# SpecWizard User Guide

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# How to Run SpecWizard

SpecWizard can run in either serial or parallel mode. To run in serial mode, just run the executable with an optional command line parameter that specifies the parameter filename:

```
./specwizard [mypars.par]
```

To run in parallel mode, ensure that the code is compiled with the -DMPI flag set, and then run it like a standard MPI program:

```
mpirun -np 5 ./specwizard [mypars.par]
```

## **Parameters**

By default specwizard looks for an ascii file called <code>specwizard.par</code> in the current directory and reads parameters from there. If the command line argument is not present then <code>SpecWizard</code> searches by default for a parameter file in the current directory named <code>specwizard.par</code>. This section contains a complete list and description of the parameters. Where units may be important for a parameter they are shown on the right hand side of the page, the subscript  $\odot$  represents solar values. If any parameters remain uninitialized then <code>SpecWizard</code> will crash on startup.

Note that this default-name parameter file is not present in this repository.

#### 2.1 Basic Runtime Control

do\_long\_spectrum [LOGICAL]

If T then we generate a long spectrum by patching together spectra from different redshifts into one composite spectrum (long spectrum mode). If F then we generate a single spectrum along an individual LOS (short spectrum mode)

nspec [INTEGER]

Number of spectra to create. For short spectra this generates the first nspec spectra per LOS file. If there are insufficient sightlines in the LOS file, nspec is reduced. For long spectra this is the total number of long spectra to generate

#### 2.2 Files and Directories

ibdir[STRING]

Location of HDF5 file containing ionization fractions of each species as a function of redshift, density and temperature

```
datadir [STRING]
```

Location of the data files. See also file\_list. OR if use\_snapshot\_file is true, this must be the directory containing the snapshot directory.

```
use_snapshot_file [LOGICAL]
```

If this is true then instead of using LOS files, SpecWizard works with snapshot files

```
snap [INT]
```

If use\_snapshot\_file is true, then SW needs to know the snapshot number explicitly.

```
use_random_los[LOGICAL]
```

If we are using a snapshot file then we have the option of specifying LOS coordinates. If this is T then LOS coordinates are random, if it is F then LOS coordinates are drawn from the file los\_coordinates\_file

```
los_coordinates_file [STRING]
```

An ascii file containing LOS coordinates for SW. The first line simply contains the number of coordinates in the file. The rest of the file has 5 columns: x y z phi theta. In Ali Rahmati's version (default in this branch), the file only has three columns: x, y, z (tab-separated). Lines of sight are always along the z axis, and z is assumed to be zero. The x and y coordinates are the (x, y)-postion of the sightline, in units of the box size. (So x and y are fractions of the total size of the box.)

```
file_list [STRING]
```

An ascii file called file\_list must be present inside of datadir. This file must contain a list of LOS files, with one file per line. If this file is not present SpecWizard will crash. Update: this variable must contain the full path to the file containing the list of LOS files. It can be in datadir or somewhere else; both work.

```
outputdir[STRING]
```

Directory to write output data to

```
output_frequency [STRING]
```

If T then write frequencies to output files, if F then work with wavelengths

gimic [LOGICAL]

If F then we are using OWLS simulations or Eagle; if T then we are using GIMIC

overwrite [LOGICAL]

If F then if the output file already exists SpecWizard will crash. If T then old files will be overwritten

urchin [LOGICAL]

If T then read the neutral fraction for H1 (Si2) from post-processed snapshot files rather than lookup the ionization balance. (Those files are not present for Eagle, to the best of my knowledge.)

urchindir [STRING]

If urchin: The directory containing the post-processed snapshot files

use\_urchin\_temperature [LOGICAL]

If urchin: If T then read the particle temperatures from post-processed snapshot files rather than use the simulation temperature

## 2.3 Output Control

SpectrumFile [STRING]

If stated, this output filename is used rather than automatic filename generation.

output\_zspaceopticaldepthweighted\_values [LOGICAL]

For both long and short spectra. Output, separately for each ion, redshift space quantities weighted by contribution to the optical depth, the quantities that are written out are: Optical depth of strongest transition, overdensity and temperature (K)

output\_realspacemassweighted\_values [LOGICAL]

