

# LOCATING PARKS WITH A MULTIOBJECTIVE OPTIMIZATION METHOD

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Pomona College

# THE PROBLEM

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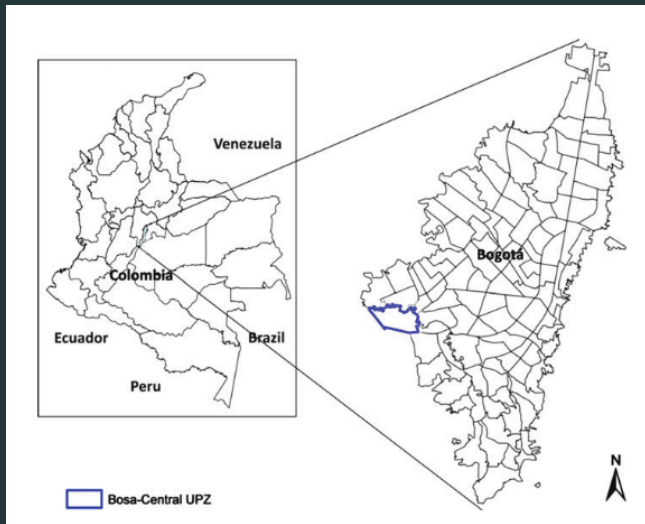
- Large city

- Large city
- Sports and recreation master plan

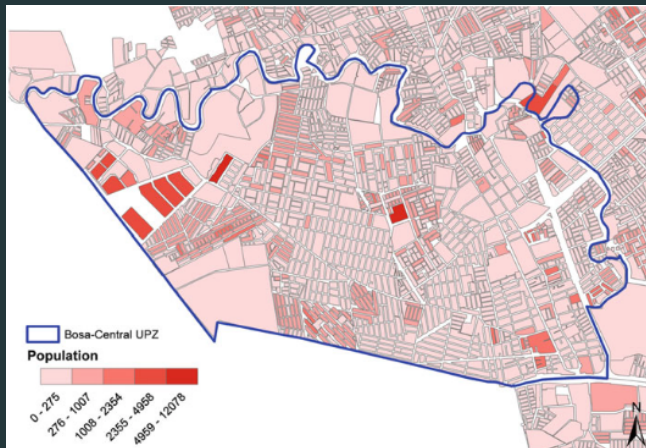
- Large city
- Sports and recreation master plan
- Instituto Distrital de Recreación y Deporte

- Large city
- Sports and recreation master plan
- Instituto Distrital de Recreación y Deporte
- A challenge

# BOGOTÁ, COLOMBIA



# BOGOTÁ, COLOMBIA





- Candidate parcels

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- Number of beneficiaries

## PARK SELECTION

- Candidate parcels
- Number of beneficiaries
- Geographic coverage

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- Sidewalk and road accessibility

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- Construction and parcel acquisition cost
- Competing objectives
- Community Based Operations Research



# THE GROUNDWORK

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- Mid-20th century development

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- Limited resources

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- Optimal

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- Linear model

- Mid-20th century development
- Limited resources
- Competing activities
- Optimal
- Linear model
- Planning activities

$$\begin{array}{ll}\text{Maximize:} & Z = c_1x_1 + c_2x_2 + \cdots + c_nx_n, \\ \text{subject to:} & a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n \leq b_1 \\ & a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n \leq b_2 \\ & \vdots \\ & a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n \leq b_m, \\ & x_1 \geq 0, x_2 \geq 0, \dots, x_n \geq 0\end{array}$$



Maximize:  $Z = c_1x_1 + c_2x_2 + \cdots + c_nx_n,$

subject to:  $a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n \leq b_1$

$$a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n \leq b_2$$

$$\vdots$$

$$a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n \leq b_m,$$

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Maximize:  $Z = c_1x_1 + c_2x_2 + \cdots + c_nx_n,$

