the issues observed with the two options.

4. BONUS: there is a way to obtain a “perfect” segmentation for the star shape. Propose one solution which might involve many more iterations, once you have checked with few iterations that behavior is stable.

```
[ ]: # 1ST image
img_to_seg=img_mask; r0 = 130; c0=125; R0 = 60
alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01; convergence_val = 1e-4;
    ↪ Niter_snake = 800;
#alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.1; convergence_val = 1e-4;
    ↪ Niter_snake = 800;
#alpha_val = 0.01 ; beta_val = 1; gamma_val = 0.01; convergence_val = 1e-4;
    ↪ Niter_snake = 800;

# 2ND image
#img_to_seg = img_star ; r0 = 64; c0=64; R0 = 50
#img_to_seg = img_star_noisy ; r0 = 64; c0=64; R0 = 50
#alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.01; convergence_val = 1e-4;
    ↪ Niter_snake = 800;

# Initialise contour
init = define_initial_circle(R0,r0,c0)

# Pre-smooth the image
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Run active contour
snake10 = active_contour(img_to_seg,
                        init, max_num_iter=10, convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)
snake_max = active_contour(img_to_seg,
                        init, max_num_iter=Niter_snake,
    ↪ convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)

# Display results
fig, ax = plt.subplots(figsize=(6, 6));
ax.imshow(img_to_seg, cmap=plt.cm.gray);
ax.plot(init[:, 1], init[:, 0], '--y', lw=1);
ax.plot(snake10[:, 1], snake10[:, 0], '-g', lw=1);
ax.plot(snake_max[:, 1], snake_max[:, 0], '-r', lw=2);
ax.set_xticks([]), ax.set_yticks([]);
ax.axis([0, img_to_seg.shape[1], img_to_seg.shape[0], 0]);

plt.show();
```

6 Seg #2:

6.0.1 Snake on a real image

We are using here `img_to_seg = img_cell` for which you have a ground truth mask of the target segmentation for the dark cell.

6.1 TODO

1. Segment left cell:

1. Run with the proposed initialisation and see that the active contour can be initialised inside the object. Give some intuition on why.

2. Segment right cell:

1. Run with the proposed initialisation and see that the active contour cannot be initialised inside the object now. Give some intuition on why.
 2. Change the parameter **Niter_smooth** while keeping snake parameters constant and give an intuition on why the final contour evolves as seen.
 3. Change the initial contour parameters to obtain a perfect segmentation.
3. BONUS: If you know that you are aiming for the darkest cell in the image, propose an automated initialisation of the initial active contour parameters `[r0 ; c0; R0]` that works on this image.

```
[ ]: # Input image and parameter values
img_to_seg = img_cell;

# 1st SEG: To segment left cell
# r0 = 150; c0=50; R0 = 30
# alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01; convergence_val = 1e-4;
↳ Niter_snake = 200;

# 2nd SEG: To segment center dark cell
r0 = 130; c0=120; R0 = 30
alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 800;

# Pre smooth the image
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Initialise contour
init = define_initial_circle(R0,r0,c0)

# Run active contour
snake30 = active_contour(img_to_seg,
                        init, max_num_iter=30, convergence=convergence_val,
```

```

        alpha=alpha_val, beta=beta_val, gamma=gamma_val)
snake = active_contour(img_to_seg,
                        init, max_num_iter=Niter_snake,
                        ↪convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)

# Display results
fig, ax = plt.subplots(figsize=(6, 6))
ax.imshow(img_to_seg, cmap=plt.cm.gray)
ax.plot(init[:, 1], init[:, 0], '--y', lw=1)
ax.plot(snake30[:, 1], snake30[:, 0], '-b', lw=1.5)
ax.plot(snake[:, 1], snake[:, 0], '-r', lw=2)
ax.set_xticks([]), ax.set_yticks([])
ax.axis([0, img_to_seg.shape[1], img_to_seg.shape[0], 0])

plt.show();

```

7 Seg # 3

7.0.1 A tool to visualise the deformations of the snake

7.1 TO DO:

1. Segment left cell:

1. Provide your comments on the deformation pattern of the snake.
2. Why iteration time steps get slower over iterations when initialising from the inside?