Only for short spectra, output real space, mass weighted quantities along the sightline. The quantities that are written out are: LOS peculiar velocity (km/s), metal mass fraction, overdensity and temperature (K)

output\_realspacenionweighted\_values [LOGICAL]

Only for short spectra, output real space  $N_{ion}$  weighted values separately for each ion. The quantities that are written out are: LOS peculiar velocity (km/s), Nion (cm<sup>-3</sup>), overdensity and temperature (K)

#### 2.4 Control of Ions

ibfactor[REAL]

Factor to rescale ionizing background with:  $I_{UV} = I_{UV} \times \text{ibfactor}$  (only used for calculation of the ionization balance)

doH1 [LOGICAL]

If T then consider H1 when calculating spectra. Other ions are switched on and off using the other flags: doHe2, doC2, doC3, doC4, doN2, doN5, doO1, doO6, doO7, doO8, doNe8, doNe9, doMg2, doSi3, doSi4, doFe2, do21cm. All of these parameters must be set (n.b.  $He2 = HeII = He^+$ )

doall [LOGICAL]

If T then override all other ion flags and force SpecWizard to consider all currently implemented ions

subtract\_Hmol [LOGICAL]

If urchin is T, then this option controls how to interpret the ionic fraction of Si2. Either (subtract\_Hmol=T)  $X_Si2 = X_H1$  or (subtract\_Hmol=F)  $X_Si2 = X_H1 + X_Hmol$ 

#### 2.5 Metal Abundance Modification

modify\_metallicity[LOGICAL]

If this is true then modify the simulation metal abundances, in one of a number of ways described by the parameters in this section. If this is F then all further variables in this section are ignored, and the simulation abundances are used

use\_smoothed\_abundance [LOGICAL]

If true, reads the smoothed element abundance in place of the true element abundance. This will not work for the Eagle line-of-sight files, which do not contain smoothed abundances.

maxz\_rel[REAL]  $Z_{\odot}$ 

If either impose\_z\_rho\_relation or log\_normal\_scatter are T, then limit the maximum metallicity with this parameter.  $Z_{\odot}$  is hardcoded into the source file specwizard\_modules.F90, and has a value of 0.0126637 (= $M_{Metal,\odot}/M_{tot,\odot}$ 

scale\_simulation\_abundances [LOGICAL]

Scale simulation metallicity by a scalar factor?

z\_rel[REAL]  $Z_{\odot}$ 

Scalar factor by which to scale metallicity, used only if scale\_simulation\_abundances is T.  $Z_{\odot}$  is hardcoded into the source file specwizard\_modules.F90, and has a value of 0.0126637 (= $M_{Metal,\odot}/M_{tot,\odot}$ 

ZC\_rel [REAL]

Scale carbon abundances by this linear value relative to their original abundance. Other metals are scaled by the parameters: <code>ZN\_rel,ZO\_rel,ZNe\_rel,ZMg\_rel,ZSi\_rel,ZFe\_rel</code>. All of which must be set. Used only if <code>modify\_metallicity</code> is T. These parameters are used to change the relative abundances of different elements.

impose\_z\_rho\_relation[LOGICAL]

impose metallicity  $z=\mathtt{z\_mean}(\rho/\rho_{mean})^{\mathtt{z\_index}},$  up to maximum metallicity  $\mathtt{maxz\_rel},$   $\rho_{mean}$  is the mean baryonic density of the Universe

z\_index [REAL]

Power-law index of  $\rho$ -Z relation, used only if <code>impose\_z\_rho\_relation</code> is T

z\_mean [REAL]  $Z_{\odot}$ 

Metallicity at mean density, if we are imposing a  $\rho\text{-}Z$  relation, used only if <code>impose\_z\_rho\_relation</code> is T

log\_normal\_scatter [LOGICAL]

If true, Divide computational volume in (z\_sig\_bin)<sup>3</sup> cells, and add lognormal metallicity with z\_sig\_dex scatter to particles in each cell

#### z\_sig\_bin [INTEGER]

Number of cells to divide the computational volume into, if we are imposing a lognormal metallicity scatter, used only if log\_normal\_scatter is T