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$\vdots$

$a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n \leq b_m,$

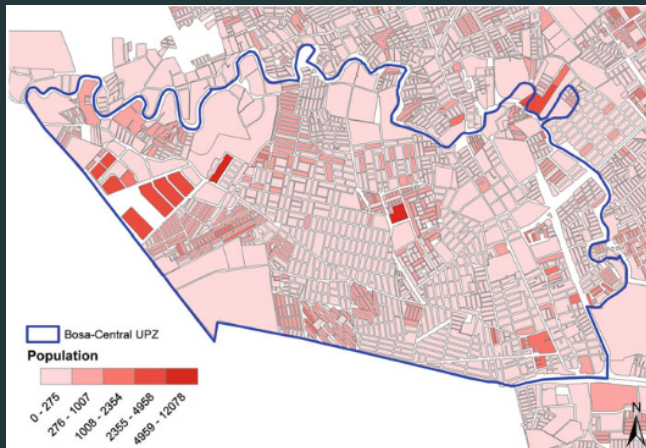
$x_1 \geq 0, x_2 \geq 0, \dots, x_n \geq 0$

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# THE MODEL

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# BOGOTÁ, COLOMBIA



- $m \times n$  grid

## SIMPLIFYING ASSUMPTIONS

- $m \times n$  grid
- One block = one square

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## SIMPLIFYING ASSUMPTIONS

- $m \times n$  grid
- One block = one square
- Every block same size
- Service area of a block is all bordering blocks (excluding candidate parcels)

- Maximize geographical coverage

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$f_1$

- Maximize geographical coverage

$f_1$

- Maximize people serviced

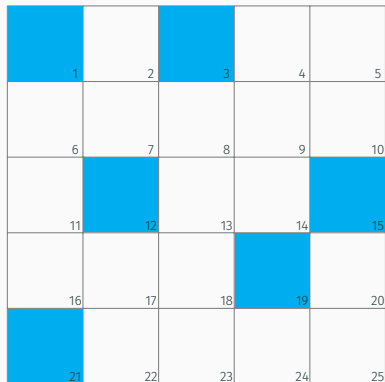
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$f_1$

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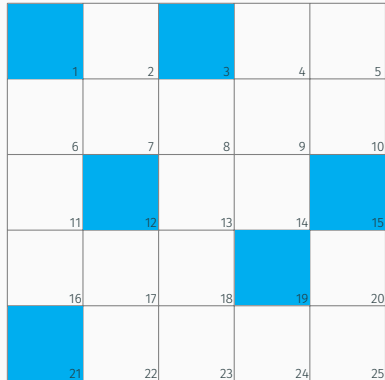
$f_3$