2. Segment right cell:

1. Use your optimal parameters from previous cell and comment on the deformation patterns.

```

[ ]: img_to_seg      = img_cell

# 1st SEG: To segment left cell
r0 = 150; c0=50; R0 = 30
alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01; convergence_val = 1e-4;
↪Niter_snake = 200;

# 2nd SEG: To segment center dark cell
#r0 = 130; c0=120; R0 = 30 # initialise inside
#alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01; convergence_val = 1e-4;
↪Niter_snake = 200;

# Pre smooth the image
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Initialise contour

```

```

init = define_initial_circle(R0,r0,c0)

# Run active contour while saving intermediate contours to see deformations
segs = []
print('start')
for i in range(1,Niter_snake,10):
    print(i, " ", end='')
    segs.append(active_contour(img_to_seg, init, max_num_iter=i,
↪convergence=convergence_val,
        alpha=alpha_val, beta=beta_val, gamma=gamma_val))

print('stop')
np.save('ANIM_contours.npy', np.array(segs))

# display animation
segs = np.load('ANIM_contours.npy')
anim = animate_snake(img_to_seg, segs);
HTML(anim.to_html5_video())

```

8 Seg # 4

8.0.1 Snake with Gradient Vector Flow (GVF)

This implementation of the GVF is performed by computing the edge map, diffusing the gradient over the whole image and directly input the GVF_edge_map to be used as external forces by setting `w_line=1` and `w_edge=0` in the `active_contour` function.

8.1 TODO:

1. Compare results when segmenting the Edge_map or GVF_map as input to the `active_contour` routine on 3 images: `img_star`, `img_star_noisy` and an image of your choice. Comment on robustness and speed differences.
2. When using GVF_map, test the effect of decreasing by a factor of 10 `alpha`, `beta` or `gamma` and interpret the effect.

```

[ ]: import gvf_elsa2
from gvf_elsa2 import gradient_field, gradient_vector_flow

# Image to seg
img_to_seg = img_star
r0 = 64; c0=64; R0 = 50

# Example of another image to test.
# NB: play with regularisation parameter mu for gradient_vector_flow on real
↪images

```

```

# img_to_seg          = img_cell
# r0 = 130; c0=120; R0 = 50 # initialise inside

alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 200;

# Initialise contour
init          = define_initial_circle(R0,r0,c0,Nber_pts=400)

# Compute edge map and gvf
img_to_seg = img_to_seg.astype(np.float32) / np.max(img_to_seg)
Edge_map    = edge_map(img_to_seg,sigma=1)

fx, fy = gradient_field(Edge_map)
gx, gy = gradient_vector_flow(fx, fy, mu=5)
GVF_map = np.sqrt(gx**2 + gy**2)

# Run active contour while saving intermediate contours to see deformations
Map_to_seg = Edge_map

# Run active contour while saving intermediate contours to see deformations
segs = []
print('start')
for i in range(1,Niter_snake,10):
    print(i, " ", end='')
    segs.append(active_contour(Map_to_seg, init, max_num_iter=i,
    ↪convergence=convergence_val,
        alpha=alpha_val, beta=beta_val, gamma=gamma_val,
        w_line=1,w_edge=0))

print('stop')
np.save('ANIM_contours.npy', np.array(segs))

# display animation
segs = np.load('ANIM_contours.npy')
anim = animate_snake(Map_to_seg, segs);
HTML(anim.to_html5_video())

```

9 Seg # 5:

9.0.1 The active contour with fixed end points

You will now run the `active_contour` with the option to maintain some points from the initial contour fixed. You are working now with the `img_nodule` which is an ultrasound showing different layers of tissue under the skin surface.

9.1 TO DO:

- Write a loop to vary the initial line vertical position by few pixels and propose a method to aggregate final contours, like for example a probability edge map.
- BONUS: Propose and implement a metric to measure the “quality” of the segmented contour, as being representative of the “interface” between two tissues.

```
[ ]: img_to_seg = img_nodule
r_left = 170; r_right=170; c_left=0; c_right = 780
#r_left = 200; r_right=190; c_left=0; c_right = 780
#r_left = 230; r_right=210; c_left=0; c_right = 780

alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 500;
w_line_val=0; w_edge_val=1

# Pre smooth the image
img_to_seg = skimage.exposure.equalize_adapthist(img_to_seg, clip_limit=0.03)
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Initialise contour
Nber_pts_contour = 300
r = np.linspace(r_left, r_right, Nber_pts_contour)
c = np.linspace(c_left, c_right, Nber_pts_contour)
init = np.array([r, c]).T

snake = active_contour(img_to_seg,
                       init,
                       ↪boundary_condition='fixed-fixed', max_num_iter=Niter_snake,
                       alpha=alpha_val, beta=beta_val, gamma=gamma_val,
                       w_line=w_line_val, w_edge=w_edge_val)

fig, ax = plt.subplots(figsize=(9, 5));
ax.imshow(img_to_seg[0:500,:], cmap=plt.cm.gray);
ax.plot(init[:, 1], init[:, 0], '--y', lw=2);
ax.plot(snake[:, 1], snake[:, 0], '-r', lw=3);
ax.set_xticks([]), ax.set_yticks([]);
ax.set(xlim=(0, 500));
plt.show();
```