#### z\_sig\_dex[REAL]

If we are adding a lognormal metallicity scatter to each particle, then in solar units,  $\log(Z) \to \log(Z) + \Sigma z \text{sig_dex}$ , where  $\Sigma$  is a Gaussian deviate with mean 0, standard deviation=1, which is selected independently for each of the  $(z_\text{sig_bin})^3$  cells. Used only if  $\log_\text{normal_scatter}$  is T

### 2.6 Noise Statistics

#### generate\_noise[LOGICAL]

Generate a noise array? If this is true then in addition to the 'Flux' variable written for each spectrum (which always contains a noise-free spectrum), there are two additional arrays written out: 'Noise\_Sigma' (standard deviation of the noise at each pixel), and 'Gaussian\_deviate' (mean=0, sigma=1 Gaussian random number for each pixel)

#### use\_noise\_file [LOGICAL]

If T then use file describing sigma as a function of flux and wavelength. If F then use sigtonoise and minnoise to generate Gaussian noise. This option works in long spectrum mode only.

#### noisefile [STRING]

If we are using noise from a file, load in noisefile, an HDF5 file that describes the standard deviation of the noise as a function of wavelength and flux. Note that this noise file can be created from observations using the noisestat.pro IDL script included in the Noise/subdirectory of the SpecWizard distribution.

#### sigtonoise [REAL]

If use\_noise\_file is false then this is the signal to noise ratio for the Gaussian noise: sigma = minnoise + (1/sigtonoise - minnoise) \* flux

#### minnoise [REAL]

If use\_noise\_file is false then this is the minimum noise level, normalized to the continuum, for the Gaussian noise: sigma = minnoise + (1/sigtonoise - minnoise) \* flux

### 2.7 Accuracy Parameters

minbother\_blue [REAL]

Accuracy parameter, minimum optical depth to consider for transitions with rest-frame wavelength shorter than that of HI Ly $\alpha$ . The smaller this number the more accurate the results, but the slower the code will run. This is the maximum optical depth allowed to be missed in a short spectrum pixel.

minbother\_red[REAL]

Accuracy parameter, minimum optical depth to consider for transitions with rest-frame wavelength longer than that of HI Ly $\alpha$ . The smaller this number the more accurate the results, but the slower the code will run. This is the maximum optical depth allowed to be missed in a short spectrum pixel.

limsigma [LOGICAL]

Accuracy parameter. If true, the line profile is only calculated over the velocity range where the optical depth is above minbother divided by the number of pixels. This means that, at most, a total amount of absorption minbother is missed in each pixel. (The minbother results still affect the spectra if this is False: they also determine whether the maximum optical depth from a real space pixel is large enough to bother adding to the optical depth spectrum.)

vpixsizekms [REAL]

km/s

Pixel size in km/s. For short spectra this represents the final output pixel size. For long spectra this represents the pixel size before rebinning into. SpecWizard will stop if this is too small compared with the other parameters. The smaller this number the more accurate the results, but the slower the code will run. Note that this also sets the resolution at which the position-space ion densities and ion-weighted temperatures and peculiar velocities are calculated. The shape and width of the spectral features can therefore be affected if this value is too low.

## 2.8 Parameters For Long Spectrum

zqso [REAL]

Redshift of the QSO

minlambda [REAL]

Å

Minimum observed wavelength in final spectrum

minlambda [REAL]

Å

Maximum observed wavelength in final spectrum

zabsmin [REAL]

Minimum allowed absorption redshift

zabsmax[REAL]

nlyman [INTEGER]

Number of Lyman lines to include (1 = Ly-alpha, 2 = Ly-beta, etc.; neg. value = use nlyman\_all = 31)

fzresol[REAL]

Bin size for simulation LOS files: dz = fzresol\*(1+z). Sight lines are drawn from files with z\_file = z + /- fzresol(1+z)/2, where z is the current redshift.

pixsize [REAL]

Å

Pixel size of final spectrum

do\_convolve\_spectrum [LOGICAL]

If T then convolve final spectrum with an instrumental broadening of  ${\tt fwhm}\ km/s$ 

fwhm [REAL]

km/s

FWHM of instrumental broadening (Gaussian), used only if  ${\tt do\_convolve\_spectrum}$  is T

# **Structure of Output Files**

Output files are HDF5, and so are organized hierarchically. At the top level there are four header groups (Units, Constants, Parameters, Header).