## EXAMPLE



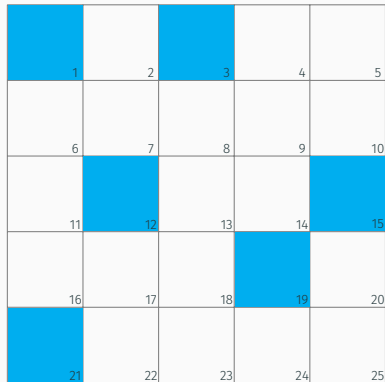
This is our  $5 \times 5$  grid city

## EXAMPLE



- Candidate parcels

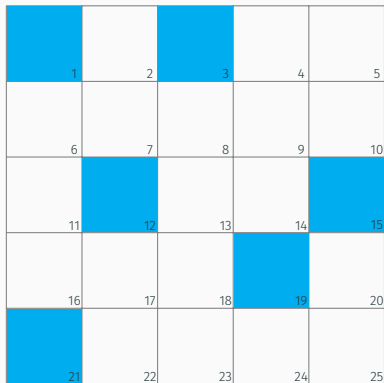
## EXAMPLE



- Candidate parcels:  $\mathcal{I} = \{1, 3, 12, 15, 19, 21\}$

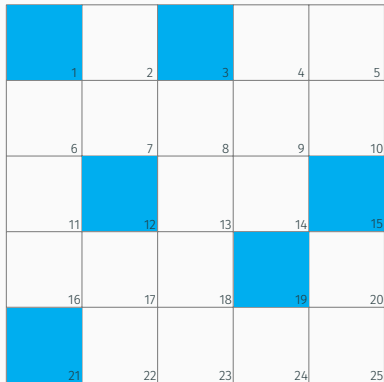


## EXAMPLE



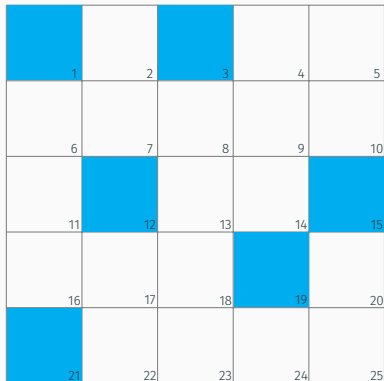
- Candidate parcels:  $\mathcal{I} = \{1, 3, 12, 15, 19, 21\}$ ;  $y_i, i \in \mathcal{I}$

## EXAMPLE



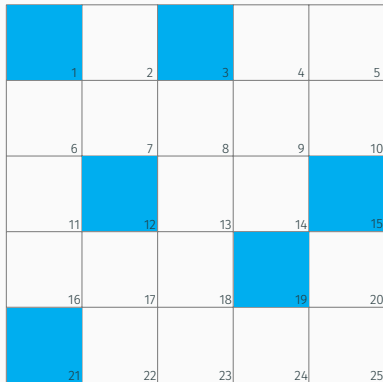
- Candidate parcels:  $\mathcal{I} = \{1, 3, 12, 15, 19, 21\}$ ;  $y_{19} = 1$

## EXAMPLE



Which candidate parcel will maximize geographical coverage?

## EXAMPLE



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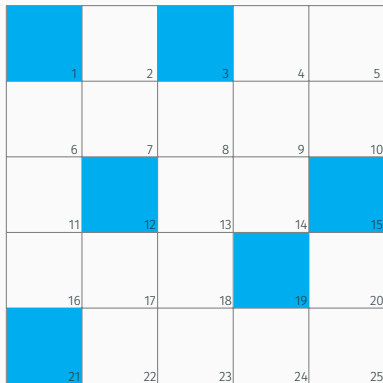
Candidate 12

## EXAMPLE

|    |    |    |    |    |
|----|----|----|----|----|
| 1  | 2  | 3  | 4  | 5  |
| 6  | 7  | 8  | 9  | 10 |
| 11 | 12 | 13 | 14 | 15 |
| 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 |

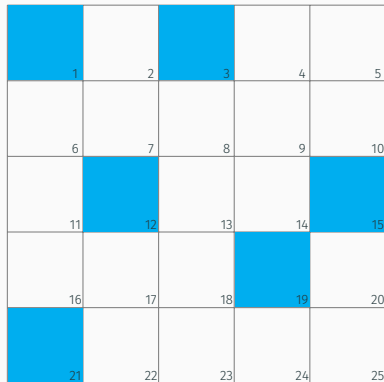
$$\cdot \mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$$

## EXAMPLE



- $\mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$ , the set of all blocks that would benefit from the construction of a new park

## EXAMPLE



- $\mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$
- $z_j, j \in \mathcal{J}, 1$  if block  $j$  is serviced by a selected parcel, 0 otherwise

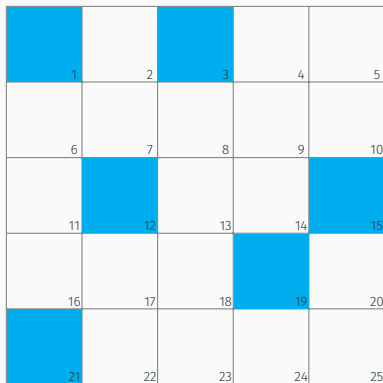
## EXAMPLE

|    |    |    |    |    |
|----|----|----|----|----|
|    |    |    |    |    |
| 1  | 2  | 3  | 4  | 5  |
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| 11 | 12 | 13 | 14 | 15 |
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- $\mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$
- $z_2 = z_6 = z_7 = 1, \quad z_4 = z_8 = z_9 = \dots = z_{24} = z_{25} = 0$

