

Introduction to Arrays

The first step to achieving your goal, is to take a moment to respect your goal. Know what it means to you to achieve it.

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Good
Evening

Today's content

01. Reverse the array & subarray
- 02 Range sum queries
03. Equilibrium Index
04. Maximum subarray sum of size k
05. Sum of all subarray sum (Google)

Q1. Given an array, Reverse the entire array

Note:- Change the given array

S.C = O(1)

arr[] = {⁰1, ¹2, ²3, ³4, ⁴5, ⁵6, ⁶7, ⁷8}
 ↑ ↑
 j i

i < j

arr[] = {8, 7, 6, 5, 4, 3, 2, 1}

Breaking point
 $i > j$

arr[] = {⁰1, ¹2, ²3, ³4, ⁴5}
 ↑ ↑
 i j

Breaking point
 $i == j$

arr[] = {5, 4, 3, 2, 1}

void reverse (int arr[])

$i = 0, j = N - 1$

while ($i < j$)

 swap (arr, i, j);

 i++;

 j--;

3

No. of iterations = $N/2$

TC: $O(N)$

SC: $O(1)$

02. Given the array of N elements. Reverse the subarr from s_i to e_i .

↳ Continuous part of arr

↳ Complete arr

↳ Single ele

$$arr[] = \{ 1, 2, 3, 4, 5, 6, 7, 8 \}$$

$$s_i = 2$$

$$e_i = 7$$

$$arr[] = \{ 1, 2, 8, 7, 6, 5, 4, 3 \}$$

```
void reverse ( int [] arr, int si, int ei){
```

```
    i = si, j = ei
```

```
    while (i < j)
```

```
        swap (arr, i, j);
```

```
        i++;
```

```
        j--;
```

TC: $O(n)$

SC: $O(1)$

01. Given arr[N] elements & Q queries

For each query : Given L & R calculate & print sum of elements in range [L R] , L & R both included

Note :- L & R are array indices such that $0 \leq L \leq R \leq N$

arr[10] =

-3	6	2	4	5	2	8	-9	3	1
0	1	2	3	4	5	6	7	8	9

pf[] =

-3	3	5	9	14	16	24	15	18	19
0	1	2	3	4	5	6	7	8	9

Queries = 5

L	R
4	8
3	7
1	3
0	4
7	7

Constraints = $1 \leq N \leq 10^3$
 $1 \leq Q \leq N$

$$= 9$$

$$= 10$$

$$= 12$$

$$= 14$$

$$= -9 \rightarrow pf[7] - pf[6] = 15 - 24 = \underline{\underline{-9}}$$

BF = For every query, iterate from L to R & print the sum.

TC: $O(Q * N)$

SC: $O(1)$

Q : Given Indian Cricket Team score , for first 10 overs of Batting .

After every over , total score is given as :

overs →	1	2	3	4	5	6	7	8	9	10
---------	---	---	---	---	---	---	---	---	---	----

sc[10] →	2	8	14	29	31	49	65	79	88	97
----------	---	---	----	----	----	----	----	----	----	----

Q1. Runs scored in 10th over =

Runs scored till 9th over + Runs scored in 10th over = Runs scored in 10 overs

$$sc[9] + x = sc[10]$$

$$\begin{aligned}x &= sc[10] - sc[9] \\&= 97 - 88 = 9\end{aligned}$$

Q2 Runs scored from 6th to 10th over

$$sc[10] - sc[5] = 97 - 31 = 66$$

03. Runs scored from 3rd over to 8th over =

$$sc[8] - sc[2] = 79 - 8 = 71$$

Total no. of runs i to j = $sc[j] - sc[i-1]$

04. Runs scored till 5th over = $sc[5]$

Total no. of runs scored from 0 to j = $sc[j]$

Generic formula

$$\begin{cases} i=0 & ans = psum[j] \\ \text{else} & ans = psum[j] - psum[i-1]; \end{cases}$$

arr =	4	6	3	-2	8
	0	1	2	3	4

psum =	4	10	13	11	19
--------	---	----	----	----	----

$\hookrightarrow sum[0-2]$

$$psum[0] = arr[0]$$

$$psum[1] = \underbrace{arr[0]}_{psum[0]} + arr[1]$$

$$psum[2] = \underbrace{ar[0] + ar[1]}_{psum[1]} + ar[2]$$

$$psum[3] = \underbrace{ar[0] + ar[1] + ar[2]}_{psum[2]} + ar[3]$$

if ($i == 0$) $psum[0] = ar[0]$:

else {

\downarrow $psum[i] = psum[i-1] + ar[i]$:

* Construct pf array

$$pf[0] = ar[0]$$

for ($i=1$; $i < n$; $i++$) {

\downarrow $psum[i] = psum[i-1] + ar[i]$:

}

$O(n)$

TC: $O(N+Q)$

SC: $O(N)$

* Answer all queries

for ($i=0$; $i < Q$; $i++$) {

\downarrow $s = L[i]$, $e = R[i]$

\downarrow if ($s == 0$) $\text{print}(psum[e])$;

\downarrow else $\text{print}(psum[e] - psum[s-1])$;

}

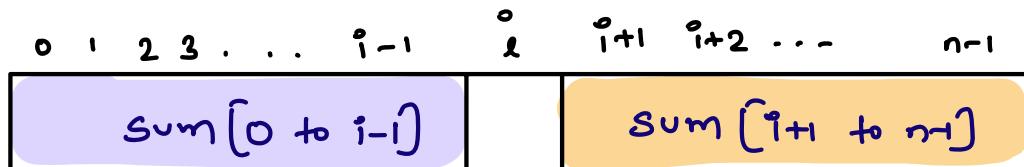
$O(Q)$

Q. Equilibrium Index

Given N array elements, count no. of equilibrium idx

An idx i is known as eqm idx

$$\text{sum of all elements before } i \text{ idx} = \text{sum of all elements after } i \text{ idx}$$



Note:- if ($i == 0$) leftsum = 0

if ($i == N-1$) righsum = 0

$ar[4] = \{ -3 \quad 2 \quad 4 \quad -1 \}$	$count = 1$
$lsum = 0 \quad -3 \quad -1 \quad 3$	
$rsum = 5 \quad 3 \quad -1 \quad 0$	

$ar[7] = \{ -7 \quad 1 \quad 5 \quad 2 \quad 3 \quad -4 \quad 3 \quad 6 \quad 0 \}$	$count = 2$
$lsum = 0 \quad -7 \quad -6 \quad -1 \quad 1 \quad -3 \quad 0$	
$rsum = 7 \quad 6 \quad 1 \quad -1 \quad 3 \quad 0 \quad 0$	

Brute force → For every index, iterate & calculate lsum & rsum. If ($lsum == rsum$) $c=c+1$;
return count:

$$TC = O(n^2)$$

$$SC = O(1)$$

Optimised step

Code → {TODO}

01. Create a pfsum array

02. For every index,

→ calculate lsum using pfsum array

→ calculate rsum using pfsum array

→ if ($lsum == rsum$)

 → $c = c + 1$

}

return c;

Q1. Given N elements, print max subarray sum of length ' k '.

$\text{arr}[10] =$	<table border="1"> <tr> <td>-3</td><td>4</td><td>-2</td><td>5</td><td>3</td><td>-2</td><td>8</td><td>2</td><td>-1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td> </tr> </table>	-3	4	-2	5	3	-2	8	2	-1	4	0	1	2	3	4	5	6	7	8	9	$k=5$
-3	4	-2	5	3	-2	8	2	-1	4													
0	1	2	3	4	5	6	7	8	9													

st end sum

0 4 7

1 5 8

2 6 12

3 7 16

4 8 10

5 9 11

Idea 1 \rightarrow For every subarr of size k , iterate & calculate the sum and update the max accordingly

TC : #subarr of size k * K

$$= O(n-k+1) * k$$

$$k=1 \rightarrow TC: O(n)$$

$$k=n \rightarrow TC: O(n)$$

$$k=\frac{n}{2} \rightarrow O(n-\frac{n}{2}+1) * \frac{n}{2}$$

$$= O(\frac{n}{2}+1) * \frac{n}{2}$$

$$\approx O(n^2)$$

<table border="1"> <tr> <td></td><td></td><td></td><td></td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td> </tr> </table>					0	1	2	3
0	1	2	3					