**Units** Conversion factors between original SPH simulation units and cgs. Whilst using SpecWizard you should not need anything in this group!

**Constants** Physical constants

Parameters Parameters from specwizard.par

**Header** The Header data from the simulation. Contains information on cosmology, etc.

At the top level there are in addition to the four header groups one additional group for each spectrum (for spectrum number N this is called <code>SpectrumN</code>), and a dataset that contains either Wavelengths (<code>Wavelength\_Ang</code>. for long spectra), or Hubble expansion velocities, corresponding to a physical coordinate (<code>VHubble\_KMpS</code> for short spectra). The contents of the individual spectrum groups will be treated separately for short and long spectra:

## 3.1 Short Spectra

Each spectrum group contains a sub-group for each ion (e.g. /Spectrum1/c4/), this group contains a scalar dataset (LogColumnDensity) containing the integrated column density of that ion, and an array, (Optical Depth), containing the optical depth of that ion as a function of hubble velocity.

If output\_realspacemassweighted\_values is true then each spectrum group contains a sub-group called RealSpaceMassWeighted, containing real space physical properties (i.e. as a function of Hubble velocity), weighted by mass. These arrays are

LOSPeculiarVelocity\_KMpS

MetalMassFraction

OverDensity

Temperature\_K

Note that the OverDensity is not the mass-weighted density in each pixel, but the density itself, used as a weight for the other datasets.

If output\_zspaceopticaldepthweighted\_values was set to true then there is an additional subgroup called

RedshiftSpaceOpticalDepthWeighted, which contains

OverDensity

Temperature\_K

LOSPeculiarVelocity\_KMpS

These are arrays of densities and temperatures, with particle properties weighted by the optical depth they contribute to each pixel. Note that this is weighted by the optical depth of the strongest transition only. If output\_realspacenionweighted\_values is set then there is another additional subgroup, called RealSpaceNionWeighted, which contains the following arrays:

LOSPeculiarVelocity\_KMpS

NIon\_CM3 (in the ion group, not RealSpaceNionWeighted)

OverDensity

Temperature\_K

These are real space quantities, weighted by Nion. If either category of real-space quantities is output, an additional array is stored: Redshift\_RealSpace, which indicates the redshift (assuming no peculiar velocities) at which the mass- and ion-weighted quantities are calculated. Warning! If all optional output is generated then output dataset can become very large!

## 3.2 Long Spectra

Each spectrum group contains an array, Flux, containing the total normalized, transmitted flux as a function of wavelength. If noise has been specified then two additional arrays are present, called Gaussian\_deviate and Noise\_Sigma. An additional group, called ShortSpectraInfo contains information so that the exact lines of sight used from the LOS files

may be looked up. Finally, the spectrum group contains a sub-group for each individual ion, if <code>output\_zspaceopticaldepthweighted\_values</code> is true then this group contains a subgroup <code>RedshiftSpaceOpticalDepthwith</code> the following arrays:

RedshiftSpaceOpticalDepthOfStrongestTransition (in the ion group, not the optical depth group; the weight itself, not optical-depth-weighted)

LogColumnDensity (in the ion group, not the optical depth group). Total value along the line of sight. Short spectrum contributions are printed in the log file if verbose is True.)

OverDensity

Temperature\_K

LOSPeculiarVelocity\_KMpS

Each of the arrays is of the same size as /Wavelength\_Ang, and describes the overdensity, temperature, and peculiar velocity of each pixel, where gas particle properties have been weighted by their contribution to the optical depth.

If output\_realspacemassweighted\_values is True, the spectrum group contains a RealSpaceMassWeighted subgroup with the following arrays:

MetalMassFraction

OverDensity (the weight itself, not mass-weighted)

Temperature\_K

LOSPeculiarVelocity\_KMpS

If output\_realspacenionweighted\_values is True, the ion groups contain a RealSpaceNionWeighted subgroup with the following arrays:

NIon\_CM3 (the weight itself, in the ion group)

OverDensity

Temperature\_K

LOSPeculiarVelocity\_KMpS

The real-space arrays show properties as a function of redshift along the line of sight (ignoring peculiar velocities), at the redshift resolution at the largest used wavelength in the spectrum. Depending on the redshift and wavelength ranges, these arrays can be very large. The redshifts these arrays correspond to are stored in the <code>Redshift\_RealSpace</code> array in the spectrum group. (It could be moved to the root group along with the wavelengths.)