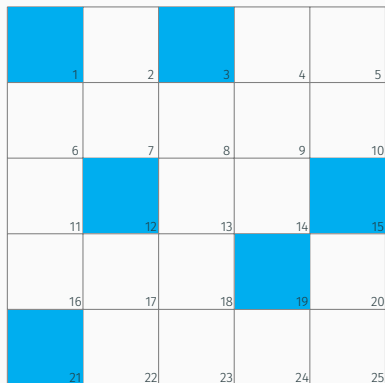


## EXAMPLE



- $\mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$
- $z_j, j \in \mathcal{J}$ , takes on value 1 if block  $j$  is serviced by a selected parcel, 0 otherwise
- $\mathcal{W}_j, j \in \mathcal{J}$ , the set of candidate parcels that serve block  $j$

## EXAMPLE



- $\mathcal{J} = \{2, 4, 6, 7, \dots, 23, 24, 25\}$
- $z_j, j \in \mathcal{J}$
- $\mathcal{W}_7 = \{1, 3, 12\}$

$$\begin{aligned} \max f_1 &= \sum_{j \in \mathcal{J}} z_j \\ \text{subject to } z_j &\leq \sum_{i \in \mathcal{W}_j} y_i, \quad j \in \mathcal{J} \\ |\mathcal{W}_j| z_j &\geq \sum_{i \in \mathcal{W}_j} y_i, \quad j \in \mathcal{J} \\ z_j &\in \{0, 1\}, \quad j \in \mathcal{J} \\ y_i &\in \{0, 1\}, \quad i \in \mathcal{I} \end{aligned}$$

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 \end{aligned}$$

## SWITCHING THE OBJECTIVE

|    |     |     |     |    |
|----|-----|-----|-----|----|
|    | 200 |     | 200 | 30 |
| 1  | 2   | 3   | 4   | 5  |
| 40 | 100 | 150 | 160 | 20 |
| 6  | 7   | 8   | 9   | 10 |
| 40 |     | 150 | 140 |    |
| 11 | 12  | 13  | 14  | 15 |
| 40 | 50  | 130 |     | 80 |
| 16 | 17  | 18  | 19  | 20 |
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## SWITCHING THE OBJECTIVE

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Which candidate parcel will maximize the number of beneficiaries?

## SWITCHING THE OBJECTIVE

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|----|-----|-----|-----|----|
|    |     |     |     |    |
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Which candidate parcel will maximize the number of beneficiaries?

$p_i, i \in \mathcal{I}$

## BOTH OBJECTIVES

|    |     |     |     |    |
|----|-----|-----|-----|----|
|    |     |     |     |    |
|    | 200 | 200 | 30  |    |
| 40 | 100 | 150 | 160 | 20 |
| 40 |     | 150 | 140 |    |
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|    | 60  | 70  | 80  | 40 |

Which candidate parcel will maximize the number of beneficiaries and the geographic coverage?

# THE SOLUTION STRATEGY

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- Maximize geographic coverage

- Maximize geographic coverage
- Maximize number of beneficiaries



$$\begin{aligned} \max f_1 &= \sum_{j \in \mathcal{J}} z_j \\ \max f_3 &= \sum_{i \in \mathcal{I}} p_i y_i \\ \text{subject to } z_j &\leq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\ |\mathcal{W}_j| z_j &\geq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\ p_{\max} &\geq \sum_{i \in \mathcal{I}} y_i \\ z_j &\in \{0, 1\}, j \in \mathcal{J} \\ y_i &\in \{0, 1\}, i \in \mathcal{I} \end{aligned}$$