10 Seg # 6

10.0.1 Your turn on proposing a motivated pipeline using the snake capabilities from the `active_contour` function

10.1 TODO:

Choose a new image in the pool provided and propose a segmentation pipeline using the `active_contour` approach. Options on points to work on include: * Pre filter the image as you wish * Manually or automatically position the initial contour * Provide one segmentation result or merge several solutions in a probability map * Detect issues in contour shape during deformations and propose an early stop criteria.

11 Seg #7

11.0.1 Test on the Geometric Level-Set formulation using the Chan-Vese model.

Skimage provides two implementations of the Chan-Vese approach: `morphological_chan_vese` and `chan_vese`.

The contours of objects are now encoded in a level set function **Phi**.

The **initialisation** tested here is with a “checkerboard” pattern for 2 classes (object and background).

For the `chan_vese` original implementation, the **hyper-parameters** include: * $\mu = 0.25$ (default) | edge regularisation terms. Similar to ‘edge length’ weight parameter. Higher μ values will produce ‘smoother’ contours. * $dt = 0.5$ (default) | delta time step for each optimisation step. * $\lambda_1=1, \lambda_2=1$ (default) | weights in the cost metric to balance inside and outside homogeneity terms. * $tol=1e-3$ (default) | Tolerance to test if the contours are “stable” and stop early.

The output contains: `cv[0]=Seg` and `cv[1]=Phi`

For the `morphological_chan_vese` implementation, the only **hyper-parameter** is the number of smoothing iterations (1 to 4 recommended).

11.1 TO DO:

1. C-V ori: Run the code on `img_hela`. Visualise and explain evolution of **Phi** over first iterations. Figure out how to see the initial **Phi** configuration.
2. Run now on `img_cell` without and with pre-processing with histogram equalisation and explain difference in results.
3. Propose and implement method(s) and metrics to compare two segmentation results when handling segmentation masks. Use the one(s) implemented to quantify the differences obtained on one test case of your choice with the two implementations of chan-vese provided here.
4. Make the level set work when initialising with “disk” on `img_MRIf`

```
[ ]: img_to_seg= img_hela  
  
# PARAMETERS
```

```

mu_val=0.5 ; lambda1_val=1; lambda2_val=1; tol_val=1e-3; dt_val=0.5
smoothing_val = 3

Num_iter_cv_ori    = 100
Num_iter_cv_fast   = 1

CHAN_VESE_ORI     = 1
Init_method       = "checkerboard" # "checkerboard" or "disk" or "small disk"
    ↪ (alternative to use to set init_level_set)

# run segmentation
if CHAN_VESE_ORI == 1:
    # STANDARD implementation from original paper
    init_ls = checkerboard_level_set(img_to_seg.shape, 45)

    cv = chan_vese(img_to_seg, mu=mu_val, lambda1=lambda1_val,
    ↪ lambda2=lambda2_val,
                    tol=tol_val, dt=dt_val,
                    max_num_iter=Num_iter_cv_ori, init_level_set=Init_method,
                    extended_output=True)

    fig, ax = plt.subplots(1,2,figsize=(7, 7))
    ax[0].imshow(img_to_seg, cmap=plt.cm.gray)
    ax[1].imshow(1-cv[0], cmap=plt.cm.gray)
    title = f'C-V with - {len(cv[2])} iterations'
    ax[1].set_title(title, fontsize=12)

else:
    # FASTER implementation implemented with morphological operators BUT LESS
    ↪ PRECISE
    cv      = morphological_chan_vese(img_to_seg, num_iter=Num_iter_cv_fast,
    ↪ smoothing=smoothing_val,
    ↪ init_level_set="checkerboard")

    fig, ax = plt.subplots(1,2,figsize=(7, 7))
    ax[0].imshow(img_to_seg, cmap=plt.cm.gray)
    ax[1].imshow(1-cv, cmap=plt.cm.gray)
    title = f'C-V_morph with - {Num_iter_cv_fast} iterations'
    ax[1].set_title(title, fontsize=12)

plt.show();

```


12 Seg # 8

12.1 Geometric active contours with balloon force

You are now also provided with a tool to track the deformation patterns of the active contour over iterations.