#### 3.3 Normalised Gaussians

We use error functions instead of the M4 kernel to obtain integrals over bins. To do so we replace the M4 SPH spline with a function which is a produce of 1D Gaussians,

$$G(x,y,z) = \left(\frac{1}{(2\pi\sigma^2)^{1/2}} \exp(-x^2/(2\sigma^2))\right) (x \to y)((x \to z)).$$
 (3.1)

We choose the relation between  $\sigma$  and h such that the functions have the same value at zero lag, so that

$$(2\pi\sigma^2)^{3/2} = \frac{\pi h^3}{8}$$

$$2\sigma^2 = \frac{h^2}{4\pi^{1/3}}$$

$$\frac{h}{2^{1/2}\sigma} = 2\pi^{1/6}.$$
(3.2)

Next we want the integral of G over a cube with side 2h to be unity. So the 1D 'truncated' Gaussian we actually use is

$$G(x) = \frac{\mathcal{N}}{(2\pi\sigma^2)^{1/2}} \exp(-x^2/(2\sigma^2))$$
 (3.3)

and we determine  $\mathcal{N}$  such that  $\int_{-h}^{h} G(x) dx = 1$ , which yields

$$\mathcal{N} = \frac{1}{2\operatorname{erf}(2\pi^{1/6})},\tag{3.4}$$

where the error function is

$$\operatorname{erf}(x) \equiv \frac{2}{\pi^{1/2}} \int_0^x \exp(-t^2) dt$$
. (3.5)

A 1D column density integral for a sightline at impact parameter b is then

$$C = \left(\frac{\mathcal{N}}{(2\pi\sigma^2)^{1/2}}\right)^3 \exp(-b^2/(2\sigma^2)) 2 \int_0^{z_+} \exp(-z^2/(2\sigma^2)) dz$$

$$= \frac{\mathcal{N}^3}{(2\pi\sigma^2 a^2)} \times \exp(-b^2/(2\sigma^2)) \operatorname{erf}(z_+/(2\sigma^2)^{1/2})$$

$$z_+ \equiv (h^2 - b^2)^{1/2}. \tag{3.6}$$

Note the appearance of the expansion factor a so that the result is a physical column-density (as opposed to a co-moving one). The mass corresponding to square pixel is then

$$\mathcal{I} = \left(\frac{\mathcal{N}}{(2\pi\sigma^2)^{1/2}}\right)^3 \left[\int_{x_1}^{x_2} \exp(-(x-x_0)^2/(2\sigma^2)) dx\right] \times [x \to y] \left[\int_{-\infty}^{\infty} \exp(-(z-z_0)^2/(2\sigma^2)) dz\right] \\
= \mathcal{N}^2 \left[\frac{1}{2} \left(\operatorname{erf}((x_2-x_0)/(2\sigma^2)^{1/2}) - \frac{1}{2}\operatorname{erf}((x_1-x_0)/(2\sigma^2)^{1/2})\right] \times [x \to y], \quad (3.7)$$

and the corresponding mean column density is  $\bar{\mathcal{C}}=\mathcal{I}/(a\,dx)^2$ , again multiplying by the scale factor a to obtain a physical column density.

# How specwizard works

Here, we give an outline of the algorithms used by specwizard to calculate the spectra. This is useful for understanding the outputs, and should hopefully be helpful for modifying or debugging the code.