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 \max f_1 &= \sum_{j \in \mathcal{J}} z_j \\
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 |\mathcal{W}_j| z_j &\geq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\
 p_{\max} &\geq \sum_{i \in \mathcal{I}} y_i \\
 z_j &\in \{0, 1\}, j \in \mathcal{J} \\
 y_i &\in \{0, 1\}, i \in \mathcal{I}
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 \max f_3 &= \sum_{i \in \mathcal{I}} p_i y_i \\
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 z_j &\in \{0, 1\}, j \in \mathcal{J} \\
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 f_1^*
 \end{aligned}$$

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 \max f_3 &= \sum_{i \in \mathcal{I}} p_i y_i \\
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 z_j &\in \{0, 1\}, j \in \mathcal{J} \\
 y_i &\in \{0, 1\}, i \in \mathcal{I} \\
 f_3^*
 \end{aligned}$$

$$\begin{aligned}
 \max f_1 &= \sum_{j \in \mathcal{J}} z_j \\
 \text{subject to } z_j &\leq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\
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 z_j &\in \{0, 1\}, j \in \mathcal{J} \\
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 \end{aligned}$$

$$f_1^* = 8 \text{ blocks}$$

$$\begin{aligned}
 \max f_3 &= \sum_{i \in \mathcal{I}} p_i y_i \\
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 p_{\max} &\geq \sum_{i \in \mathcal{I}} y_i \\
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$$f_3^*$$

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 p_{\max} &\geq \sum_{i \in \mathcal{I}} y_i \\
 z_j &\in \{0, 1\}, j \in \mathcal{J} \\
 y_i &\in \{0, 1\}, i \in \mathcal{I}
 \end{aligned}$$

$$f_3^* = 810 \text{ people}$$

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- $\alpha_k$  maximum acceptable deterioration for objective  $k$

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- $k = 1, 3$



- compromise threshold:  $(1 - \alpha_k)$
- $\alpha_k$  maximum acceptable deterioration for objective  $k$
- $k = 1, 3$
- $\alpha_1 = 40\%$  means objective function 1 must be at least 60% as optimal as the solution acquired in isolation

$$\begin{aligned}
& \max f_3 = \sum_{i \in \mathcal{I}} p_i y_i \\
& \text{subject to } z_j \leq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\
& |\mathcal{W}_j| z_j \geq \sum_{i \in \mathcal{W}_j} y_i, j \in \mathcal{J} \\
& p_{\max} \geq \sum_{i \in \mathcal{I}} y_i \\
& \sum_{j \in \mathcal{J}} z_j \geq (1 - \alpha_1) f_1^* \\
& z_j \in \{0, 1\}, j \in \mathcal{J} \\
& y_i \in \{0, 1\}, i \in \mathcal{I}
\end{aligned}$$

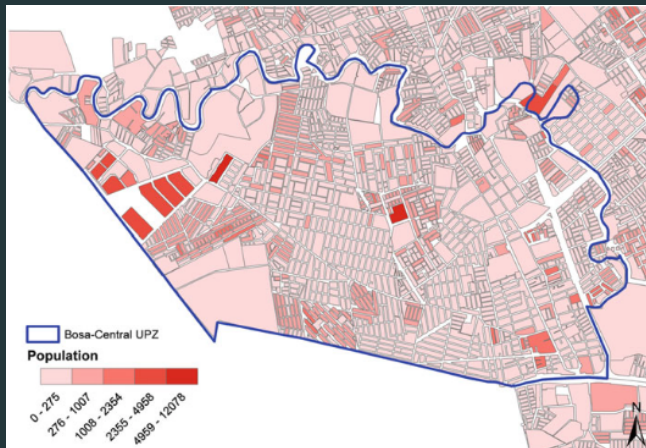
# SOLUTION

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[Graphic of larger example will go here]

[table of solutions for previous example will go here]