$$\boxed{n-k+1}$$

$$k=1 \quad \text{Ans} = 4$$

$$k=2 \quad \text{Ans} = 3$$

$$k=3 \quad \text{Ans} = 2$$

$$k=4 \quad \text{Ans} = 1$$

TC: $O(n^2)$

SC: $O(1)$

Use psum approach \longrightarrow

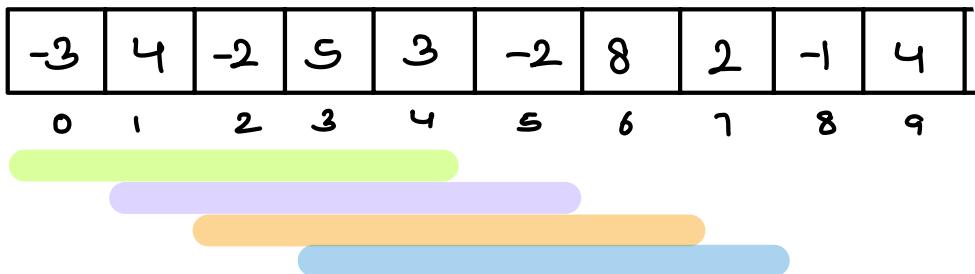
TC: $O(n)$

SC: $O(n)$

Idea 3 \rightarrow Sliding Window

TC: $O(n)$ SC: $O(1)$

$ar[10] =$



K=5

st end sum

0 4 7

1 5 $sum = sum - ar[0] + ar[5] = 8$

2 6 $sum = 8 - ar[1] + ar[6] = 12$

3 7 $sum = 12 - ar[2] + ar[7] = 16$

4 8 sum \rightarrow

5 9 sum \rightarrow

```
int maxsubarraysum ( int [] ar , int k )
```

ans = -∞ . sum = 0

```
for( i=0 ; i<k ; i++ ) {
```

sum = sum + ar[i]

}

$\left. \right\} K \text{ iterations}$

1 window

```
ans = max( ans , sum ) .
```

s = 1 , e = k

```
while ( e < n )
```

sum = sum - ar[s-1] + ar[e]

ans = max(ans , sum) .

s = s + 1 ;

e = e + 1 ;

}

$\left. \right\} (n-k) \text{ iteration}$

$$TC = O(k + n - k) \approx O(n)$$

$$SC = O(1)$$

Q Given an $ar[n]$, return sum of all subarr sums.

$$ar[4] : \{ \underset{0}{6}, \underset{1}{8}, \underset{2}{-1}, \underset{3}{7} \}$$

Ans = 94

<u>subarr</u>		<u>sum</u>	
[0 0]	$\rightarrow 6$	6	$6 * 4 = 24$
[0 1]	$\rightarrow 6 + 8$	14	$8 * 6 = 48$
[0 2]	$\rightarrow 6 + 8 + (-1)$	13	$-1 * 6 = -6$
[0 3]	$\rightarrow 6 + 8 + (-1) + 7$	20	$7 * 4 = 28$
[1 1]	$\rightarrow 8$	8	
[1 2]	$\rightarrow 8 + (-1)$	7	
[1 3]	$\rightarrow 8 + (-1) + 7$	14	
[2 2]	$\rightarrow (-1)$	-1	
[2 3]	$\rightarrow -1 + 7$	6	
[3 3]	$\rightarrow 7$	7	

Ideal \rightarrow for every subarr, iterate & get the sum \rightarrow add it to the total sum

for ($i=0 \rightarrow n-1$)

 for ($j=i \rightarrow n-1$)

 sum = 0;

 for ($k=i \rightarrow j$) {

 sum += arr[k];

 }

 totalSum += sum;

 3

TC: $O(n^3)$

SC: $O(1)$

* Psum approach \rightarrow TC: $O(n^2)$

SC: $O(n)$

* Contribution technique \rightarrow Find the count of the no. of times a particular ele is contributing * particular ele

$$\text{arr}[] = \{ 3, -2, 4, -1, 2, 6 \}$$

In how many subarrays, index 3 will be present

<u>st</u>	<u>end</u>	subarr =
0	3	(0,3) (0,4) (0,5)
1	4	(1,3) (1,4) (1,5)
2	5	(2,3) (2,4) (2,5)
3		(3,3) (3,4) (3,5)

$$\text{Ans} = 4 * 3 = 12$$

$$\text{arr}[] = \{1 \ 2 \ 3 \ 4\}$$

0 1 2 3

In how many subarray, index 1 is present

<u>st</u>	<u>end</u>	Total no. of subarray = $2 * 3 = 6$
0	1	
1	2	
	3	

* Given N elements, how many subarrays have this i^{th} idx present

$$\text{arr}[] = \underbrace{\{a_0 \ a_1 \ a_2 \ \dots \ a_{i-1} \ a_i\}}_{(i+1)} \ * \ \underbrace{\{a_{i+1} \ \dots \ a_{n-1}\}}_{(n-i)}$$

No. of times a particular ele is going to contribute = $(i+1) * (n-i)$

$$\text{arr}[] = \{ 6, 8, 1, 7, 3 \}$$

$$(i+1) = 4$$

$$* (n-i) = 4$$

$$\text{No. of times } i^{\text{th}} \text{ ele is} = 4$$

going to contribute

Overall contribution = $24 + 48 + (-6) + 28 = \underline{\underline{94}}$

#

```
for (i=0; i<n; i++) {
    int count = (i+1) * (n-i)
    sum = sum + arr[i] * count;
}
```

TC = O(n)

SC = O(1)