The geometric active contour routine is **morphological_geodesic_active_contour** which deforms a level set function with local speed values. It has the following **hyper-parameters** : * Thresh_cont_val = 'auto'=> np.percentile(image, 40) (default if 'auto') | pixels < Thresh_cont_val are considered borders. The evolution of the contour will stop on these pixels. Threshold_mask_balloon = image > threshold / np.abs(Balloon_weight) * Balloon_weight = 1 (default) | weight of the balloon force. Can be negative to inflate/deflate * Smooth_cont_iter = 1 (default) | Number of times a smoothing operator is applied per iteration

13 TO DO:

- Segment the img_cell with the provided configuration in line 1 to inflate the initial contour. What is the issue?
- Now Segment the img_cell with the provided configuration in line 2 to deflate the initial contour. Adjust balloon parameter accordingly. Fix the issues observed to get a perfect segmentation in 30 iterations.
- Segment the img_MRIB image with the configuration in line 3 set to inflate an initial contour. Comment issues seen with high and low smoothness regularisation over 300 iterations.
- Now propose and run a setup to attempt to segment the gray matter contours in img_MRIB or some structure in another image. Comment on your choice of parameters, number of iterations and observed quality of contours.

```
[ ]: img_to_seg = img_cell ; r0 = 130; c0 = 125 ; R0 = 30 # inflate
#img_to_seg = img_cell ; r0 = 130; c0 = 125 ; R0 = 70 # deflate
#img_to_seg = img_MRIB ; r0 = 500 ; c0 = 530 ; R0 = 30 # for spine and inflate

SMOOTHING      = 0; Niter_smooth = 3
INV_EDGE_MAP = 1; # needed when using the Balloon force

img_ori      = img_to_seg

# Hyper parameters for snake and balloon
Thresh_cont_val = 'auto' ; Balloon_weight = 1 ; Smooth_cont_iter = 1 ;
Niter_snake      = 100

# smoothing
if SMOOTHING:
    img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Test segment directly on edge image [QUESTION: WHY IS THE RESULT DIFFERENT?]
```

```

if INV_EDGE_MAP:
    img_to_seg = skimage.segmentation.inverse_gaussian_gradient(img_to_seg) #
    ↪ Compute the magnitude of the gradients in the image and then inverts the
    ↪ result in the range [0, 1]

# Print threshold used by "auto"
print(np.percentile(img_to_seg, 40))

# initialise call back
evolution = []
callback = store_evolution_in(evolution)

# Initialise contour
init_ls = skimage.segmentation.disk_level_set(img_to_seg.shape,
    ↪ center=[r0,c0], radius=R0)

# Run geodesic active contour
ls = morphological_geodesic_active_contour(
    img_to_seg, Niter_snake, init_ls,
    smoothing=Smooth_cont_iter, balloon=Balloon_weight,
    threshold=Thresh_cont_val,
    iter_callback=callback);

fig, axes = plt.subplots(2, 2, figsize=(8, 8));
ax = axes.flatten();

ax[0].imshow(img_ori, cmap="gray");
ax[0].set_axis_off();
ax[0].contour(ls, [0.5], colors='r');
ax[0].set_title("Morphological GAC segmentation", fontsize=12);

ax[1].imshow(img_to_seg, cmap="gray");
ax[1].set_axis_off();
ax[1].contour(ls, [0.5], colors='r');
ax[1].set_title("Morphological GAC segmentation", fontsize=12);

ax[2].imshow(ls, cmap="gray");
ax[2].set_axis_off();
contour = ax[2].contour(evolution[0], [0.5], colors='r');
contour.collections[0].set_label("Contours");
title = f'Morphological GAC Curve evolution';
ax[2].set_title(title, fontsize=12);
for i in range(1, Niter_snake-1, 5):
    contour = ax[2].contour(evolution[i], [0.01], linewidths=0.5, colors='y');

```

```
plt.show();
```

```
[ ]:
```