# BOGOTÁ, COLOMBIA



$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_2 = \sum_{i \in \mathcal{I}} \left( \sum_{\{k \in \mathcal{E}_{\mathcal{P}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i - \sum_{\{k \in \mathcal{E}_{\mathcal{N}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i \right)$$



$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_2 = \sum_{i \in \mathcal{I}} \left( \sum_{\{k \in \mathcal{E}_{\mathcal{P}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i - \sum_{\{k \in \mathcal{E}_{\mathcal{N}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i \right)$$

$$\max f_3 = \sum_{i \in \mathcal{I}} p_i y_i$$

$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_2 = \sum_{i \in \mathcal{I}} \left( \sum_{\{k \in \mathcal{E}_{\mathcal{P}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i - \sum_{\{k \in \mathcal{E}_{\mathcal{N}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i \right)$$

$$\max f_3 = \sum_{i \in \mathcal{I}} p_i y_i$$

$$\max f_4 = \sum_{i \in \mathcal{I}} v_i y_i$$

$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_2 = \sum_{i \in \mathcal{I}} \left( \sum_{\{k \in \mathcal{E}_{\mathcal{P}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i - \sum_{\{k \in \mathcal{E}_{\mathcal{N}} : d_{ik} \leq r^e\}} \left( 1 - \frac{d_{ik}}{r^e} \right) y_i \right)$$

$$\max f_3 = \sum_{i \in \mathcal{I}} p_i y_i$$

$$\max f_4 = \sum_{i \in \mathcal{I}} v_i y_i$$

$$\max f_5 = \sum_{i \in \mathcal{I}} e_i y_i$$

$$\max f_1 = \sum_{j \in \mathcal{J}} z_j$$

$$\max f_2 = \sum_{i \in \mathcal{I}} \left( \sum_{\{k \in \mathcal{E}_{\mathcal{P}} : d_{ik} \leq r^e\}} \left(1 - \frac{d_{ik}}{r^e}\right) y_i - \sum_{\{k \in \mathcal{E}_{\mathcal{N}} : d_{ik} \leq r^e\}} \left(1 - \frac{d_{ik}}{r^e}\right) y_i \right)$$

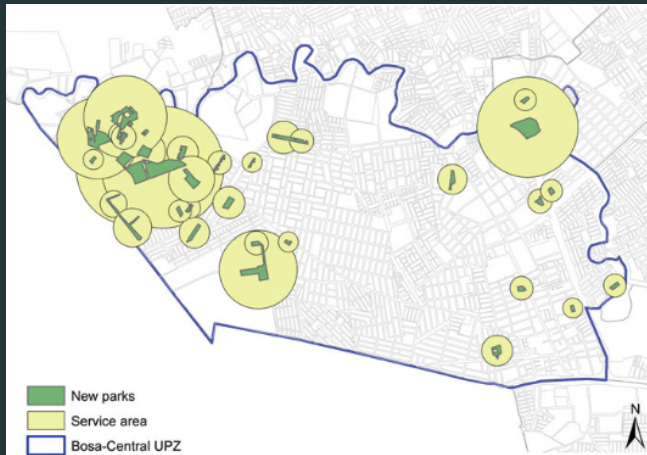
$$\max f_3 = \sum_{i \in \mathcal{I}} p_i y_i$$

$$\max f_4 = \sum_{i \in \mathcal{I}} v_i y_i$$

$$\max f_5 = \sum_{i \in \mathcal{I}} e_i y_i$$

$$\min f_6 = \sum_{i \in \mathcal{I}} (c_i^l + c_i^b) y_i$$

# BOGOTÁ, COLOMBIA



# THE CONCLUSION

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- Park location case study

- Park location case study
- Community Based Operations Research



## KEY POINTS

- Park location case study
- Community Based Operations Research
- Linear program

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- Multiobjective problem

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- Worked through an example

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## KEY POINTS

- Park location case study
- Community Based Operations Research
- Linear program
- Multiobjective problem
- Worked through an example
- Solutions
- Difficult process!

THE END

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QUESTIONS?