### 4.1 Short spectra

When calculating short spectra, the SPH particle data is first interpolated to a 1-dimensional grid along the line of site. This is then used to calculated the optical depth as a function of line of sight velocity. In these calculations, positions are periodic with the box size, as in the simulations being post-processed. Similarly, line-of-sight velocities are taken to be periodic, with a period equal to the Hubble flow across the box.

subroutine projectdata Looping over the SPH particles, the ion content is calculated for each. The ionization balance is calculated from the density, temperature, and redshift, by interpolating the ionization tables. The total ion content then follows from the ionization fraction, mass, and element abundance. To calculate the ion density in each cell along the line of sight in position space, the chosen kernel is used, scaled with the smoothing length of the particle. Depending on the integration option, the kernel is either evaluated at the cell centre or integrated over the line of sight between cell edges (second option only available for a Gaussian kernel). Besides the ion densities themselves, the velocity along the line of sight and the temperature are needed for each cell. The ion-weighted temperatures and velocities are used for this. The number of cells in position space is equal to the number of pixels in velocity space.

subroutine makespectra, subroutine computespectrum From the ion densities, velocties, and temperatures in the cells, along with the cell sizes

and atomic data, the optical depth as a function of line of sight velocity is calculated. Looping over cell with position x along the line of sight, each cell is treated as a single absorbing cloud. Each cell's absorption is modelled as a single Gaussian line. (Damping wings are ignored, but can be added in further post-processing). The total (integrated) optical depth is set by the column density in the cell, and the width by thermal broadening. (Additional turbulent broadening should be possible, but is not recently tested.) It's centre is set at  $xH(z)+v_p$ , where  $v_p$  is the ion-weighted peculiar velocity in the cell. The Gaussian is either integrated over the cell or evaluated at the cell centre (ntegrate\_thermprof\_exactly).

### 4.2 Long spectra

To make long spectra, line-of-sight (los) files are needed in the current implementation. These are simulation outputs at smaller time intervals than the Eagle snapshots, containing all particles intersecting a set of 100 lines of sight through the box at each output time. These lines of sight are along the X or Z axis of the simulation, and the axes and positions are randomly chosen. Specwizard chooses lines of sight randomly from all files within some redshift difference  $\Delta z$  of the end redshift of the last segment <code>zcurrent</code>, set by the <code>fzresol</code> parameter.

The lines of sight (files, los numbers, positions, and axes) used are stored in the specwizard output. The positions are in the same units as coordinates in the simulation; for Eagle, that's  $\mathrm{cMpc}\,\mathrm{h}^{-1}$ .

The short spectra are calculated in the same way as in short spectrum mode, except that the densities are rescaled by the expansion factor at the redshift of the sightline segment (acurrent/zcurrent), rather than that of the line-of-sight file or snapshot. The same is true for cosmological calculations, such as local Hubble factors.

These short spectra are then interpolated onto a wavelength grid. The output\_frequency options allows frequency outputs, but the calculations are still done in wavelength space; the output file simply contains the fixed- $\Delta$ - $\lambda$ -grid spectra, but the spectrum bin array is converted to frequency units (MHz). The resolution at which the spectra are calculated is set by the pixel size chosen in velocity space.

The spectra are finally binned to that fixed- $\Delta$ - $\lambda$ -grid, simply averaging the values that contributes to the same final pixel. This may cause small discrepancies between flux and optical depth spectra. For weighted average spectra, the binning respects the weighting. (The weighted quantities are multiplied by the weights before binning, then divided by the binned weights.)

Weighted line of sight properties are a function of line of sight position for the real space quantities, and wavelength for the redshift space quantities. Optical-depth-weighted averages account for contributions by the strongest (first listed) transition for each ion only.

spline\_interpolate adds interpolated values to values already in the output array. Great for optical depths of different lines, but requires caution for averaged quantities.

Note that in the spectrum calculations, short spectra are calculated as a function of  $\Delta v$ , the velocity difference according to the Hubble flow and peculiar velocity with line of sight coordinate zero (assuming zero peculiar velocity there). For each pixel, this gives

$$1 + z_{\text{pix}} = (1 + z_0)(1 + \Delta v_{\text{pix}}/c), \tag{4.1}$$

in the limit of small  $\Delta v$ , with  $z_0$  the redshift at the zero position of the line of sight. Using

$$\lim_{n \to \infty} (1 + x/n)^n = \exp(x),$$
(4.2)

$$1 + z_{\text{pix}} = (1 + z_0) \exp(\Delta v_{\text{pix}}/c)$$
 (4.3)

for general  $\Delta v$ . This is used in the subroutine insertspectra, where the spectra are tabulated as a function of log wavelength, linear in  $\Delta v$ . This is also where the logs and exps in the setup of the long spectra come from.